

SCALAR(WIMP)S 2015

with a focus on gamma-ray signatures

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Belgium



SCALARS 2015
Warsaw, Poland, 03-07 December 2015



S(CALAR)WIMPS 2015

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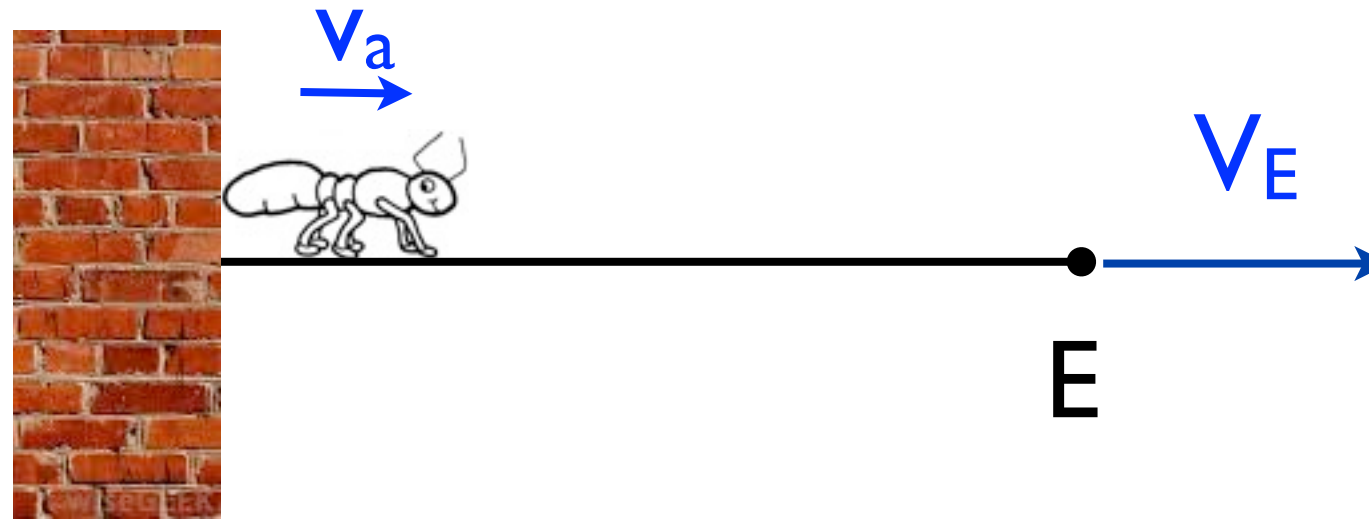


SCALARS 2015
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About Lev Okun



Q1. Can the ant reach the end E of the string if $V_E > v_a$?

Q2. If so, how long would it take ?

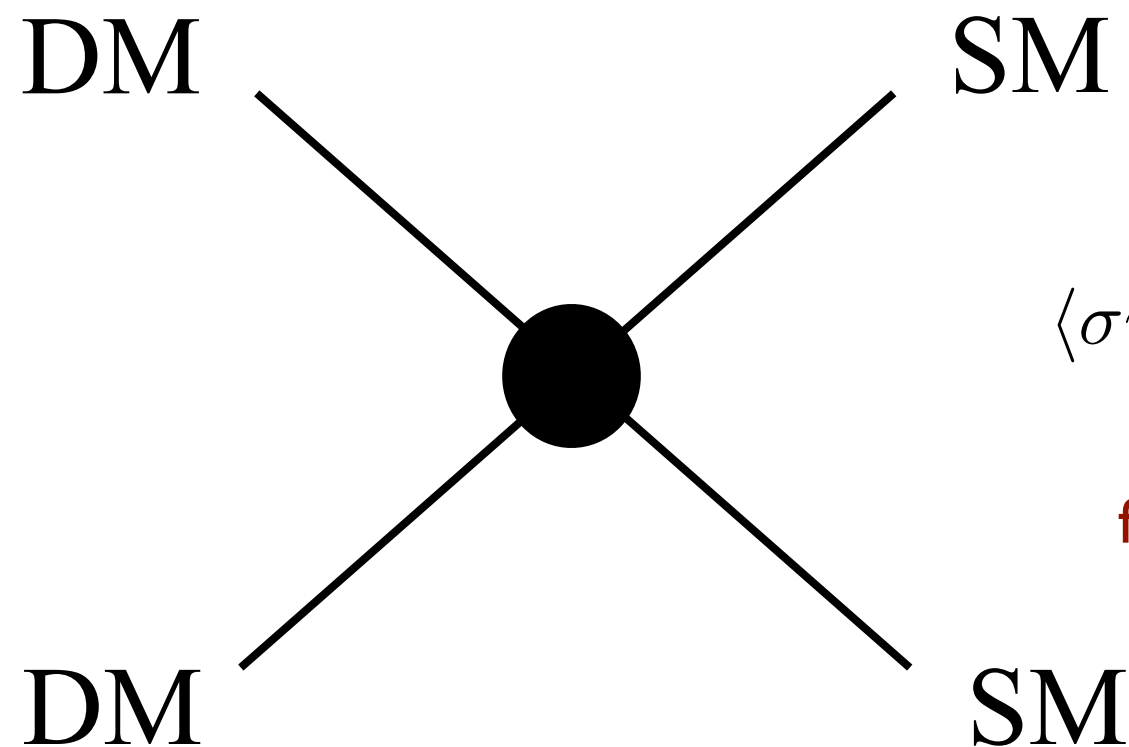
$V_E = \text{const}$

Q3. What if $dV_E/dt > 0$?

Hint: the story goes, according to Lev Okun, that A. Sakharov gave the answer(s) in one second

DM AS A WIMP

(weakly interacting massive particle)



$$\langle \sigma v \rangle \approx 3 \cdot 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$$

Benchmark value
for DM indirect detection



freeze-out in early universe

WHY WIMP MODELS?

Why not? We don't know what DM is made of

2 canonical DM candidates

The neutralino

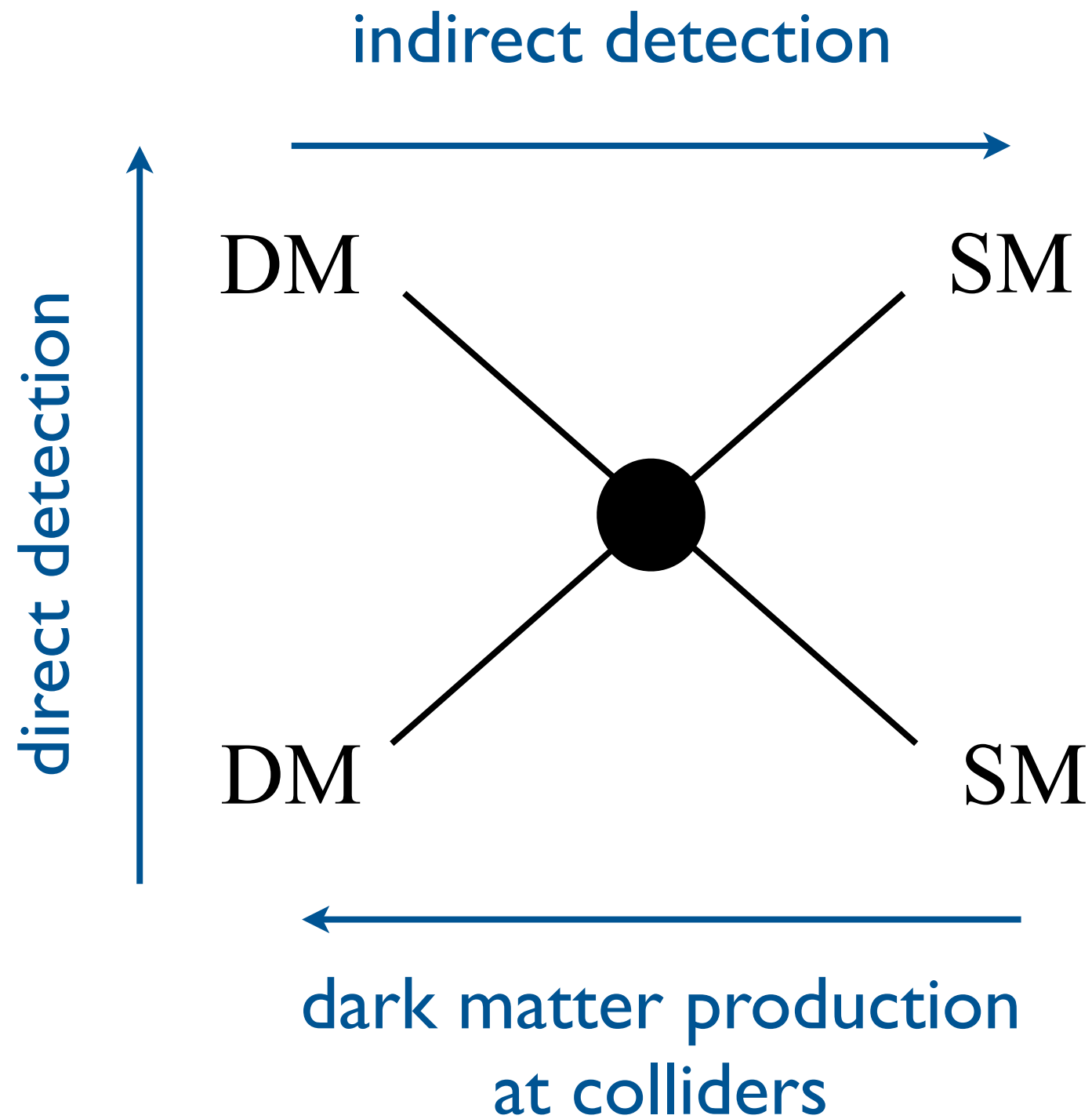
SUSY may not exist

The strong CP axion

Not a WIMP

May be subdominant DM

WHY WIMP MODELS?



WHY A SCALAR WIMP?

Possible relation to Higgs sector

The Higgs Portal

See Gavela's talk

$$\mathcal{L}_{\text{SM}} \supset -\frac{\mu^2}{2}|H|^2$$



$$\mathcal{L} \supset -\lambda_{hs}|S|^2|H|^2$$



Dim 2

$$\sim -\lambda_{hs}\frac{v^2}{2}|S|^2$$

weak scale mass?

Patt & Wilczek (2006) "The Higgs portal"

Hempfling (1996)

Espinosa & Quiros (2007)

Hambye & MT (2007)

....

See also Lindner's talk

WHY A SCALAR WIMP?

Minimality I.0

DM as SM scalar singlet

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{m_S^2}{2} S^2 - \frac{\lambda_S}{4} S^4 - \frac{\lambda_{hs}}{2} S^2 |H|^2$$



$$S \xrightarrow{Z_2} -S$$

$$H \xrightarrow{Z_2} H$$

Zee & Silveira (1985) “Phantom matter”
Veltman & Yndurain (1989)
Mc Donald (1994)
Burgess, Pospelov & ter Veldhuis (2001)
...

Remark: Z_2 may be a remnant of a gauge symmetry e.g. Matter Parity in $\text{SO}(10)$

Krauss & Wilczek (1986)
Kadastik, Kannike & Raidal, arXiv:0902.2475
...

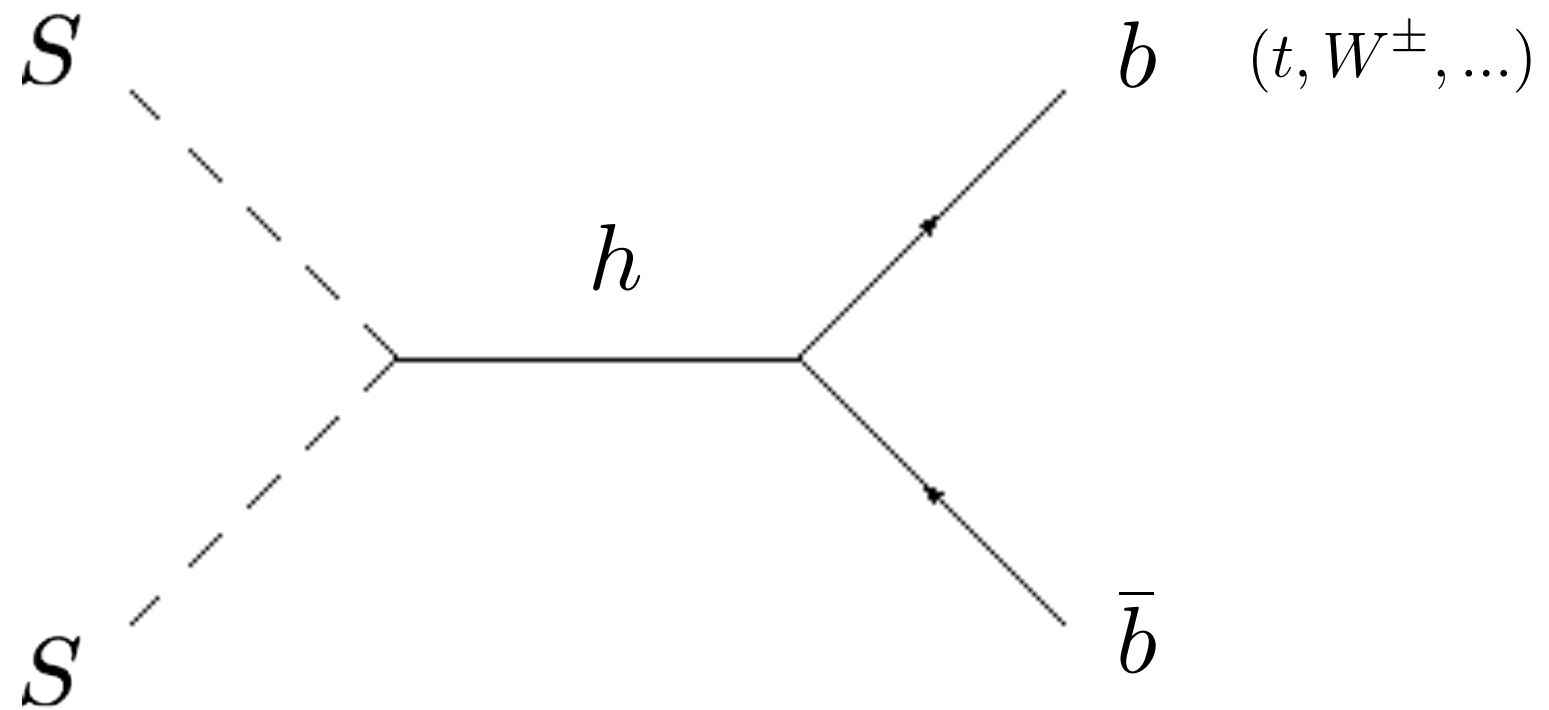
CAVEAT

$$\langle S \rangle = 0 \quad (\text{unbroken } Z_2 \text{ symmetry})$$

Scalar DM at the EW scale (hierarchy problem)

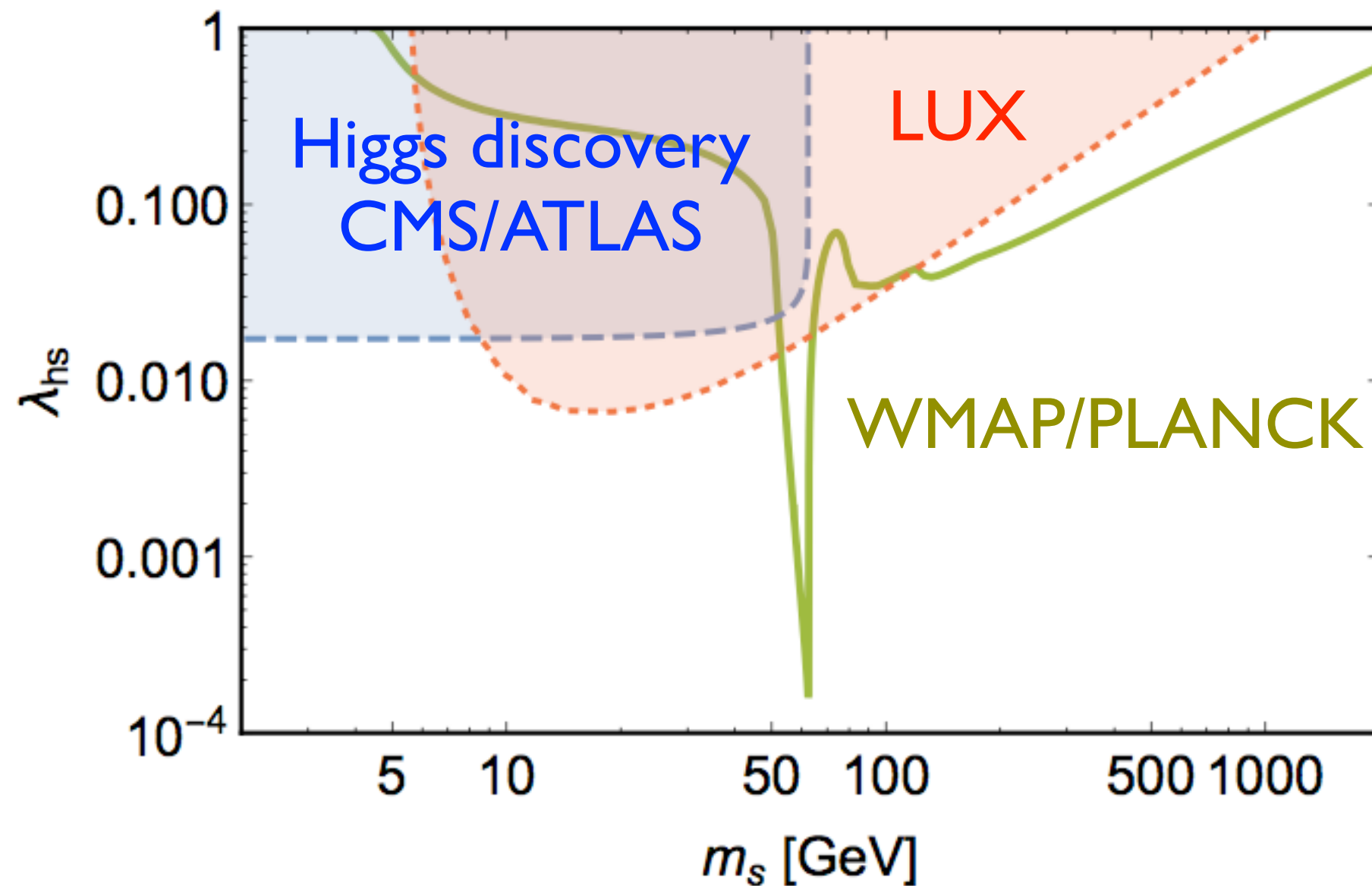
indirect detection

direct detection



**dark matter production
at colliders**

Very simple and (by now) very constrained model



WHY A SCALAR WIMP?

Minimality2.0

SU(2) multiplets

(aka Minimal Dark Matter)

Inert Doublet

Ma & Deshpande (1978)
 Barbieri, Hall & Rychkov (2006)
 Lopez Honorez, Nezri, Oliver & MT (2007)
 ...
 See Kraml, Swiezewska, Robens,...
 talks

Quantum numbers			DM can decay into
SU(2) _L	U(1) _Y	Spin	
2	1/2	0	EL
2	1/2	1/2	EH
3	0	0	HH^*
3	0	1/2	LH
3	1	0	HH, LL
3	1	1/2	LH
4	1/2	0	HHH^*
4	1/2	1/2	(LHH^*)
4	3/2	0	HHH
4	3/2	1/2	(LHH)
5	0	0	(HHH^*H^*)
5	0	1/2	—
7	0	0	$(\chi\chi\chi H^\dagger H)$

~ Higgsino-like

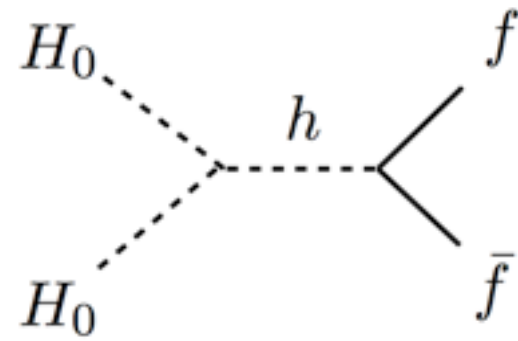
~ Wino-like

Fermionic 5-plet

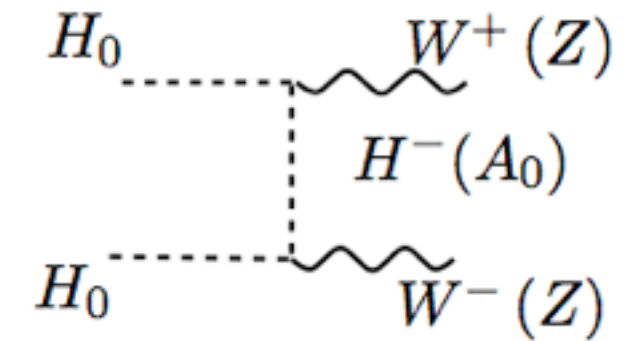
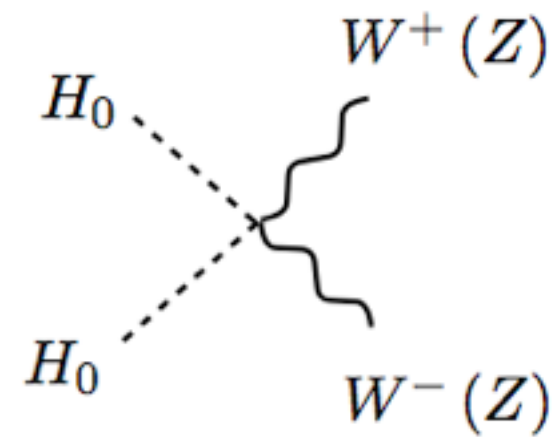
Scalar 7-plet



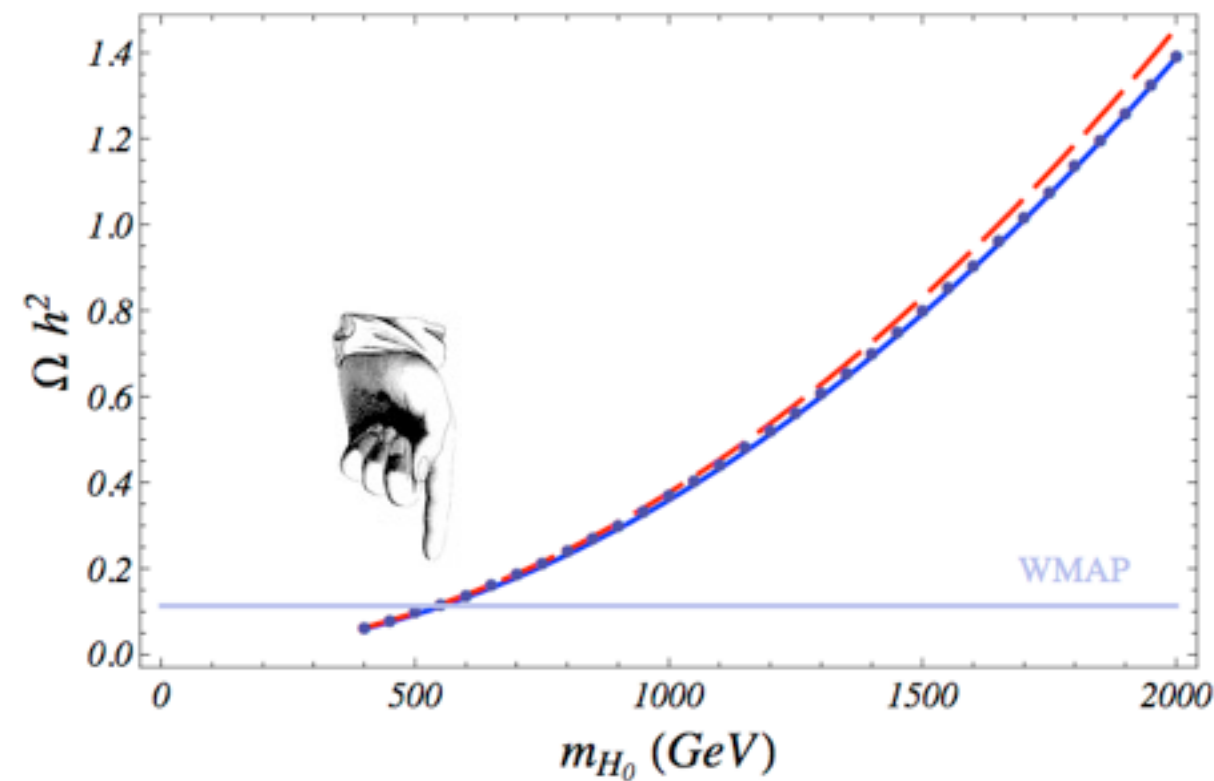
singlet



multiplet



Naturally Heavy $\sim$ TeV WIMPs



WHY A SCALAR WIMP?

The Devil is in the details

I. VECTOR LIKE PORTAL

Based on:

F. Giacchino, L. Lopez Honorez & MT, arXiv:1307.6480 & arXiv:1405.6921
A. Ibarra, F. Giacchino, L. Lopez Honorez, MT & S. Wild, arXiv:1511.04452

II. MDM SCALAR 7-PLET

Based on:

C. Garcia-Cely, A. Ibarra, A. Lamperstorfer & MT, arXiv:1507.05536

I. VECTOR-LIKE PORTAL*

$$\mathcal{L} \supset y_l S \bar{\Psi} l_R + h.c.$$

Diagram illustrating the Lagrangian term $\mathcal{L} \supset y_l S \bar{\Psi} l_R + h.c.$ with field assignments:

- S : real singlet scalar
- $\bar{\Psi}$: vector-like lepton (or quark)
- l_R : SM light lepton (or quark)

Z_2 symmetry

$$\begin{aligned} S &\xrightarrow{Z_2} -S \\ \Psi &\xrightarrow{Z_2} -\Psi \end{aligned}$$

S is our dark matter

* We call it the Vector-like Portal following Fileviez Perez & Wise, arXiv:1303.1452

IT'S A TOY MODEL

(aka simplified model)

Scalar cousin of bino-like DM

Majorana DM
with slepton or squark mediator

$$\chi \tilde{l}^\dagger l_R \quad \chi \tilde{q}^\dagger q_R$$

See also Laura Covi's
talk for a variation on
this model

Appears in top-down scenarios

eg 6D model with spinless KK photon $\sim S$

eg Dobrescu & Ponton, arXiv:hep-th/0401032

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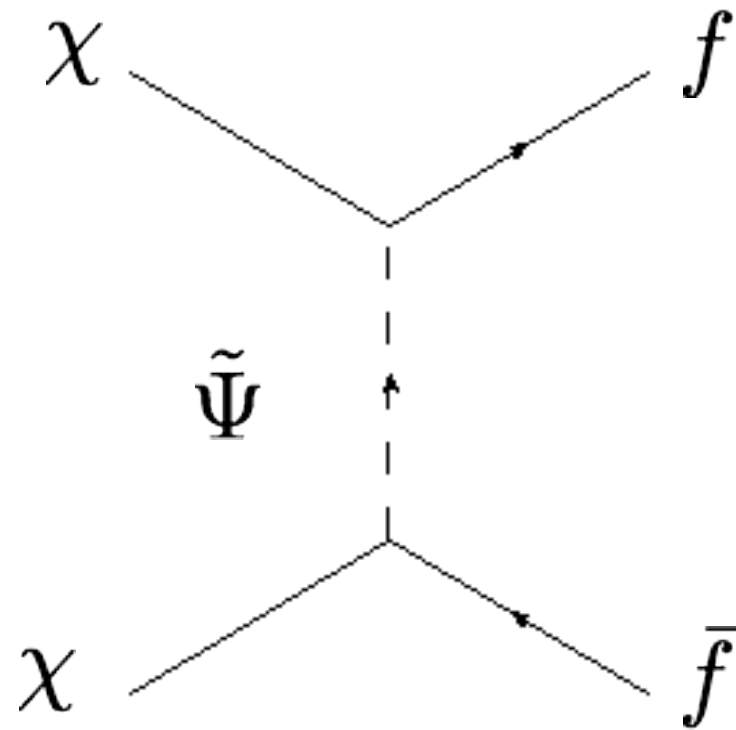
eg 6D model with spinless KK photon $\sim S$

eg Dobrescu & Ponton, arXiv:hep-th/0401032

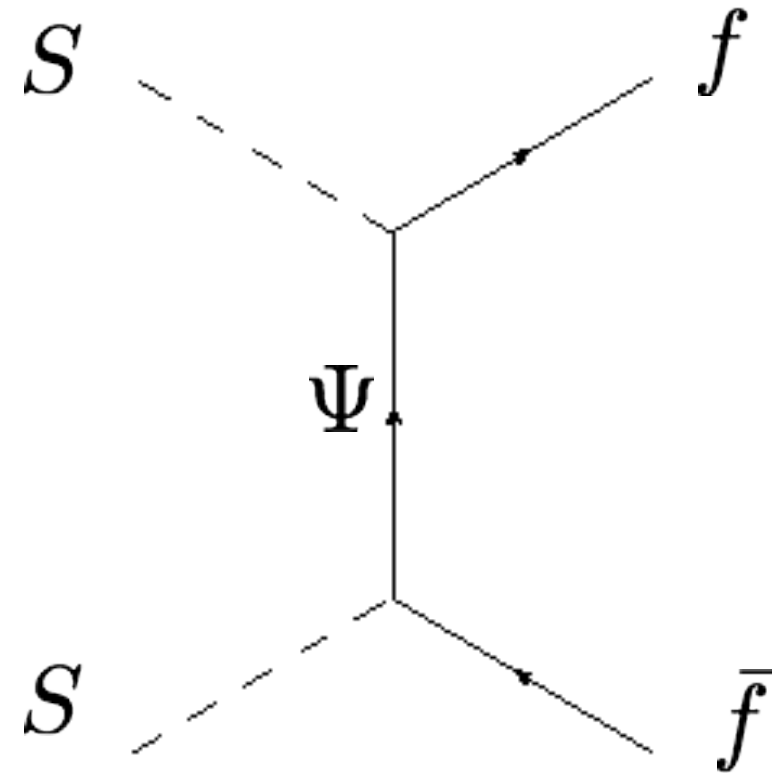


A benchmark dark matter model
with strong gamma ray spectral features

Majorana vs Real Scalar into light SM fermions



VS



p-wave



$$\sigma v(\chi\chi \rightarrow l\bar{l}) = \frac{g_l^4}{48\pi} \frac{v^2}{m_\chi^2} \frac{1+r^4}{(1+r^2)^4}$$

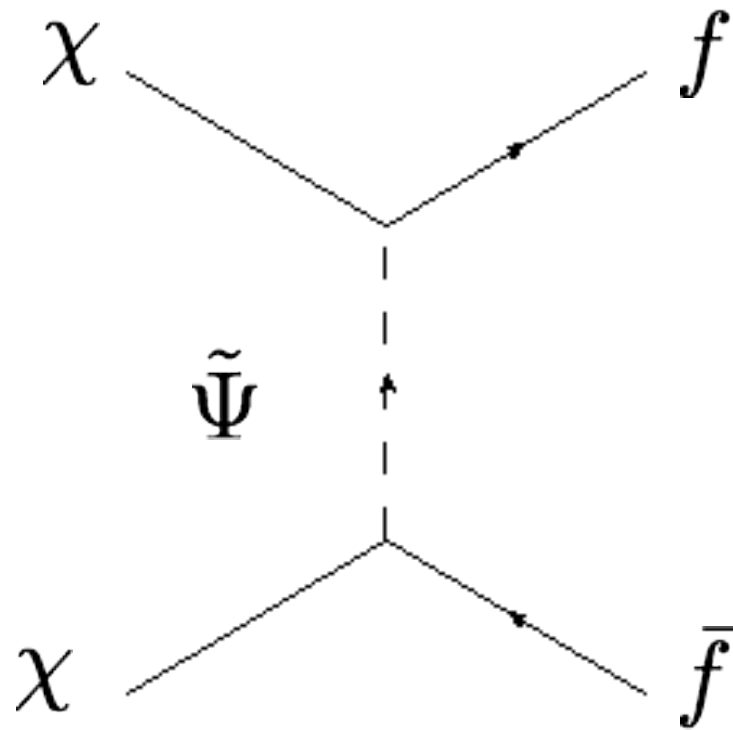
$$r = \frac{m_{\tilde{\Psi}}}{m_\chi} \geq 1$$

Goldberg

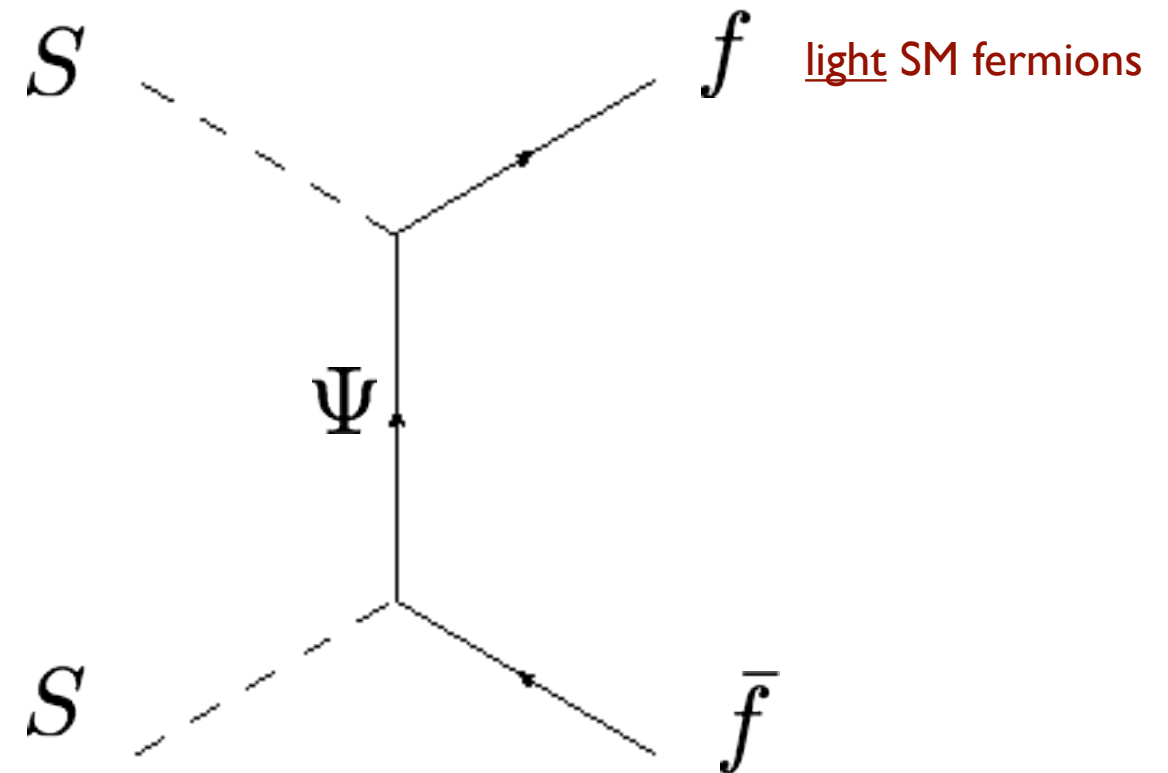
«Constraint on the Photino mass from cosmology»

Phys.Rev.Lett. 50 (1983) 1419

MAJORANA vs REAL SCALAR



VS



p-wave



$$\sigma v(\chi\chi \rightarrow l\bar{l}) = \frac{g_l^4}{48\pi} \frac{v^2}{m_\chi^2} \frac{1+r^4}{(1+r^2)^4}$$

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«Constraint on the Photino mass from cosmology»

Phys.Rev.Lett. 50 (1983) 1419

d-wave



$$\sigma v(SS \rightarrow l\bar{l}) = \frac{y_l^4}{60\pi} \frac{v^4}{m_S^2} \frac{1}{(1+r^2)^4}$$

$$r = \frac{m_\psi}{m_S} \geq 1$$

Toma, arXiv:1307.6181

Giacchino, Lopez Honorez & M.T. arXiv:1307.6480

MAJORANA vs REAL SCALAR

$$\mathcal{O} = \bar{\chi} \gamma^\mu \gamma_5 \chi \bar{\psi}_f \gamma_\mu \gamma_5 \psi_f$$

vs

$$\mathcal{O}_T = \partial_\mu S \partial_\nu S \Theta_{f_R}^{\mu\nu}$$

↑
FERMION
STRESS-ENERGY TENSOR

p-wave



$$\sigma v(\chi\chi \rightarrow l\bar{l}) = \frac{g_l^4}{48\pi} \frac{v^2}{m_\chi^2} \frac{1+r^4}{(1+r^2)^4}$$

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Toma, arXiv:1307.6181

Giacchino, Lopez Honorez & MT, arXiv:1307.6480

Consequences?

Consider first coupling to light leptons

It is simpler

It is relevant for indirect detection

I. Annihilation in early universe

$$v \sim 0.3$$

➔ $\text{DM DM} \rightarrow f \bar{f}$ more suppressed for scalar DM
than for Majorana

II. Annihilation at Galactic Centre ? $v_{\text{GC}} \sim 10^{-3}$

$\text{DM DM} \rightarrow f \bar{f}$ completely irrelevant

➔ Radiative corrections relevant ?

$$\text{DM DM} \rightarrow \gamma\gamma$$

Digammas

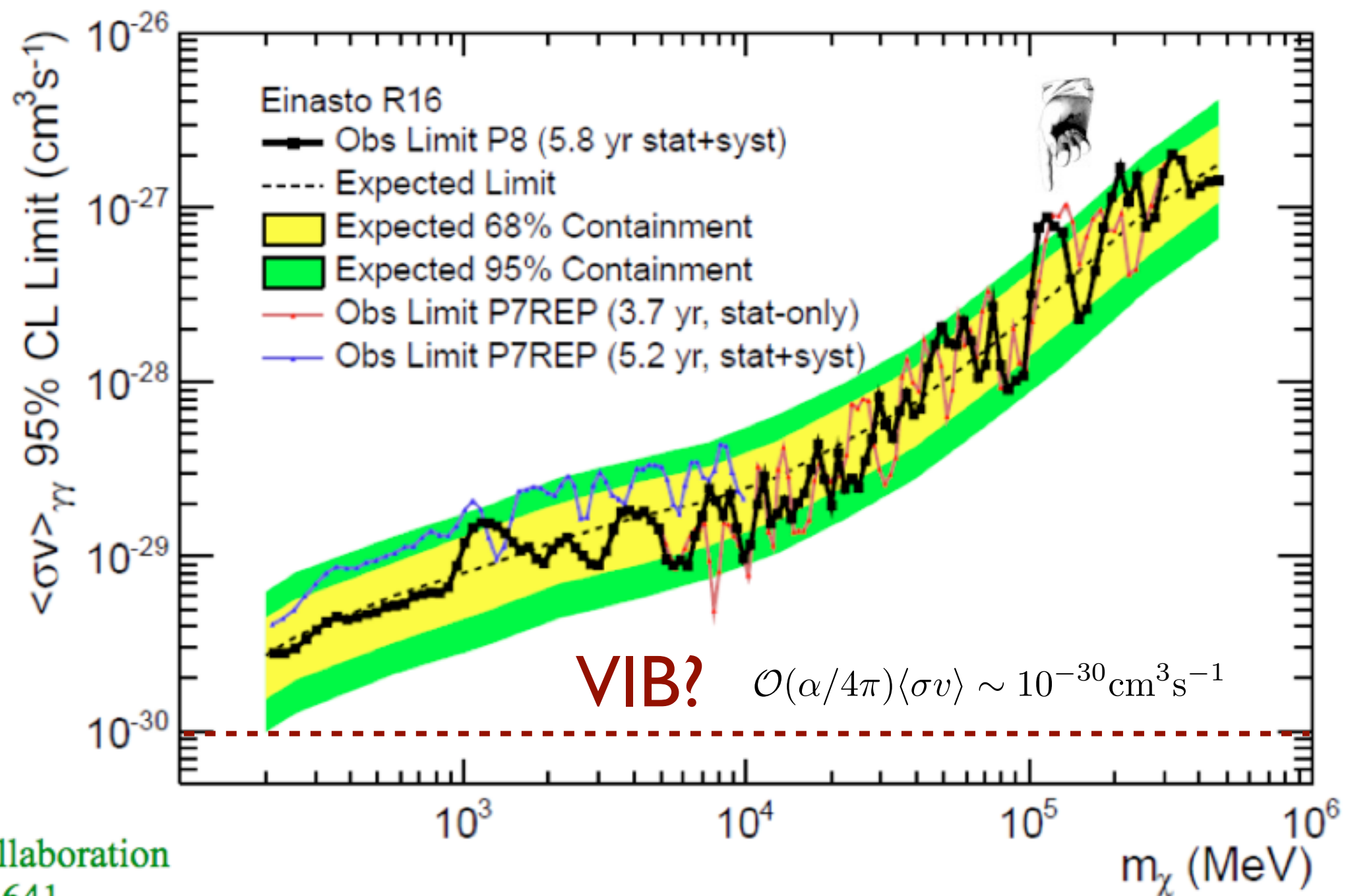
$$\text{DM DM} \rightarrow f \bar{f} \gamma$$

Bremsstrahlung

both are s-wave (velocity independent) but expected to be small...

Relic abundance

$$\langle\sigma v\rangle \approx 3 \cdot 10^{-26} \text{cm}^3 \cdot \text{s}^{-1}$$



Fermi-LAT collaboration
arXiv:1503.02641

digammas?

$$\mathcal{O}(\alpha^2/16\pi^2)\langle\sigma v\rangle \sim 10^{-32} \text{cm}^3 \text{s}^{-1}$$

DM smoking gun signatures - digammas

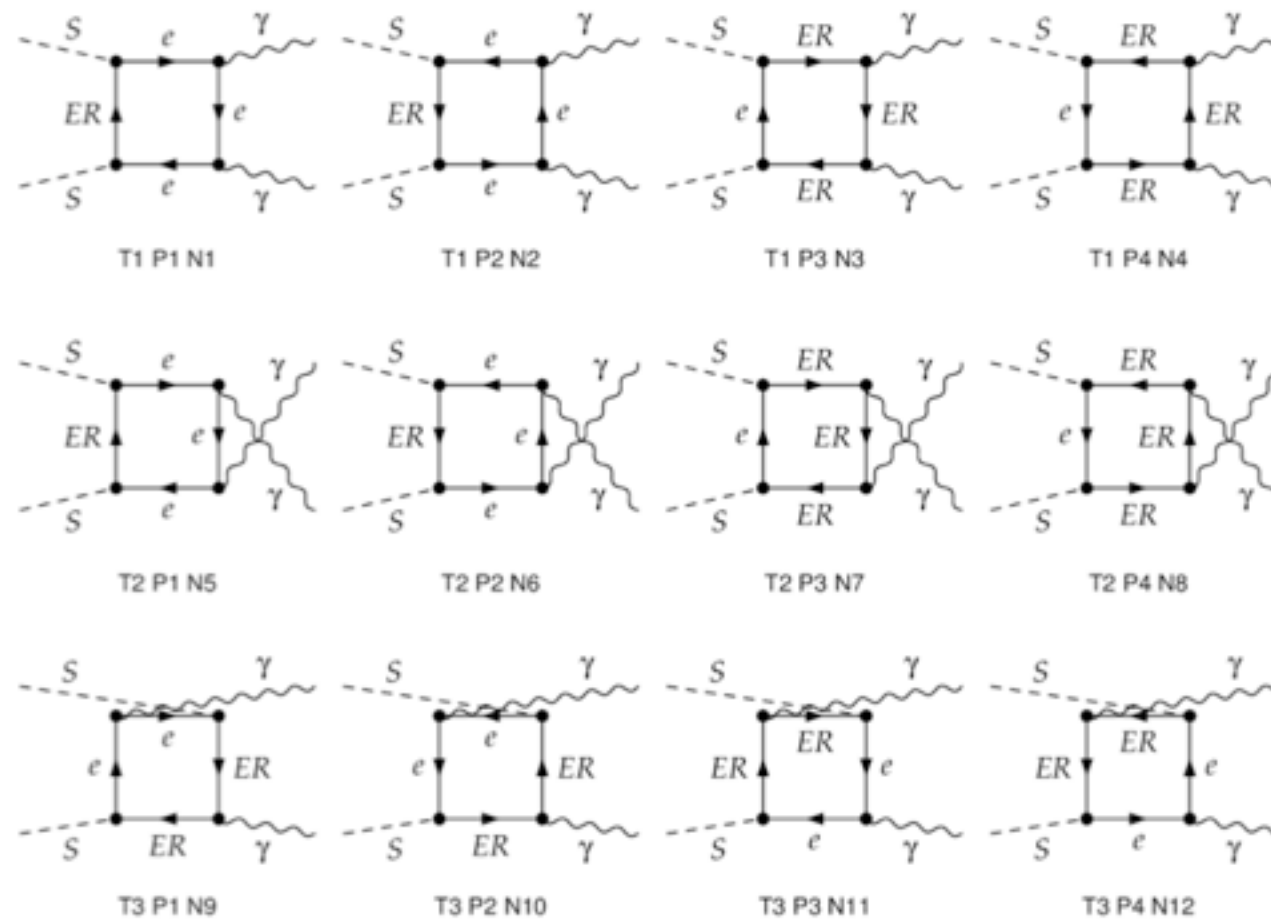
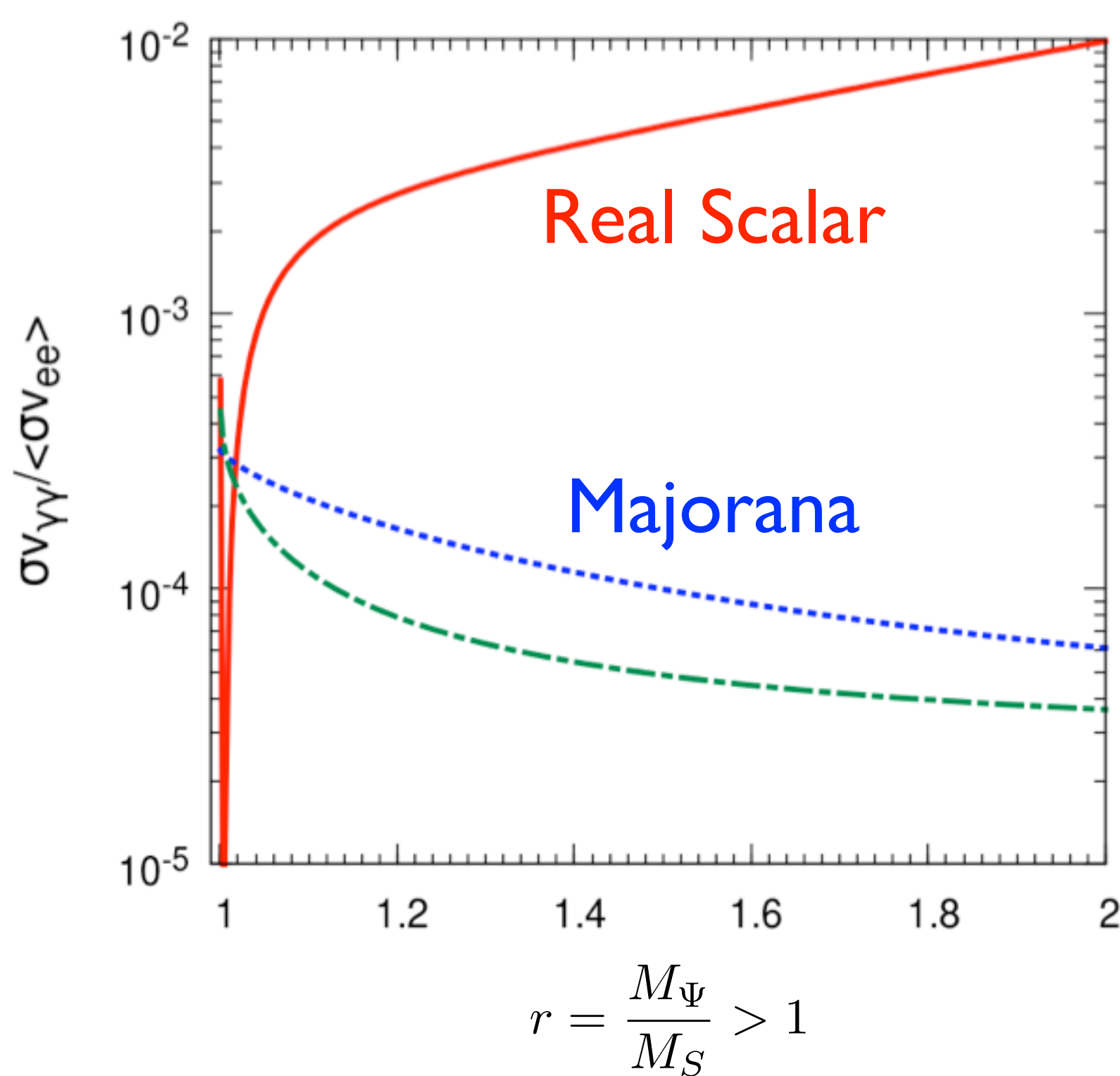


Figure 1: Box diagrams relevant for the $SS \rightarrow \gamma\gamma$ process

1. no astrophysical counterparts
2. $E_\gamma = M_{\text{DM}}$



DM smoking gun signatures - digammas



$$\sim 10^{-28} \text{cm}^3 \text{s}^{-1}$$

$\mathcal{O}(100)$ larger
than expected!

$$\sim 10^{-31} \text{cm}^3 \text{s}^{-1}$$

$$\mathcal{O}(\alpha^2/16\pi^2)\langle\sigma v\rangle$$

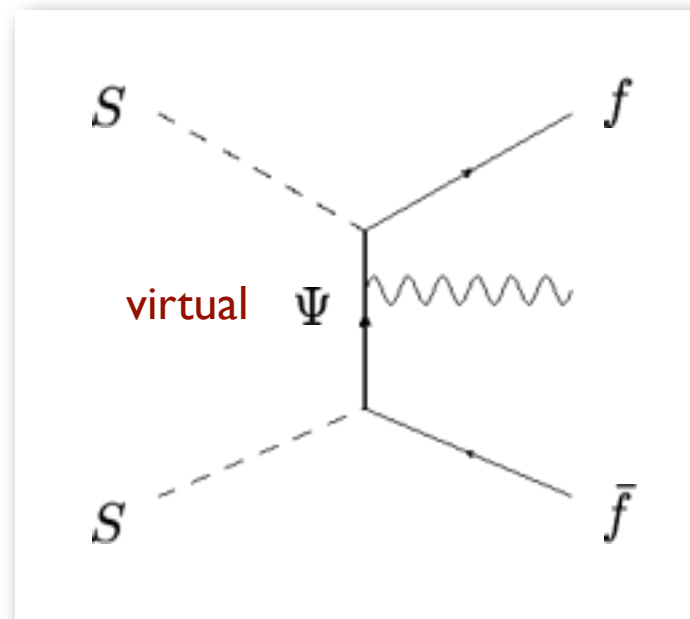
Ibarra, Toma, Totzauer & Wild
arXiv:1405.6917
Giacchino, Lopez Honorez & MT
arXiv:1405.6921

Smoking gun signatures - virtual internal Bremsstrahlung

Bergstrom (1989)

Flores, Olive & Rudaz (1989)

Bergstrom, Bringmann & Edsjo (2008)



Barger, Keung & Marfatia

arXiv:1111.4523

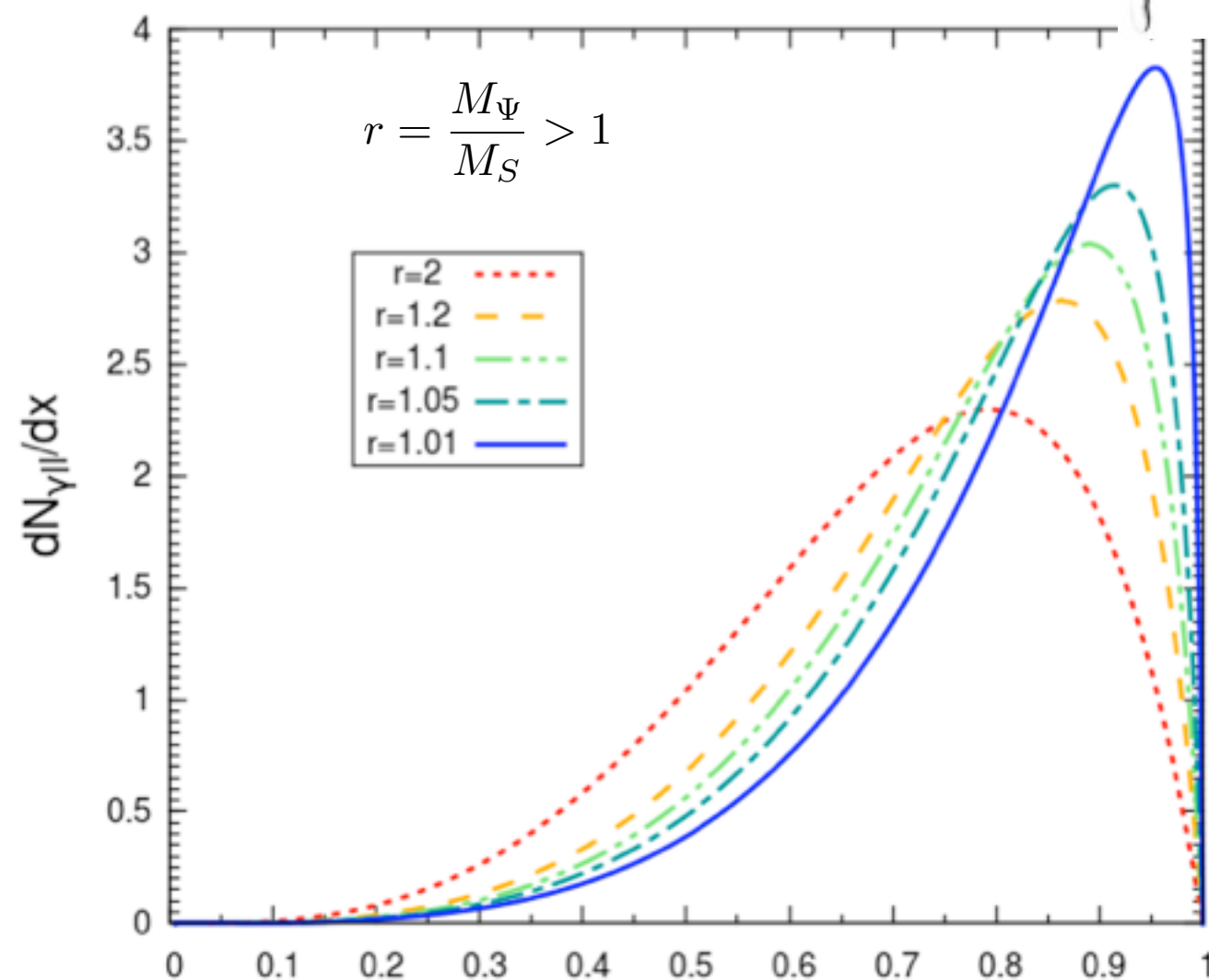
Takashi Toma

arXiv:1307.6181

Giacchino, Lopez Honorez & M.T.

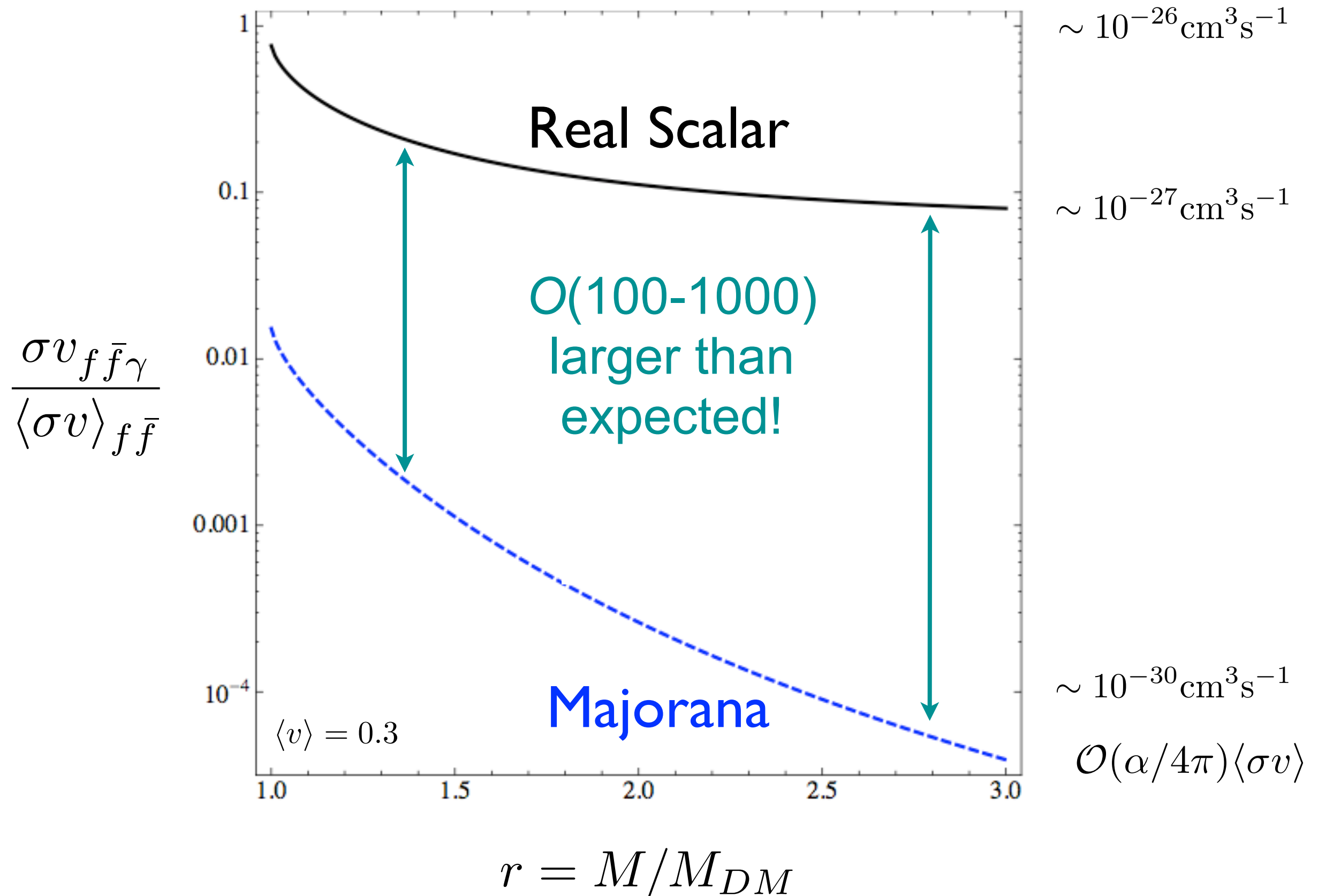
arXiv:1307.6480

$$E_\gamma \sim M_{DM}$$

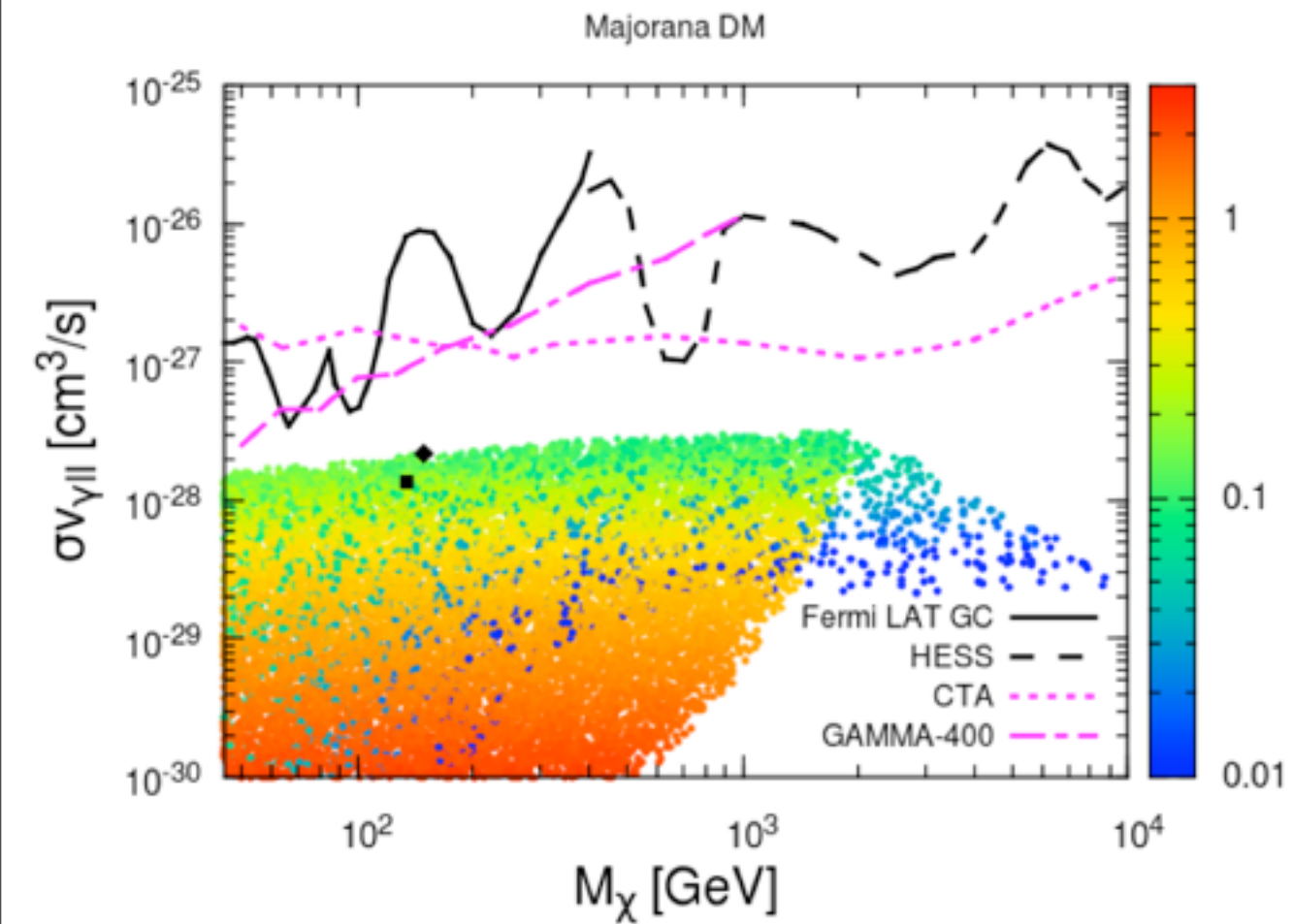


$$x = \frac{E_\gamma}{M_{DM}}$$

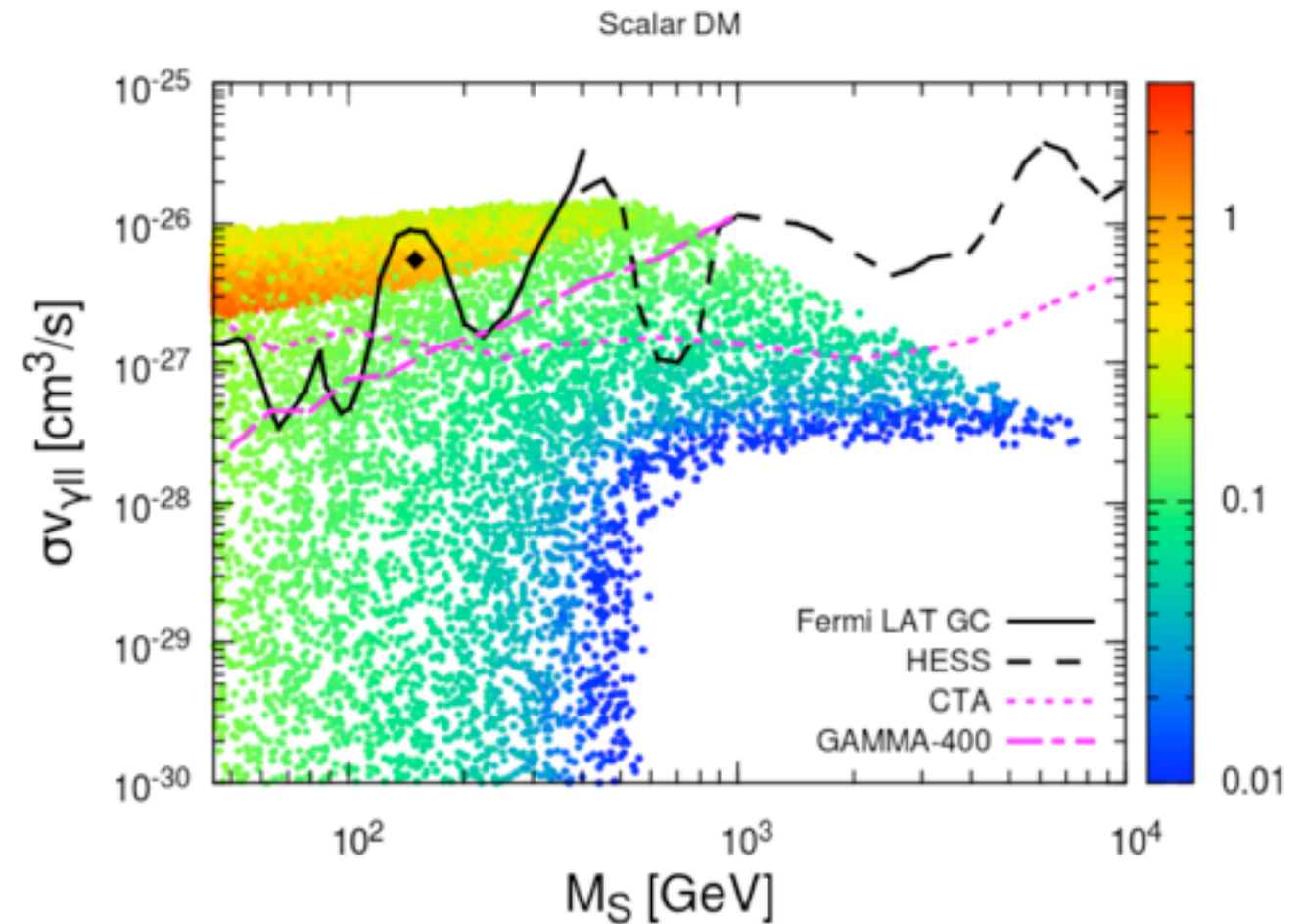
Smoking gun signatures - virtual internal Bremsstrahlung



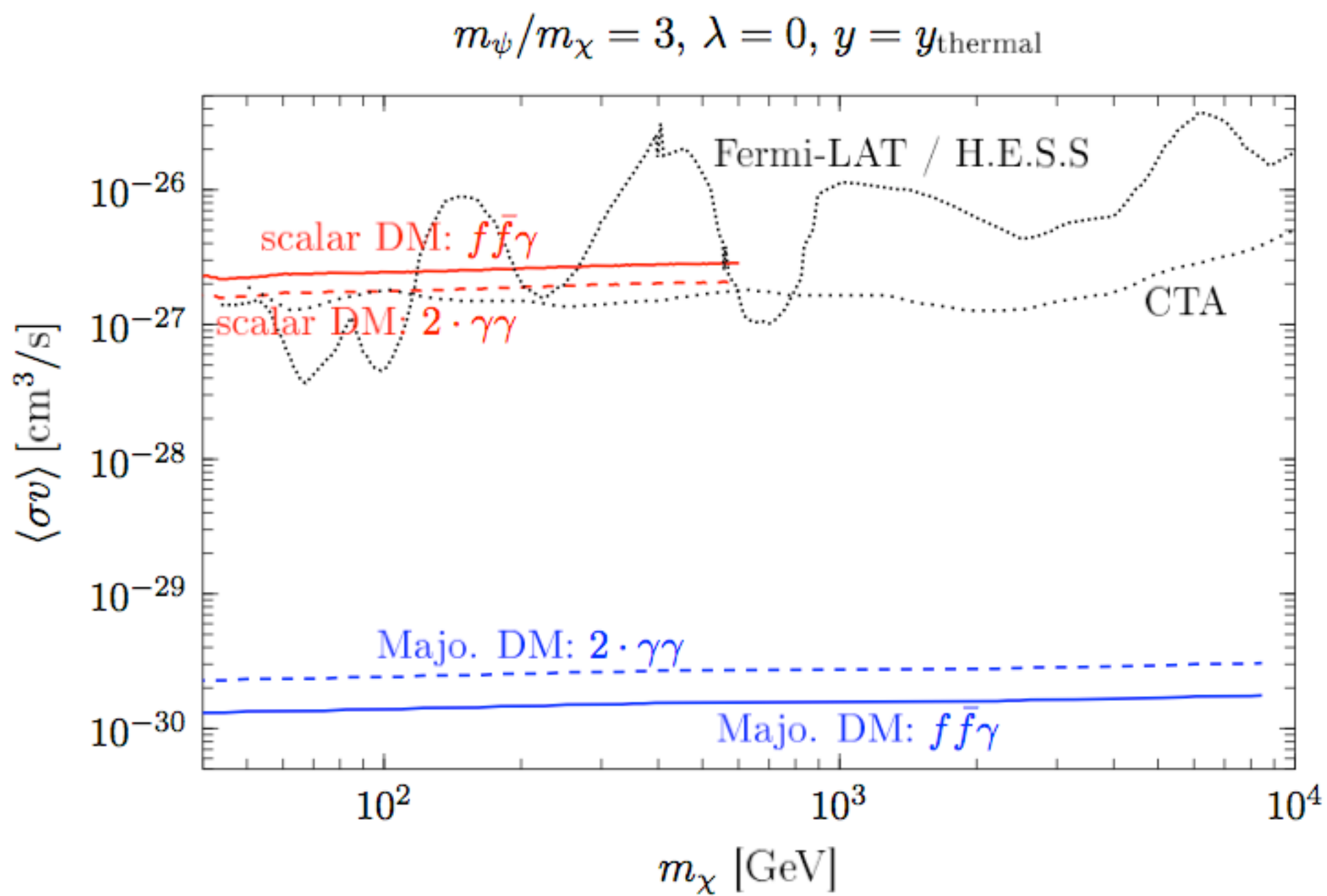
Majorana DM



Real scalar DM



Giacchino, Lopez Honorez & MT, arXiv:1307.6480
See also
Takashi Toma, arXiv:1307.6181



Gluon Bremsstrahlung?

$$\mathcal{L} \supset y_l S \bar{\Psi} l_R + h.c. \quad \rightarrow \quad \mathcal{L} \supset y_q S \bar{\Psi} q_R + h.c.$$

$$\frac{\langle \sigma v \rangle_{g\bar{q}q}}{\langle \sigma v \rangle_{\gamma\bar{q}q}} = \frac{N_c^2 - 1}{2N_c} \frac{\alpha_s}{Q^2 \alpha} \quad \begin{array}{l} \sim 40 \text{ (up-like quarks)} \\ \sim 150 \text{ (down-like quarks)} \end{array}$$

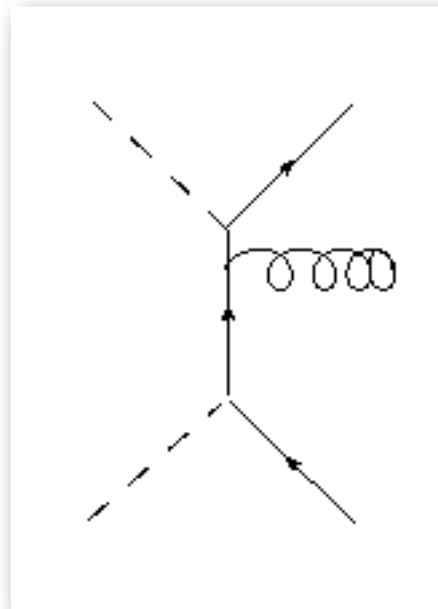
$$\langle \sigma v \rangle_{q\bar{q}} \ll \langle \sigma v \rangle_{q\bar{q}g}$$

EVEN IN EARLY UNIVERSE

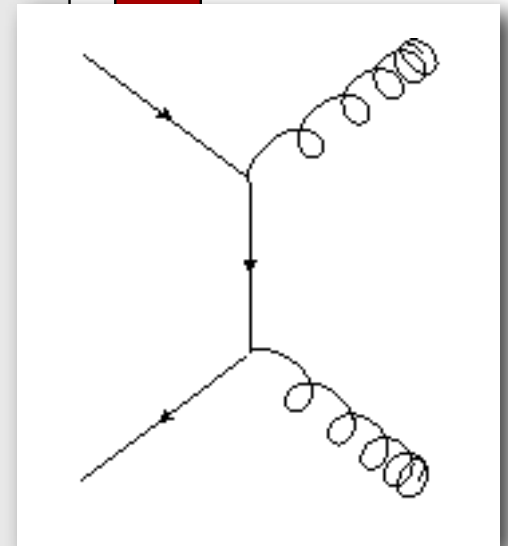
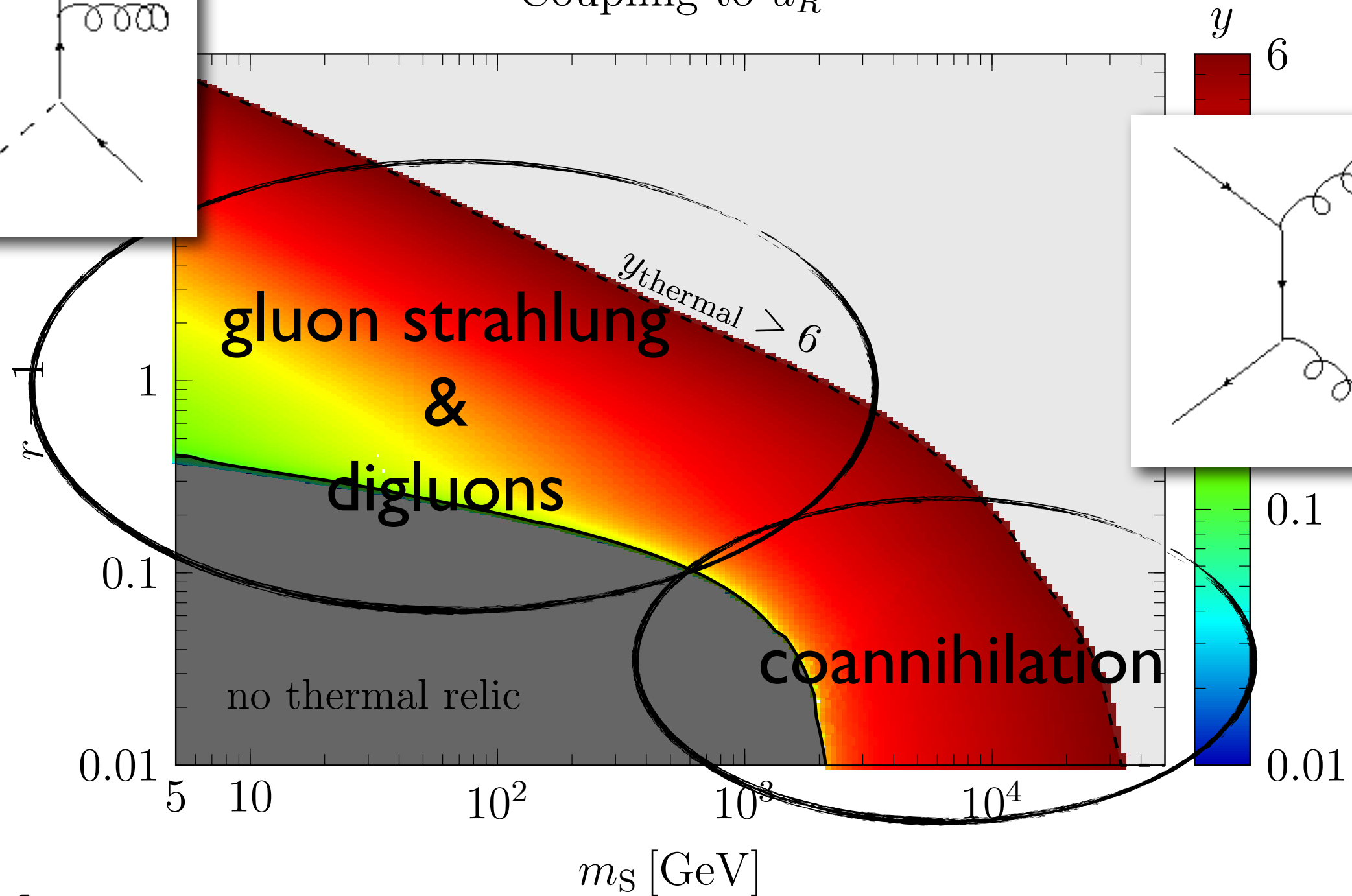


RELIC ABUNDANCE FROM
GLUON BREMSSTRAHLUNG
AND/OR DI-GLUONS!!!

THERMAL CANDIDATES



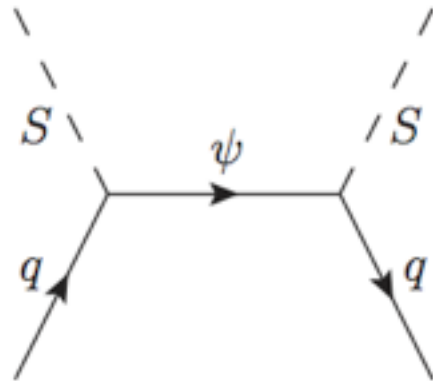
Coupling to u_R



$$r = \frac{M_\Psi}{M_S} > 1$$

Giacchino, Ibarra, Lopez Honorez, M.T. & Wild, arXiv:1511.04452

DIRECT DETECTION

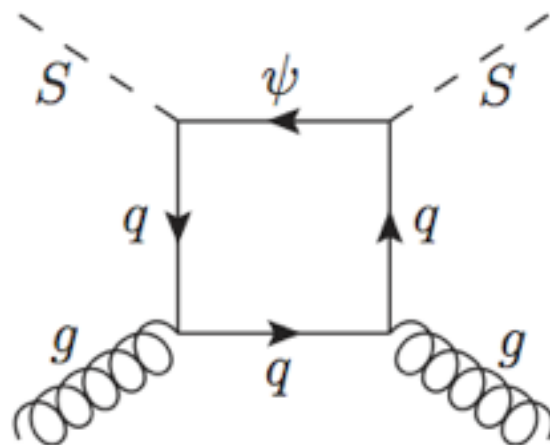


$$\mathcal{L}_q = C_S^q m_q S^2 \bar{q} q + C_T^q (\partial_\mu S)(\partial_\nu S) \mathcal{O}_{q, \text{twist-2}}^{\mu\nu}$$

$$\mathcal{O}_{q, \text{twist-2}}^{\mu\nu} \equiv \frac{i}{2} \left(\bar{q} \gamma^\mu \partial^\nu q + \bar{q} \gamma^\nu \partial^\mu q - \frac{g^{\mu\nu}}{2} \bar{q} \not{\partial} q \right)$$

Drees & Nojiri (Majorana case, '93)

Giacchino, Ibarra, Lopez Honorez, MT & Wild '15



$$\mathcal{L}_g = C_S^g \frac{\alpha_S}{\pi} S^2 G^{\mu\nu} G_{\mu\nu}$$

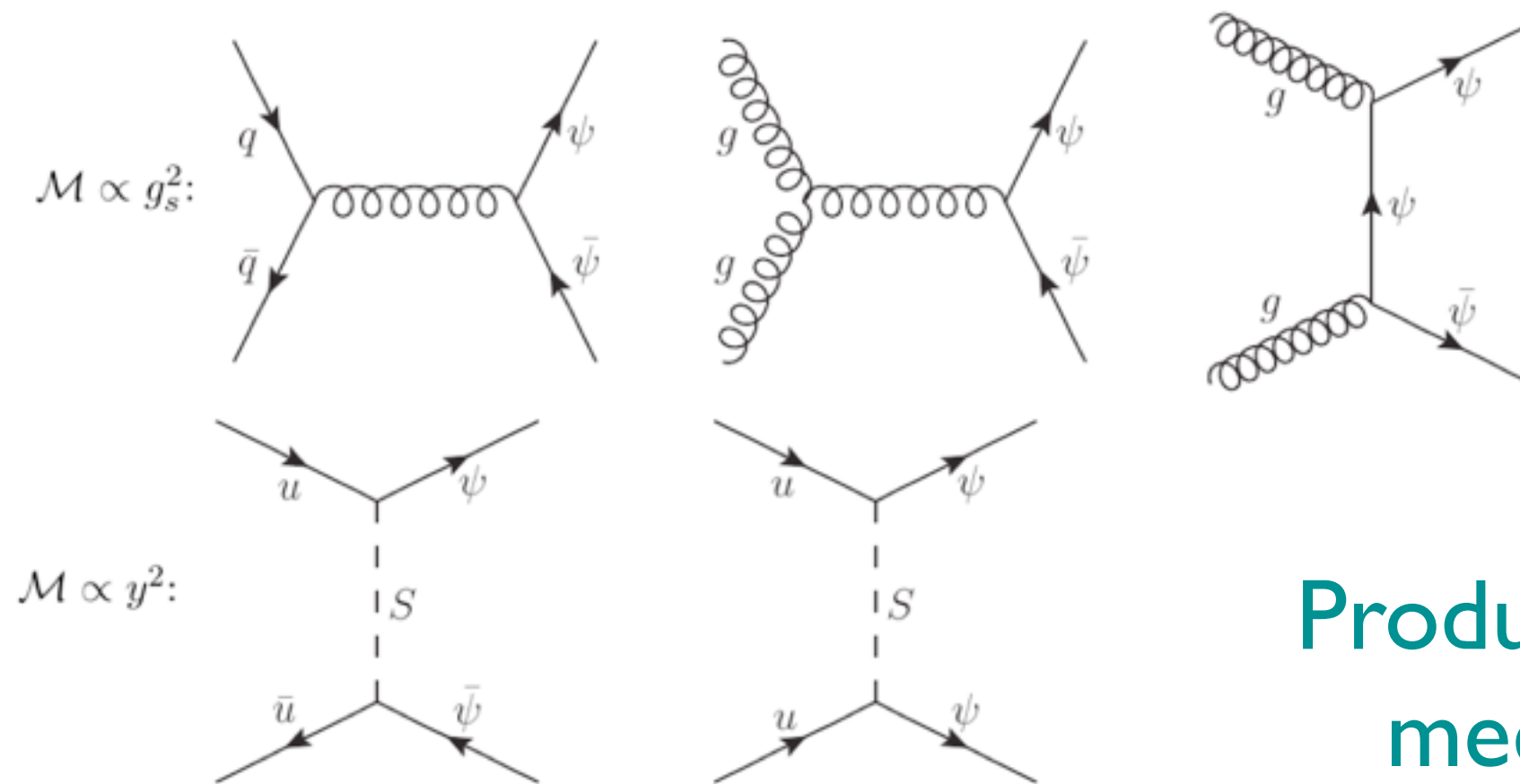


Hisano, Nagai & Nagata, arXiv:1502.02244

Drees & Nojiri (Majorana case, '93)

$$\frac{f_N}{m_N} = C_S^q f_{T_q}^{(N)} + \frac{3}{4} C_T^q m_S^2 (q^{(N)}(2) + \bar{q}^{(N)}(2)) - \frac{8}{9} C_S^g f_{T_G}^{(N)}$$

CONSTRAINTS FROM LHC

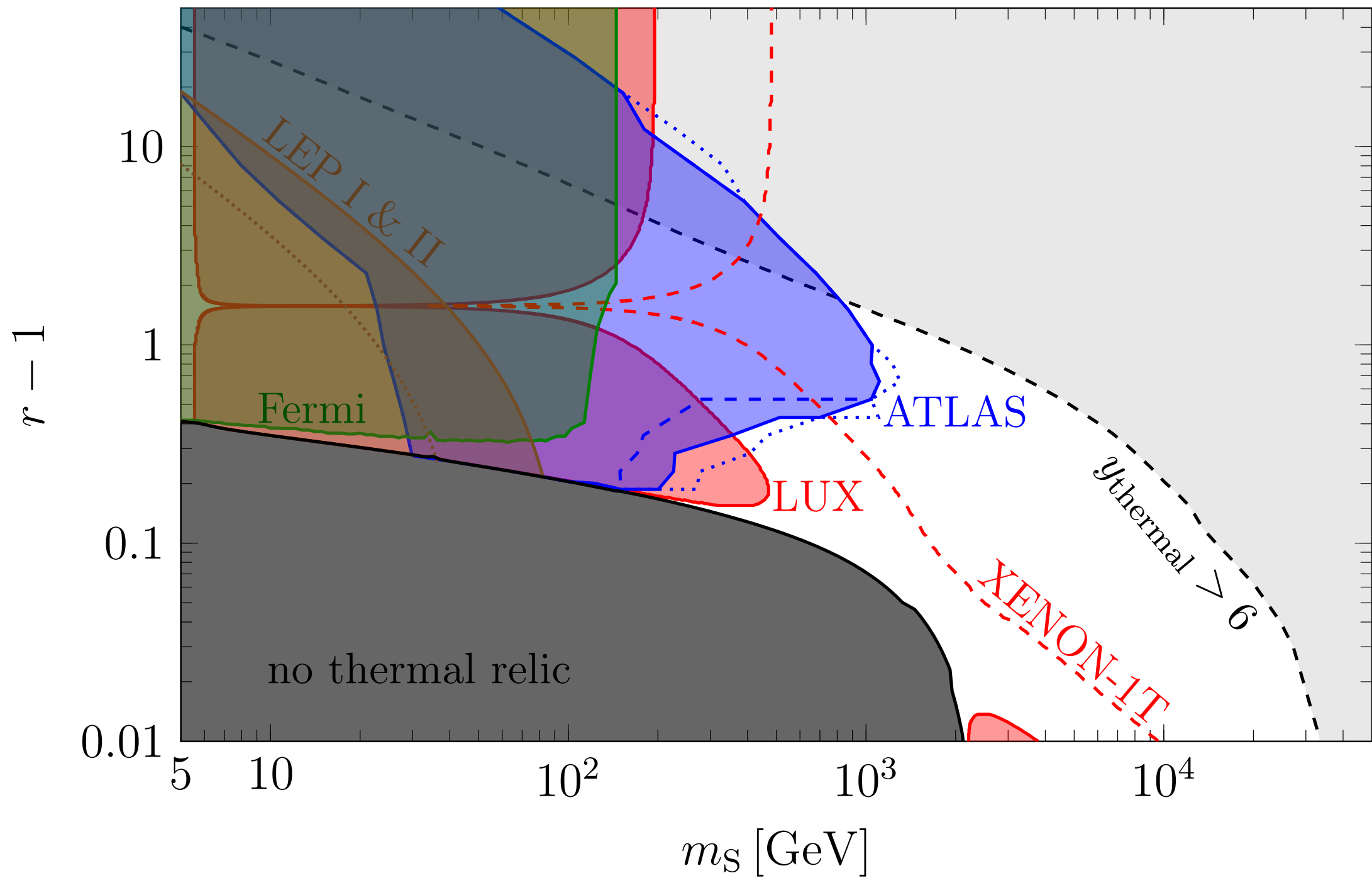


Production of colored mediator @ LHC

Signal = n jets + missing E_T

Small r: extra jets alleviate softness
Large r: extra jets improve S/B

Coupling to u_R



II. MDM SCALAR 7-PLET



A benchmark for multi-TeV dark matter

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} (|D_\mu \chi|^2 - M^2 |\chi|^2)$$

$$\chi = \begin{pmatrix} \text{DM}^{3+} \\ \text{DM}^{2+} \\ \text{DM}^+ \\ \text{DM} \\ -\text{DM}^- \\ \text{DM}^{2-} \\ -\text{DM}^{3-} \end{pmatrix}$$

Mass splitting
through loop corrections

$$M_Q - M_{Q'} \approx (Q^2 - Q'^2) \Delta$$

$$\Delta \equiv \alpha_2 \sin^2 \left(\frac{\theta_W}{2} \right) M_W \approx 166 \text{ MeV}$$

II. MDM SCALAR 7-PLET



A benchmark for multi-TeV dark matter

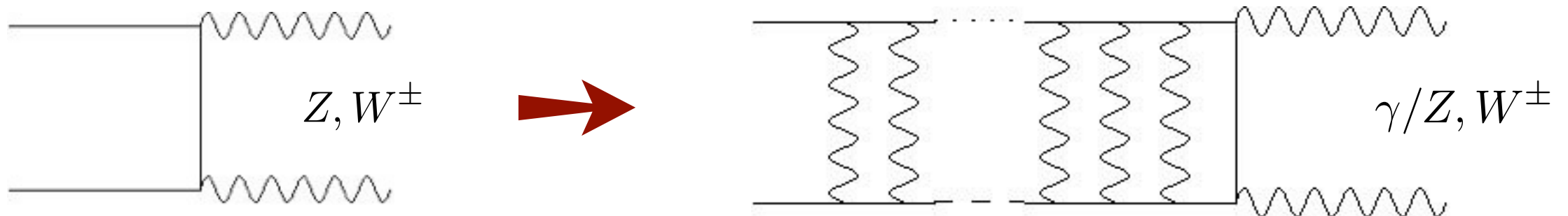
$$M_7 \sim 25 \text{ TeV}$$

Cirelli, Strumia & Tamburini (2007)

1. Many co-annihilation channels

2. Sommerfeld effects $M_7 \gg M_{W/Z}$

} σ_{eff}

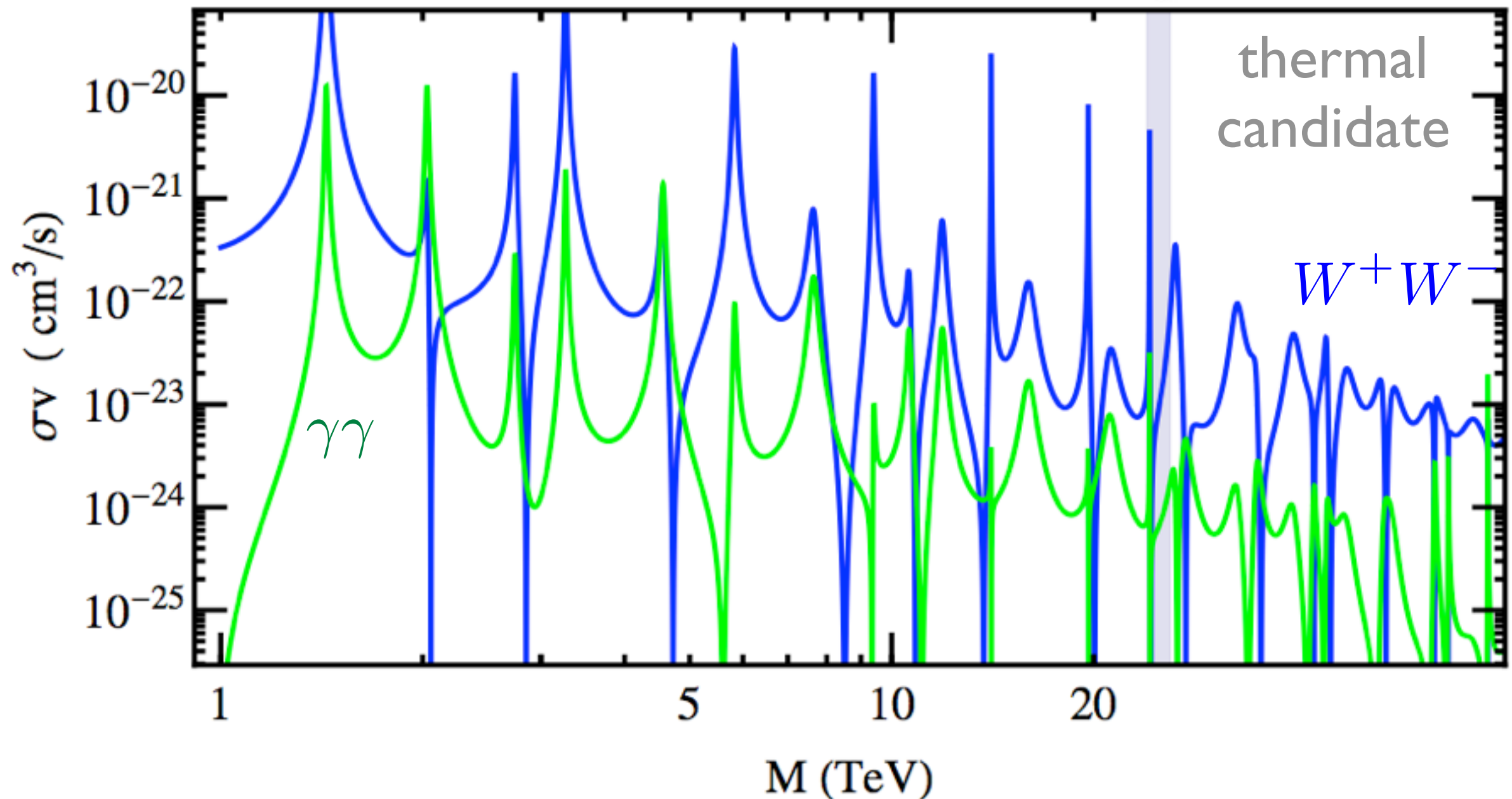


Sommerfeld leads to peaks and dips in the annihilation cross sections

Strumia, Cirelli & Tambirini (2007)

$$v_{GC} \sim 10^{-3}$$

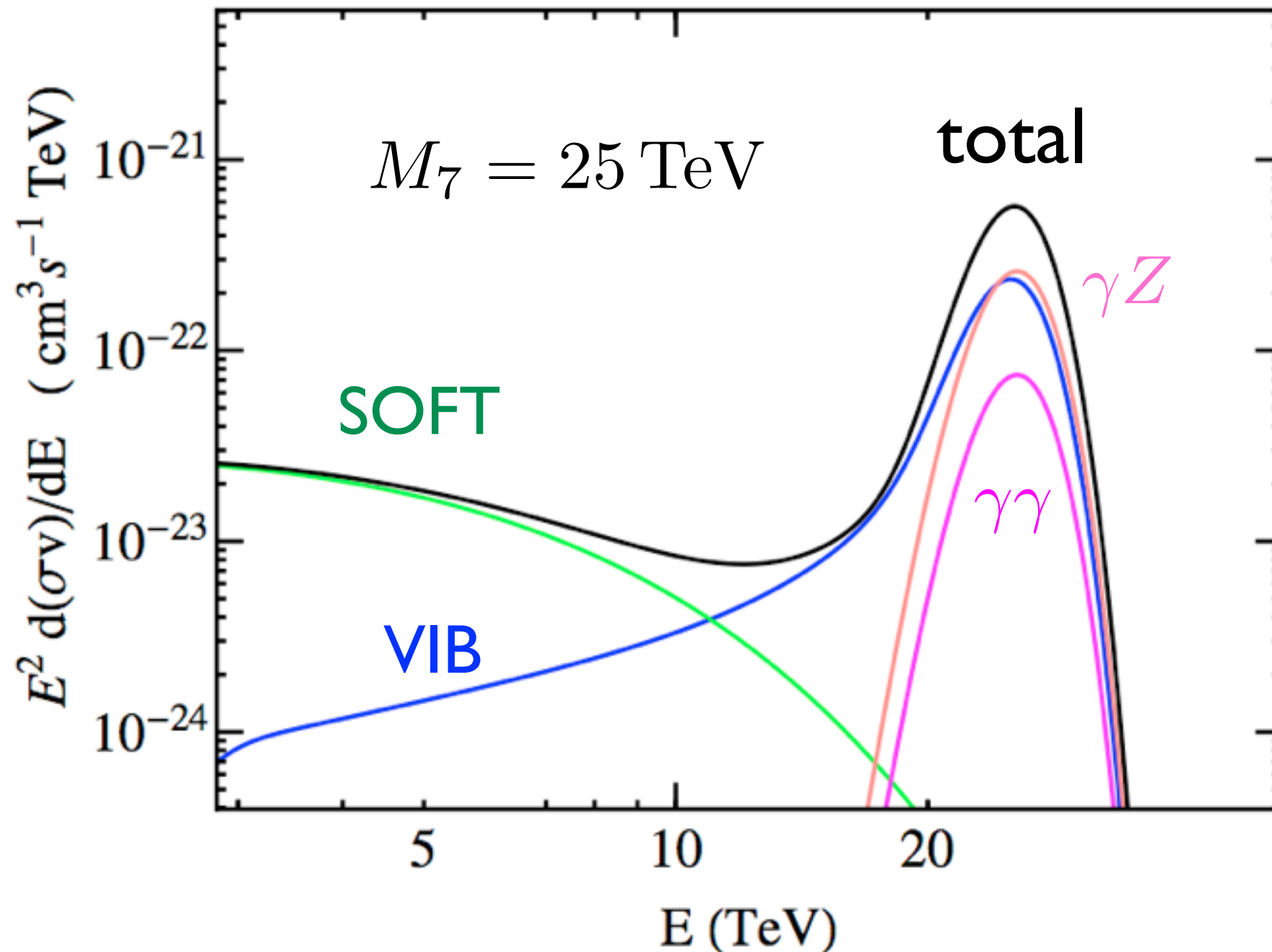
Scalar 7-plet



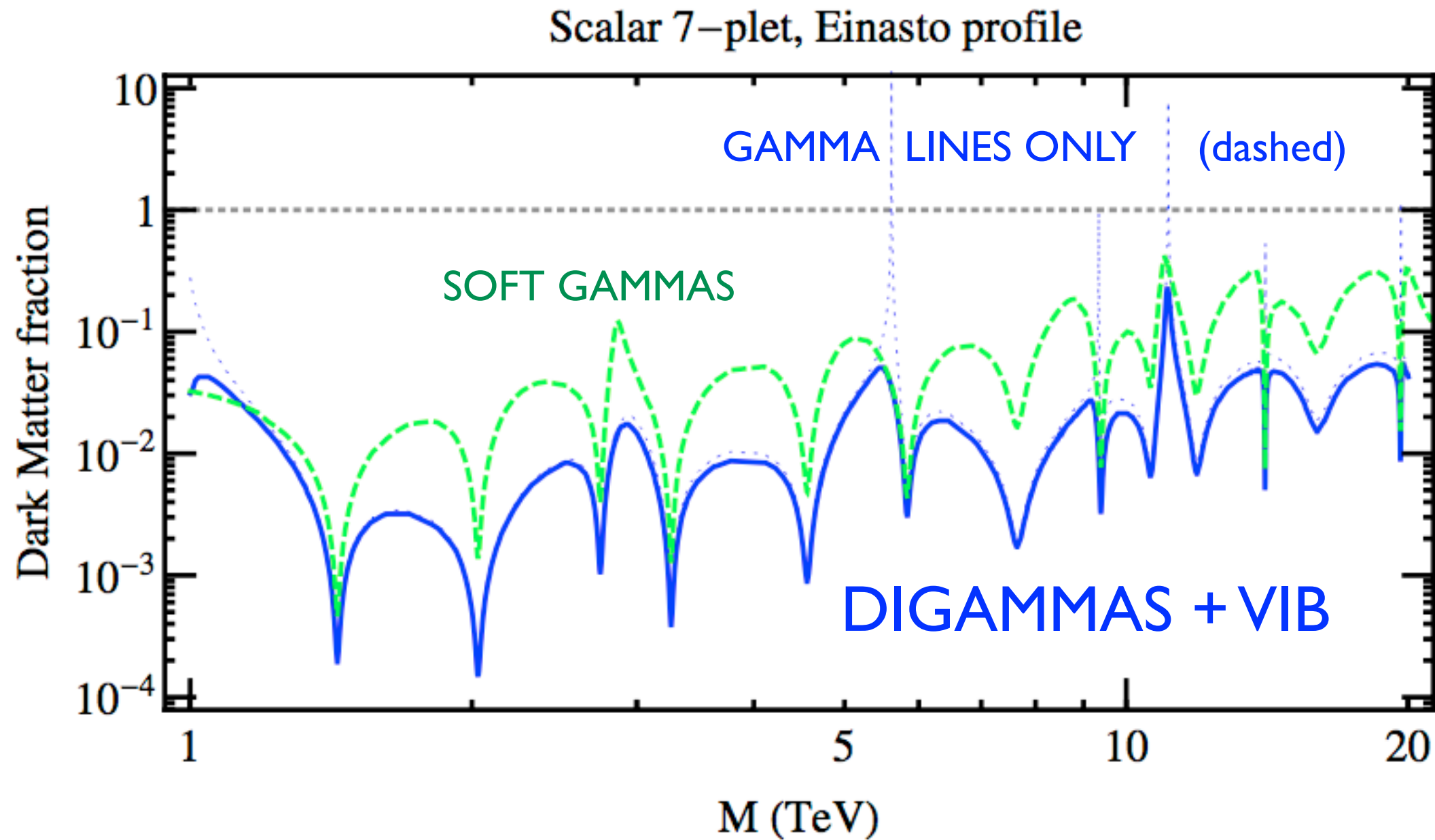
Garcia-Cely, Ibarra, Lamperstorfer & MT, arXiv:1507.05536

See also Cirelli, Hambye, Panci, Sala & Taoso, arXiv:1507.05519 (fermionic 5-plet)

7-plet components are **nearly degenerate**
so **VIB** is also important

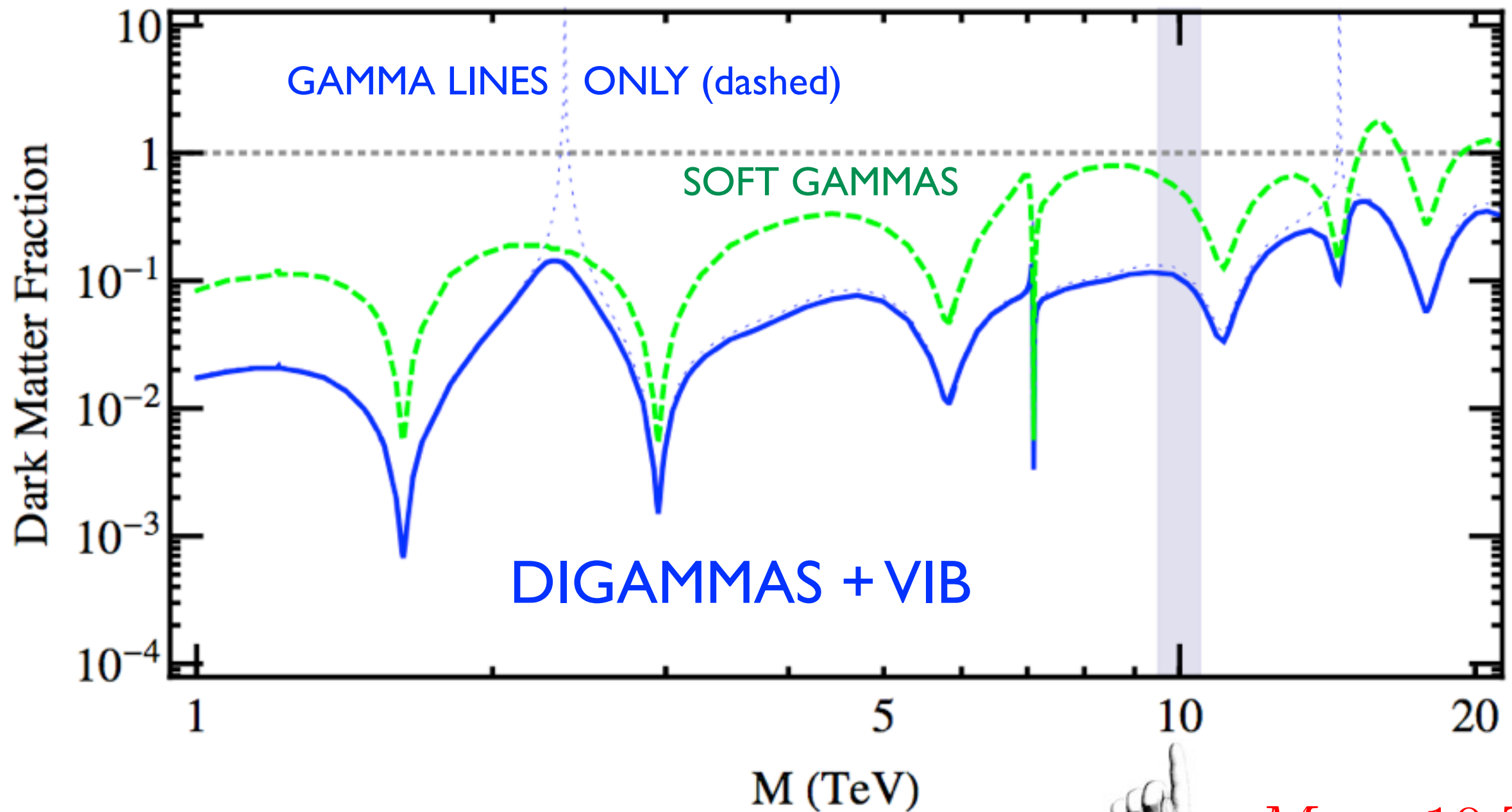


H.E.S.S. LIMITS



H.E.S.S. LIMITS

Fermionic 5-plet, Einasto profile

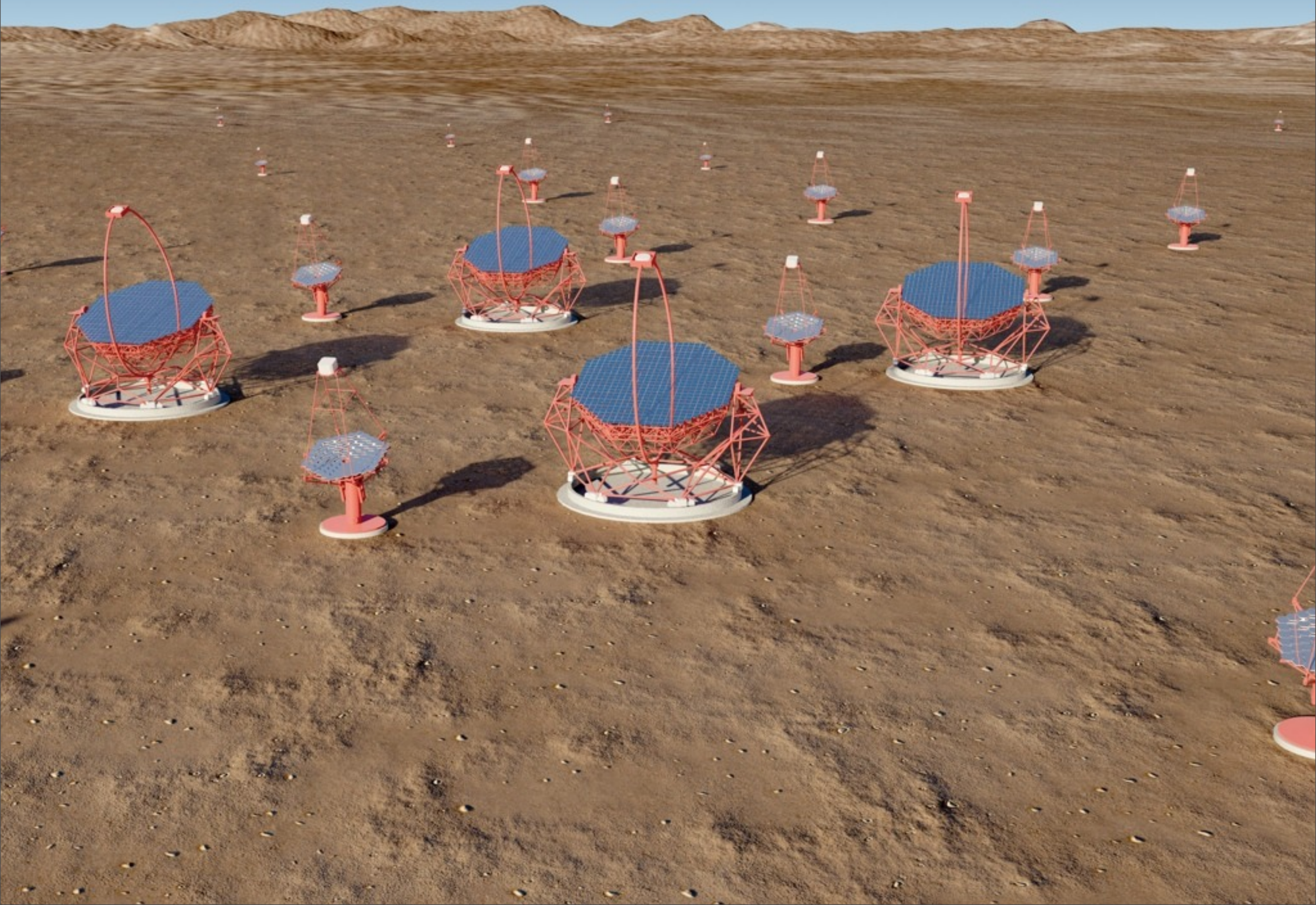


$M_5 \sim 10 \text{ TeV}$

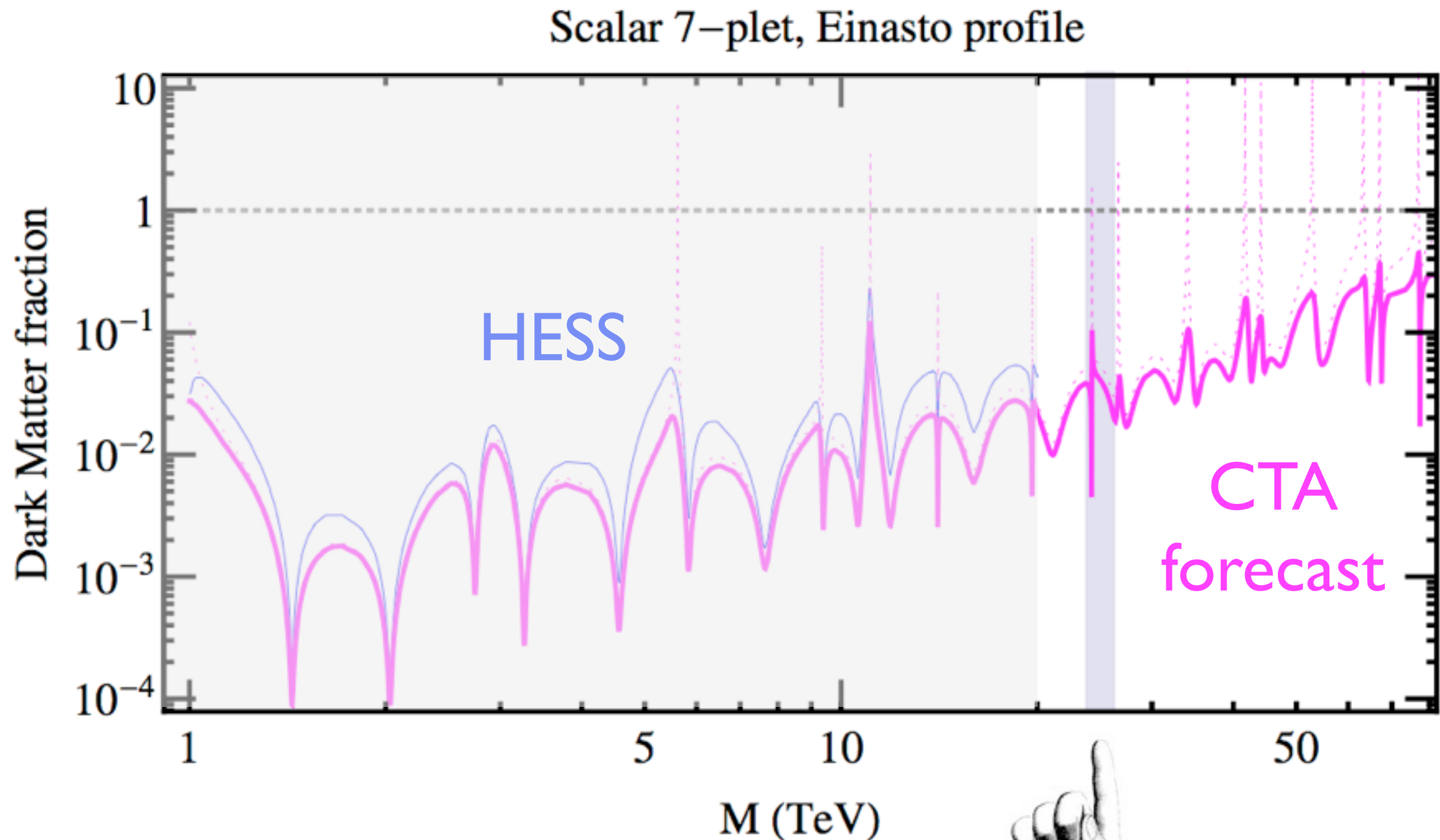
Thermal fermionic 5-plet candidate
constrained by H.E.S.S.

Garcia-Cely, Ibarra, Lamperstorfer & MT, arXiv:1507.05536
Cirelli, Hambye, Panci, Sala & Taoso, arXiv:1507.05519

CERENKOV TELESCOPE ARRAY



H.E.S.S. LIMITS vs CTA FORECAST



Thermal scalar 7-plet needs CTA
(a 200 million € project)

$$M_7 \sim 25 \text{ TeV}$$

SWIMP

Super Weakly Interacting Massive Particle (Laura Covi's talk)

or

Scalar Weakly Interacting Massive Particle ;-)



SWIMP the Simple

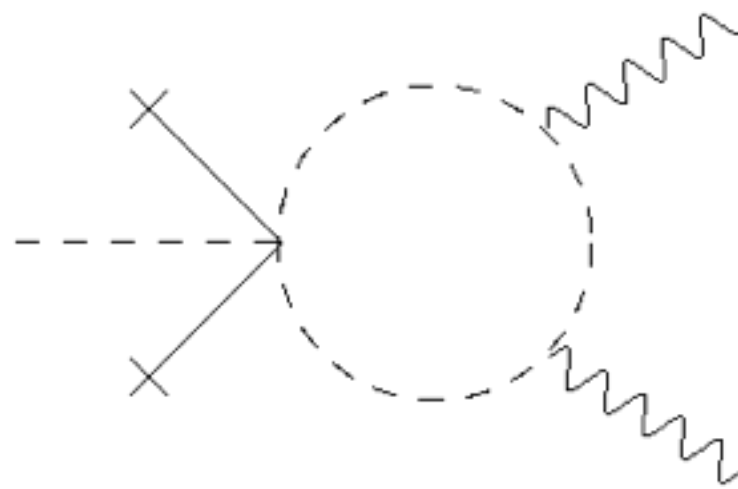
SWIMP

To stay true and loyal to once's friends even though times might be rough

Backup slides

II. MDM SCALAR 7-PLET

$$7 \otimes 7 \otimes 7 = \dots \oplus 3_S \oplus \dots \quad \rightarrow \quad \mathcal{O}_5 = \frac{1}{\Lambda} (\chi_7^3)^a (\tilde{H}^\dagger \tau^a H)$$



$$\Lambda \sim 10^{15} \text{ GeV}$$

$$M_\chi \sim \text{TeV}$$

$$\rightarrow \tau_\chi \sim 10^{-8} \text{ s}$$

$$\chi \xrightarrow{Z_2} -\chi$$

I st: MAJORANA

I. S-WAVE ANNIHILATION
IS MASS SUPPRESSED



$$\sigma v \propto y_f^4 \frac{m_f^2}{M_\chi^4}$$

Goldberg
«Constraint on the Photino mass from
cosmology»
Phys.Rev.Lett. 50 (1983) 1419

S-WAVE INITIAL STATE

$$\chi \xrightarrow{\quad \rightarrow \quad} \xleftarrow{\quad \leftarrow \quad} \chi$$

$$^{2S+1}L_J(J^{PC}) = {}^1S_0(0^{-+})$$

$$|S=0\rangle = \frac{1}{2} (|\downarrow\rangle|\uparrow\rangle - |\uparrow\rangle|\downarrow\rangle)$$

FINAL STATE

$$f_R \xleftarrow{\quad \leftarrow \quad} \xleftarrow{\quad \leftarrow \quad} \times \xrightarrow{\quad \rightarrow \quad} \bar{f}_L$$

chiral coupling!

$$\bar{\psi}_f \gamma_5 \psi_f$$

$$\mathcal{O}_{\text{s-wave}} = \cancel{m_f} \bar{\chi} \gamma_5 \chi \bar{\psi}_f \gamma_5 \psi_f$$

I st: MAJORANA



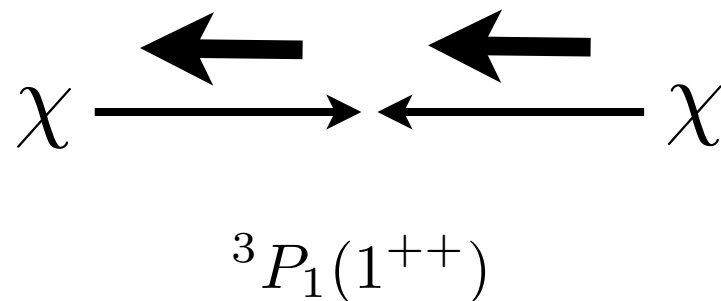
II. P-WAVE IN CHIRAL LIMIT



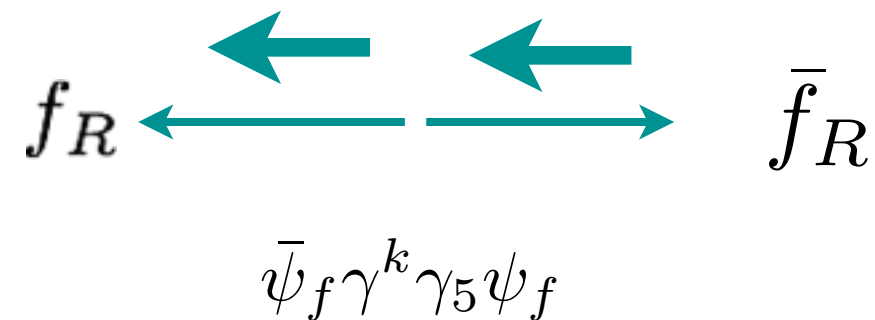
$$\sigma v(\chi\chi \rightarrow l\bar{l}) = \frac{g_l^4}{48\pi} \frac{v^2}{m_\chi^2} \frac{1+r^4}{(1+r^2)^4}$$

$$r = \frac{m_{\tilde{l}}}{m_\chi} \geq 1$$

P-WAVE INITIAL STATE



FINAL STATE



$$\mathcal{O} = \bar{\chi} \gamma^\mu \gamma_5 \chi \bar{\psi}_f \gamma_\mu \gamma_5 \psi_f$$

Goldberg
«Constraint on the Photino mass from
cosmology»
Phys.Rev.Lett. 50 (1983) 1419

2nd: REAL SCALAR



D-WAVE IN CHIRAL LIMIT



$$\sigma v(SS \rightarrow l\bar{l}) = \frac{y_l^4}{60\pi} \frac{v^4}{m_S^2} \frac{1}{(1+r^2)^4}$$

$$r = \frac{m_\psi}{m_S} \geq 1$$

Rem: I don't know of any other instance

Takashi Toma
arXiv:1307.6181
Giacchino, Lopez Honorez & M.T. arXiv:1307.6480

WHY D-WAVE SUPPRESSION?

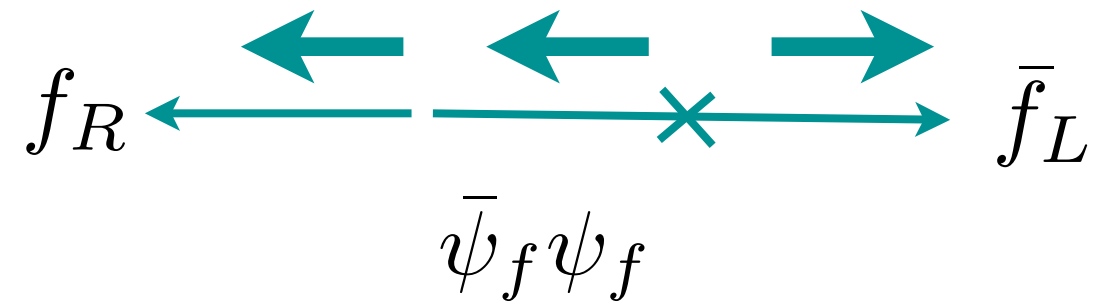
S-WAVE INITIAL STATE

$$S \longrightarrow \longleftarrow S$$

$$^1S_0(0^{++})$$

chirally suppressed

FINAL STATE



$$f_R \longleftarrow \longleftarrow \text{X} \longrightarrow \longrightarrow \bar{f}_L$$

$$\bar{\psi}_f \psi_f$$



$$\mathcal{O}_S = m_f S^2 \bar{\psi}_f \psi_f$$

WHY D-WAVE SUPPRESSION?

S-WAVE INITIAL STATE

$$S \longrightarrow \longleftarrow S$$

$$^1S_0(0^{++})$$

chirally suppressed



$$\mathcal{O}_S = m_f S^2 \bar{\psi}_f \psi_f$$

FINAL STATE

$$f_R \longleftarrow \longleftarrow \times \longrightarrow \bar{f}_L$$

$$\bar{\psi}_f \psi_f$$

P-WAVE INITIAL STATE

pseudoscalar

$$P \longrightarrow \longleftarrow S$$

scalar

$$^1P_1(1^{--})$$

a complex scalar could
have p-wave annihilation



$$\mathcal{O} = P \overleftrightarrow{\partial}_\mu S \bar{\psi}_f \gamma^\mu \psi_f$$

FINAL STATE

$$f_R \longleftarrow \longleftarrow \bar{f}_R$$

$$\bar{\psi}_f \gamma^k \psi_f$$

WHY D-WAVE SUPPRESSION?

S-WAVE INITIAL STATE

$$S \longrightarrow \longleftarrow S$$

$$^1S_0(0^{++})$$

chirally suppressed



$$\mathcal{O}_S = m_f S^2 \bar{\psi}_f \psi_f$$

FINAL STATE

$$f_R \longleftarrow \longleftarrow \times \longrightarrow \bar{f}_L$$

$$\bar{\psi}_f \psi_f$$

D-WAVE INITIAL STATE

scalar

$$S \longrightarrow \longleftarrow S$$

scalar

$$^1D_2(2^{++})$$

d-wave
in chiral limit



$$\mathcal{O}_T = \partial_\mu S \partial_\nu S \Theta_{f_R}^{\mu\nu}$$

FERMION
STRESS-ENERGY TENSOR

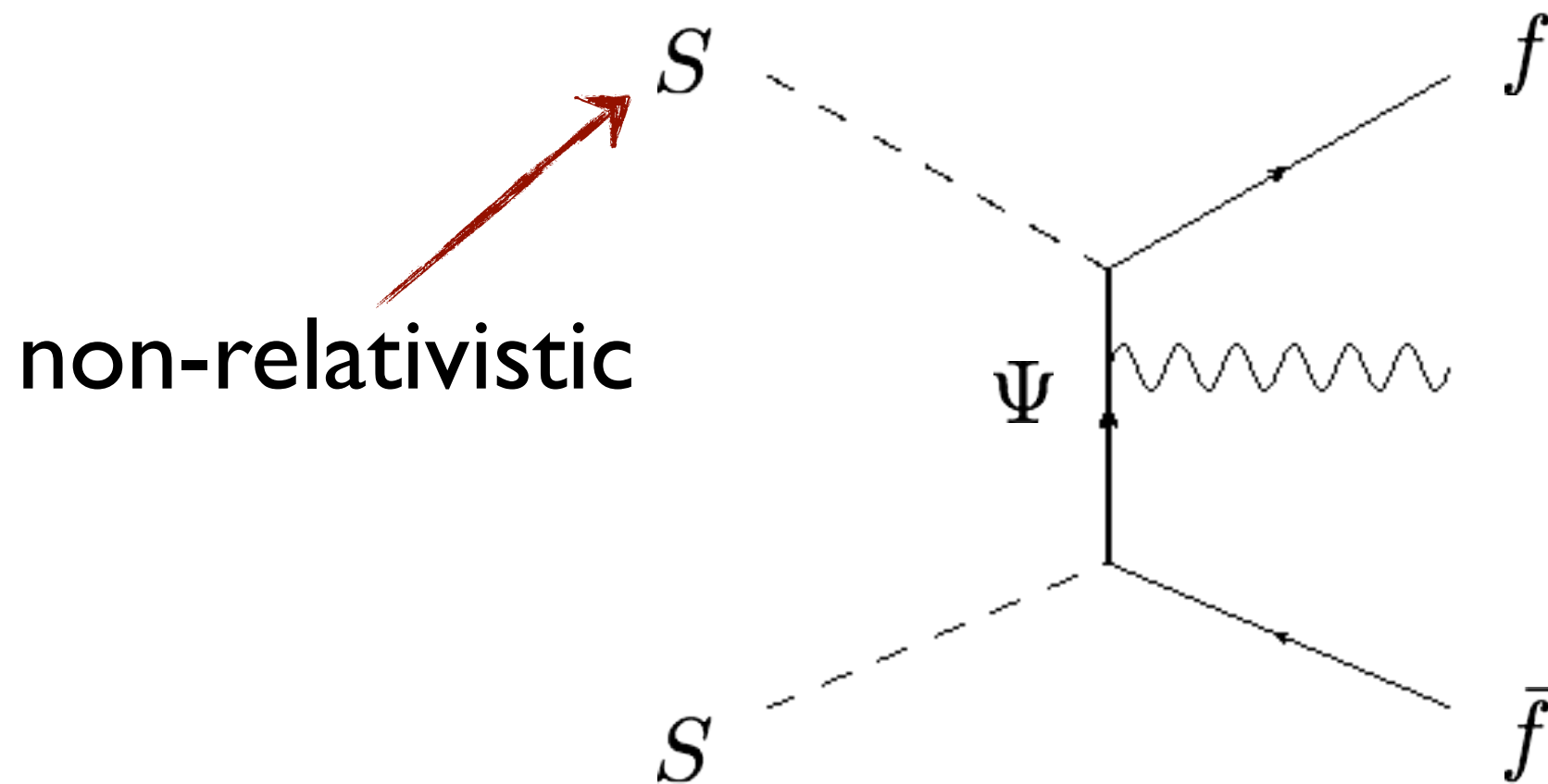


FINAL STATE

$$f_R \longleftarrow \longleftarrow \longrightarrow \bar{f}_R$$

$$\Theta^{ij} = \frac{i}{2} \bar{\psi}_f (\gamma^i \overrightarrow{\partial}^j - \gamma^j \overleftarrow{\partial}^i) \psi_f$$

WHY VIRTUAL INTERNAL BREMSSTRAHLUNG?

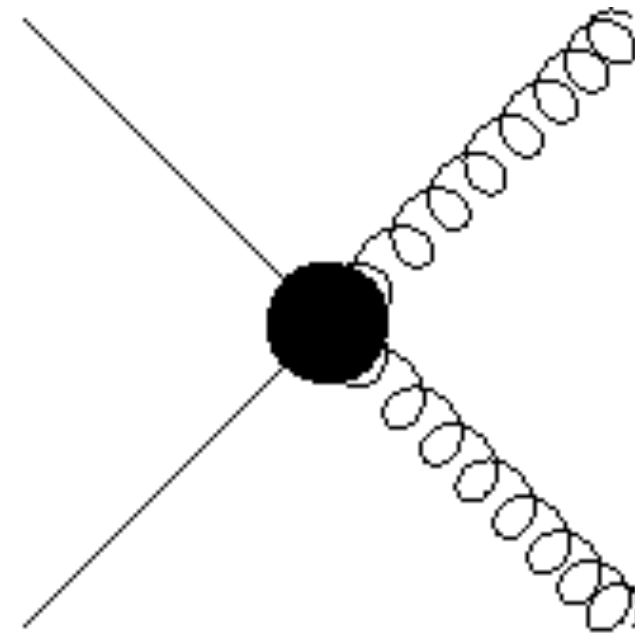
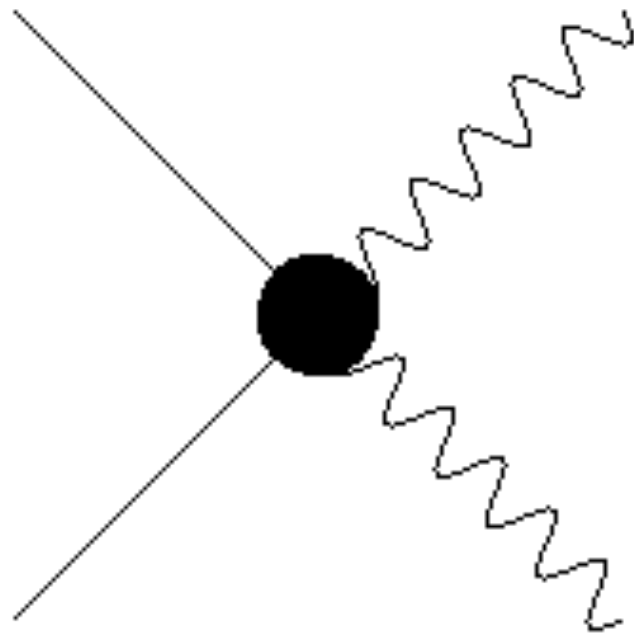


$$\mathcal{M} \propto ((p_S - p_f)^2 - M_\Psi^2)^{-1} \sim (M_S^2 - 2E_f M_S - M_\Psi^2)^{-1}$$

if $M_S \sim M_\Psi$ peaks for $E_f \sim 0$

indirect detection

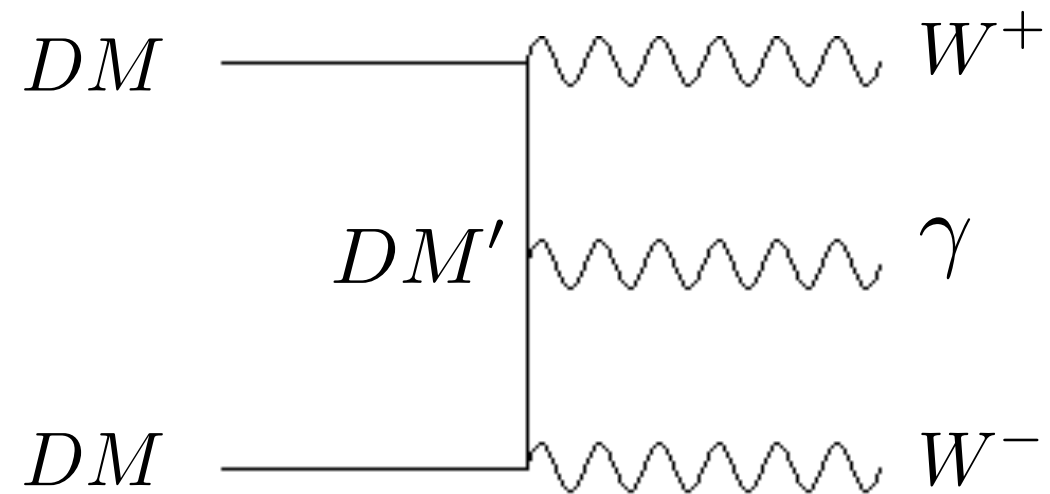
relic abundance



$$\frac{\sigma v_{gg}}{\sigma v_{\gamma\gamma}} = \mathcal{O}(100)$$

**naturally strong
digamma lines!**

VIB = VIRTUAL INTERNAL BREMSSTRAHLUNG



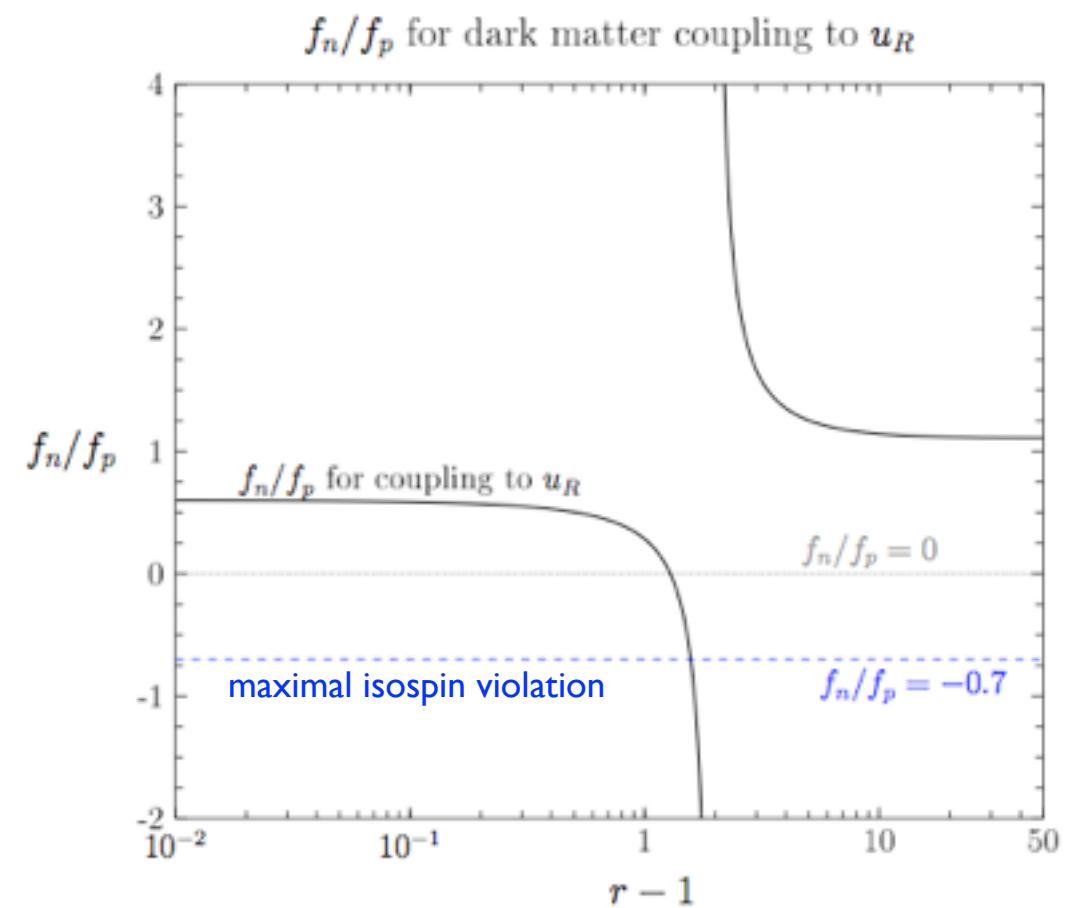
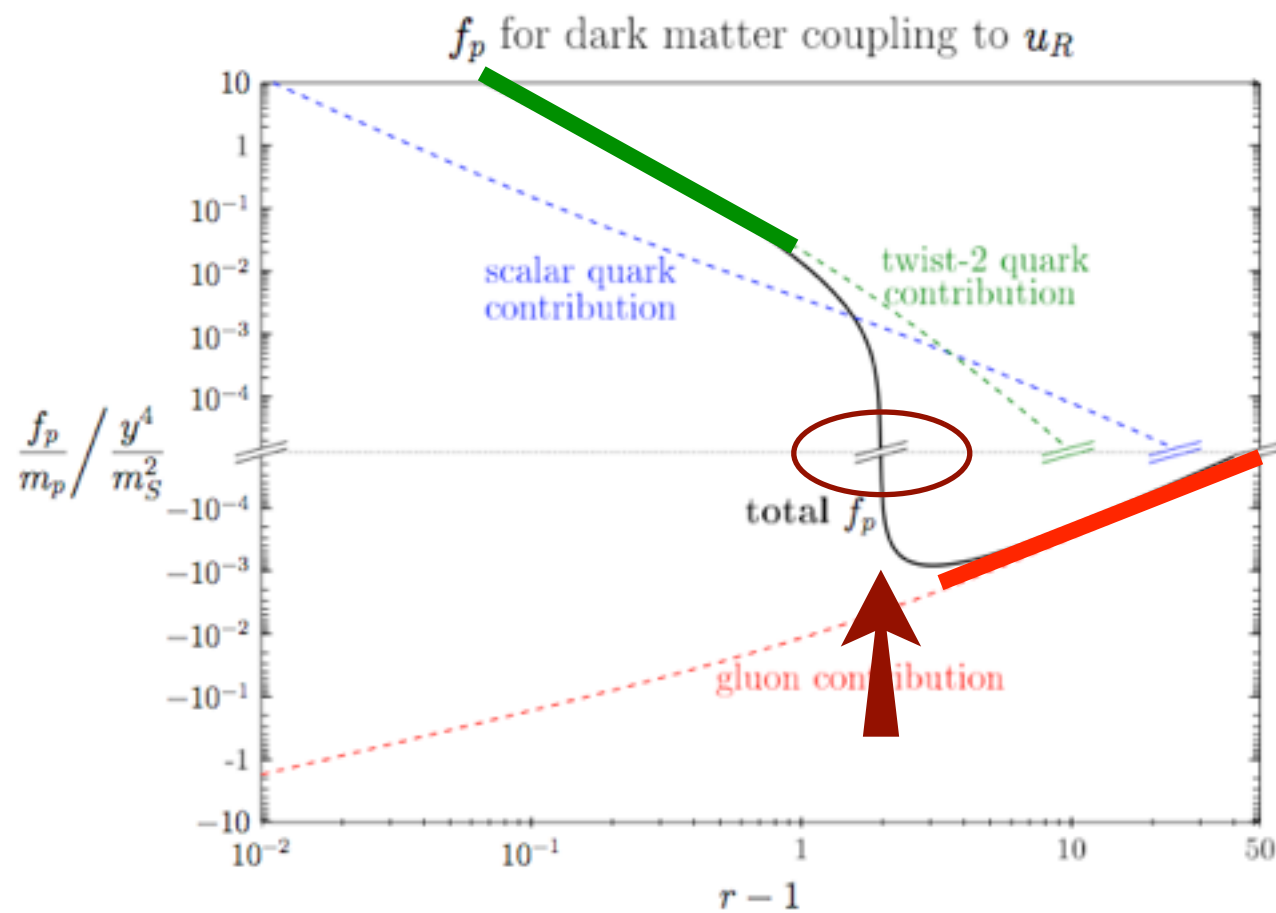
$$\mathcal{M} \propto \frac{1}{(p_{DM} - p_W)^2 - M_{DM'}^2} \sim \frac{1}{M_{DM}^2 - 2E_W M_{DM} - M_{DM'}^2} \sim \frac{1}{E_W}$$

Effectively $\sigma_{W^+W^-\gamma} \sim \sigma_{W^\pm\gamma}$



DIRECT DETECTION

isospin violation effects



destructive interference

$$\frac{f_N}{m_N} = C_S^q f_{T_q}^{(N)} + \frac{3}{4} C_T^q m_S^2 (q^{(N)}(2) + \bar{q}^{(N)}(2)) - \frac{8}{9} C_S^g f_{T_G}^{(N)}$$

twist-2 gluons

II. MDM SCALAR 7-PLET



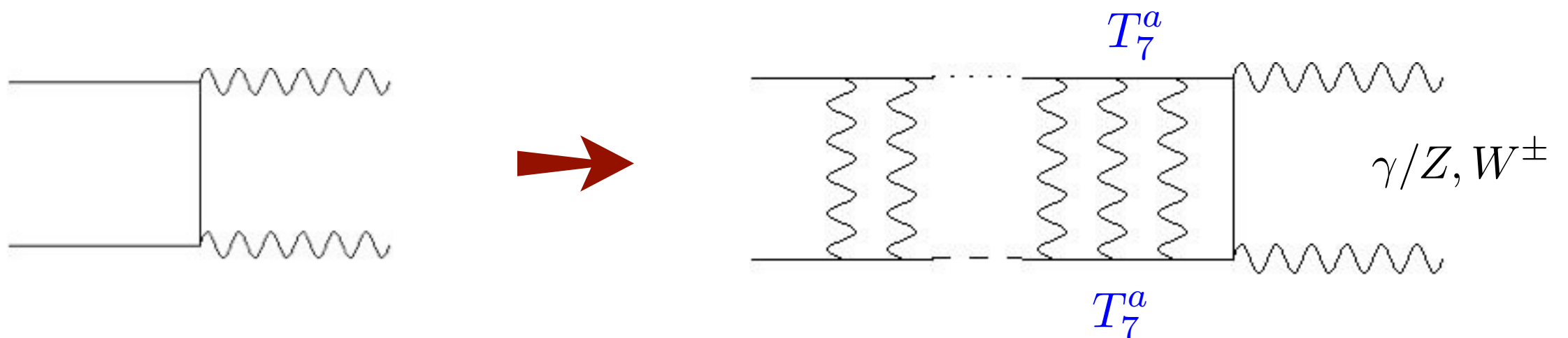
a benchmark for multi-TeV dark matter

$$M_7 \sim 25 \text{ TeV}$$

Cirelli, Strumia & Tamburini (2007)

1. Many co-annihilation channels.

2. Sommerfeld effects $M_7 \gg M_{W/Z}$



$$7 \otimes 7 = \dots \oplus 5_s \oplus \mathfrak{z}_A \oplus 1_s$$

$$V_{5/1}(r) \approx \frac{g_2^2}{r} T_7^a \otimes T_7^a|_{5/1} = \frac{g_2^2}{2r} \left(T_{5/1}^2 - 2 T_7^2 \right) = \begin{cases} V_5(r) = -\frac{9g_2^2}{r} \\ V_1(r) = -\frac{12g_2^2}{r} \end{cases}$$

