

Gauge-Higgs Unification from EW to GUT

Yutaka Hosotani



Funatsu, Hatanaka, YH, 1510.06550 (PRD)
YH, Yamatsu, 1504.03817 (PTEP), 1511.01674 (PoS)

Scalars 2015, Warsaw, 7 December 2015

In search of a **Principle**
for the **125 GeV Higgs scalar boson**

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which

regulates Higgs couplings,
explains EW sym breaking,
solves the gauge-hierarchy prob.

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Gauge-Higgs unification

Gauge-Higgs EW unification

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gauge theory

A_M

in 5 dim.

Gauge-Higgs EW unification

gauge theory A_M *in 5 dim.*

4-dim. components A_μ

U

4D gauge fields
 γ, W, Z

Gauge-Higgs EW unification

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in 5 dim.

4-dim. components A_μ

extra-dim. component A_y

4D gauge fields
 γ, W, Z

4D Higgs fields
 H
Aharonov-Bohm phase
 θ_H

Gauge-Higgs EW unification

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4D gauge fields
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Aharonov-Bohm phase
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Hosotani mechanism

EW symmetry breaking

$SO(5) \times U(1)$ gauge-Higgs unification

Agashe, Contino, Pomarol 2005

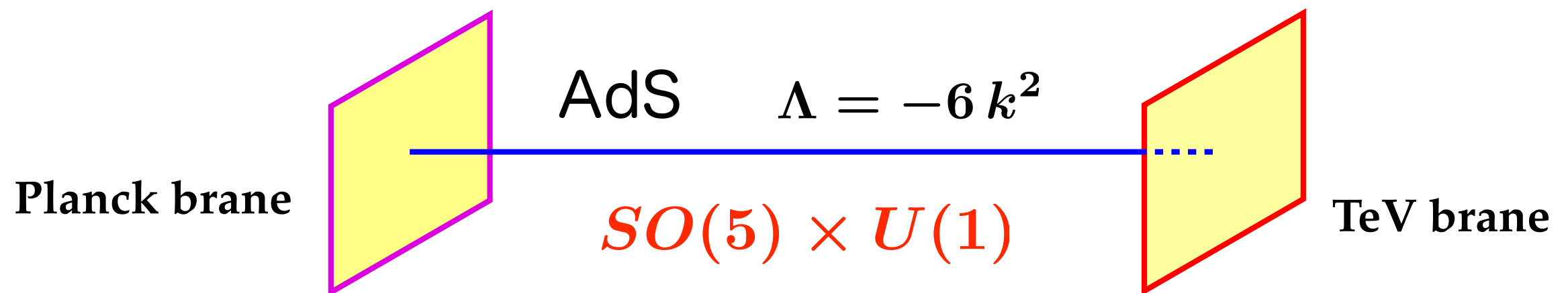
YH, Sakamura 2006

Medina, Shah, Wagner 2007

YH, Oda, Ohnuma, Sakamura 2008

YH, Noda, Uekusa 2009

Funatsu, Hatanaka, YH, Orikasa, Shimotani 2013, 2014



$SO(5) \times U(1)$ gauge-Higgs unification

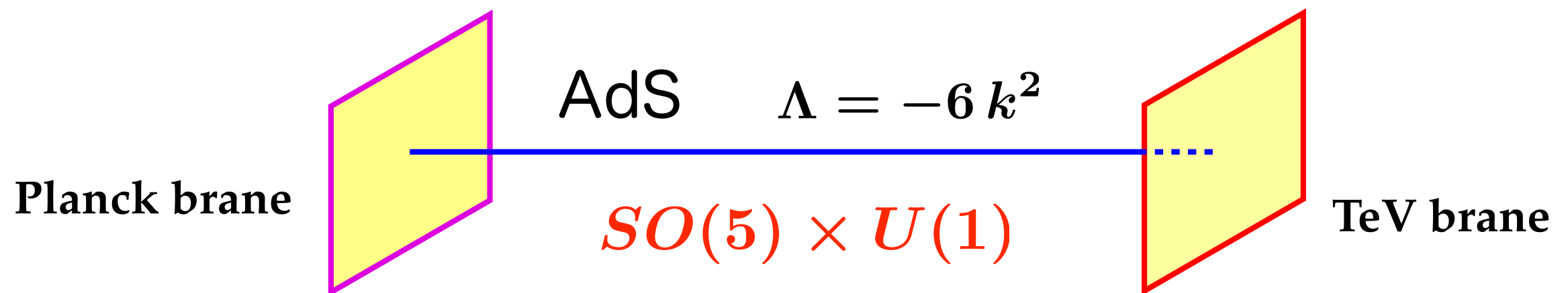
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$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, -y) = P_0 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, y) P_0^\dagger$$

$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, \pi R - y) = P_1 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, \pi R + y) P_1^\dagger$$

Orbifold BC : P_0, P_1

4D gauge bosons and Higgs

Orbifold BC: P_0 , P_1

$$P_0 = P_1 = \begin{pmatrix} -1 & & & & \\ & -1 & & & \\ & & -1 & & \\ & & & -1 & \\ & & & & +1 \end{pmatrix}$$

$$SO(5) \rightarrow SO(4) \simeq SU(2)_L \times SU(2)_R$$

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$W \ Z \ \gamma$

$$A_\mu \sim \begin{pmatrix} \boxed{} \end{pmatrix}$$

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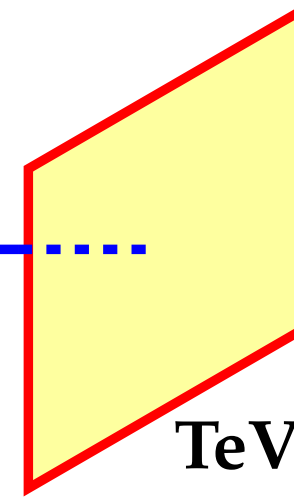
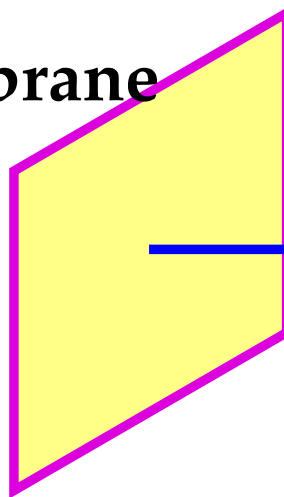


Higgs

$$A_y \sim \begin{pmatrix} \begin{matrix} \phi_1 \\ \phi_2 \\ \phi_3 \\ \phi_4 \end{matrix} \\ \boxed{} \end{pmatrix} \quad \Phi = \begin{bmatrix} \phi_1 + i\phi_2 \\ \phi_4 - i\phi_3 \end{bmatrix}$$

$SO(5) \times U(1)$ EW

Planck brane



TeV brane

$SO(5) \times U(1)$ EW

Planck brane

quarks/leptons

TeV brane

$$\Psi_5 \begin{pmatrix} T \\ B \\ t_L \\ b_L \\ t'_R \\ b'_R \end{pmatrix}_{\frac{2}{3}} \quad \begin{pmatrix} U \\ D \\ X \\ Y \\ b'_R \end{pmatrix}_{-\frac{1}{3}}$$

vector rep

SO(5)xU(1) EW

Planck brane

Brane scalar

$$\hat{\Phi} \left(0, \frac{1}{2}\right)$$

Brane fermion

$$\begin{pmatrix} \hat{T}_R \\ \hat{B}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{U}_R \\ \hat{D}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{X}_R \\ \hat{Y}_R \end{pmatrix}$$

$$\left(\frac{1}{2}, 0\right)$$

quarks/leptons

$$\Psi_5 \begin{pmatrix} T \\ B \\ t_L \\ b_L \\ t'_R \\ b'_R \end{pmatrix} \frac{2}{3} \quad \begin{pmatrix} U \\ D \\ X \\ Y \\ b'_R \end{pmatrix} -\frac{1}{3}$$

vector rep

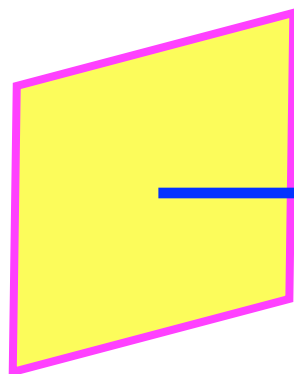
dark fermions

Ψ_4 **spinor rep**

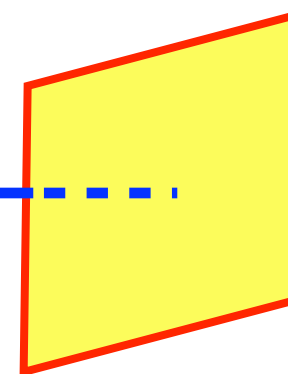
TeV brane

Planck brane

TeV brane

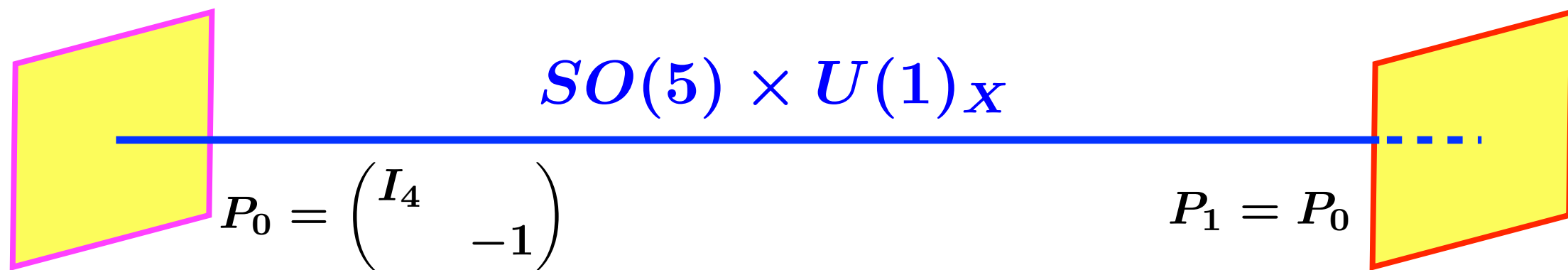


$$SO(5) \times U(1)_X$$



Planck brane

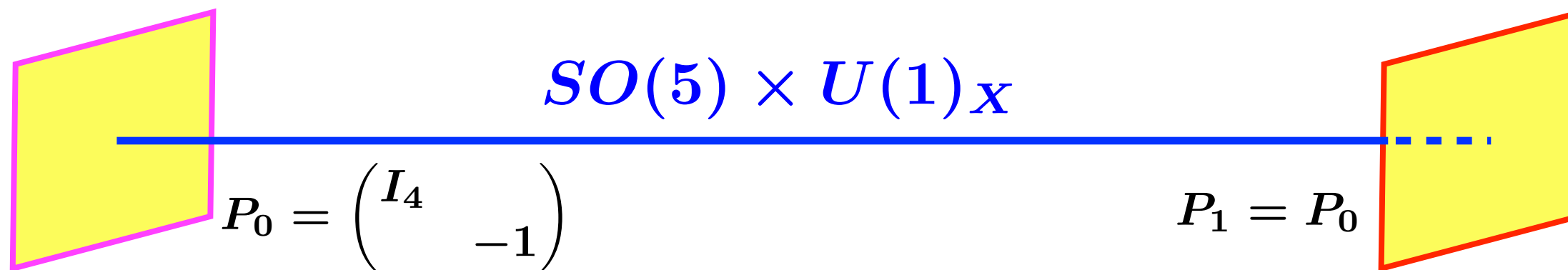
TeV brane



$\Rightarrow SO(4) \times U(1)_X$
B.C.

Planck brane

TeV brane

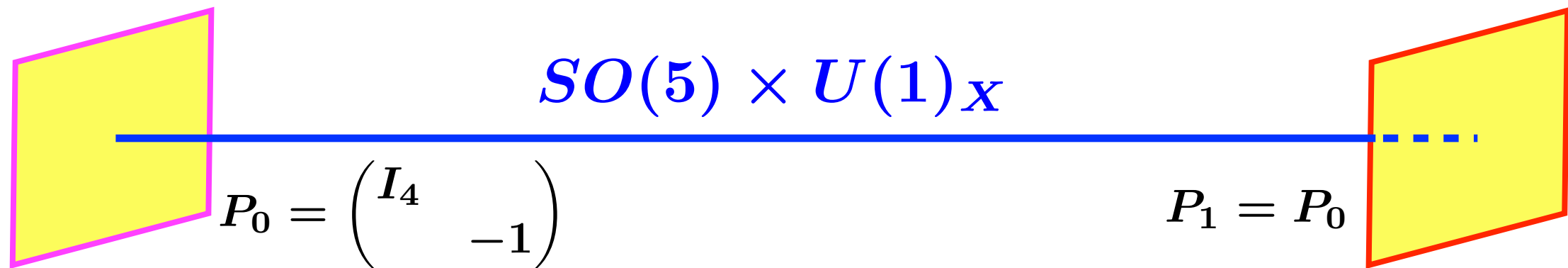


$\Rightarrow$ $SO(4) \times U(1)_X$
B.C.

$\Rightarrow$ $SU(2)_L \times U(1)_Y$
 $\langle \hat{\Phi} \rangle$

Planck brane

TeV brane



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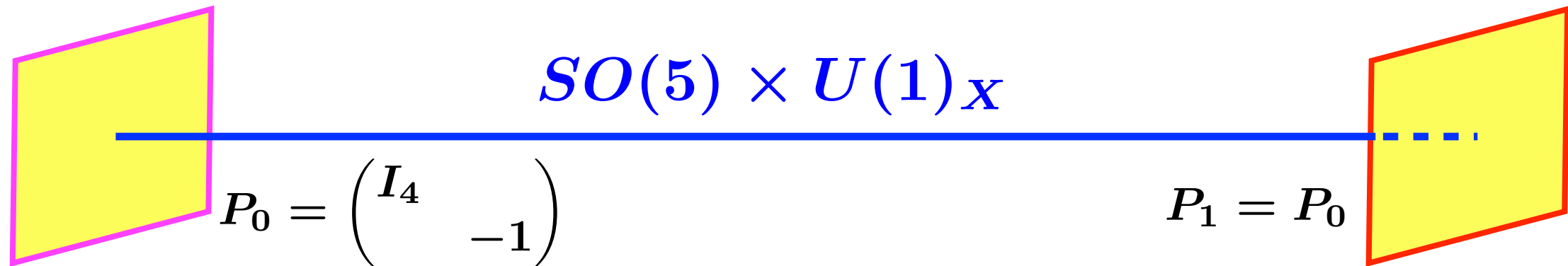
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 $\langle \hat{\Phi} \rangle$

Higgs boson : AB phase $\hat{\theta}_H(x) = \theta_H + \frac{H(x)}{f_H}$

$$e^{i\hat{\theta}_H(x)} \sim \exp \left\{ ig \int dy A_y \right\}$$

Planck brane

TeV brane



$\Rightarrow$ $SO(4) \times U(1)_X$
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$$e^{i\hat{\theta}_H(x)} \sim \exp \left\{ ig \int dy A_y \right\}$$

Hosotani mechanism

$\Rightarrow U(1)_{EM}$

Why GH ?

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“Gauge principle” for Higgs

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m_H : finite gauge hierarchy prob : solved

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No vacuum instability problem

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“Almost” SM at low energies, 8TeV LHC

Higgs decay: $\mu \sim \mu_{\text{SM}} \cdot \cos^2 \theta_H$

$$\theta_H < 0.1$$

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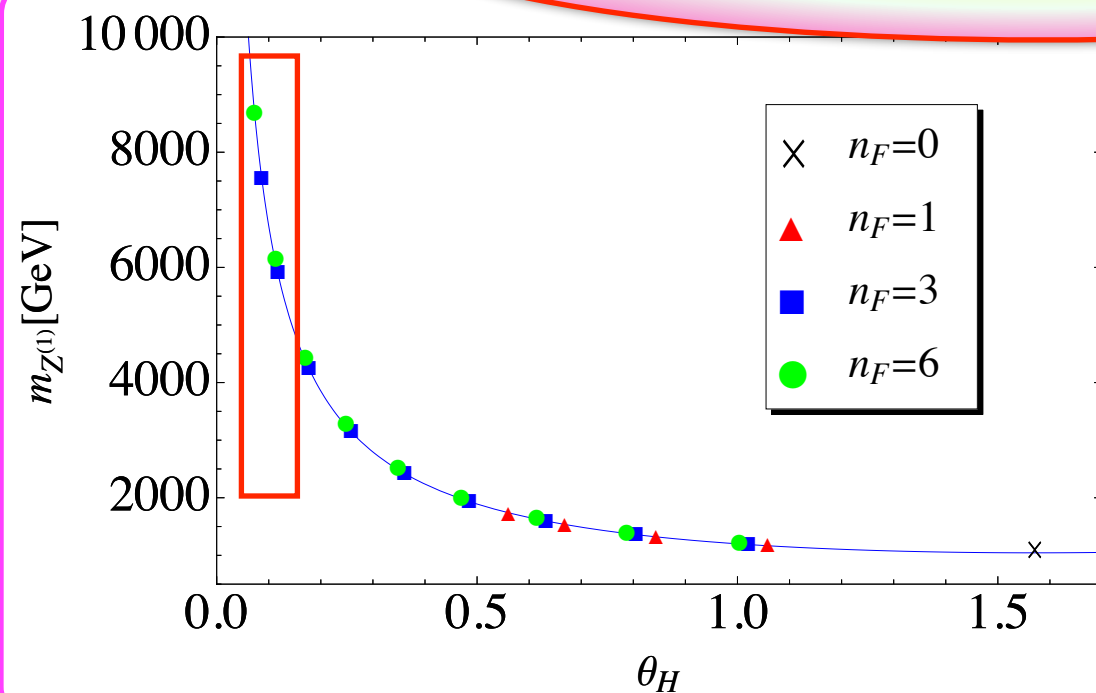
Higgs decay: $\mu \sim \mu_{\text{SM}} \cdot \cos^2 \theta_H$

$$\theta_H < 0.1$$

and predictions

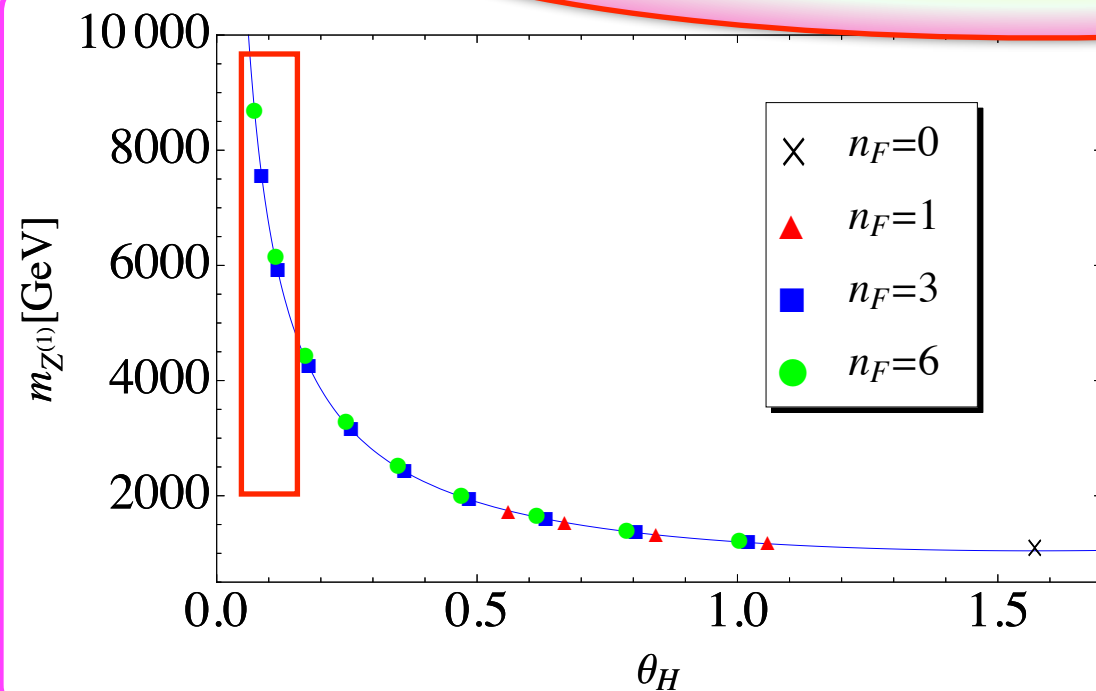
Universality in θ_H

Universality in θ_H



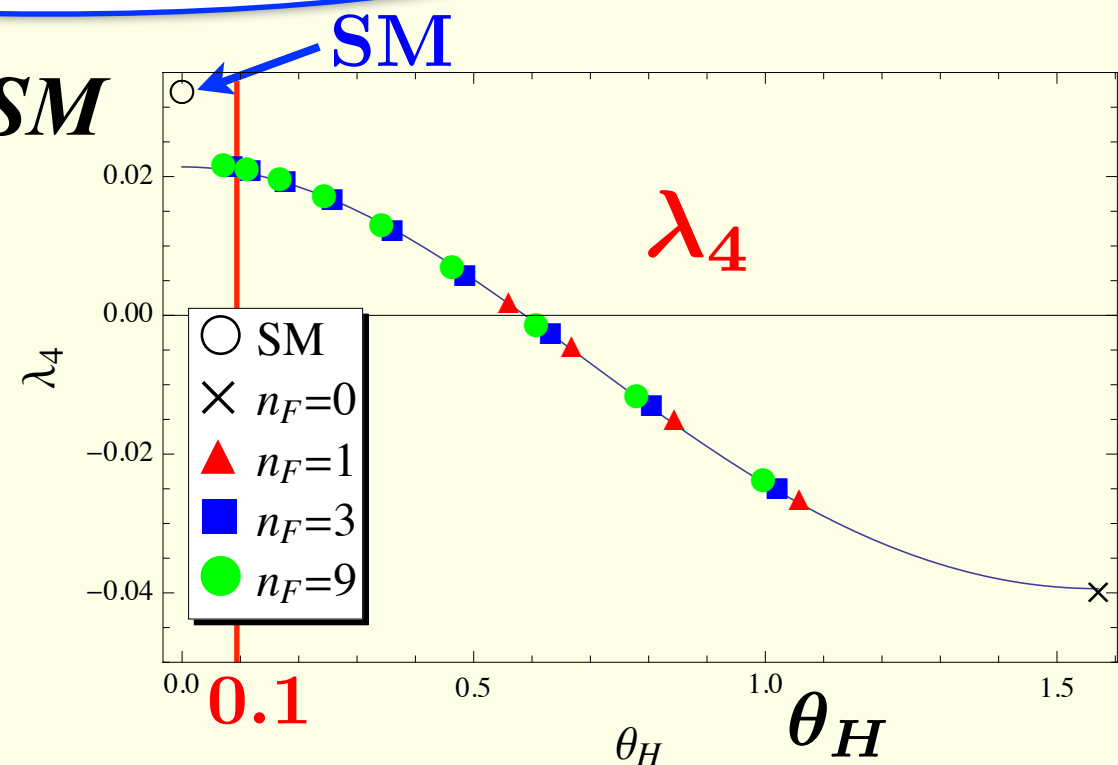
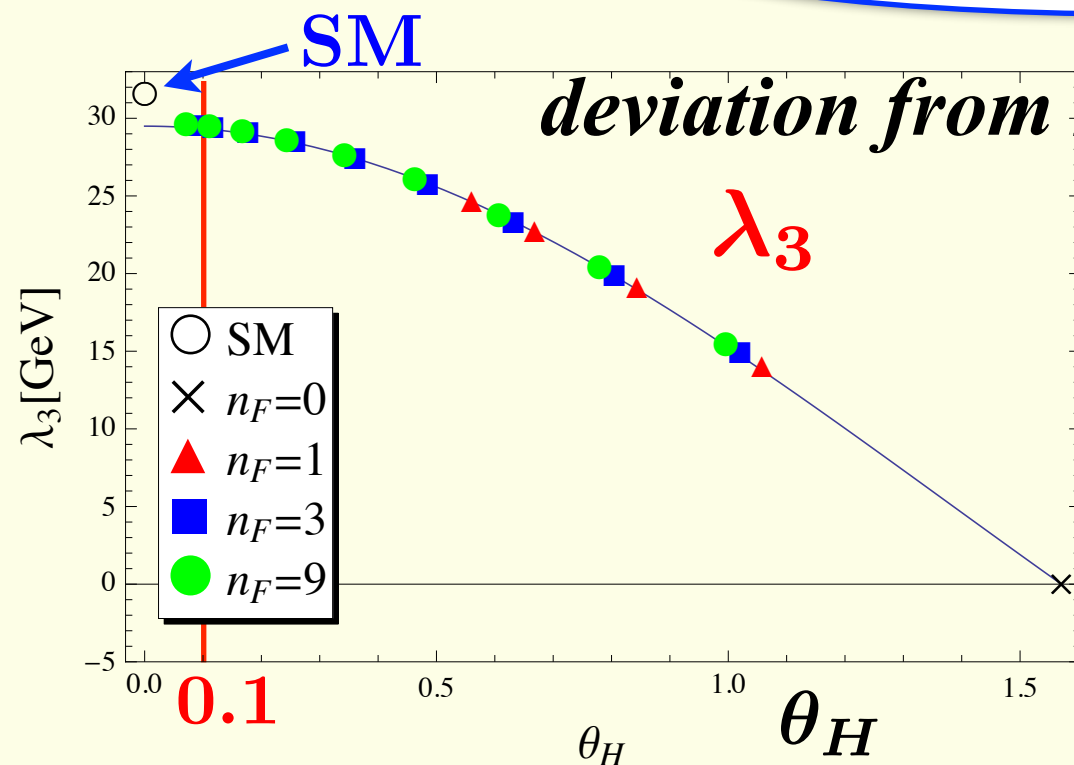
$$m_{Z^{(1)}} \sim \frac{1044 \text{ GeV}}{(\sin \theta_H)^{0.808}}$$

Universality in θ_H



$$m_{Z^{(1)}} \sim \frac{1044 \text{ GeV}}{(\sin \theta_H)^{0.808}}$$

Higgs self-couplings



Loop corrections

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$$V_{\text{eff}}(\theta_H), m_H$$

finite !

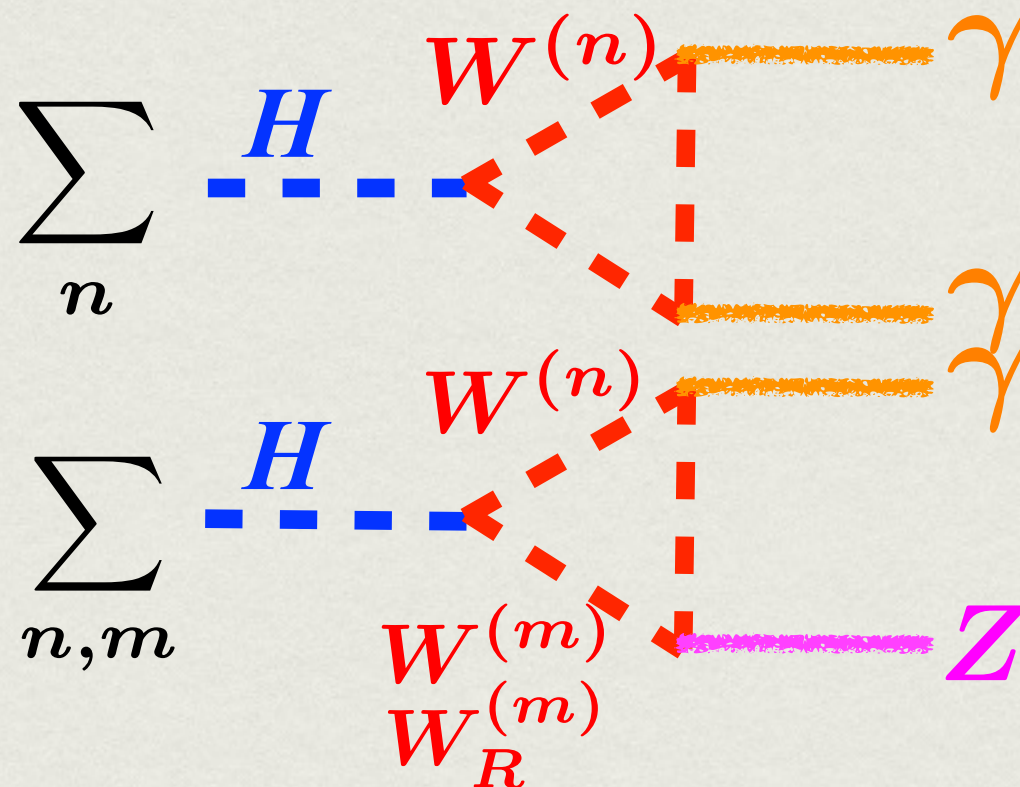
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$$H \rightarrow \gamma\gamma, Z\gamma$$

Funatsu, Hatanaka, YH
1510.06550 (PRD)



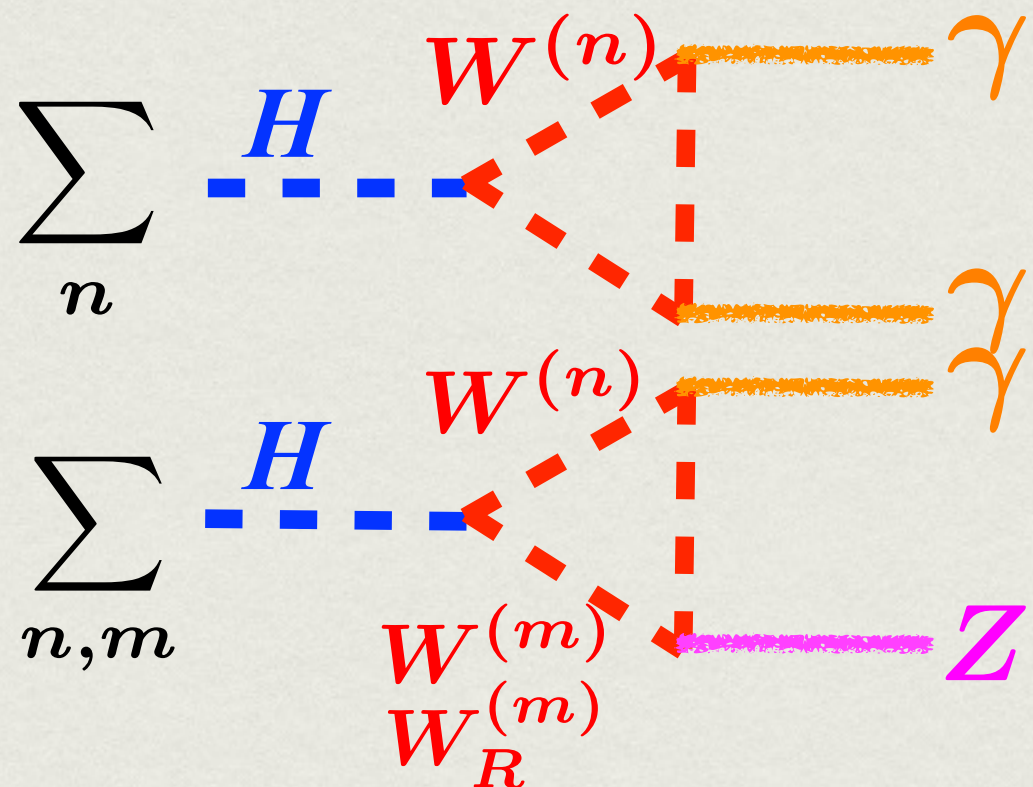
Loop corrections

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$$H \rightarrow \gamma\gamma, Z\gamma$$

Funatsu, Hatanaka, YH
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$$\sum_{n=1}^{\infty} \sum_j \frac{a_{n,j}}{n} = \text{finite !!!}$$

$$O(a_{n,j}) = 1$$

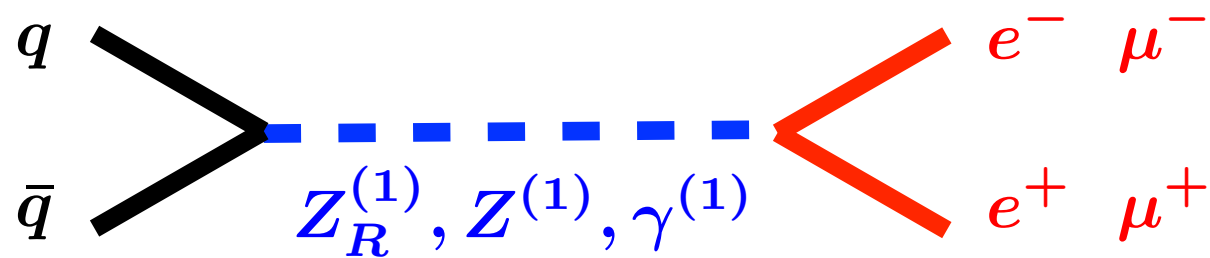
$O(1\%)$

corrections to SM

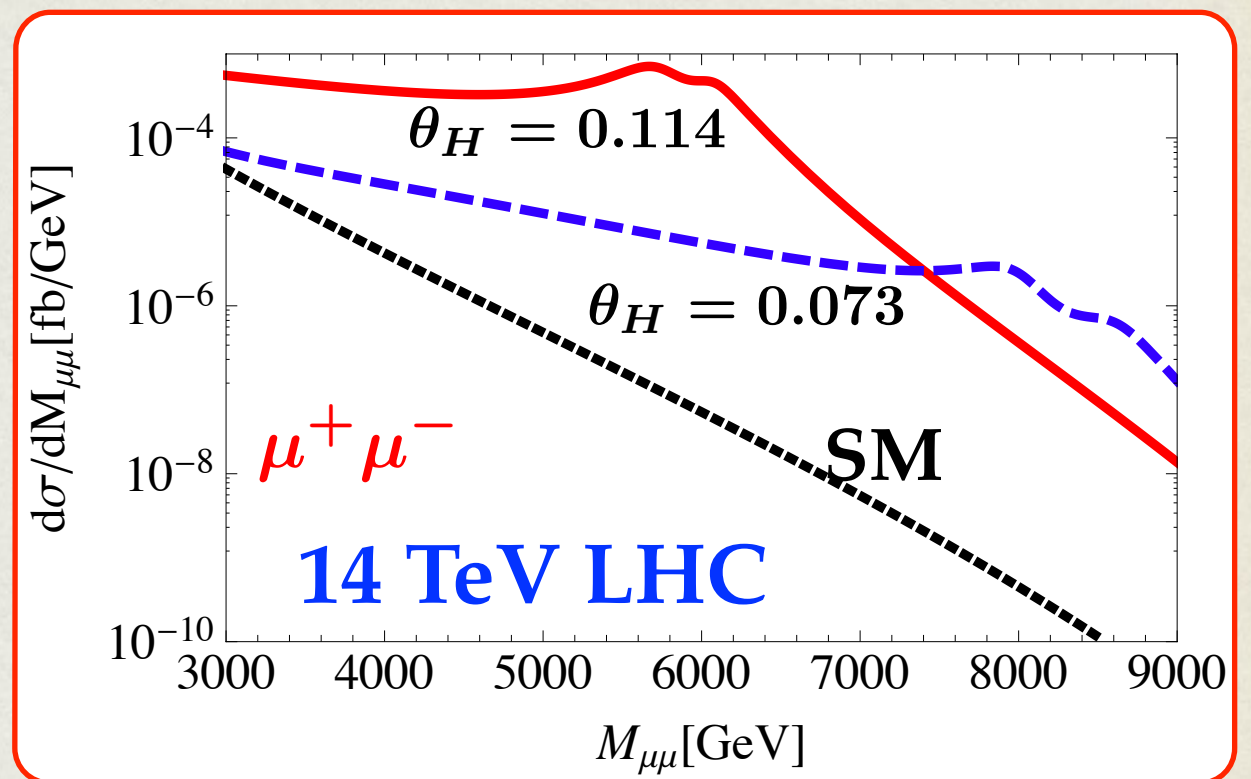
Z' search

W' search

Z' search

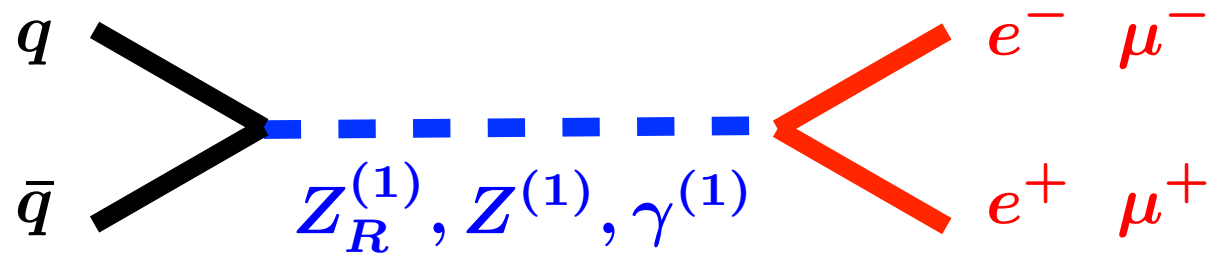


clear signals

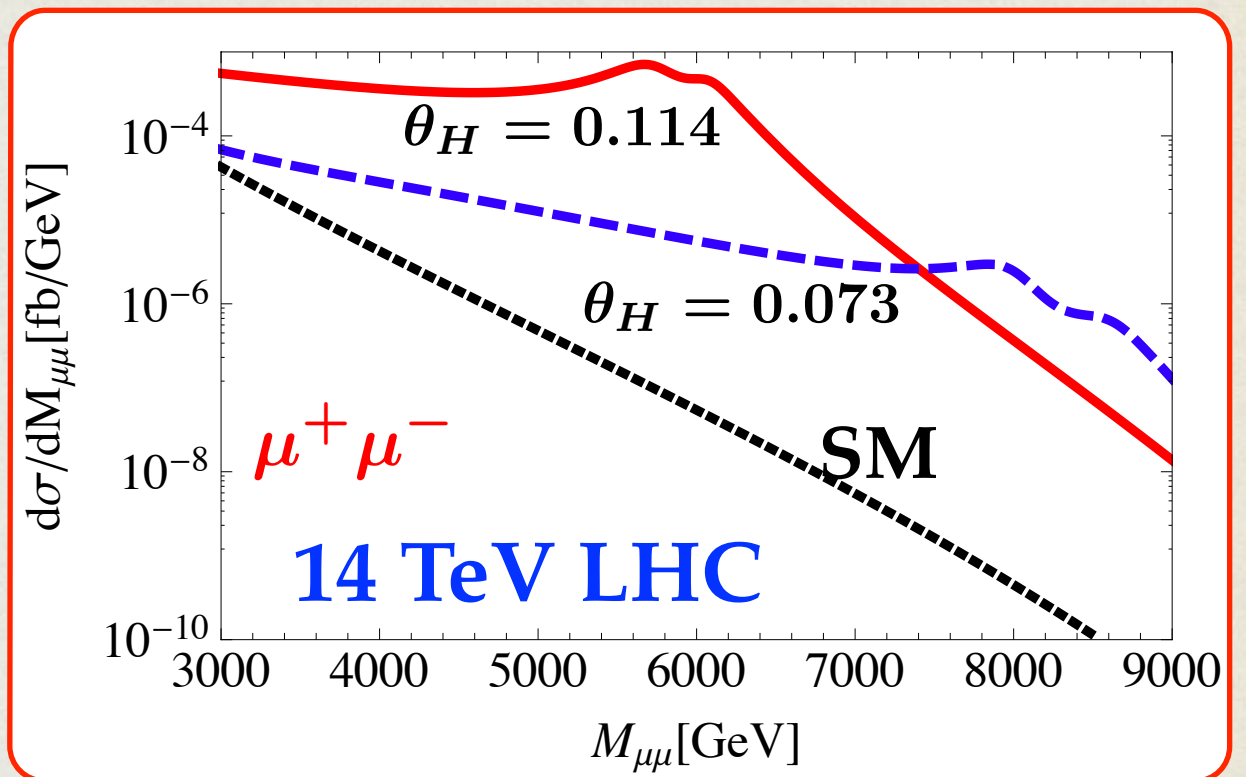


W' search

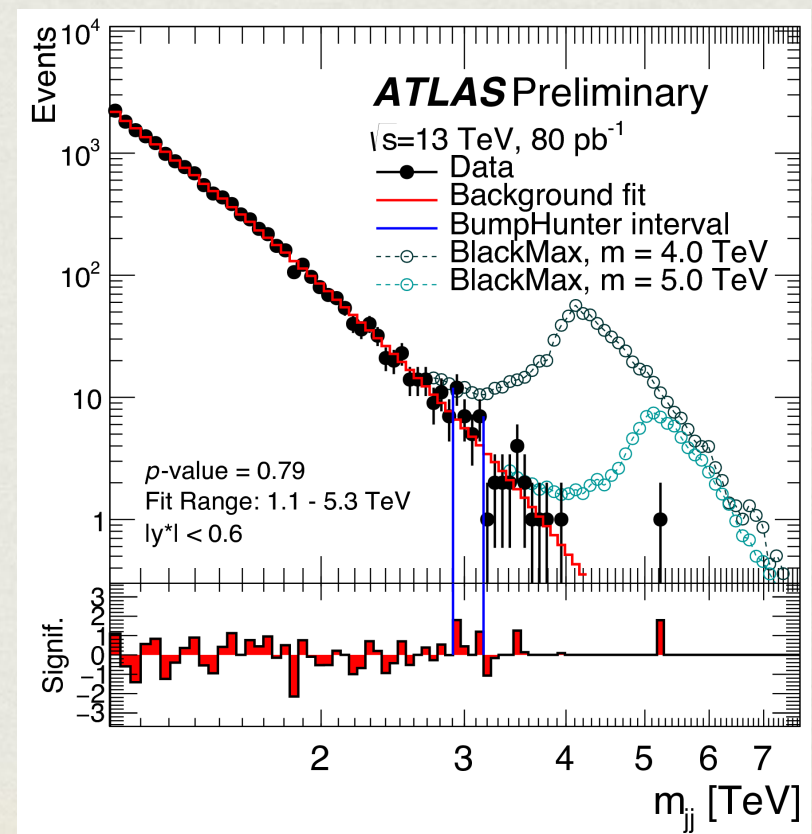
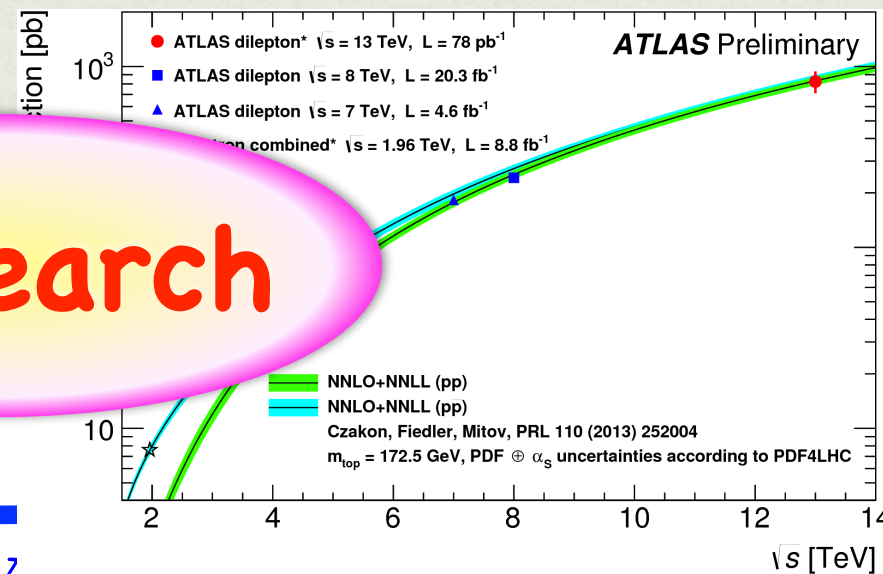
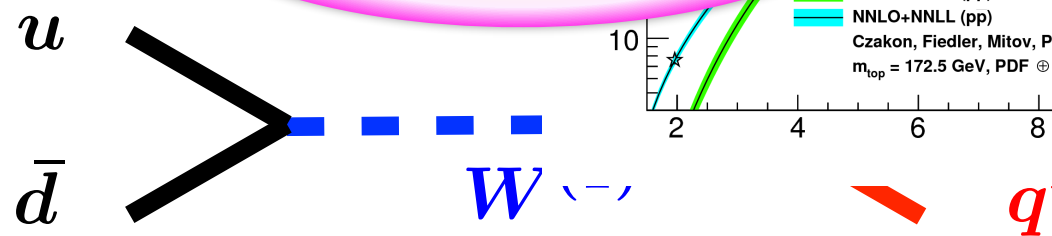
Z' search



clear signals



W' search



What is next?

What is next?

Gauge-Higgs Grand Unification

EM + Weak + Strong

What is next?

Gauge-Higgs Grand Unification

EM + Weak + Strong

$SO(5) \times U(1)$ GHU

?

Burdman, Nomura, NPB656 (2003)

Haba, YH, Kawamura, Yamashita, PRD70 (2004)

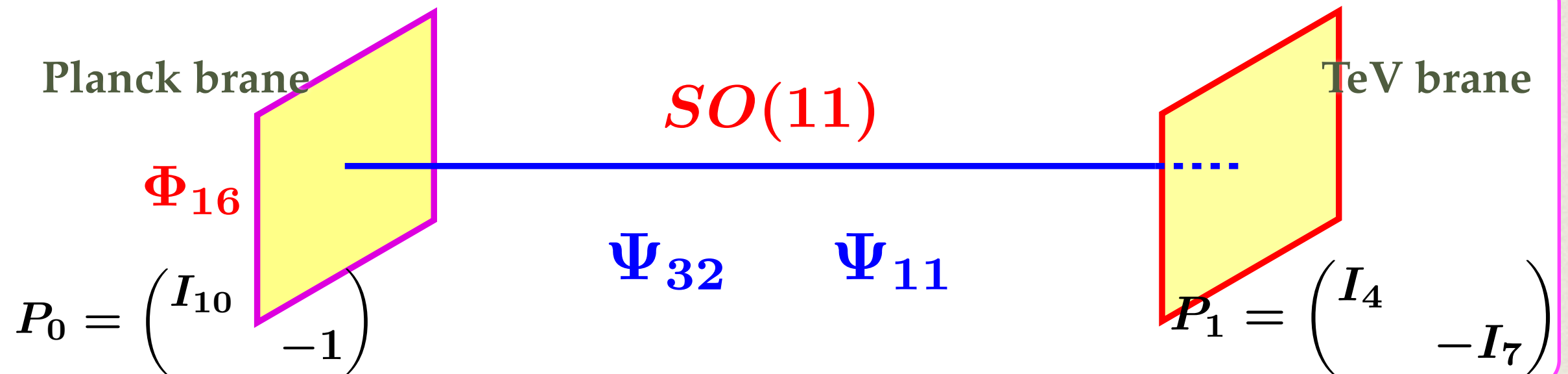
Lim, Maru, PLB653 (2007)

Kojima, Takenaga, Yamashita, PRD84 (2011)

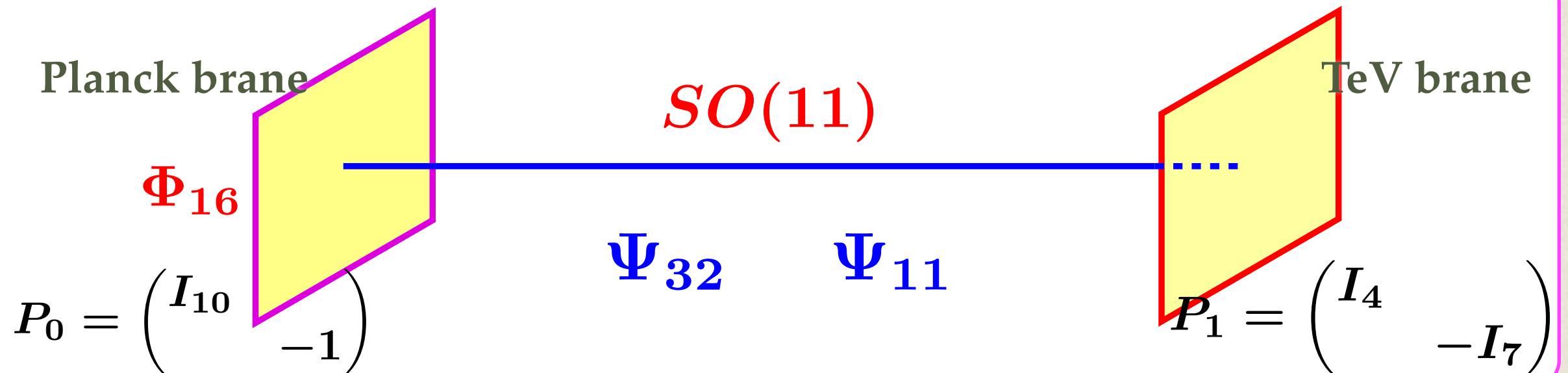
Frigerio, Serra, Varagnolo, JHEP 1106 (2011)

YH, Yamatsu, 1504.03817 (PTEP), 1511.01674

SO(11) gauge-Higgs grand unification in RS

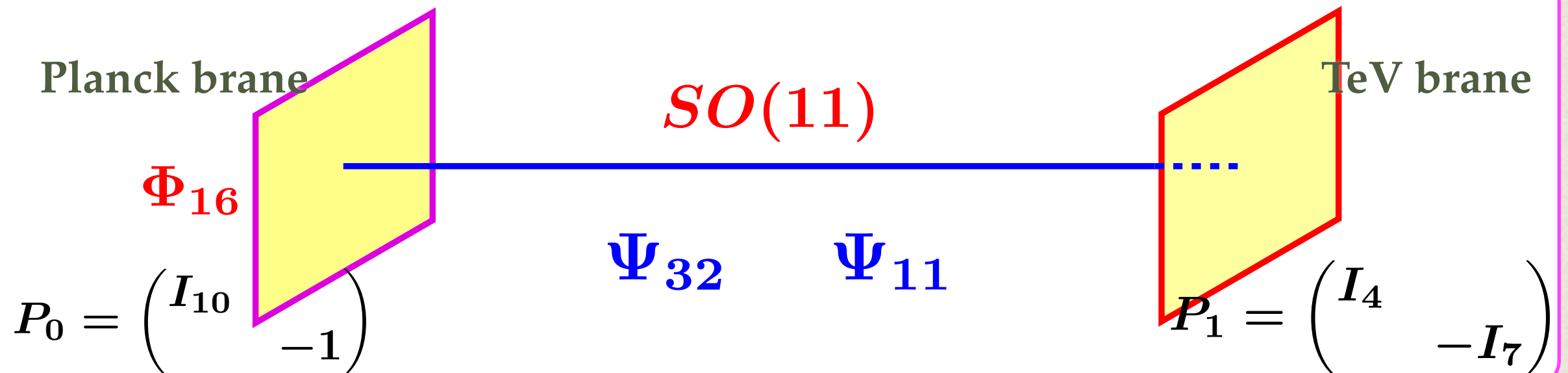


SO(11) gauge-Higgs grand unification in RS



$$A_\mu : \begin{pmatrix} \begin{matrix} SO(4) \\ (+, +) \end{matrix} & (+, -) & (-, -) \\ & \begin{matrix} (+, +) \\ SO(6) \end{matrix} & (-, +) \end{pmatrix}$$

SO(11) gauge-Higgs grand unification in RS



$A_\mu :$

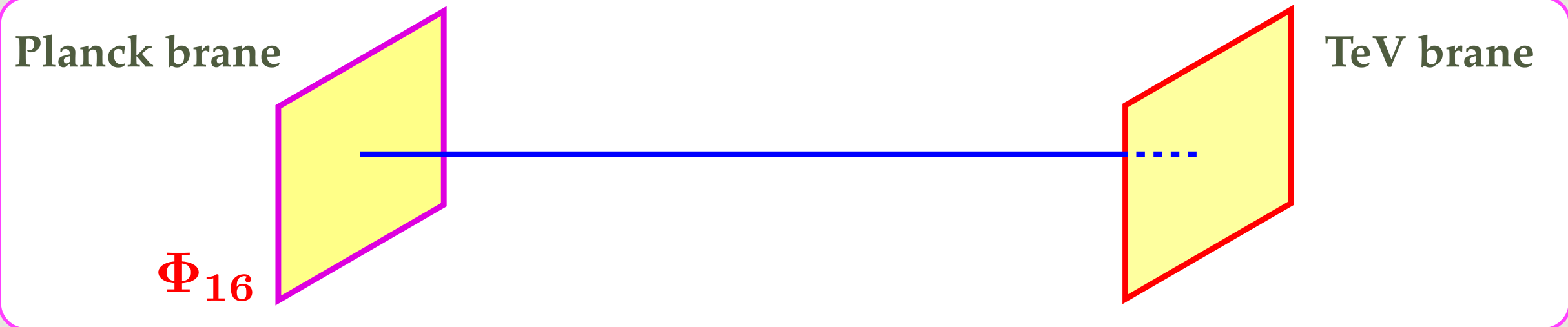
$SO(4)$ $(+, +)$	$(+, -)$	$(-, -)$
$(+, +)$	$SO(6)$	$(-, +)$

Higgs doublet

$A_y :$

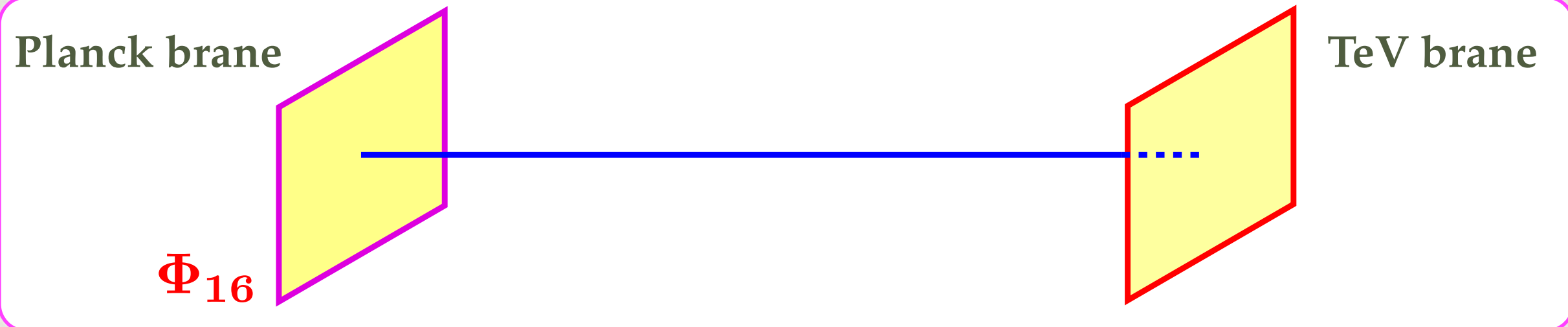
$(-, -)$	$(-, +)$	$(+, +)$
	$(-, -)$	$(+, -)$

$$SO(4) \times SO(6) \rightarrow SU(2)_L \times SU(3)_C \times U(1)_Y$$



$$(D_\mu \Phi_{16})^\dagger D^\mu \Phi_{16} \delta(y) \rightarrow g^2 \langle \Phi_{16}^\dagger \rangle A^\mu A_\mu \langle \Phi_{16} \rangle \delta(y)$$

$$SO(4) \times SO(6) \rightarrow SU(2)_L \times SU(3)_C \times U(1)_Y$$

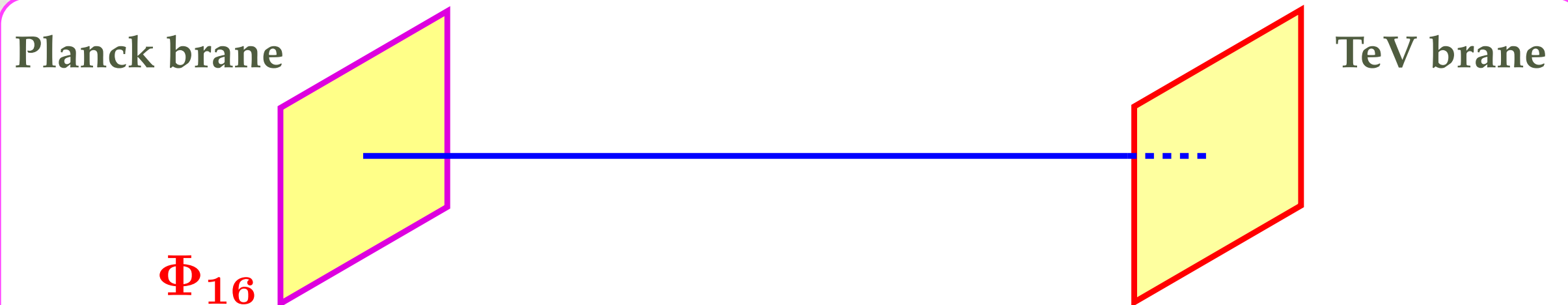


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$$Q_Y = \frac{1}{2}(T_{12} - T_{34}) - \frac{1}{3}(T_{56} + T_{78} + T_{9,10})$$

$$Q_{EM} = T_{12} - \frac{1}{3}(T_{56} + T_{78} + T_{9,10})$$

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$$\Rightarrow g'_Y = \sqrt{\frac{3}{5}} g_w, \quad e = \sqrt{\frac{3}{8}} g_w \quad \Rightarrow \sin^2 \theta_W = \frac{3}{8}$$

Planck brane

Quarks & Leptons

TeV brane

$$P_0^{\text{sp}} = I_{16} \otimes \sigma^3$$

Ψ_{32}

$$P_1^{\text{sp}} = I_2 \otimes \sigma^3 \otimes I_8$$

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$$P_1^{\text{sp}} = I_2 \otimes \sigma^3 \otimes I_8$$

$$\Psi_{32} = \begin{pmatrix} \Psi_{16} \\ \Psi_{\overline{16}} \end{pmatrix}$$

$$\Psi_{16} =$$

$$\begin{pmatrix} \nu \\ e \\ \tilde{d}_1 \\ \tilde{u}_1 \\ u_3 \\ d_3 \\ \tilde{d}_2 \\ \tilde{u}_2 \\ u_1 \\ d_1 \\ \tilde{e} \\ \tilde{\nu} \\ u_2 \\ d_2 \\ \tilde{d}_3 \\ \tilde{u}_3 \end{pmatrix}$$

$$\Psi_{\overline{16}} =$$

$$\begin{pmatrix} \tilde{d}'_3 \\ \tilde{u}'_3 \\ u'_2 \\ d'_2 \\ \tilde{e}' \\ \tilde{\nu}' \\ u'_1 \\ d'_1 \\ \tilde{d}'_2 \\ \tilde{u}'_2 \\ u'_3 \\ d'_3 \\ \tilde{d}'_1 \\ \tilde{u}'_1 \\ \nu' \\ e' \end{pmatrix}$$

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$$\Psi_{16} =$$

Fits well.

$$\begin{pmatrix} \nu \\ e \\ \tilde{d}_1 \\ \tilde{u}_1 \\ u_3 \\ d_3 \\ \tilde{d}_2 \\ \tilde{u}_2 \\ u_1 \\ d_1 \\ \tilde{e} \\ \tilde{\nu} \\ u_2 \\ d_2 \\ \tilde{d}_3 \\ \tilde{u}_3 \end{pmatrix} \begin{pmatrix} \nu_L \\ e_L \\ \text{zero modes} \\ \begin{pmatrix} u_{3L} \\ d_{3L} \end{pmatrix} \\ \begin{pmatrix} u_{1L} \\ d_{1L} \end{pmatrix} \\ \begin{pmatrix} u_{2L} \\ d_{2L} \end{pmatrix} \end{pmatrix}$$

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Scales

Scales

Size of 5th dim

$$\frac{\pi}{L}$$

fully 5-dim.

Weak scale

$$m_{\text{EW}}$$

Scales

Size of 5th dim

$$\frac{\pi}{L}$$

fully 5-dim.

KK scale

$$m_{\text{KK}} = \pi k e^{-kL} \sim \frac{\sqrt{kL}}{\sin \theta_H} m_W > 4 \text{ TeV}$$

Weak scale

$$m_{\text{EW}}$$

Scales

Size of 5th dim

$$\frac{\pi}{L}$$

fully 5-dim.

GUT scale

$$m_{\text{GUT}}$$

coupling unification ?

KK scale

$$m_{\text{KK}} = \pi k e^{-kL} \sim \frac{\sqrt{kL}}{\sin \theta_H} m_W > 4 \text{ TeV}$$

Weak scale

$$m_{\text{EW}}$$

QCD scale:

$$\Lambda_{\text{QCD}}$$

Size of 5th dim

$$\frac{\pi}{L}$$

GUT scale

$$m_{\text{GUT}}$$

KK scale

$$m_{\text{KK}}$$

Weak scale

$$m_{\text{EW}}$$

QCD scale:

$$\Lambda_{\text{QCD}}$$

Size of 5th dim

$$\frac{\pi}{L}$$

GUT scale

$$m_{\text{GUT}}$$

KK scale

$$m_{\text{KK}}$$

GUT structure above m_{KK}

Weak scale

$$m_{\text{EW}}$$

QCD scale:

$$\Lambda_{\text{QCD}}$$

Size of 5th dim

$$\frac{\pi}{L}$$

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$$m_{\text{GUT}}$$

KK scale

$$m_{\text{KK}}$$

Weak scale

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QCD scale:

$$\Lambda_{\text{QCD}}$$

RGE (Yamatsu)

$$\alpha_1, \alpha_2, \alpha_3 \rightarrow 0$$

rapidly

$$m_{\text{GUT}} \sim 100 m_{\text{KK}}$$

almost

GUT structure above m_{KK}

Size of 5th dim

$$\frac{\pi}{L}$$

GUT scale

$$m_{\text{GUT}}$$

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GUT structure above m_{KK}

Proton decay ?

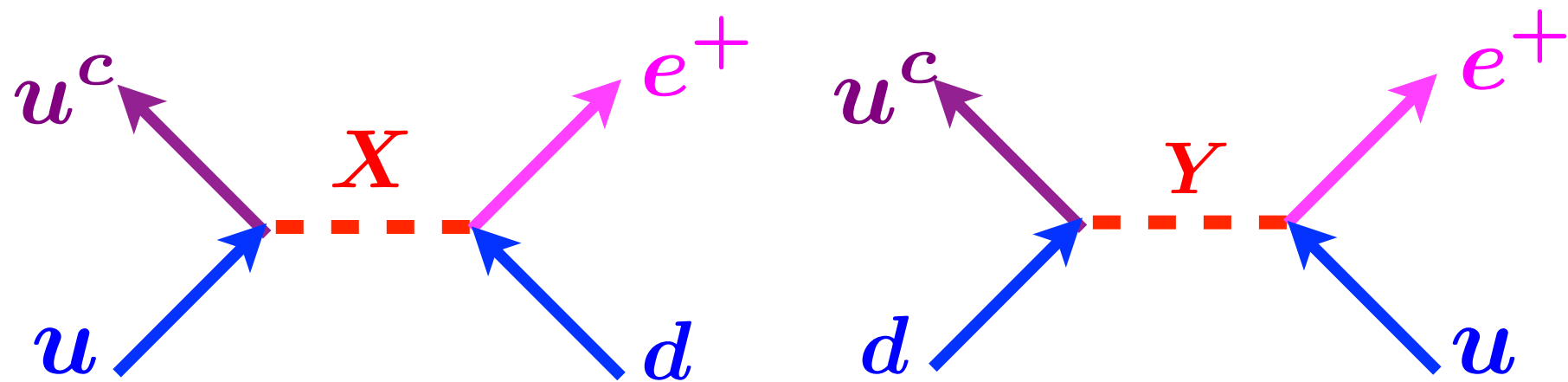
Proton decay in 4D GUT

4D SU(5) GUT

$$\begin{array}{ccc} \bar{5} & \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} & d_L^c \\ 10 & \begin{pmatrix} u_L \\ d_L \end{pmatrix} & u_L^c \quad e_L^c \end{array}$$

4D SO(10) GUT

$$16 = 1 + \bar{5} + 10$$



$$p \rightarrow \pi^0 e^+$$

Proton decay - forbidden

$$\Psi_{16} = \begin{pmatrix} \nu \\ e \\ \tilde{d}_1 \\ \tilde{u}_1 \\ u_3 \\ d_3 \\ \tilde{d}_2 \\ \tilde{u}_2 \\ u_1 \\ d_1 \\ \tilde{e} \\ \tilde{\nu} \\ u_2 \\ d_2 \\ \tilde{d}_3 \\ \tilde{u}_3 \end{pmatrix} \quad \begin{pmatrix} \nu_L \\ e_L \\ \\ \\ u_{3L} \\ d_{3L} \\ \\ \\ u_{1L} \\ d_{1L} \\ \\ \\ u_{2L} \\ d_{2L} \end{pmatrix} \quad \Psi_{\overline{16}} = \begin{pmatrix} \tilde{d}'_3 \\ \tilde{u}'_3 \\ u'_2 \\ d'_2 \\ \tilde{e}' \\ \tilde{\nu}' \\ u'_1 \\ d'_1 \\ \tilde{d}'_2 \\ \tilde{u}'_2 \\ u'_3 \\ d'_3 \\ \tilde{d}'_1 \\ \tilde{u}'_1 \\ \nu' \\ e' \end{pmatrix} \quad \begin{pmatrix} \\ \\ u_{2R} \\ d_{2R} \\ \\ \\ u_{1R} \\ d_{1R} \\ \\ \\ u_{3R} \\ d_{3R} \\ \\ \\ \nu_R \\ e_R \end{pmatrix} \quad \Psi_{32} = \begin{pmatrix} \Psi_{16} \\ \Psi_{\overline{16}} \end{pmatrix}$$

Proton decay - forbidden

$$\Psi_{16} = \begin{pmatrix} \nu \\ e \\ \tilde{d}_1 \\ \tilde{u}_1 \\ u_3 \\ d_3 \\ \tilde{d}_2 \\ \tilde{u}_2 \\ u_1 \\ d_1 \\ \tilde{e} \\ \tilde{\nu} \\ u_2 \\ d_2 \\ \tilde{d}_3 \\ \tilde{u}_3 \end{pmatrix} \quad \begin{pmatrix} \nu_L \\ e_L \\ \\ \\ u_{3L} \\ d_{3L} \\ \\ \\ u_{1L} \\ d_{1L} \\ \\ \\ u_{2L} \\ d_{2L} \\ \\ \end{pmatrix}$$

$$\Psi_{\overline{16}} = \begin{pmatrix} \tilde{d}'_3 \\ \tilde{u}'_3 \\ u'_2 \\ d'_2 \\ \tilde{e}' \\ \tilde{\nu}' \\ u'_1 \\ d'_1 \\ \tilde{d}'_2 \\ \tilde{u}'_2 \\ u'_3 \\ d'_3 \\ \tilde{d}'_1 \\ \tilde{u}'_1 \\ \nu' \\ e' \end{pmatrix} \quad \begin{pmatrix} \\ \\ u_{2R} \\ d_{2R} \\ \\ \\ u_{1R} \\ d_{1R} \\ \\ \\ u_{3R} \\ d_{3R} \\ \\ \nu_R \\ e_R \end{pmatrix}$$

$$\Psi_{32} = \begin{pmatrix} \Psi_{16} \\ \Psi_{\overline{16}} \end{pmatrix}$$

N_Ψ
conservation

$$p \rightarrow \pi^0 e^+$$

$$N_\Psi = 3 \quad N_\Psi = -1$$

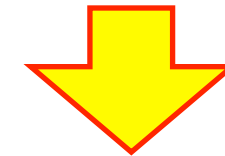
Proton decay - forbidden

$$\Psi_{16} = \begin{pmatrix} \nu \\ e \\ \tilde{d}_1 \\ \tilde{u}_1 \\ u_3 \\ d_3 \\ \tilde{d}_2 \\ \tilde{u}_2 \\ u_1 \\ d_1 \\ \tilde{e} \\ \tilde{\nu} \\ u_2 \\ d_2 \\ \tilde{d}_3 \\ \tilde{u}_3 \end{pmatrix} \quad \begin{pmatrix} \nu_L \\ e_L \\ \\ \\ u_{3L} \\ d_{3L} \\ \\ \\ u_{1L} \\ d_{1L} \\ \\ \\ u_{2L} \\ d_{2L} \\ \\ \end{pmatrix}$$

$$\Psi_{\overline{16}} = \begin{pmatrix} \tilde{d}'_3 \\ \tilde{u}'_3 \\ u'_2 \\ d'_2 \\ \tilde{e}' \\ \tilde{\nu}' \\ u'_1 \\ d'_1 \\ \tilde{d}'_2 \\ \tilde{u}'_2 \\ u'_3 \\ d'_3 \\ \tilde{d}'_1 \\ \tilde{u}'_1 \\ \nu' \\ e' \end{pmatrix} \quad \begin{pmatrix} \\ \\ u_{2R} \\ d_{2R} \\ \\ \\ u_{1R} \\ d_{1R} \\ \\ \\ u_{3R} \\ d_{3R} \\ \\ \\ \nu_R \\ e_R \end{pmatrix}$$

$$\Psi_{32} = \begin{pmatrix} \Psi_{16} \\ \Psi_{\overline{16}} \end{pmatrix}$$

N_Ψ
conservation



no proton decay

$$p \not\rightarrow \pi^0 e^+$$

$$N_\Psi = 3 \quad N_\Psi = -1$$

Summary

$SO(5) \times U(1)$ Gauge-Higgs EW Unification

$SO(11)$ Gauge-Higgs Grand Unification

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Dynamical EW sym breaking

Consistent at low energies

Predictions for 14 TeV LHC

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$SO(11)$ Gauge-Higgs Grand Unification

$SO(11)$ structure above m_{KK}

Proton decay naturally forbidden