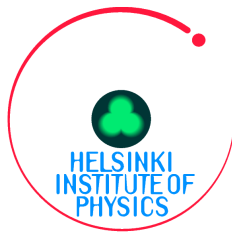


Flavon-Induced Lepton Flavour Violation

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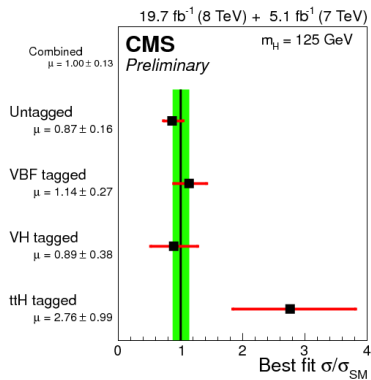
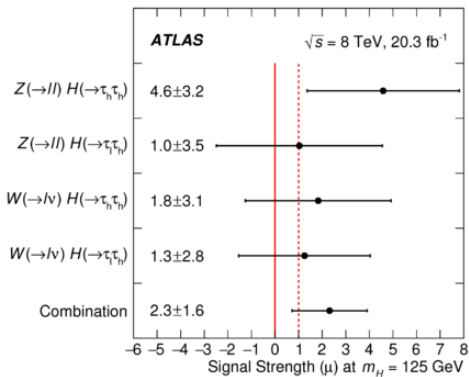


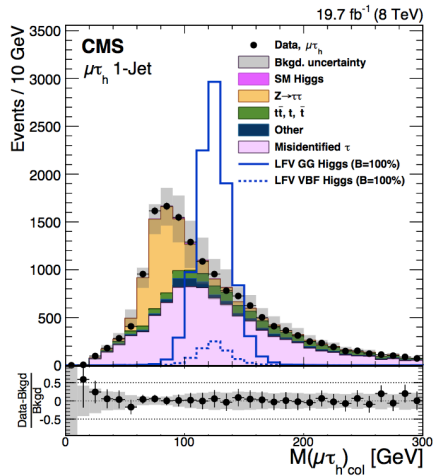
In collaboration with
K. Huitu & N. Koivunen & O. Lebedev
work in progress

Scalars 2015, Warsaw

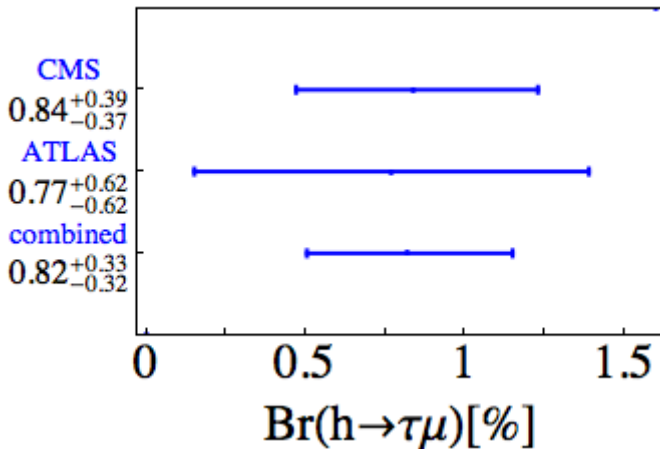
- 1 Introduction
- 2 Bounds from CLFV processes
- 3 Gauged $U(1)$ Froggat-Nielsen symmetry
- 4 Discrete Froggat-Nielsen symmetry
- 5 Results and conclusion

The Higgs has been discovered





Naive combined result $\text{BR}(h \rightarrow \mu\tau)$



Charged Lepton Flavour Violation in SM

The lepton Yukawa part of the SM Lagrangian:

$$\begin{aligned}\mathcal{L}_{SM} &\supset \frac{v_h}{\sqrt{2}} Y_{ij} \bar{l}_{L,i} l'_{R,j} \left(1 + \frac{h}{v_h}\right) \\ &\equiv v_h \bar{l}_L Y_{\text{diag}} l_R + \bar{l}_L \frac{Y_{\text{diag}}}{\sqrt{2}} l_R h\end{aligned}$$

CLFV processes are **absent** in SM.

To produce CLFV → go Beyond SM

The Froggatt-Nielsen mechanism

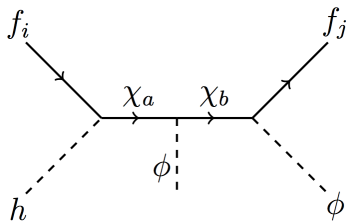
Froggat-Nielsen mechanism - global $U(1)$ symmetry

A **Higgs** doublet and a **flavon** singlet:

$$H = \begin{pmatrix} 0 \\ \frac{v_h + h}{\sqrt{2}} \end{pmatrix}, \quad \Phi = \begin{pmatrix} \frac{v_\phi + \phi}{\sqrt{2}} \end{pmatrix}$$

$U(1)$ -invariant Yukawa-like couplings:

$$c_{ia} f_i \chi_a \frac{h}{\sqrt{2}}, \quad b_{ja} f_j \chi_a \frac{\phi}{\sqrt{2}}$$



Froggat-Nielsen mechanism

The effective operators after integrating out the **heavy fermions**:

$$c_{ij}^f \bar{f}_{L,i} f_{R,j} \frac{h}{\sqrt{2}} \left(\frac{\phi}{\sqrt{2}\Lambda} \right)^x, \quad q_{\bar{L},i} + q_{R,j} + q_h + q_\phi x = 0$$

Particle	$\bar{f}_{L,i}$	$f_{R,i}$	h	ϕ
$U(1)$ charge	$q_{\bar{L},i}$	$q_{R,i}$	q_h	q_ϕ

After SSB:

$$\mathcal{L}_{Yukawa} \supset c_{ij}^f \left(\frac{v_\phi}{\sqrt{2}\Lambda} \right)^{-\frac{1}{q_\phi}(q_{\bar{L},i} + q_{R,j} + q_h)} \bar{f}_{L,i} f_{R,j} \frac{h}{\sqrt{2}}$$

The SM Yukawa coupling ($q_\phi = -1, q_h = 0$)

$$Y_{ij}^f = c_{ij}^f \epsilon^{\overbrace{(q_{\bar{L},i} + q_{R,j})}^{n_{ij}}} \quad \text{with} \quad \epsilon = \frac{v_\phi}{\sqrt{2}\Lambda}$$

Froggat-Nielsen mechanism

Leptonic part of the Lagrangian

$$\mathcal{L}_{\text{eff.}} \supset \frac{v_h}{\sqrt{2}} Y_{ij} \bar{l}_{L,i} l'_{R,j} \left(1 + \frac{h}{v_h}\right) + n_{ij} v_h Y_{ij} \frac{\phi}{v_\phi} \bar{l}_{L,i} l'_{R,j}$$

$$Y_{\text{diag}} = U_L Y_{ij} U_R^\dagger$$

$$\mathcal{L}_{\text{eff.}} \supset \bar{l}_L M_{\text{diag}} l_R + \bar{l}_L \frac{Y_{\text{diag}}}{\sqrt{2}} l_R h + \frac{\kappa_{ij}}{v_\phi} \bar{l}_{L,i} l_{R,j} \phi + h.c.$$

CLFV processes with coupling

$$\tilde{\kappa}_{ij} = \frac{\kappa_{ij}}{v_\phi} = \frac{1}{v_\phi} \left[m_j \sum_{k=1}^3 q_{\bar{L},k} (U_L)_{ik} (U_L)_{jk}^* + m_i \sum_{k=1}^3 q_{R,k} (U_R)_{ik} (U_R)_{jk}^* \right]$$

Higgs-flavon mixing

The scalar potential

$$V(H, \Phi) = -\mu_h^2(H^\dagger H) + \lambda_h(H^\dagger H)^2 - \mu_\phi^2(\Phi^\dagger \Phi) + \lambda_\phi(\Phi^\dagger \Phi)^2 + \lambda_{h\phi}(H^\dagger H)(\Phi^\dagger \Phi)$$

with

$$H = \begin{pmatrix} 0 \\ \frac{v_h + h}{\sqrt{2}} \end{pmatrix}, \quad \Phi = \begin{pmatrix} v_\phi + \phi \\ \sqrt{2} \end{pmatrix}$$

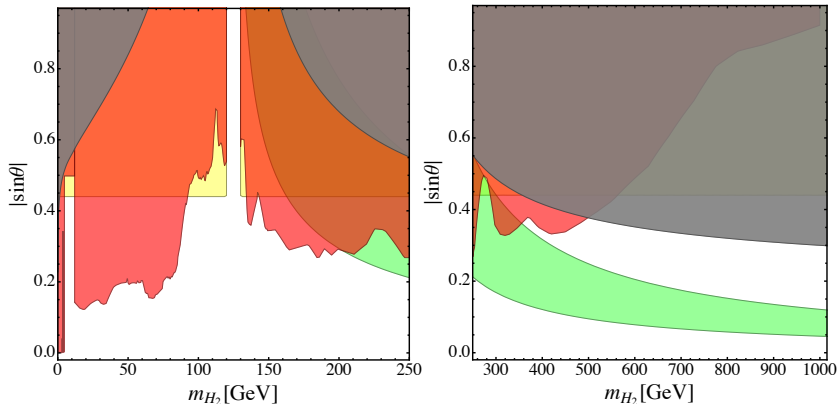
The physical states

$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} \equiv \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \phi \end{pmatrix}$$

where

$$\tan 2\theta = \frac{\lambda_{h\phi} v_h v_\phi}{\lambda_h v_h^2 - \lambda_\phi v_\phi^2}$$

How much Higgs-flavon mixing is allowed?



Excluded at 95 % CL by direct searches (red), precision tests (gray), and H_1 couplings measurements (yellow). [Falkowski,Gross,Lebedev '15]

Bounds from CLFV processes

Observable	Present limit	Experiment
$\text{BR}(\mu \rightarrow eee)$	1.0×10^{-12}	SINDRUM
$\text{BR}(\tau \rightarrow eee)$	3.0×10^{-8}	HFAG
$\text{BR}(\tau \rightarrow \mu\mu\mu)$	2.0×10^{-8}	HFAG
$\text{BR}(\mu \rightarrow e\gamma)$	5.7×10^{-13}	MEG
$\text{BR}(\tau \rightarrow \mu\gamma)$	4.4×10^{-8}	HFAG
$\text{BR}(\tau \rightarrow e\gamma)$	3.3×10^{-8}	HFAG
$\text{BR}(\mu\text{-}e, Au)$	7.0×10^{-13}	Bertl <i>et. al.</i>

Gauged $U(1)$ Froggatt-Nielsen symmetry

Gauged $U(1)$ Froggat-Nielsen symmetry

$G_{SM} \times U'(1)$ symmetry $\rightarrow$ new gauge field with **new gauge coupling**

$$\mathcal{L} \supset D'_\mu \phi^* D'^\mu \phi + g_4 B'_\mu \sum_i q_i \bar{\psi}_{SM_i} \gamma^\mu \psi_{SM_i} + \bar{\chi} (i\partial_\mu + g_4 q' B'_\mu) \gamma^\mu \chi$$

with

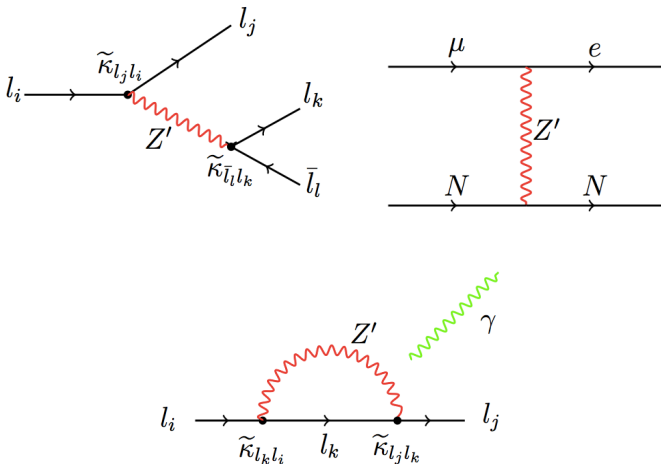
$$D'_\mu = \partial_\mu - i g_4 q' B'_\mu$$

The new massive gauge boson

$$m_{Z'} = |g_4 q_\phi v_\phi| = g_4 v_\phi$$

with $q_\phi = -1$.

CLFV processes mediated by Z'



Gauged $U(1)$ FN symmetry

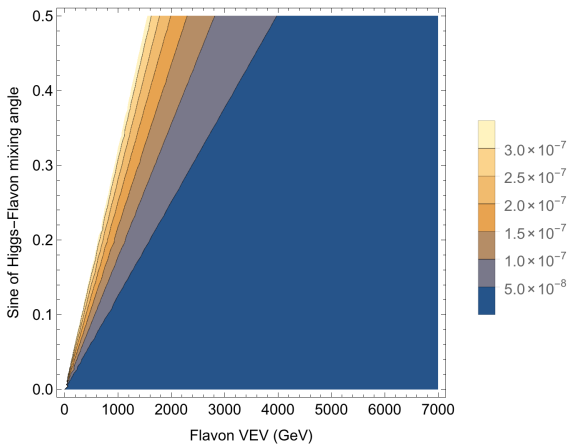
A texture for $\epsilon = 0.01$ satisfying all CLFV bounds

Particle	e_L	e_R	μ_L	μ_R	τ_L	τ_R	H	ϕ
$U'(1)$ charge	2	1	1	1	0	1	0	-1

$$Y = \begin{pmatrix} \epsilon^3 & \epsilon^3 & \epsilon^3 \\ \epsilon^2 & \epsilon^2 & \epsilon^2 \\ \epsilon & \epsilon & \epsilon \end{pmatrix}, \quad \tilde{\kappa} = \frac{1}{v_\phi} \begin{pmatrix} 10^{-3} & 4 \times 10^{-5} & 8 \times 10^{-4} \\ 2 \times 10^{-7} & 0.2 & -0.07 \\ 2.4 \times 10^{-7} & -4 \times 10^{-3} & 1.8 \end{pmatrix}$$

The strongest bound: the $\mu \rightarrow eee$ process leads to $v_\phi > 7 \text{ TeV}$

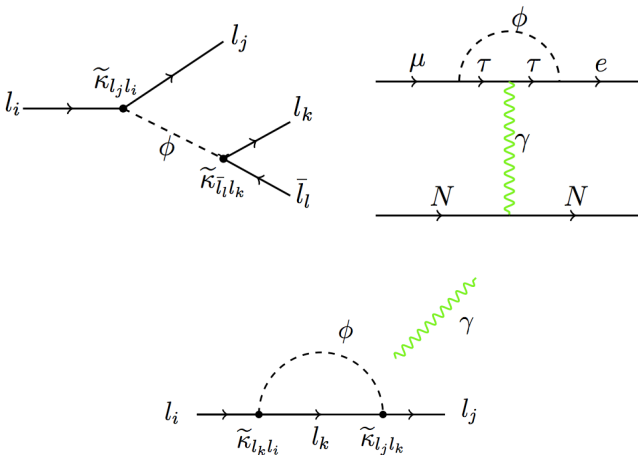
The $\text{BR}(h \rightarrow \mu\tau)$ for $v_\phi > 7 \text{ TeV}$



Discrete Froggatt-Nielsen symmetry

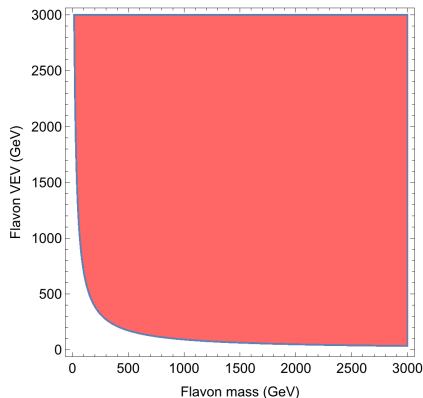
Negligible Higgs-flavon mixing ($\lambda_{h\phi} = 0$)

CLFV processes mediated by **pure flavon**, ϕ



Negligible Higgs-flavon mixing ($\lambda_{h\phi} = 0$)

Strongest bound: the $\mu \rightarrow e\gamma$ process



No contribution to $\text{BR}(h \rightarrow \mu\tau)$

Non-negligible Higgs-flavon mixing ($\lambda_{h\phi} \neq 0$)

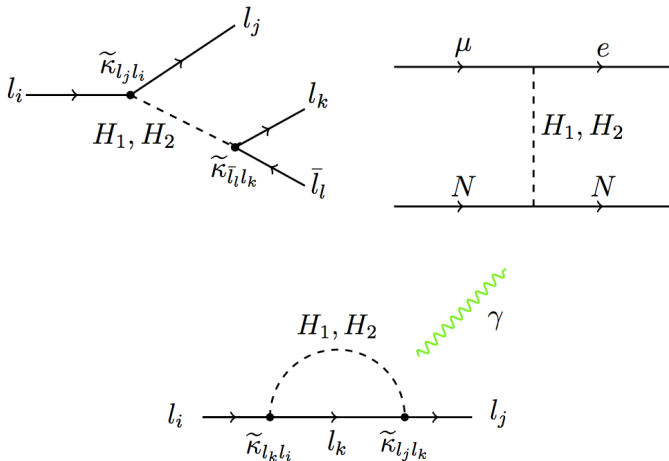
The physical states

$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} \equiv \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h \\ \phi \end{pmatrix}$$

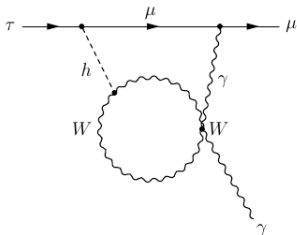
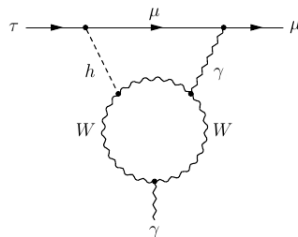
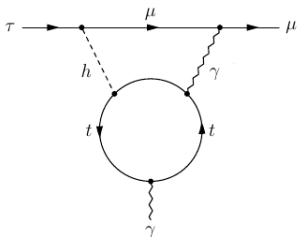
both contribute to CLFV terms

$$\begin{aligned} \mathcal{L} \supset & \left[\cos \theta \frac{y_{ij}^e}{\sqrt{2}} + \sin \theta \tilde{\kappa}_{ij} \right] \bar{l}_i P_R l_j H_1 + \left[\cos \theta \frac{y_{ij}^e}{\sqrt{2}} + \sin \theta \tilde{\kappa}_{ji}^* \right] \bar{l}_i P_L l_j H_1 \\ & + \left[\cos \theta \tilde{\kappa}_{ij} - \sin \theta \frac{y_{ij}^e}{\sqrt{2}} \right] \bar{l}_i P_R l_j H_2 + \left[\cos \theta \tilde{\kappa}_{ji}^* - \sin \theta \frac{y_{ij}^e}{\sqrt{2}} \right] \bar{l}_i P_L l_j H_2 \end{aligned}$$

CLFV processes mediated by H_1 and H_2



CLFV processes mediated by H_1 and H_2



One example

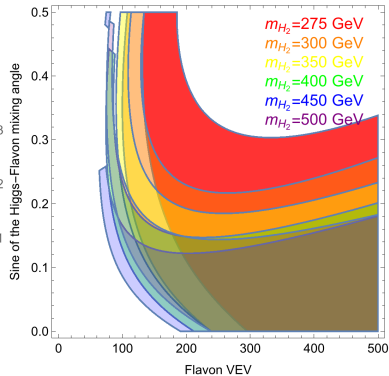
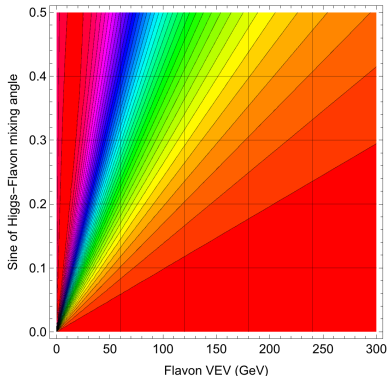
The discrete charge assignments for $\epsilon = 0.1$

Particle	e_L	e_R	μ_L	μ_R	τ_L	τ_R	H	ϕ
Charge	6	0	4	0	2	1	0	-1

The texture satisfying all CLFV bounds

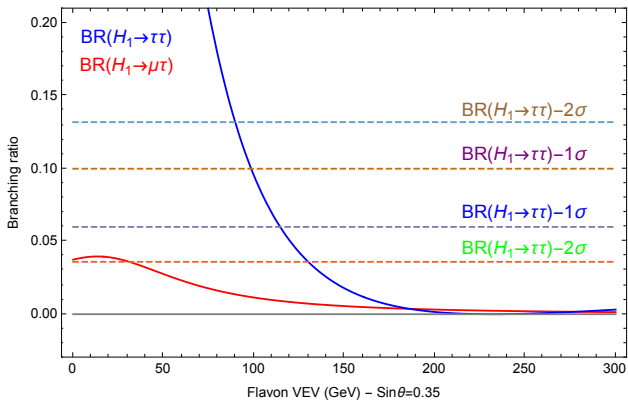
$$Y = \begin{pmatrix} \epsilon^6 & \epsilon^6 & \epsilon^7 \\ \epsilon^4 & \epsilon^4 & \epsilon^5 \\ \epsilon^2 & \epsilon^2 & \epsilon^3 \end{pmatrix}, \quad \tilde{\kappa} = \frac{1}{v_\phi} \begin{pmatrix} 0.003 & -0.0003 & -0.0008 \\ -0.004 & 0.5 & 0.1 \\ 0.08 & -0.9 & 4.5 \end{pmatrix}$$

$\text{BR}(h \rightarrow \mu\tau)$



For $\sin \theta = 0.35$, $v_\phi = 110$ GeV, $m_\phi = 400$ GeV $\rightarrow \text{BR}(h \rightarrow \mu\tau) \simeq 0.01$

$\text{BR}(h \rightarrow \tau\tau)$



Summary

- The combined result for $\text{BR}(h \rightarrow \mu\tau) = 0.8 \pm 0.3$.
- CLFVs are absent in the SM.
- Froggatt-Nielsen mechanism with a discrete symmetry is capable of producing a $\text{BR}(h \rightarrow \mu\tau) \sim 0.1$ while satisfying all bounds.