

# Leptogenesis after Inflation in a Pati-Salam Model

Stuart Raby

Planck 2017  
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DEPARTMENT OF  
PHYSICS

# Subcritical Hybrid Inflation in a Pati-Salam Model

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# Outline

- Subcritical hybrid F-term inflation
- Re-heating
- Pati-Salam 3 family model  
with  $D_4$  family symmetry &  $\mathbb{Z}_4^R$  symmetry
- Yukawa Unification – 3<sup>rd</sup> family only
- Global  $\chi^2$  fits & predictions
- Conclusions

# Subcritical hybrid F-term inflation

B. Charles Bryant & S. Raby [arXiv:1601.03749](#)

Following work on subcritical hybrid D-term inflation by

Buchmuller, Domcke & Schmitz

[J. Cosmol. Astropart. Phys. 11, 006 \(2014\)](#)

Buchmuller & Ishiwata [PRD91, 081302 \(2015\)](#)

$$\begin{aligned}
W_I = & \Phi \left( \kappa \overline{S^c} S^c + m Y + \alpha H H \right) + \lambda X \left( \overline{S^c} S^c - \frac{v_{PS}^2}{2} \right) \\
& + S^c \Sigma S^c + \overline{S^c} \Sigma \overline{S^c} \\
K = & \frac{1}{2} \left( \Phi + \Phi^\dagger \right)^2 + \left( S^c \right)^\dagger S^c + Y^\dagger Y + X^\dagger X \left[ 1 - c_X \frac{X^\dagger X}{M_{Pl}^2} + \alpha_X \left( \frac{X^\dagger X}{M_{Pl}^2} \right)^2 \right]
\end{aligned}$$

$$SU(4)_C \times SU(2)_L \times SU(2)_R \times \mathbb{Z}_4^R$$

$$\begin{aligned}
\Phi, X &= (1, 1, 1, 2), \quad S^c = (\overline{4}, 1, \overline{2}, 0), \quad \overline{S^c} = (4, 1, 2, 0) \\
\Sigma &= (6, 1, 1, 2), \quad Y = (1, 1, 1, 0), \quad H = (1, 2, \overline{2}, 0)
\end{aligned}$$

$$\begin{aligned}
S^c &= \exp(i T_{SU(4)_C/SU(3)} \phi_u^c) \exp(i T_{SU(2)_R/U(1)_R} \phi_e^c) \begin{pmatrix} 0 & \frac{1}{\sqrt{2}} \exp(i T) V^c \\ d_S^c & 0 \end{pmatrix} \\
\overline{S^c} &= \exp(-i T_{SU(4)_C/SU(3)}^T \bar{\phi}_u^c) \exp(-i T_{SU(2)_R/U(1)_R}^T \bar{\phi}_e^c) \begin{pmatrix} 0 & \frac{1}{\sqrt{2}} \exp(-i T) V^c \\ \bar{d}_S^c & 0 \end{pmatrix}
\end{aligned}$$

$$W_I = \Phi (\kappa \overline{S^c} S^c + m Y + \alpha H H) + \lambda X \left( \overline{S^c} S^c - \frac{v_{PS}^2}{2} \right) \\ + S^c \Sigma S^c + \overline{S^c} \Sigma \overline{S^c}$$

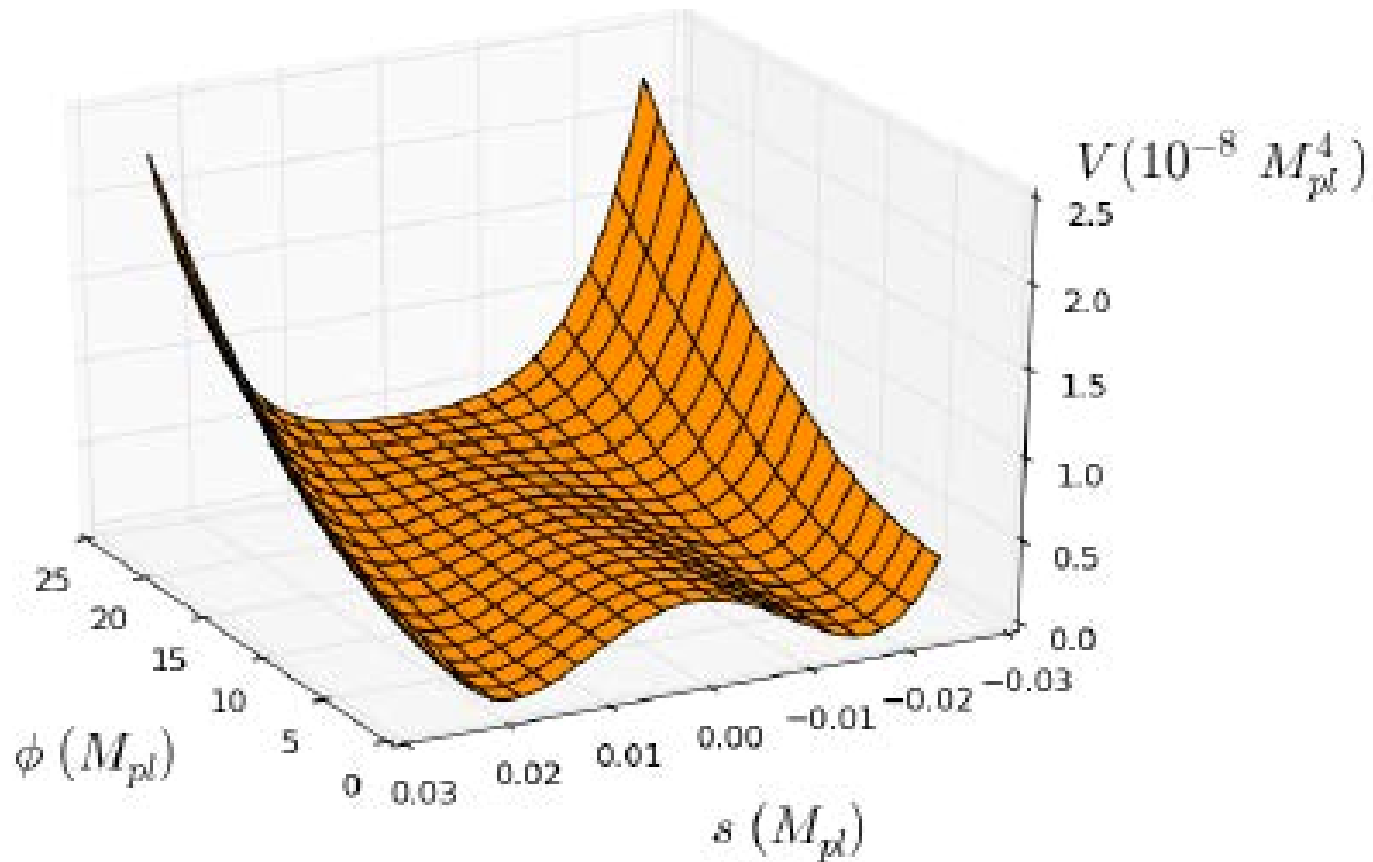
$$S^c = \exp(i T_{SU(4)_C/SU(3)} \phi_u^c) \exp(i T_{SU(2)_R/U(1)_R} \phi_e^c) \begin{pmatrix} 0 & \frac{1}{\sqrt{2}} \exp(i T) V^c \\ d_S^c & 0 \end{pmatrix} \\ \bar{S}^c = \exp(-i T_{SU(4)_C/SU(3)}^T \bar{\phi}_u^c) \exp(-i T_{SU(2)_R/U(1)_R}^T \bar{\phi}_e^c) \begin{pmatrix} 0 & \frac{1}{\sqrt{2}} \exp(-i T) V^c \\ \bar{d}_S^c & 0 \end{pmatrix}$$

$$\Phi \supset \frac{a + i\phi}{\sqrt{2}}, \quad V^c \supset \frac{s + i\tau}{\sqrt{2}}, \quad Y \supset \frac{y + iu}{\sqrt{2}}$$

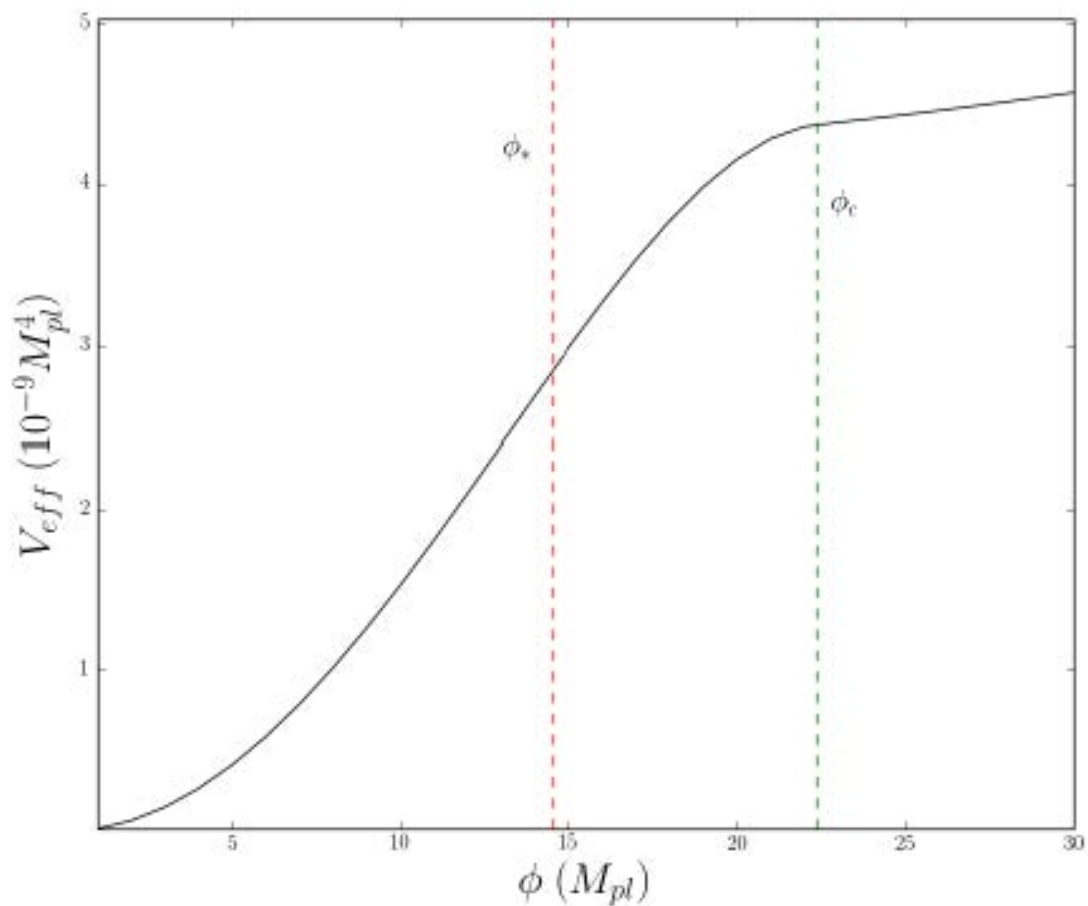
$$s = \sigma + \sqrt{2}v_{PS} \text{ and } y = h - \kappa v_{PS}^2 / \sqrt{2}m$$

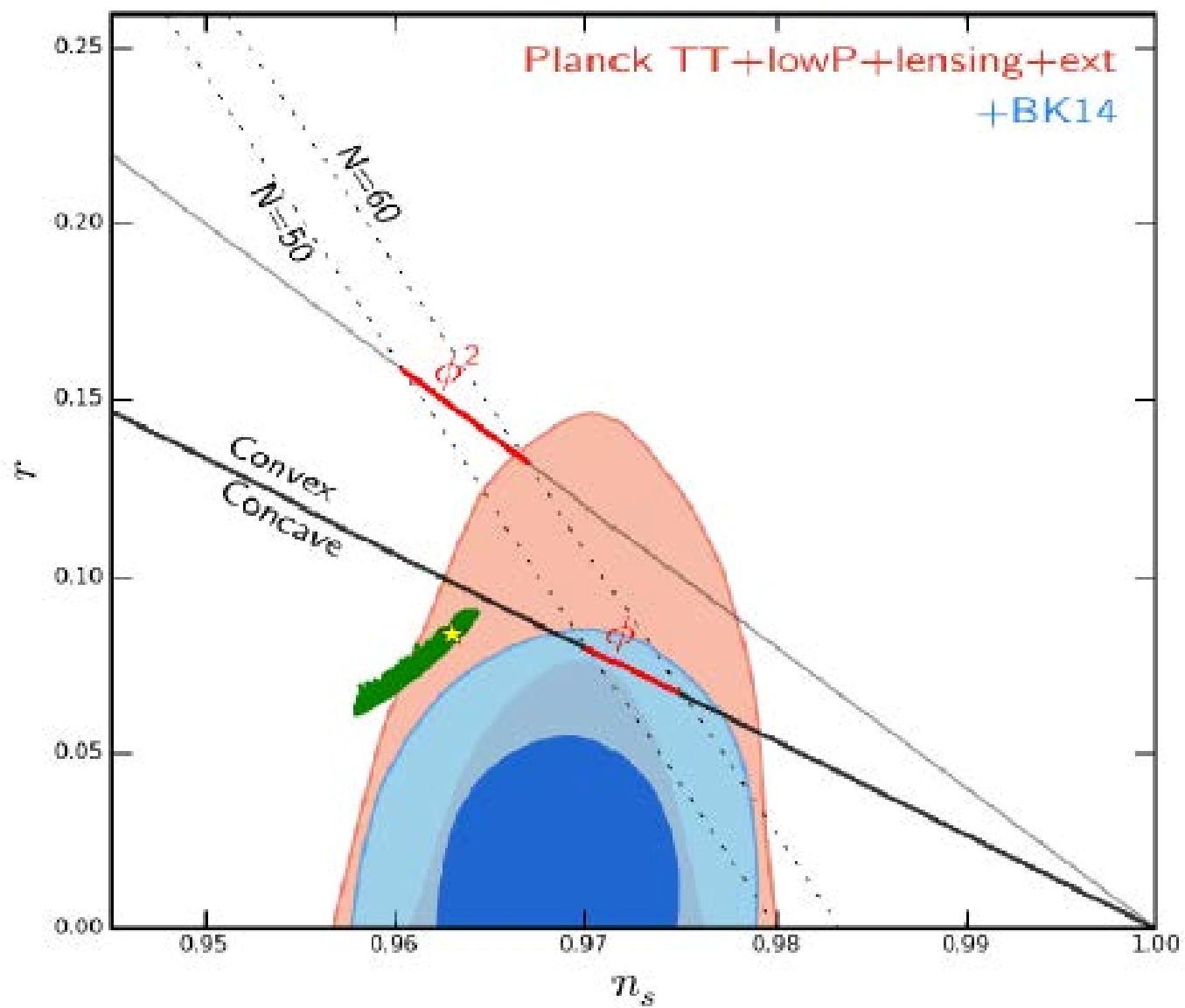
$$V(\phi, s, 0) \simeq \frac{\lambda^2 v_{PS}^4}{4} + \frac{1}{4} (\kappa^2 \phi^2 - \lambda^2 v_{PS}^2) s^2 + \frac{\lambda^2}{16} s^4 + \frac{1}{2} m^2 \phi^2$$

$$\phi_c \equiv \frac{\lambda v_{PS}}{\kappa} \quad \kappa \ll \lambda \quad s_{\min}^2(\phi) = 2v_{PS}^2 \left( 1 - \frac{\phi^2}{\phi_c^2} \right)$$



$$V_{eff}(\phi) = \frac{\lambda^2 v_{PS}^4}{2} \frac{\phi^2}{\phi_c^2} \left[ \left( 1 + \frac{m^2}{\kappa^2 v_{PS}^2} \right) - \frac{\phi^2}{2\phi_c^2} \right] \simeq \frac{\lambda^2 v_{PS}^4}{2} \frac{\phi^2}{\phi_c^2} \left[ 1 - \frac{\phi^2}{2\phi_c^2} \right]$$





At the end of inflation

$$\rho_\phi^0 \approx 5 \times 10^{-11} M_{pl}^4 \quad , \quad \rho_\sigma^0 \approx 7 \times 10^{-14} M_{pl}^4$$

$$\mathcal{W}_\Phi = \alpha \Phi \mathcal{H} \mathcal{H}$$

$$\Gamma_{\phi \rightarrow \tilde{h}_u^0 \tilde{h}_d^0 + \tilde{h}_u^+ \tilde{h}_d^-} \approx \frac{\alpha^2}{8\pi} m$$

Reheat temperature

$$T_R^\phi = \left( \frac{90}{\pi^2 g_*} \Gamma_\phi^2 M_{pl}^2 \right)^{1/4} \Rightarrow T_R^\phi \simeq 2 \times 10^{10} \left( \frac{\alpha}{10^{-4}} \right) \left( \frac{m}{10^{-6} M_{Pl}} \right)^{1/2} \text{ GeV}$$

At the end of inflation  $\mathcal{W}_\Phi = \alpha \Phi \mathcal{H} \mathcal{H}$

A word about leptogenesis

Instant preheating can non-perturbatively create Higgses every time inflaton VEV vanishes

Then when inflaton VEV reaches a maximum the Higgs gets heavy and can decay into right-handed neutrinos and radiation. Right-handed neutrinos decay and produce non-zero lepton asymmetry.

$\varepsilon_3 < 0$  good ,  $\varepsilon_{1,2} > 0$  bad

Problem : reheat temperature is too high and Lepton asymmetry is washed out !!

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# SO(10) Grand Unification

Georgi

Fritzsch & Minkowski

spinor repn.  
of SO(10) -  
16

tensor product  
of 5 spin  $\frac{1}{2}$   
w/even no. + signs

| State       | Y<br>$= \frac{2}{3}\Sigma(C) - \Sigma(W)$ | Color<br>C spins | Weak<br>W spins |
|-------------|-------------------------------------------|------------------|-----------------|
| $\bar{\nu}$ | 0                                         | - - -            | --              |
| $\bar{e}$   | 2                                         | - - -            | ++              |
| $u_r$       | $\frac{1}{3}$                             | + - -            | - +             |
| $d_r$       |                                           | + - -            | + -             |
| $u_b$       |                                           | - + -            | - +             |
| $d_b$       |                                           | - + -            | + -             |
| $u_y$       |                                           | - - +            | - +             |
| $d_y$       |                                           | - - +            | + -             |
| $\bar{u}_r$ | $-\frac{4}{3}$                            | - + +            | --              |
| $\bar{u}_b$ |                                           | + - +            | --              |
| $\bar{u}_y$ |                                           | + + -            | --              |
| $\bar{d}_r$ | $\frac{2}{3}$                             | - + +            | ++              |
| $\bar{d}_b$ |                                           | + - +            | ++              |
| $\bar{d}_y$ |                                           | + + -            | ++              |
| $\nu$       | -1                                        | + + +            | - +             |
| e           |                                           | + + +            | + -             |

1

10

5

$$\text{SO}(10) \rightarrow \text{SU}(5) \otimes \text{U}(1)$$

$$\rightarrow \text{SO}(6) \otimes \text{SO}(4) \approx \text{SU}(4)_C \otimes \text{SU}(2)_L \otimes \text{SU}(2)_R$$

$$Q = \begin{pmatrix} u & u & u & \nu \\ d & d & d & e \end{pmatrix} \quad \bar{Q} = \begin{pmatrix} \bar{u} & \bar{u} & \bar{u} & \bar{\nu} \\ \bar{d} & \bar{d} & \bar{d} & \bar{e} \end{pmatrix}$$

$$Q = (4, 2, 1)$$

$$\bar{Q} = (\bar{4}, 1, \bar{2})$$

Lepton number is the 4<sup>th</sup> Color !!

Pati-Salam  $\text{SU}(4)_C \times \text{SU}(2)_L \times \text{SU}(2)_R$

$$Q_{EM} = \frac{1}{2}(B - L) + T_L^3 + T_R^3$$

# Unique $\mathbb{Z}_4^R$ symmetry for the MSSM

Lee, Raby, Ratz, Ross, Shieren, Schmidt-Hoberg & Vaudrevange  
Phys.Lett. B694, 491-495 (2011)  
Nucl.Phys. B850, 1-30 (2011)

Kappl, Peterson, Raby, Ratz, Schieren & Vaudrevange  
Nucl.Phys. B847, 2325-349 (2011)

$\mathbb{Z}_4^R$  symmetry - anomaly cancelled by Green-Schwartz

$$A_{SU(4)_C - SU(4)_C - \mathbb{Z}_4^R} = A_{SU(2)_L - SU(2)_L - \mathbb{Z}_4^R} = A_{SU(2)_R - SU(2)_R - \mathbb{Z}_4^R} = 1(\text{mod}(2))$$

Forbids  $QQQQ, Q^c Q^c Q^c Q^c, QQQ^c Q^c, HH$   
 $S^c Q^c Q^c Q^c + \dots$

$$\text{under } \mathbb{Z}_4^R : S \rightarrow S + \frac{i}{2} \Delta_{GS}$$

$$\langle W \rangle_{np} \sim \exp(-\langle S \rangle) \sim m_{3/2} M_{Pl}^2$$

$$\Rightarrow \frac{m_{3/2}}{M_{Pl}^2} QQQQ, m_{3/2} HH$$

Suppresses  $\mu$  and Dimension 5 proton decay ops.  
Preserves R parity !!

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Soft SUSY breaking terms

$m_{16}^2$  Universal scalar masses

$m_{10}^2 \pm \Delta m_H^2 \rightarrow NUHM2$

$A_0$  Universal  $A$  parameter,  $\mu, \tan\beta$

$M_i (\lambda_i \lambda_i), i = 1, 2, 3$

$M_i = M_{1/2}$

$m_{16}, m_{10} \pm \Delta m_H^2, A_0, M_{1/2}, \mu, \tan\beta$

# Yukawa Unification & Soft SUSY breaking

|                                               |                               |
|-----------------------------------------------|-------------------------------|
| Blazek, Dermisek & Raby                       | PRL 88, 111804 (2002)         |
|                                               | PRD 65, 115004 (2002)         |
| Baer & Ferrandis,                             | PRL 87, 211803 (2001)         |
| Auto, Baer, Balazs, Belyaev, Ferrandis & Tata | JHEP 0306:023 (2003)          |
| Tobe & Wells                                  | NPB 663, 123 (2003)           |
| Dermisek & Raby                               | Phys. Lett. B 622, 327 (2005) |
| Baer, Kraml, Sekmen & Summy                   | JHEP 0909:005 (2009)          |
| Anandakrishnan, Raby & Wingerter              | arXiv:1212.0542               |
| Anandakrishnan & Raby                         | arXiv:1303.5125               |
| Anandakrishnan, Bryant & Raby                 | arXiv:1404.5628               |
| Poh & Raby                                    | arXiv:1505.00264              |

$$\lambda \quad \overline{Q}_3 \quad H \quad Q_3$$

$$\lambda_t = \lambda_b = \lambda_\tau = \lambda_{\nu_\tau} \equiv \lambda$$

Note, CANNOT predict top mass due to large SUSY threshold corrections to bottom and tau mass

Hall, Rattazzi & Sarid

Carena, Olechowski, Pokorski & Wagner

So instead use Yukawa unification to predict soft SUSY breaking masses !!

## Bottom mass corrections

$$\frac{\delta m_b}{m_b} \propto \frac{\alpha_3 \mu M_{\tilde{g}} \tan \beta}{m_{\tilde{b}}^2} + \frac{\lambda_t^2 \mu A_t \tan \beta}{m_{\tilde{t}}^2} + \log \text{corr.}$$

$$\frac{\delta m_b}{m_b} \leq -2\%$$

Needed to fit data

$$\mu M_{\tilde{g}} > 0 \quad \Rightarrow \quad \mu A_t < 0$$

Anandakrishnan, Raby & Wingerter

arXiv:1212.0542

Anandakrishnan, Bryant & Raby

arXiv:1404.5628

Global  $\chi^2$  analysis  
3<sup>rd</sup> family only

# Yukawa Unification

$$\lambda \quad 16_3 \quad 10 \quad 16_3$$

~ Universal Gaugino Masses

Fit t,b,tau requires

$$A_0 \approx -2m_{16} \quad m_{10} \approx \sqrt{2}m_{16}$$

$$m_{16} > \text{few TeV} \quad \mu, M_{1/2} \ll m_{16}$$

$$\tan \beta \approx 50$$

# Inverted scalar mass hierarchy

Bagger, Feng, Polonsky & Zhang  
PLB473, 264 (2000)

Third family scalars lighter than first two !

Suppresses flavor & CP violation

$$A_0 \approx -2m_{16} \quad m_{10} \approx \sqrt{2}m_{16}$$

$$m_{16} > \text{few TeV} \quad \mu, M_{1/2} \ll m_{16}$$

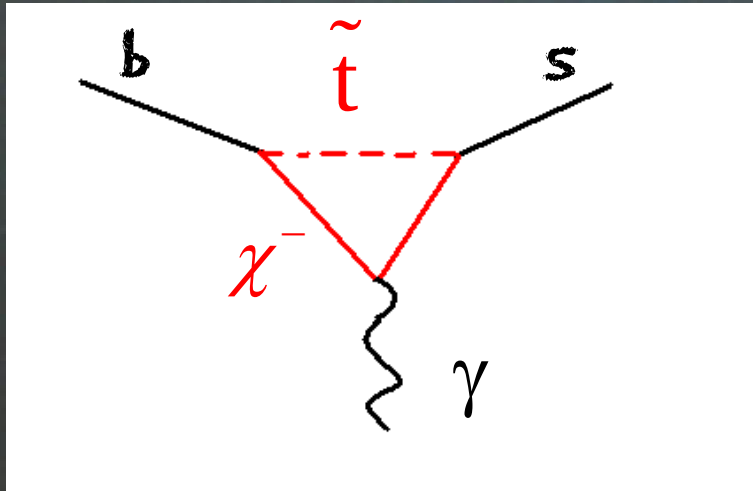
$$\tan \beta \approx 50$$

Heavy scalars

# Need Heavy scalars !

$$BR(B \rightarrow X_s \gamma) = (3.55 \pm 0.26) \times 10^{-4} \quad \text{Exp.}$$

$$BR(B \rightarrow X_s \gamma)_{SM} = (3.15 \pm 0.23) \times 10^{-4} \quad \text{NNLO Th.}$$



$$C_7^{eff} = C_7^{SM} + C_7^{SUSY}$$

$$C_7^{eff} \approx \mp C_7^{SM}$$

$$C_7^{\chi^+} \propto \frac{\mu A_t}{\tilde{m}_2} \tan \beta \times \text{sign}(C_7^{SM}) \approx \begin{Bmatrix} -2C_7^{SM} \\ 0 \end{Bmatrix}$$

$$\mu M_{\tilde{g}} > 0 \Rightarrow \mu A_t < 0$$

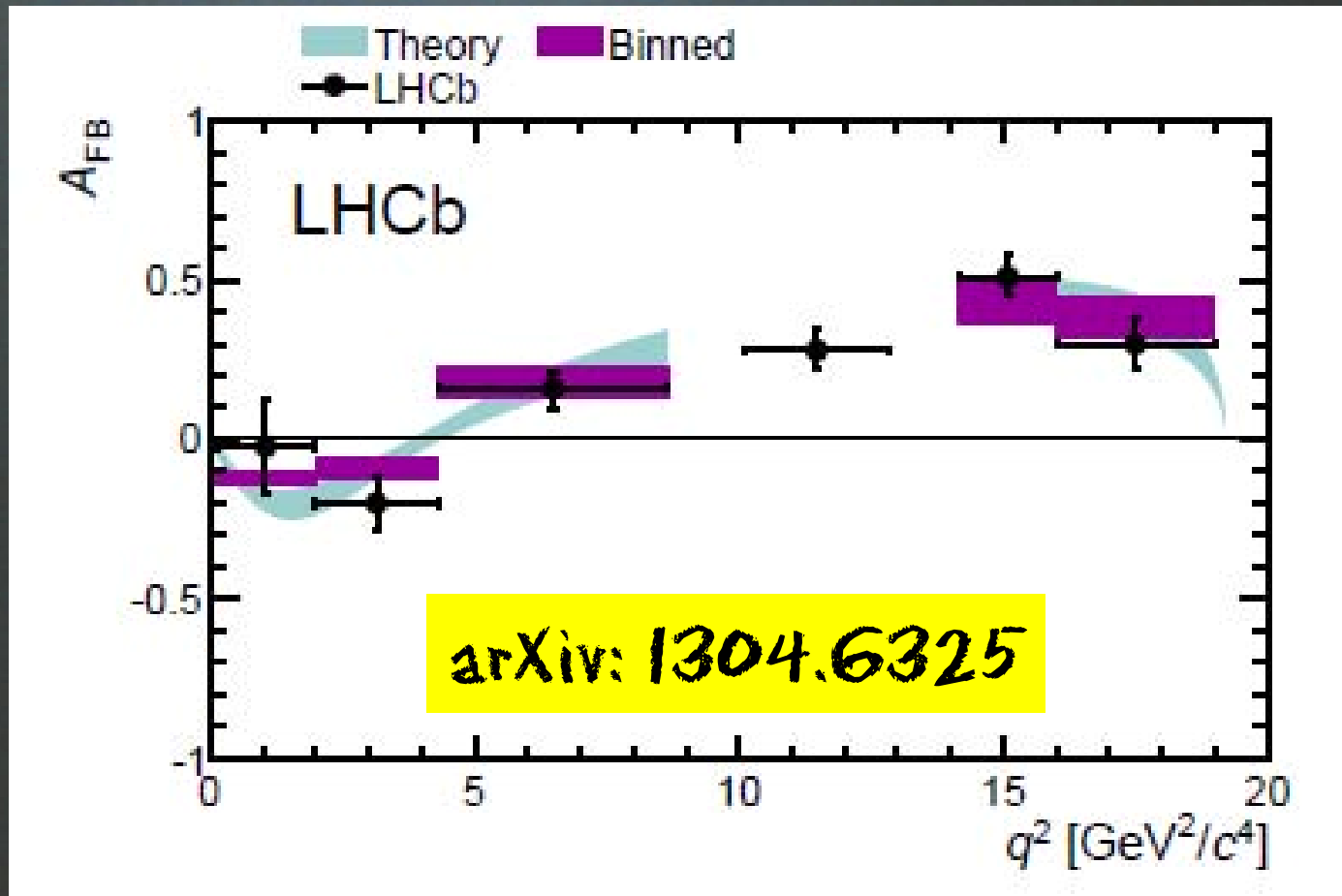
$$m_{16} \sim 4-5 \text{ TeV}$$

light squarks and sleptons !!

$$C_7^{\chi^+} \approx -2C_7^{\text{SM}} \quad \text{or}$$

$$C_7 = C_7^{\text{SM}} + C_7^{\chi^+} \approx -C_7^{\text{SM}}$$

*LHCb*  $\text{BR}(B \rightarrow K^* \mu^+ \mu^-)$  favors  $C_7 \approx +C_7^{\text{SM}}$



tension between  $b \rightarrow s \gamma$  &  $b \rightarrow s l^+ l^-$

Albrecht, Altmannshofer, Buras, Guadagnoli, & Straub  
JHEP 0710:055 (2007)

$$C_7^{\chi^+} \approx 0 \quad \text{or}$$

$$C_7 = C_7^{\text{SM}} + C_7^{\chi^+} \approx +C_7^{\text{SM}}$$

$$\Rightarrow m_{16} \geq 8 \text{ TeV}$$

Albrecht, Altmannshofer, Buras, Guadagnoli, & Straub  
**JHEP 0710:055 (2007)**

|                                                      |        |
|------------------------------------------------------|--------|
| $m_{16}$                                             | 10000  |
| $\mu$                                                | 1200   |
| $\text{BR}(B_s \rightarrow \mu^+ \mu^-) \times 10^8$ | 2.1    |
| $\hat{s}_0$                                          | 0.14   |
| $\text{BR}(\mu \rightarrow e \gamma) \times 10^{13}$ | 0.0026 |
| $\delta a_\mu^{\text{SUSY}} \times 10^{10}$          | +0.52  |
| $M_{h_0}$                                            | 129    |
| $M_A$                                                | 842    |
| $m_{\tilde{t}_1}$                                    | 1903   |
| $m_{\tilde{b}_1}$                                    | 2366   |
| $m_{\tilde{\tau}_1}$                                 | 3933   |
| $m_{\tilde{\chi}_1^0}$                               | 60     |
| $m_{\tilde{\chi}_1^+}$                               | 120    |
| $m_{\tilde{g}}$                                      | 506    |

Albrecht, Altmannshofer, Buras, Guadagnoli, & Straub  
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Light Higgs  
SM-like

# $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ : Light Higgs SM-like

SM:  $3 \times 10^{-9}$

MSSM:  $\sim (\tan \beta)^6 / m_A^4$

CDF  $1.8^{+1.8}_{-0.9} \times 10^{-8}$  (95% CL) w/  $7 \text{ fb}^{-1}$

LHCb  $(2.9^{+1.1}_{-1.0}) \times 10^{-9}$

w/  $1 \text{ fb}^{-1}$  (7TeV) +  $2 \text{ fb}^{-1}$  (8TeV)

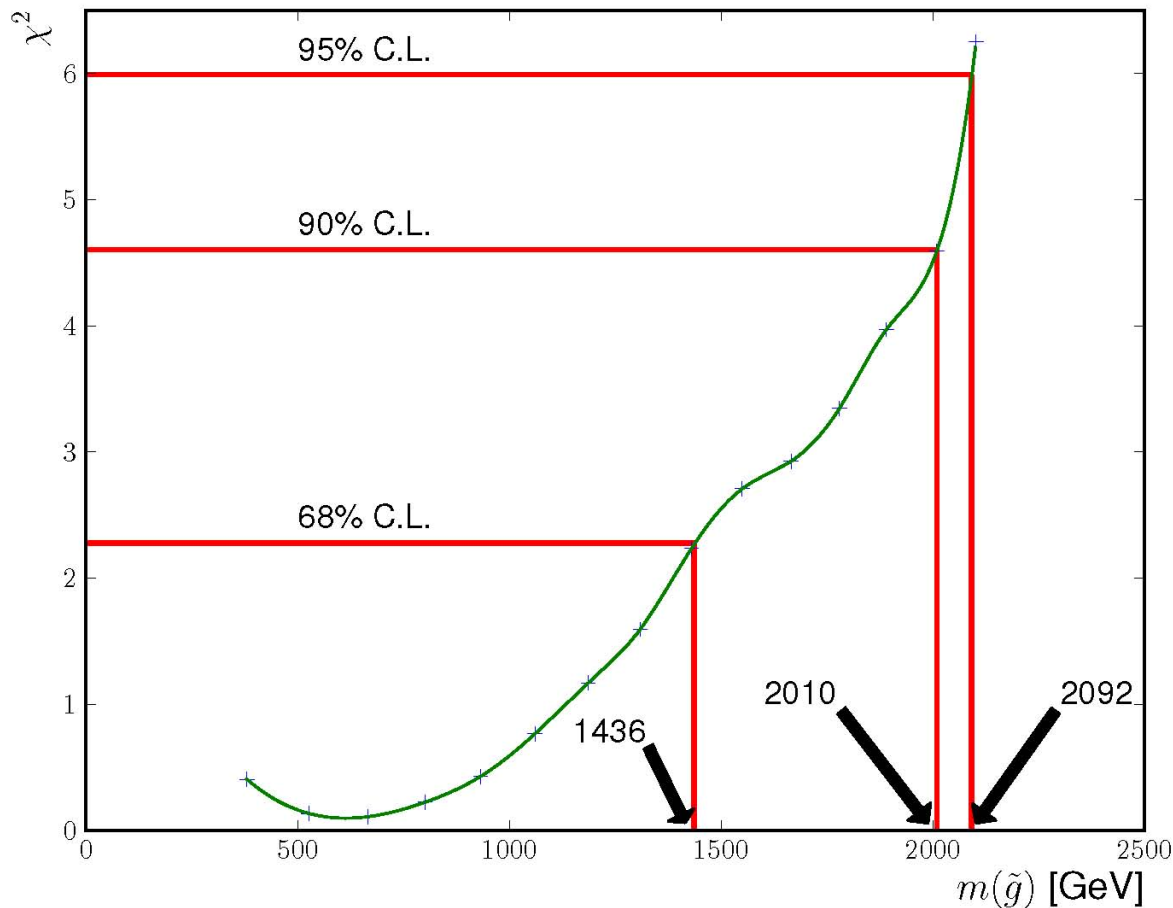
$m_A \geq 1 \text{ TeV}$

$m_A \sim m_H \sim m_{H^\pm} \Rightarrow h \text{ SM-like}$

# Gluino mass bound - Third family only

Anandakrishnan, Raby & Wingerter

$m_{16} = 20 \text{ TeV}$ ,  $M_{1/2}$  varied  $\rightarrow$  2 d.o.f.



# Summary

## First order results

### Third family only

- Universal scalar masses  $\sim 25$  TeV
- Third family scalars much lighter
- Light Higgs is SM-like
- Gluinos want to be light,  
But constrained by data !

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Three family model  
gives good fits  
to low energy data

In this talk we introduce a new  
Yukawa sector with  
two new real parameters

First before – then after adding  
New parameters

$$\begin{aligned}
W_{\text{PS}} = & \lambda Q_3 \mathcal{H} Q_3^c + Q_a \mathcal{H} F_a^c + F_a \mathcal{H} Q_a^c \\
& + \bar{F}_a^c \left( M_F F_a^c + 15 \frac{\phi_a}{\hat{M}} Q_3^c + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a^c + A Q_a^c \right) \\
& + \bar{F}_a \left( M_F F_a + 15 \frac{\phi_a}{\hat{M}} Q_3 + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a + A Q_a \right)
\end{aligned}$$

$$\{Q_3, Q_a, F_a\} = (4, 2, 1, 1), \quad \{Q_3^c, Q_a^c, F_a^c\} = (\bar{4}, \bar{2}, 1, 1)$$

$\phi_a, \theta_a, B_2, A$  flavon fields

$a = 1, 2$   $D_4$  family index

$$M_F \propto 1 + \alpha X + \beta Y, \quad \langle 15 \rangle \propto B - L$$

# Global $\chi^2$ analysis

| Sector           | #  | Parameters                                                           |
|------------------|----|----------------------------------------------------------------------|
| gauge            | 3  | $\alpha_G, M_G, \epsilon_3,$                                         |
| SUSY (GUT scale) | 5  | $m_{16}, M_{1/2}, A_0, m_{H_u}, m_{H_d},$                            |
| textures         | 11 | $\epsilon, \epsilon', \lambda, \rho, \sigma, \tilde{\epsilon}, \xi,$ |
| neutrino         | 3  | $M_{R_1}, M_{R_2}, M_{R_3},$                                         |
| SUSY (EW scale)  | 2  | $\tan \beta, \mu$                                                    |

Poh & Raby [arXiv:1505.00264](#)

24 parameters at GUT scale

45 Low energy observables

Before  $m_{16} = 25 \text{ TeV}$

| Observable                        | Fit      | Exp.     | Pull   | $\sigma$ |
|-----------------------------------|----------|----------|--------|----------|
| $M_Z$                             | 91.1876  | 91.1876  | 0.0000 | 0.4535   |
| $M_W$                             | 80.4507  | 80.3850  | 0.1633 | 0.4025   |
| $1/\alpha_{\text{em}}$            | 137.7125 | 0.0073   | 0.9825 | 0.6886   |
| $G_\mu \times 10^5$               | 1.1732   | 1.1664   | 0.5798 | 0.0117   |
| $\alpha_3(M_Z)$                   | 0.1188   | 0.1185   | 0.4140 | 0.0008   |
| $M_t$                             | 174.1882 | 173.2100 | 0.7927 | 1.2340   |
| $m_b(m_b)$                        | 4.1954   | 4.1800   | 0.4220 | 0.0366   |
| $m_\tau$                          | 1.7781   | 1.7768   | 0.1417 | 0.0089   |
| $M_b - M_c$                       | 3.1568   | 3.4500   | 0.9175 | 0.3196   |
| $m_c(m_c)$                        | 1.2595   | 1.2750   | 0.5993 | 0.0258   |
| $m_s(2\text{GeV})$                | 0.0939   | 0.0950   | 0.2147 | 0.0050   |
| $m_d / m_s(2\text{GeV})$          | 0.0701   | 0.0513   | 2.8052 | 0.0067   |
| $1/Q^2$                           | 0.0018   | 0.0019   | 0.5139 | 0.0001   |
| $M_\mu$                           | 0.1056   | 0.1057   | 0.1818 | 0.0005   |
| $M_e \times 10^4$                 | 5.1145   | 5.1100   | 0.1749 | 0.0256   |
| $ V_{us} $                        | 0.2244   | 0.2253   | 0.6763 | 0.0014   |
| $ V_{cb} $                        | 0.0404   | 0.0408   | 0.1729 | 0.0021   |
| $ V_{ub}  \times 10^3$            | 3.1033   | 3.8500   | 0.8681 | 0.8601   |
| $ V_{td}  \times 10^3$            | 8.8101   | 8.4000   | 0.6817 | 0.6016   |
| $ V_{ts} $                        | 0.0396   | 0.0400   | 0.1531 | 0.0027   |
| $\sin 2\beta$                     | 0.6270   | 0.6820   | 2.8562 | 0.0193   |
| $\epsilon_K$                      | 0.0022   | 0.0022   | 0.2052 | 0.0002   |
| $\Delta M_{B_s} / \Delta M_{B_d}$ | 35.3739  | 35.0345  | 0.0479 | 7.0854   |
| $\Delta M_{B_d} \times 10^{13}$   | 3.9433   | 3.3370   | 0.7681 | 0.7894   |

| Observable                                                                         | Fit      | Exp.     | Pull    | $\sigma$ |
|------------------------------------------------------------------------------------|----------|----------|---------|----------|
| $m_{21}^2 \times 10^5$                                                             | 7.6562   | 7.5550   | 0.1886  | 0.5364   |
| $m_{31}^2 \times 10^3$                                                             | 2.4631   | 2.4620   | 0.0077  | 0.1455   |
| $\sin^2 \theta_{12}$                                                               | 0.3170   | 0.3070   | 0.2689  | 0.0370   |
| $\sin^2 \theta_{23}$                                                               | 0.6264   | 0.5125   | 0.8722  | 0.1305   |
| $\sin^2 \theta_{13}$                                                               | 0.0149   | 0.0218   | 2.1658  | 0.0032   |
| $\theta_{13} \approx 7^\circ$                                                      |          |          |         |          |
| $M_h$                                                                              | 124.5054 | 125.7000 | 0.3947  | 3.0265   |
| $BR(B \rightarrow s\gamma) \times 10^4$                                            | 2.6840   | 3.4300   | 0.5789  | 1.2887   |
| $BR(B_s \rightarrow \mu^+\mu^-) \times 10^9$                                       | 3.0247   | 2.8000   | 0.2429  | 0.9252   |
| $BR(B_d \rightarrow \mu^+\mu^-) \times 10^{10}$                                    | 1.1022   | 3.9000   | 1.7323  | 1.6151   |
| $BR(B \rightarrow \tau\nu) \times 10^5$                                            | 6.1884   | 11.4000  | 1.3727  | 3.7966   |
| $BR(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6\text{GeV}^2} \times 10^8$      | 4.7640   | 3.4000   | 0.2707  | 5.0381   |
| $BR(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16\text{GeV}^2} \times 10^8$ | 7.5110   | 5.6000   | 0.1336  | 14.3059  |
| $q_0^2(A_{\text{FB}}(B \rightarrow K^*\mu^+\mu^-))$                                | 3.6690   | 4.9000   | 0.9579  | 1.2850   |
| $F_L(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6\text{GeV}^2}$                 | 0.7225   | 0.6500   | 0.2149  | 0.3374   |
| $F_L(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16\text{GeV}^2}$            | 0.3108   | 0.3300   | 0.0726  | 0.2644   |
| $P_2(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6\text{GeV}^2}$                 | 0.0228   | 0.3300   | 2.5196  | 0.1219   |
| $P_2(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16\text{GeV}^2}$            | -0.4336  | -0.5000  | 0.3364  | 0.1974   |
| $P'_4(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6\text{GeV}^2}$                | 0.5820   | 0.5800   | 0.0050  | 0.4001   |
| $P'_4(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16\text{GeV}^2}$           | 1.2190   | -0.1800  | 1.7066  | 0.8198   |
| $P'_5(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6\text{GeV}^2}$                | -0.4455  | 0.2100   | 2.2578  | 0.2903   |
| $P'_5(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16\text{GeV}^2}$           | -0.7116  | -0.7900  | 0.1552  | 0.5052   |
| Total $\chi^2$                                                                     |          |          | 48.8413 |          |

New Yukawa sector with  
two new real parameters

Now after adding  
New parameters

$$\begin{aligned}
W_{\text{PS}} = & \lambda Q_3 \mathcal{H} Q_3^c + Q_a \mathcal{H} F_a^c + F_a \mathcal{H} Q_a^c \\
& + \bar{F}_a^c \left( M_F F_a^c + 15 \frac{\phi_a}{\hat{M}} Q_3^c + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a^c + A Q_a^c + \Theta' Q_a^c + \frac{\tilde{\Theta}_a}{\hat{M}} Q_a^c \right) \\
& + \bar{F}_a \left( M_F F_a + 15 \frac{\phi_a}{\hat{M}} Q_3 + 15 \frac{\tilde{\phi}_a}{\hat{M}} Q_a + A Q_a + \Theta' Q_a - \frac{\tilde{\Theta}_a}{\hat{M}} Q_a \right)
\end{aligned}$$

$$\{Q_3, Q_a, F_a\} = (4, 2, 1, 1), \quad \{Q_3^c, Q_a^c, F_a^c\} = (\bar{4}, \bar{2}, 1, 1)$$

$$\phi_a, \theta_a, B_2, A, \left\{ \tilde{\theta}_a, \theta' \right\} \quad \text{flavon fields}$$

$$a = 1, 2 \quad D_4 \text{ family index}$$

$$M_F \propto 1 + \alpha X + \beta Y, \quad \langle 15 \rangle \propto B - L$$

$$\tilde{\theta}_a, \theta' \text{ terms added (real), } \alpha, \beta \text{ now complex}$$

$$\begin{aligned}
\mathcal{W}_{neutrino} &= \bar{S}^c (\lambda_2 N_a Q_a^c + \lambda_3 N_3 Q_3^c) \\
&\quad - \frac{1}{2} (\lambda'_2 Y N_a N_a + \frac{\tilde{\theta}_a \tilde{\theta}_b}{\hat{M}} N_a N_b + \lambda'_3 Y N_3 N_3) \\
&= \frac{\lambda_2^2}{2 M_1} (\bar{S}^c Q_1^c)^2 + \frac{\lambda_2^2}{2 M_2} (\bar{S}^c Q_2^c)^2 + \frac{\lambda_3^2}{2 M_3} (\bar{S}^c Q_3^c)^2,
\end{aligned}$$

$$M_1 = \lambda'_2 Y, \quad M_2 = \lambda'_2 Y + \frac{\tilde{\theta}_2^2}{\hat{M}}, \quad M_3 = \lambda'_3 Y$$

$$\Rightarrow \frac{1}{2} M_{R_1} \overline{\nu_1} \nu_1 + \frac{1}{2} M_{R_2} \overline{\nu_2} \nu_2 + \frac{1}{2} M_{R_3} \overline{\nu_3} \nu_3$$

$$\begin{aligned}
Y_u &= \begin{pmatrix} -\tilde{\theta}G_{1,-\frac{4}{3};1,\frac{1}{3}}^- & \epsilon'G_{1,-\frac{4}{3};1,\frac{1}{3}}^- + \theta'G_{1,-\frac{4}{3};1,\frac{1}{3}}^+ & -\epsilon\xi G_{1,-\frac{4}{3}} \\ -\epsilon'G_{1,-\frac{4}{3};1,\frac{1}{3}}^- + \theta'G_{1,-\frac{4}{3};1,\frac{1}{3}}^+ & \tilde{\epsilon}G_{1,-\frac{4}{3};1,\frac{1}{3}}^- & -\epsilon G_{1,-\frac{4}{3}} \\ \epsilon\xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \\
Y_d &= \begin{pmatrix} -\tilde{\theta}G_{-3,\frac{2}{3};1,\frac{1}{3}}^- & \epsilon'G_{-3,\frac{2}{3};1,\frac{1}{3}}^- + \theta'G_{-3,\frac{2}{3};1,\frac{1}{3}}^+ & -\epsilon\xi G_{-3,\frac{2}{3}} \\ -\epsilon'G_{-3,\frac{2}{3};1,\frac{1}{3}}^- + \theta'G_{-3,\frac{2}{3};1,\frac{1}{3}}^+ & \tilde{\epsilon}G_{-3,\frac{2}{3};1,\frac{1}{3}}^- & -\epsilon G_{-3,\frac{2}{3}} \\ \epsilon\xi G_{1,\frac{1}{3}} & \epsilon G_{1,\frac{1}{3}} & \lambda \end{pmatrix}, \\
Y_e &= \begin{pmatrix} \tilde{\theta}G_{-3,-1;1,2}^- & -\epsilon'G_{-3,-1;1,2}^- + \theta'G_{-3,-1;1,2}^+ & 3\epsilon\xi G_{1,2} \\ \epsilon'G_{-3,-1;1,2}^- + \theta'G_{-3,-1;1,2}^+ & 3\tilde{\epsilon}G_{-3,-1;1,2}^- & 3\epsilon G_{1,2} \\ -3\epsilon\xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix}, \\
Y_\nu &= \begin{pmatrix} \tilde{\theta}G_{-3,-1;5,0}^- & -\epsilon'G_{-3,-1;5,0}^- + \theta'G_{-3,-1;5,0}^+ & 3\epsilon\xi G_{5,0} \\ \epsilon'G_{-3,-1;5,0}^- + \theta'G_{-3,-1;5,0}^+ & 3\tilde{\epsilon}G_{-3,-1;5,0}^- & 3\epsilon G_{5,0} \\ -3\epsilon\xi G_{-3,-1} & -3\epsilon G_{-3,-1} & \lambda \end{pmatrix},
\end{aligned}$$

$$G_{x,y} = \frac{M_0}{M_\chi} = \frac{1}{1 + \alpha x + \beta y}$$

$$G_{x_1,y_1;x_2,y_2}^\pm = G_{x_1,y_1} \pm G_{x_2,y_2}$$

# New Global $\chi^2$ analysis

| Sector           | Input Parameters                                                                                                                                         | No. |
|------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------|-----|
| Gauge            | $\alpha_G, M_G, \epsilon_3$                                                                                                                              | 3   |
| SUSY (GUT scale) | $m_{16}, M_{1/2}, A_0, m_{H_u}, m_{H_d}$                                                                                                                 | 5   |
| Yukawa Textures  | $\lambda, \epsilon, \tilde{\epsilon}, \epsilon', \xi, \alpha, \beta, \theta', \tilde{\theta}, \phi_{\epsilon'}, \phi_{\xi}, \phi_{\alpha}, \phi_{\beta}$ | 13  |
| Neutrino         | $M_{R_1}, M_{R_2}, M_{R_3}$                                                                                                                              | 3   |
| SUSY (EW Scale)  | $\tan \beta, \mu$                                                                                                                                        | 2   |
| Total            |                                                                                                                                                          | 26  |

Poh, Raby and Wang arXiv:1703.09309

Vary 24 parameters at GUT/EW scale -  
 $m_{16}, M_{1/2}$  fixed

51 Observables in  $\chi^2$  function

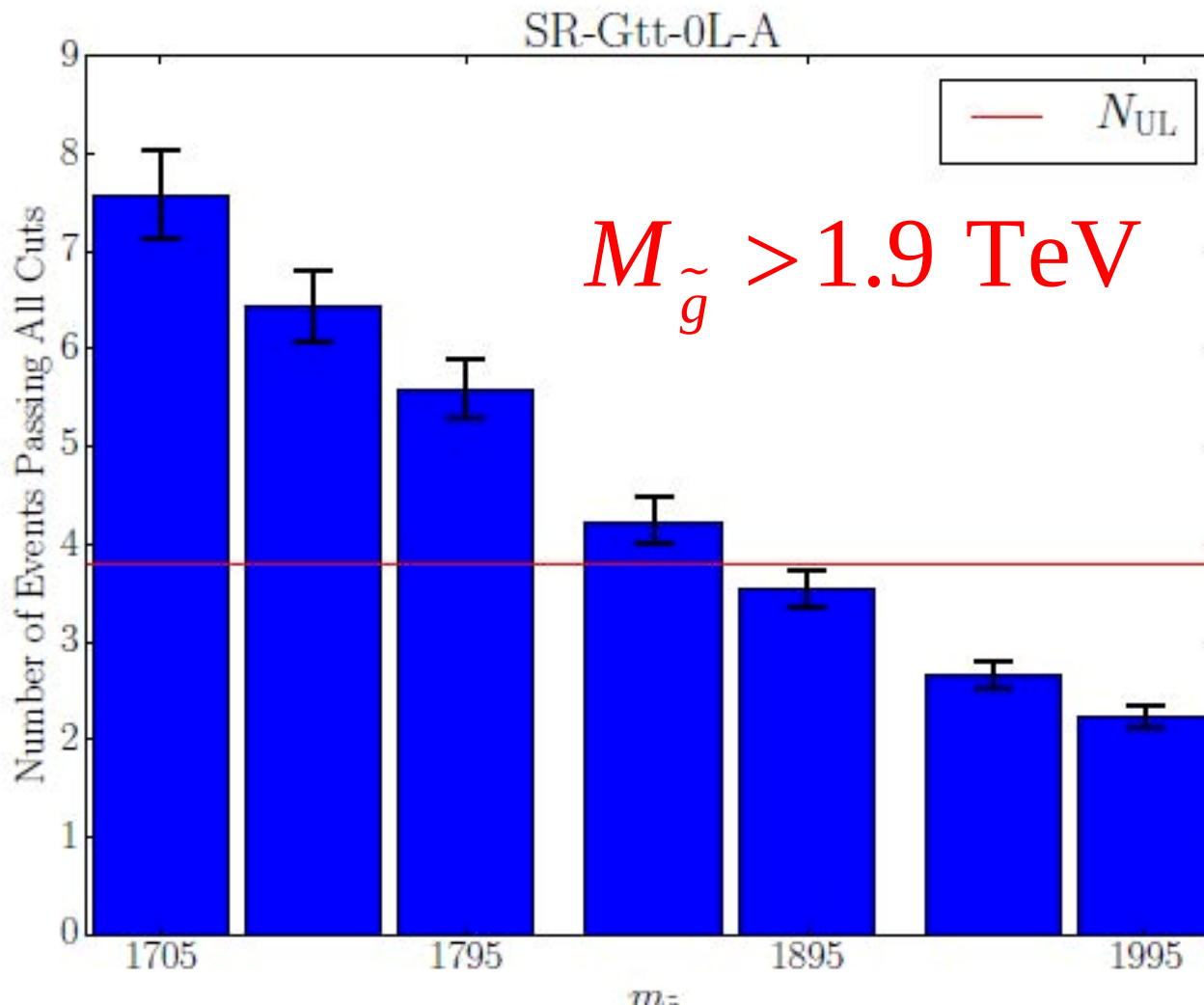
|                            |       |       |
|----------------------------|-------|-------|
| $m_{16}/\text{TeV}$        | 20    | 25    |
| $M_{\tilde{g}}/\text{TeV}$ | 1.90  | 1.90  |
| $g\tilde{\chi}_1^0$        | 0.000 | 0.000 |
| $g\tilde{\chi}_2^0$        | 0.002 | 0.001 |
| $g\tilde{\chi}_3^0$        | 0.005 | 0.007 |
| $g\tilde{\chi}_4^0$        | 0.002 | 0.004 |
| $t\bar{b}\tilde{\chi}_1^+$ | 0.234 | 0.186 |
| $t\bar{b}\tilde{\chi}_2^+$ | 0.274 | 0.322 |
| $t\bar{t}\tilde{\chi}_1^0$ | 0.019 | 0.023 |
| $t\bar{t}\tilde{\chi}_2^0$ | 0.054 | 0.039 |
| $t\bar{t}\tilde{\chi}_3^0$ | 0.113 | 0.105 |
| $t\bar{t}\tilde{\chi}_4^0$ | 0.097 | 0.106 |
| $b\bar{b}\tilde{\chi}_1^0$ | 0.010 | 0.011 |
| $b\bar{b}\tilde{\chi}_2^0$ | 0.064 | 0.054 |
| $b\bar{b}\tilde{\chi}_3^0$ | 0.082 | 0.082 |
| $b\bar{b}\tilde{\chi}_4^0$ | 0.044 | 0.059 |

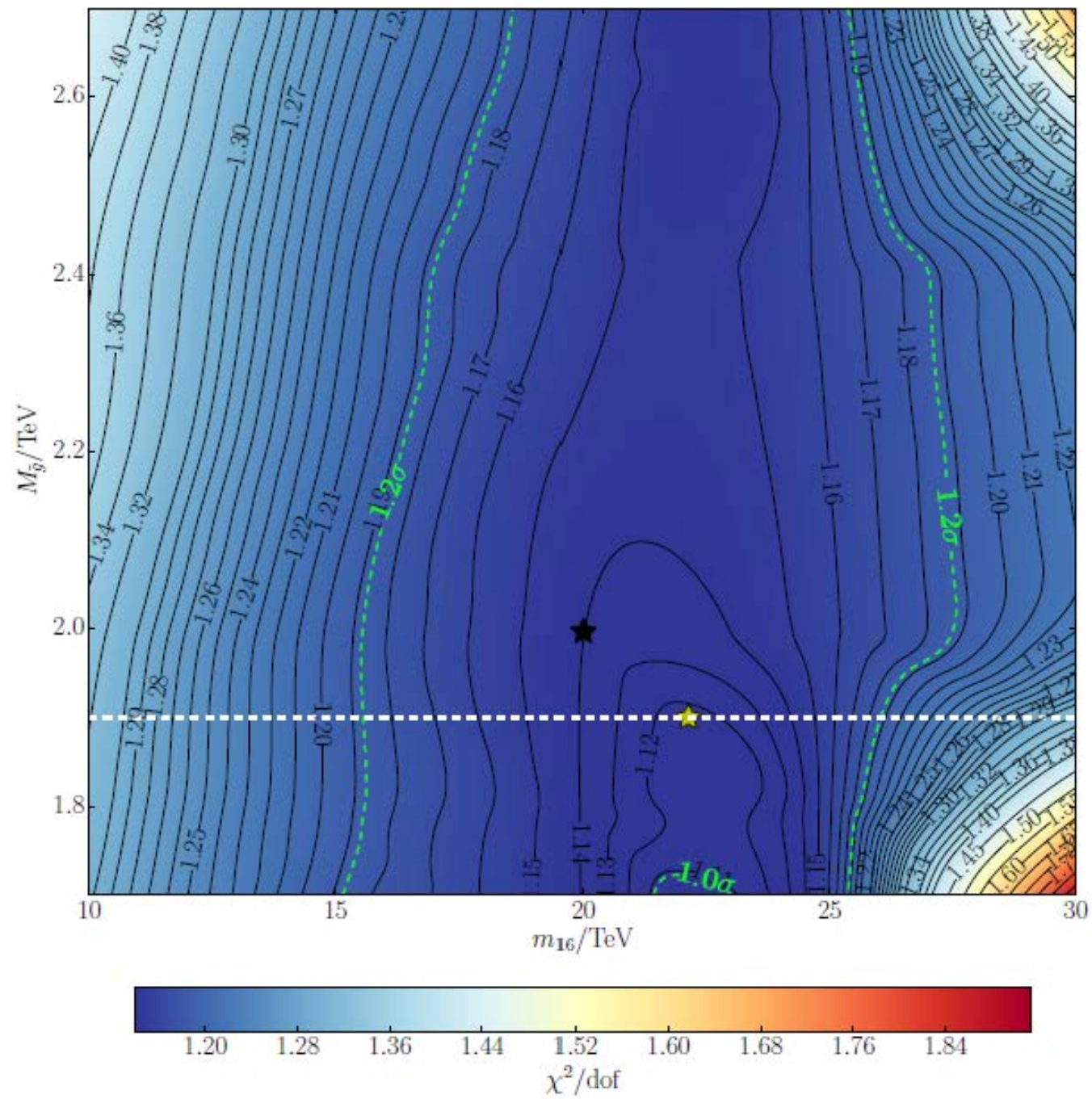
Bound on gluino mass ??

NOT simplified model

Compare to ATLAS &  
CMS data

$$N^{\text{Signal Leptons}} = 0, N^{\text{Jet}} \geq 8, N_{b\text{-jet}} \geq 3, p_T^{\text{jet}} > 30 \text{ GeV}, E_T^{\text{miss}} > 400 \text{ GeV}, \\ \Delta\phi_{\min}^{4j} > 0.4 \text{ rad}, m_{T,\min}^{b\text{-jets}} > 80 \text{ GeV}, m_{\text{eff}}^{\text{incl}} > 2000 \text{ GeV}, M_J^{\Sigma} > 200 \text{ GeV}$$





Benchmark point with  $m_{16} = 20.0 \text{ TeV}$ ,  $M_{\tilde{g}} = 2.00 \text{ TeV}$

| Sector           | Input Param.                  | Best Fit |
|------------------|-------------------------------|----------|
| Gauge            | $1/\alpha_G$                  | 26.0     |
|                  | $M_G/10^{16} \text{ GeV}$     | 2.25     |
|                  | $\epsilon_3/\%$               | -1.68    |
| SUSY (GUT scale) | $m_{16}/\text{TeV}$           | 20.0     |
|                  | $m_{1/2}/\text{GeV}$          | 660      |
|                  | $A_0/\text{TeV}$              | -40.6    |
|                  | $(m_{H_d}/m_{16})^2$          | 1.98     |
|                  | $(m_{H_u}/m_{16})^2$          | 1.61     |
| Neutrino         | $M_{R_1}/10^9 \text{ GeV}$    | 4.62     |
|                  | $M_{R_2}/10^{11} \text{ GeV}$ | 8.32     |
|                  | $M_{R_3}/10^{13} \text{ GeV}$ | 4.71     |
| SUSY (EW Scale)  | $\tan \beta$                  | 50.4     |
|                  | $\mu/\text{GeV}$              | 630      |

| Sector          | Input Param.                  | Best Fit |
|-----------------|-------------------------------|----------|
| Yukawa Textures | $\lambda$                     | 0.617    |
|                 | $\lambda\epsilon$             | 0.0326   |
|                 | $\lambda\tilde{\epsilon}$     | 0.0100   |
|                 | $\lambda\epsilon'$            | -0.00300 |
|                 | $\lambda\xi$                  | 0.00201  |
|                 | $\alpha$                      | 0.138    |
|                 | $\beta$                       | 0.0277   |
|                 | $\theta'/10^{-5}$             | 5.03     |
|                 | $\tilde{\theta}/10^{-5}$      | 2.92     |
|                 | $\phi_{\epsilon'}/\text{rad}$ | -0.277   |
|                 | $\phi_{\xi}/\text{rad}$       | 3.41     |
|                 | $\phi_{\alpha}/\text{rad}$    | 0.963    |
|                 | $\phi_{\beta}/\text{rad}$     | -1.26    |

Benchmark point with  $m_{16} = 20.0 \text{ TeV}$ ,  $M_{\tilde{g}} = 2.00 \text{ TeV}$

| Observable                       | Fit       | Exp.      | Pull   | $\sigma$ |
|----------------------------------|-----------|-----------|--------|----------|
| $M_Z/\text{GeV}$                 | 91.1876   | 91.1876   | 0.0000 | 0.4514   |
| $M_W/\text{GeV}$                 | 80.4734   | 80.3850   | 0.2238 | 0.3949   |
| $1/\alpha_{\text{em}}$           | 137.3435  | 137.0360  | 0.4478 | 0.6867   |
| $G_\mu/10^{-5} \text{ GeV}^{-2}$ | 1.1761    | 1.1664    | 0.8264 | 0.0118   |
| $\alpha_3(M_Z)$                  | 0.1177    | 0.1181    | 0.4791 | 0.0008   |
| $M_t/\text{GeV}$                 | 174.0978  | 173.2100  | 0.4161 | 2.1338   |
| $m_b(m_b)/\text{GeV}$            | 4.3264    | 4.1850    | 1.0388 | 0.1362   |
| $m_\tau/\text{MeV}$              | 1776.0100 | 1776.8600 | 0.0428 | 19.8568  |
| $(M_b - M_c)/\text{GeV}$         | 3.3028    | 3.4500    | 0.4098 | 0.3592   |
| $m_c(m_c)/\text{GeV}$            | 1.2685    | 1.2700    | 0.0442 | 0.0332   |
| $m_s(2 \text{ GeV})/\text{MeV}$  | 97.7602   | 98.0000   | 0.0393 | 6.0987   |
| $m_s/m_d(2 \text{ GeV})$         | 18.5692   | 19.5000   | 0.3843 | 2.0519   |
| $Q$                              | 21.5785   | 23.0000   | 0.6256 | 2.2725   |
| $m_u(2 \text{ GeV})/\text{MeV}$  | 2.6880    | 2.3000    | 0.7758 | 0.5002   |
| $m_d(2 \text{ GeV})/\text{MeV}$  | 5.2646    | 4.7500    | 1.1417 | 0.4508   |
| $M_\mu/\text{MeV}$               | 105.2131  | 105.6584  | 0.2053 | 2.1690   |
| $M_e/\text{MeV}$                 | 0.5108    | 0.5110    | 0.0278 | 0.0057   |
| $ V_{ud} $                       | 0.9745    | 0.9742    | 0.0622 | 0.0049   |
| $ V_{us} $                       | 0.2245    | 0.2248    | 0.2615 | 0.0013   |
| $ V_{ub} /10^{-3}$               | 3.9904    | 4.1300    | 0.2305 | 0.6056   |
| $ V_{cd} $                       | 0.2244    | 0.2200    | 0.8509 | 0.0051   |
| $ V_{cs} $                       | 0.9735    | 0.9950    | 1.2853 | 0.0167   |
| $ V_{cb} /10^{-3}$               | 44.1574   | 40.7500   | 1.4038 | 2.4272   |
| $ V_{td} /10^{-3}$               | 7.9898    | 8.2000    | 0.3378 | 0.6222   |
| $ V_{ts} /10^{-3}$               | 43.6115   | 40.0000   | 1.2691 | 2.8458   |
| $ V_{tb} $                       | 0.9990    | 1.0090    | 0.3179 | 0.0314   |
| $\sin 2\beta$                    | 0.6922    | 0.6910    | 0.0672 | 0.0173   |
| $\epsilon_K/10^{-3}$             | 2.0225    | 2.2330    | 1.0379 | 0.2028   |

|                                                                                  |          |          |         |          |
|----------------------------------------------------------------------------------|----------|----------|---------|----------|
| $\Delta M_{B_s}/\Delta M_{B_d}$                                                  | 43.7269  | 34.8479  | 1.0037  | 8.8463   |
| $\Delta M_{B_d}/10^{-10} \text{ MeV}$                                            | 2.9005   | 3.3540   | 0.7802  | 0.5812   |
| $m_{21}^2/10^{-5} \text{ eV}^2$                                                  | 7.3484   | 7.3750   | 0.0658  | 0.4044   |
| $m_{31}^2/10^{-3} \text{ eV}^2$                                                  | 2.5096   | 2.5000   | 0.0726  | 0.1323   |
| $\sin^2 \theta_{12}$                                                             | 0.2960   | 0.2975   | 0.0915  | 0.0166   |
| $\sin^2 \theta_{23}$                                                             | 0.4419   | 0.4435   | 0.0599  | 0.0266   |
| $\sin^2 \theta_{13}$                                                             | 0.0217   | 0.0215   | 0.1493  | 0.0010   |
| $M_h/\text{GeV}$                                                                 | 122.7975 | 125.0900 | 0.4854  | 4.7225   |
| $BR(b \rightarrow s\gamma)/10^{-6}$                                              | 299.9500 | 332.0000 | 0.2243  | 142.9017 |
| $BR(B_s \rightarrow \mu^+\mu^-)/10^{-9}$                                         | 5.1836   | 2.9500   | 1.6808  | 1.3289   |
| $BR(B_d \rightarrow \mu^+\mu^-)/10^{-9}$                                         | 0.1223   | 0.4000   | 1.8234  | 0.1523   |
| $BR(B \rightarrow \tau\nu)/10^{-6}$                                              | 96.4950  | 106.0000 | 0.1822  | 52.1761  |
| $BR(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}/10^{-7}$      | 0.5456   | 0.3400   | 0.3567  | 0.5765   |
| $BR(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}/10^{-7}$ | 0.7904   | 0.5600   | 0.1531  | 1.5055   |
| $q_0^2(A_{\text{FB}}(B \rightarrow K^*\mu^+\mu^-))/\text{GeV}^2$                 | 3.8492   | 4.9000   | 0.7921  | 1.3265   |
| $F_L(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$             | 0.7522   | 0.6500   | 0.2917  | 0.3503   |
| $F_L(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$        | 0.3514   | 0.3300   | 0.0725  | 0.2952   |
| $P_2(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$             | 0.0679   | 0.3300   | 1.4536  | 0.1803   |
| $P_2(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$        | -0.4333  | -0.5000  | 0.3381  | 0.1973   |
| $P'_4(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$            | 0.5788   | 0.5800   | 0.0029  | 0.4007   |
| $P'_4(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$       | 1.2177   | -0.1800  | 1.7055  | 0.8195   |
| $P'_5(B \rightarrow K^*\mu^+\mu^-)_{1 \leq q^2 \leq 6 \text{ GeV}^2}$            | -0.3221  | 0.2100   | 2.0721  | 0.2568   |
| $P'_5(B \rightarrow K^*\mu^+\mu^-)_{14.18 \leq q^2 \leq 16 \text{ GeV}^2}$       | -0.7119  | -0.7900  | 0.1545  | 0.5053   |
| Total $\chi^2$                                                                   |          |          | 30.9061 |          |

|                                                      |       |       |       |       |
|------------------------------------------------------|-------|-------|-------|-------|
| $m_{16}/\text{TeV}$                                  | 20    | 25    | 20    | 25    |
| $M_{\tilde{g}}/\text{TeV}$                           | 2.00  | 2.00  | 2.60  | 2.60  |
| $\chi^2/\text{dof}$                                  | 1.14  | 1.16  | 1.18  | 1.17  |
| $m_{\tilde{t}_1}/\text{TeV}$                         | 3.68  | 4.70  | 3.70  | 4.65  |
| $m_{\tilde{t}_2}/\text{TeV}$                         | 4.38  | 5.52  | 4.43  | 5.49  |
| $m_{\tilde{b}_1}/\text{TeV}$                         | 4.17  | 5.32  | 4.17  | 5.23  |
| $m_{\tilde{b}_2}/\text{TeV}$                         | 4.32  | 5.47  | 4.36  | 5.43  |
| $m_{\tilde{\tau}_1}/\text{TeV}$                      | 7.47  | 9.30  | 7.52  | 9.27  |
| $m_{\tilde{\tau}_2}/\text{TeV}$                      | 12.2  | 15.2  | 12.2  | 15.2  |
| $m_{\tilde{\chi}_1^0}/\text{GeV}$                    | 352   | 352   | 474   | 474   |
| $m_{\tilde{\chi}_2^0}/\text{GeV}$                    | 586   | 636   | 650   | 665   |
| $m_{\tilde{\chi}_1^+}/\text{GeV}$                    | 585   | 636   | 646   | 661   |
| $m_{\tilde{\chi}_2^+}/\text{GeV}$                    | 710   | 751   | 911   | 914   |
| $(M_A \approx M_{H^0} \approx M_{H^\pm})/\text{TeV}$ | 5.18  | 6.39  | 5.39  | 6.67  |
| $\text{edm}_e/10^{-32} \text{ e cm}$                 | -3.46 | -1.77 | -4.47 | -2.28 |
| $\text{BR}(\mu \rightarrow e\gamma)/10^{-17}$        | 2.08  | 0.922 | 1.84  | 0.869 |
| $\sin \delta$                                        | 0.759 | 0.935 | 0.644 | 0.993 |

# Conclusions

Pati-Salam  $\times \mathbb{Z}_4^R$  yields Sub-Critical Hybrid Inflation  
consistent with Bicep2-Keck-Planck data with inflation at  
"GUT" scale and MSSM at low energy

- SO(10)/PS Yukawa unification
- Inverted scalar mass hierarchy
- Light Higgs - SM-like
- Three family model fits low energy data !!
- $2.7 \geq m_{\tilde{g}} \geq 1.9 \text{ TeV}$
- Third family  $\tilde{g}$  scalars significantly lighter  
than first two  $\Rightarrow$   
 $\tilde{g} \rightarrow t\bar{b}\chi^-, \bar{t}b\chi^+, t\bar{t}\chi_i^0, b\bar{b}\chi_i^0$
- Not simplified model !