

# Forward-backward asymmetry in the gauge-Higgs unification at the International Linear Collider

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arXiv:1905.10007

Scalars2019  
13th SEPTEMBER 2019

# Gauge-Higgs Unification

$$A_M = (A_\mu, A_y)$$


Higgs boson

The Higgs mass is protected by a gauge symmetry

The Higgs boson obtains **finite** mass at 1-loop level

Effective potential is written by Wilson line phase

$$\theta_H \equiv g \int_C dy \langle A_y \rangle$$

Hosotani mechanism

Y. Hosotani (1983)

H. Hatanaka, T. Inami, C.S. Lim (1998)

# $\text{SO}(5) \times \text{U}(1)$ GHU

On the Randall-Sundrum warped (AdS) spacetime

$$ds^2 = e^{-2ky} \eta_{\mu\nu} dx^\mu dx^\nu + dy^2$$



- Agashe, Contino, Pomarol (2005)
- Contino, Da Rold, Pomarol (2007)
- Medina, Shah, Wagner (2007)
- Sakamura, Hosotani (2007)
- Hosotani, Oda, Ohnuma, Sakamura (2008)
- SF, Hatanaka, Hosotani, Orikasa, Shimotani (2013)

# $\text{SO}(5) \times \text{U}(1)$ GHU

$$SO(5) \times U(1)_X$$

$$\xrightarrow{\text{B.C.}} SO(4) \times U(1)_X$$

$$\simeq SU(2)_L \times SU(2)_R \times U(1)_X$$

$$\xrightarrow{\text{Brane int.}} SU(2)_L \times U(1)_Y$$

$$\xrightarrow{\text{Hosotani mechanism}} U(1)_{\text{EM}}$$

$W_R, Z_R$

$W, Z, \gamma$

# Higgs couplings

$$\begin{pmatrix} HWW \\ HZZ \end{pmatrix} \approx \boxed{\text{SM value}} \times \cos \theta_H$$

$$\frac{\Gamma(H \rightarrow WW)}{\Gamma(H \rightarrow ZZ)} \approx \boxed{\text{SM value}} \times \cos^2 \theta_H$$

$\sin \theta_H$  corresponds to  $\xi$  in MCHMs

$\Gamma(H \rightarrow \gamma\gamma)$  and  $\Gamma(H \rightarrow Z\gamma)$  are evaluated in  
SF, Hatanaka, Hosotani, Orikasa, Shimotani (2013)  
SF, Hatanaka, Hosotani (2015)

# Parameters

One parameter  $e^{kL} \rightarrow \theta_H, m_{\text{KK}}$  is determined

↓ Upper bound by LHC

$\theta_H$	$e^{kL}$	$ c_t $	$m_{\text{KK}}$ (GeV)
0.10	$2.90 \times 10^4$	0.16116	8063
0.09	$1.70 \times 10^4$	0.11646	8721
0.08	$1.01 \times 10^4$	0.008914	9544

↑ Lower bound from top-mass realisation

small  $\theta_H \Leftrightarrow$  large KK scale

# Fermion Localisation

$$\Psi_{L,R}(x,y) = \frac{e^{\frac{3}{2}ky}}{\sqrt{L}} \sum_{n=0}^{\infty} \psi_{L,R}^{(n)}(x) \frac{f_{L,R}^{(n)}(y)}{\sqrt{N(n)}},$$

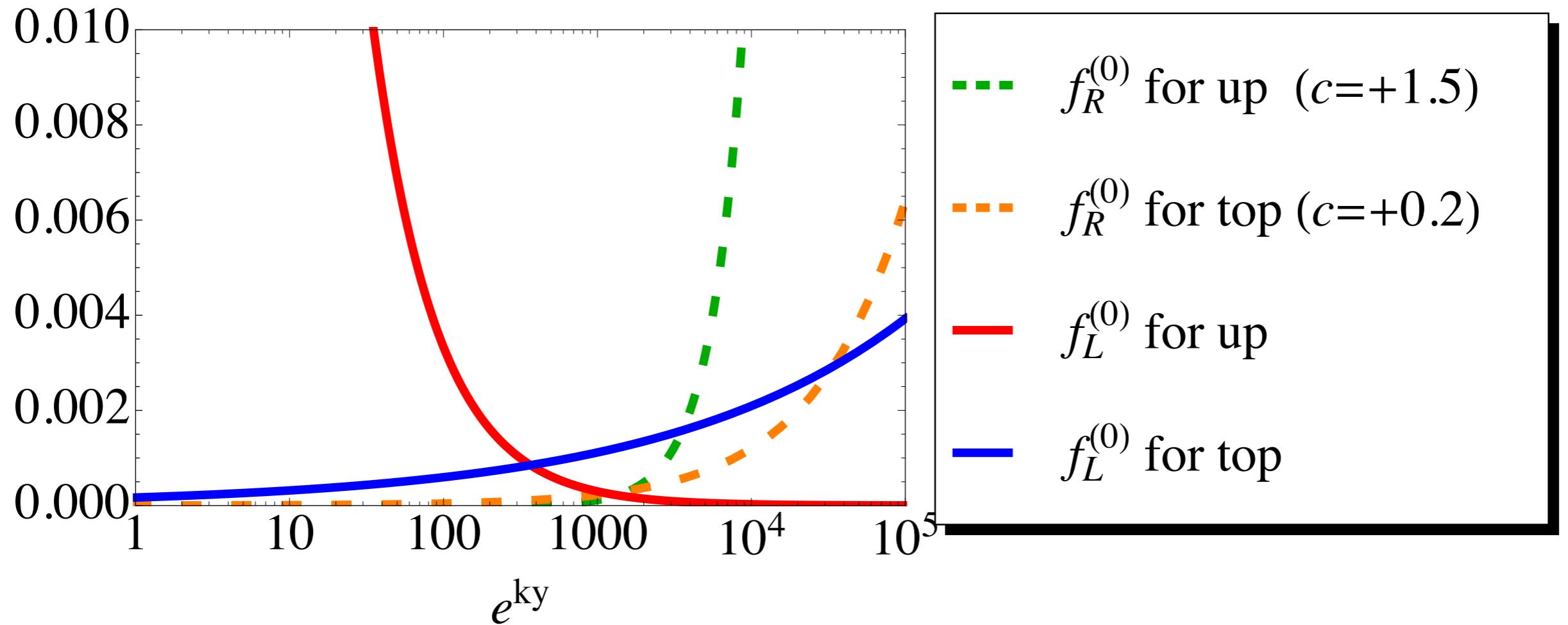
$$f_{L,R}^{(0)}(y) = e^{(\frac{1}{2}\mp c)ky}$$

Left-handed : localised toward the UV brane ( $c>+1/2$ )  
the IR brane ( $c<+1/2$ )

Right-handed : localised toward the IR brane ( $c > -1/2$ )  
the UV brane ( $c < -1/2$ )

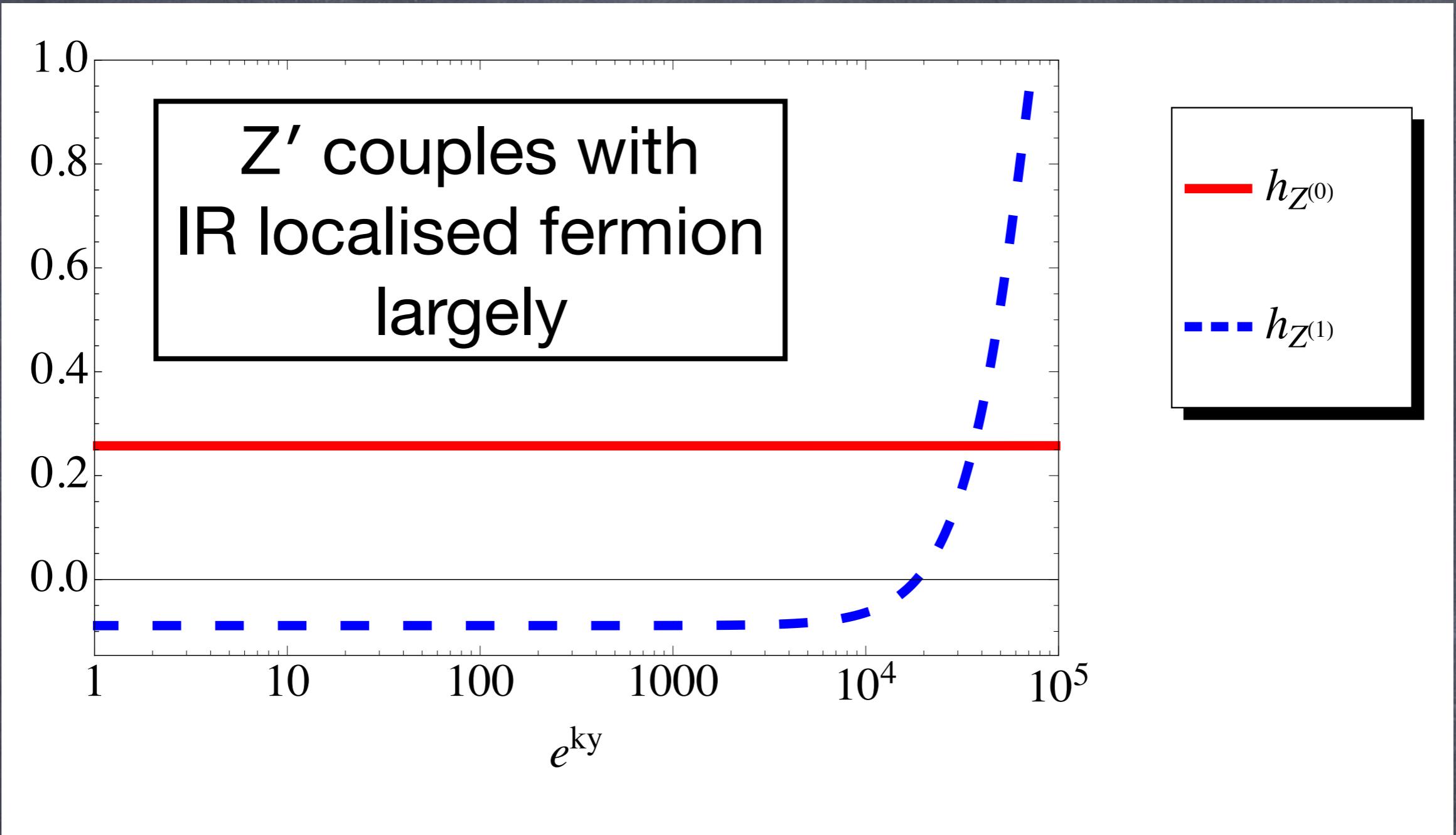
$c \rightarrow -c$ , the left- and right-handed are reversed  
**mass is invariant**

# Fermion Localisation



$c>0$  case

# Gauge Boson Localisation



$Z^{(0)}$ : localised toward the IR brane very slightly  
 $Z^{(1)}$ : localised toward the IR brane

# Z<sup>(1)</sup>-couplings

Z<sup>(1)</sup>-boson couplings in  $g_W / \cos\theta_W$  unit  
for  $\sin^2\theta_W = 0.2312$  and  $\theta_H = 0.10$ ,

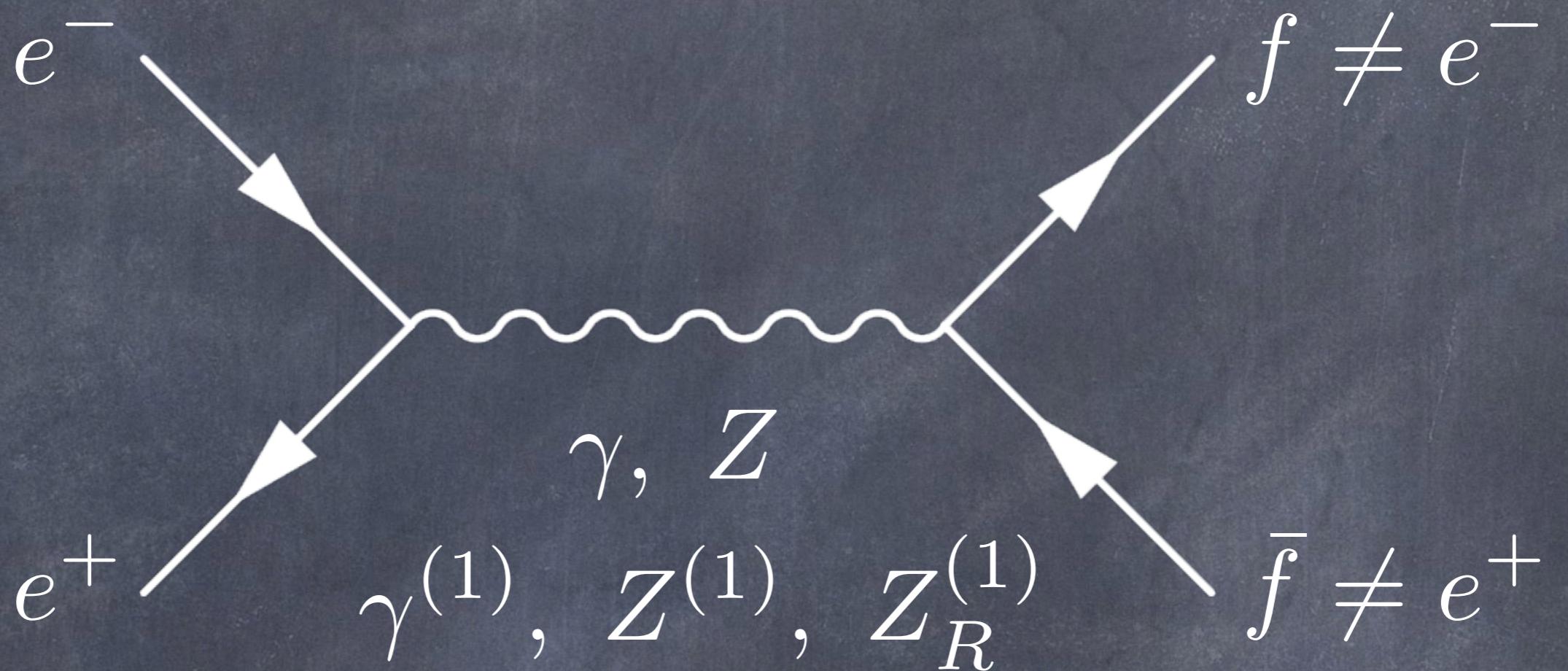
	$g_{Z^{(1)} e_L}$	$g_{Z^{(1)} e_R}$
$c_e > 0$	+0.0987	+0.9148
$c_e < 0$	-1.0535	-0.0858

large asymmetry of Z' couplings

Only  $c_l > 0$  is considered in this work

Z' masses: 7–8 TeV, decay width: 0.4–2 TeV

# Processes



Tree level only

Bhabha process: not yet

# Polarisation

Ignoring the Higgs exchange,

$$\frac{d\sigma}{d \cos \theta} = \frac{1}{4} \left[ (1 - P_{e^-})(1 + P_{e^+}) \frac{d\sigma_{LR}}{d \cos \theta} + (1 + P_{e^-})(1 - P_{e^+}) \frac{d\sigma_{RL}}{d \cos \theta} \right]$$

$P = +1$  : right-handed

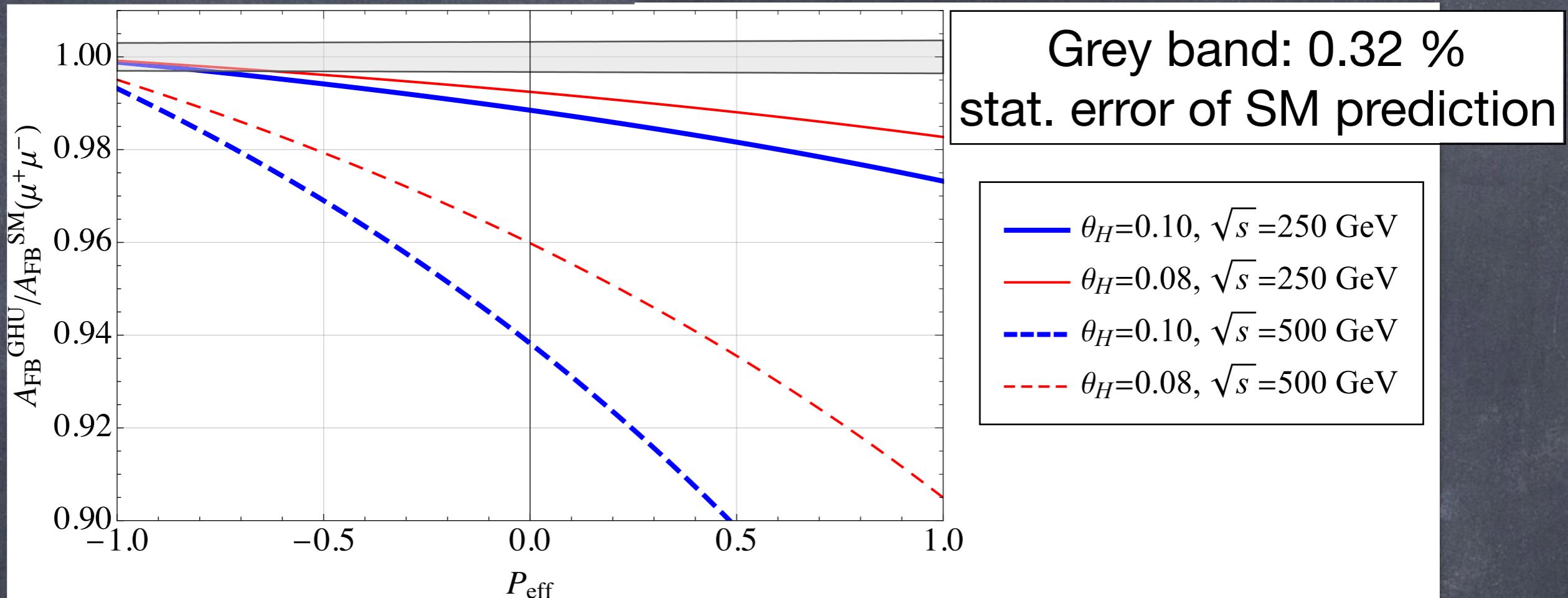
$P = -1$  : left-handed

It is rewritten by  $P_{\text{eff}} = \frac{P_{e^-} - P_{e^+}}{1 - P_{e^-} P_{e^+}}$  as

$$\frac{d\sigma}{d \cos \theta} = \frac{(1 - P_{e^+} P_{e^-})}{4} \left[ (1 - P_{\text{eff}}) \frac{d\sigma_{LR}}{d \cos \theta} + (1 + P_{\text{eff}}) \frac{d\sigma_{RL}}{d \cos \theta} \right]$$

$$e^+ e^- \rightarrow \mu^+ \mu^-$$

Deviation of AFB from SM ( $c_l > 0$ )



-1.1 % for  $P_{\text{eff}} = 0, \quad \theta_H = 0.10, \sqrt{s} = 250 \text{ GeV}$

-2.5 % for  $P_{\text{eff}} = 0.887, \quad //$

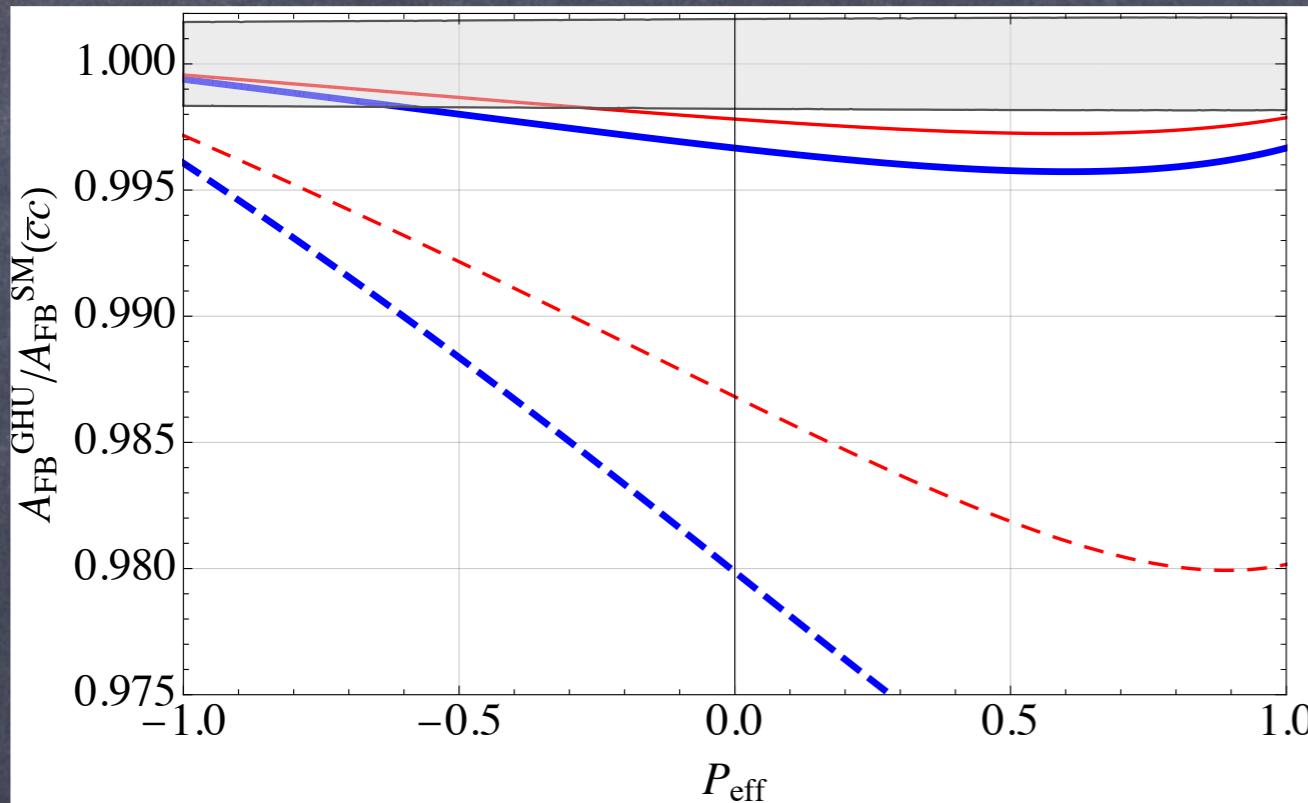


## Deviation of AFB from SM

Grey band: 0.17 %  
stat. error of SM prediction

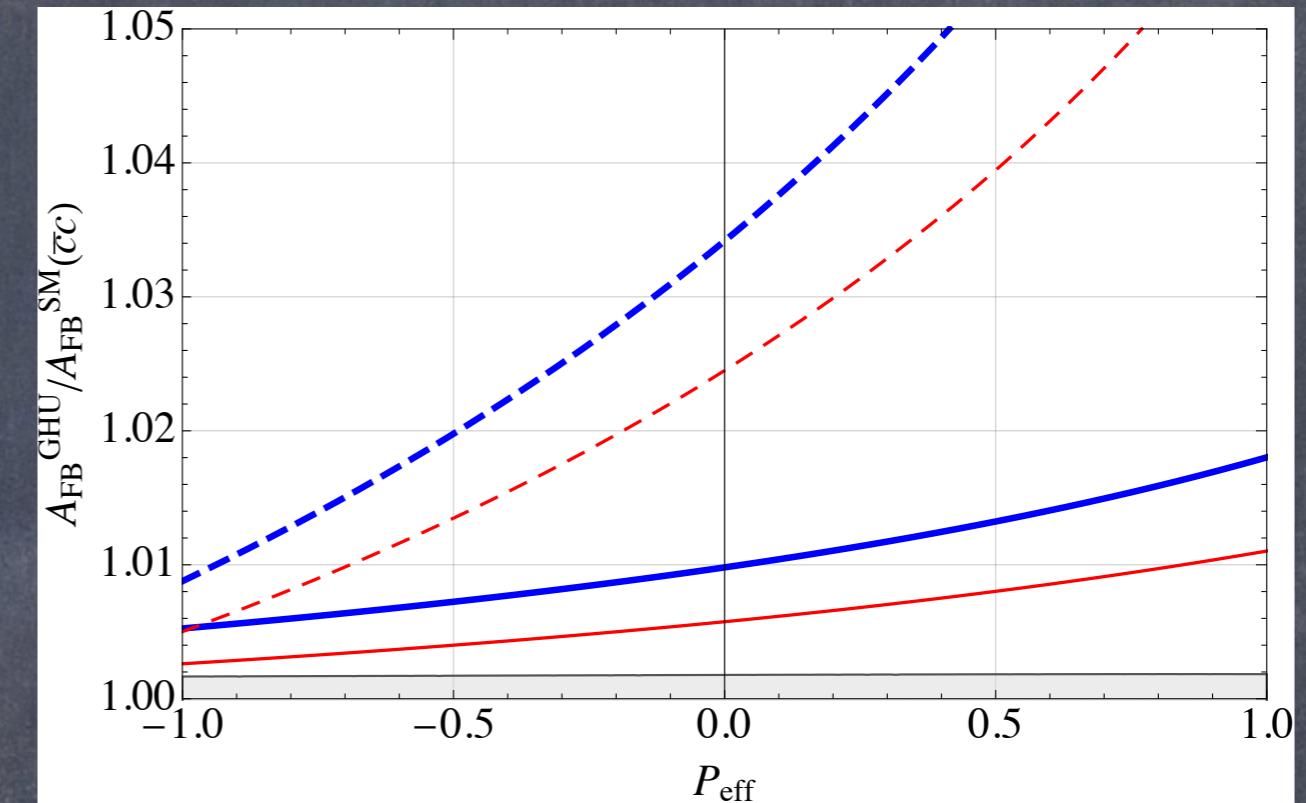
$C_c > 0$

$C_c < 0$



-0.33 % for  $P_{\text{eff}} = 0$

-0.38 % for  $P_{\text{eff}} = 0.887$



+0.98 % for  $P_{\text{eff}} = 0$

+1.68 % for  $P_{\text{eff}} = 0.887$

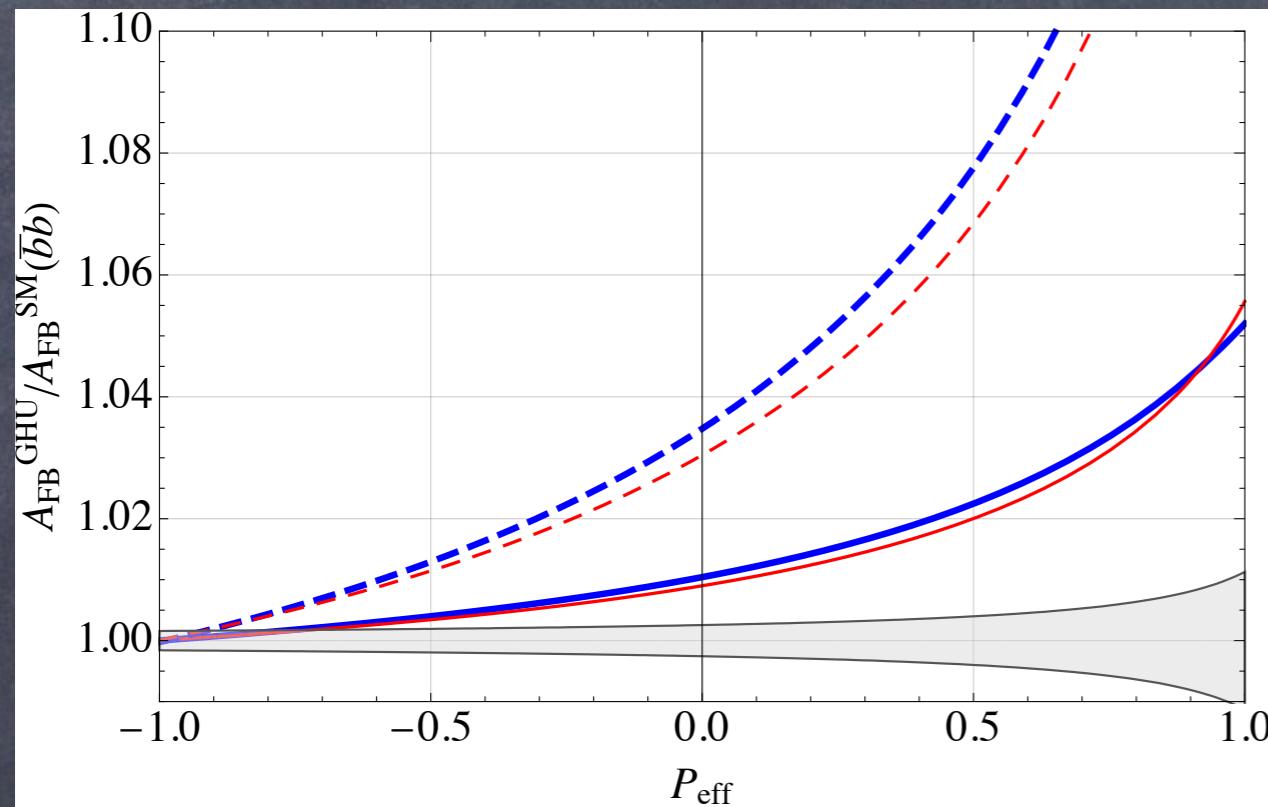
$(\theta_H = 0.10, \sqrt{s} = 250 \text{ GeV})$



Deviation of AFB from SM

Grey band: 0.11–0.80 %  
stat. error of SM prediction

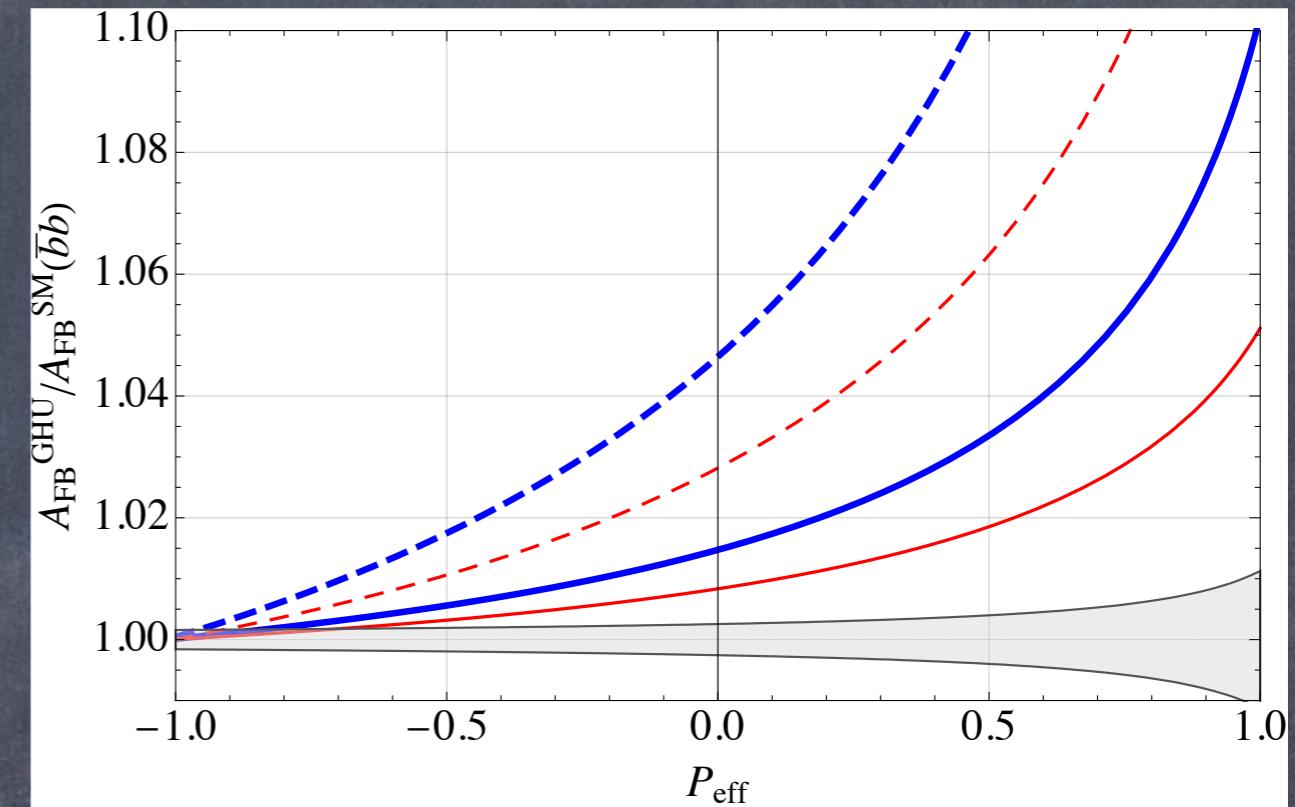
$C_b > 0$



+1.0 % for  $P_{\text{eff}} = 0$

+4.2 % for  $P_{\text{eff}} = 0.887$

$C_b < 0$



+1.5 % for  $P_{\text{eff}} = 0$

+7.3 % for  $P_{\text{eff}} = 0.887$

( $\theta_H = 0.10$ ,  $\sqrt{s} = 250$  GeV)

# Summary

- gauge-Higgs unification is a solution to the fine-tuning problem of the Higgs mass
- KK photon, Z, ZR are Z's  
They have large coupling asymmetries
- 7 TeV Z' effects are seen by  $\sqrt{s} = 250$  GeV