

Lepton flavor specific extended Higgs model

Based on 10.1103/PhysRevD.107.095001 [[arXiv:2301.08641 \[hep-ph\]](#)]

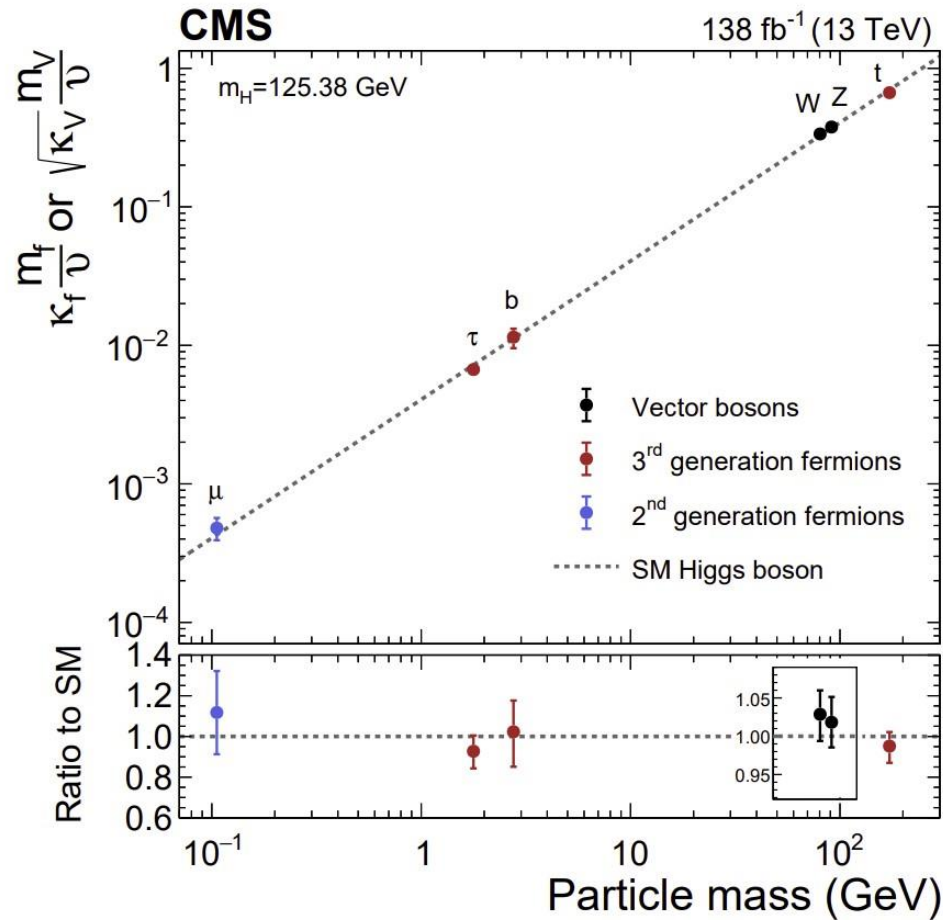
Bernardo Gonçalves

In collaboration with Matthew Knauss and Marc Sher

Outline

- Motivation
- The model (scalar sector, couplings, theoretical constraints)
- Benchmarks models
 - The model without $(q\tau)$ - (μe) mixing
 - The aligned model (constraints and signatures)
- Final remarks

Motivation



Taken from *A portrait of the Higgs boson by the CMS experiment ten years after the discovery*, Nature 607 (2022) 60

Muon-specific 2HDM (Abe, Sato, and Yagyu):

- The muon and the remaining fields couple to different Higgs doublets
- A Z_4 symmetry makes the model free of tree-level FCNC and restricts the structure of Yukawa couplings
- Muon interactions of scalars can be substantially enhanced or suppressed relative to those with tau leptons

Can the three leptonic generations couple to different *Higgses*?

Extending the muon-specific 2HDM

Our idea: each of the charged leptons couples to a different Higgs doublet

$$\Phi_e + \Phi_\mu + \Phi_\tau$$

Symmetry $(Z_4)_e \times (Z_4)_\mu \times (Z_4)_\tau$: no tree-level FCNC and diagonal Yukawa matrix

	L_ℓ	ℓ_R	Φ_ℓ	Other fields
$(Z_4)_\ell$	i	i	-1	1

Simplest implementation: 4HDM in which the fourth Higgs couples to quarks Φ_q

Lepton Flavor Specific Extended Higgs Model

The model: scalar sector

Fixing notation...

Scalar potential: $V = V_2 + V_4$

$$\begin{aligned} V_2 = & m_{qq}^2 \Phi_q^\dagger \Phi_q + \dots \\ & + [m_{qe}^2 (\Phi_q^\dagger \Phi_e) + \dots \\ & + \text{H.c.}] \end{aligned}$$

$$\begin{aligned} V_4 = & \lambda_1^q (\Phi_q^\dagger \Phi_q)^2 + \dots \\ & + \lambda_3^{qe} (\Phi_q^\dagger \Phi_q) (\Phi_e^\dagger \Phi_e) + \dots \\ & + \lambda_4^{qe} (\Phi_q^\dagger \Phi_e) (\Phi_e^\dagger \Phi_q) + \dots \\ & + \frac{1}{2} [\lambda_5^{qe} (\Phi_q^\dagger \Phi_e)^2 + \dots + \text{H.c.}] \end{aligned}$$

The model: scalar sector

Fixing notation...

Scalar potential: $V = V_2 + V_4$

$$\begin{aligned} V_2 = & m_{\underbrace{q}_{\text{orange}}\underbrace{q}_{\text{orange}}}^2 \Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{q}_{\text{orange}}} + \dots \\ & + [m_{\underbrace{qe}_{\text{purple}}}^2 (\Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{e}_{\text{purple}}}) + \dots \\ & + \text{H.c.}] \end{aligned}$$

$$\begin{aligned} V_4 = & \lambda_{\underbrace{1}_{\text{orange}}}^{\underbrace{q}_{\text{orange}}} (\Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{q}_{\text{orange}}})^2 + \dots \\ & + \lambda_{\underbrace{3}_{\text{purple}}}^{\underbrace{qe}_{\text{purple}}} (\Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{q}_{\text{orange}}}) (\Phi_{\underbrace{e}_{\text{purple}}}^\dagger \Phi_{\underbrace{e}_{\text{purple}}}) + \dots \\ & + \lambda_{\underbrace{4}_{\text{purple}}}^{\underbrace{qe}_{\text{purple}}} (\Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{e}_{\text{purple}}}) (\Phi_{\underbrace{e}_{\text{purple}}}^\dagger \Phi_{\underbrace{q}_{\text{orange}}}) + \dots \\ & + \frac{1}{2} [\lambda_{\underbrace{5}_{\text{purple}}}^{\underbrace{qe}_{\text{purple}}} (\Phi_{\underbrace{q}_{\text{orange}}}^\dagger \Phi_{\underbrace{e}_{\text{purple}}})^2 + \dots + \text{H.c.}] \end{aligned}$$

The model: scalar sector

Fixing notation...

Higgs doublets:

$$\Phi_i = \begin{pmatrix} \phi_i^+ \\ (v_i + \phi_i + i\chi_i)/\sqrt{2} \end{pmatrix}, \quad (i = q, e, \mu, \tau)$$

$$v_q = v \cos \beta_2 \cos \beta_3 \cos \beta_4$$

$$v_e = v \sin \beta_2 \cos \beta_3 \cos \beta_4$$

$$v_\mu = v \sin \beta_3 \cos \beta_4$$

$$v_\tau = v \sin \beta_4$$

Rotation to the Higgs basis

$$\begin{pmatrix} h_0 \\ H_1 \\ H_2 \\ H_3 \end{pmatrix} = \mathcal{O}_\beta \begin{pmatrix} \phi_q \\ \phi_e \\ \phi_\mu \\ \phi_\tau \end{pmatrix}$$

$$\mathcal{O}_\beta = \begin{pmatrix} c_{\beta_2} c_{\beta_3} c_{\beta_4} & s_{\beta_2} c_{\beta_3} c_{\beta_4} & s_{\beta_3} c_{\beta_4} & s_{\beta_4} \\ -s_{\beta_2} & c_{\beta_2} & 0 & 0 \\ -c_{\beta_2} c_{\beta_3} & -s_{\beta_2} s_{\beta_3} & c_{\beta_3} & 0 \\ -c_{\beta_2} c_{\beta_3} s_{\beta_4} & -s_{\beta_2} c_{\beta_3} s_{\beta_4} & -s_{\beta_3} s_{\beta_4} & c_{\beta_4} \end{pmatrix}$$

The model: scalar sector

Fixing notation...

Rotations to the mass basis:

SCALAR SECTOR

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \end{pmatrix} = \mathcal{O}_\alpha \begin{pmatrix} \phi_q \\ \phi_e \\ \phi_\mu \\ \phi_\tau \end{pmatrix}$$

$$\mathcal{O}_\alpha = \mathbf{R}_{34} \mathbf{R}_{24} \mathbf{R}_{23} \mathbf{R}_{14} \mathbf{R}_{13} \mathbf{R}_{12}$$

$$\mathbf{R}_{24} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & c_{\alpha_{24}} & 0 & s_{\alpha_{24}} \\ 0 & 0 & 1 & 0 \\ 0 & -s_{\alpha_{24}} & 0 & c_{\alpha_{24}} \end{pmatrix}$$

The model: scalar sector

Fixing notation...

Rotations to the mass basis:

PSEUDOSCALAR SECTOR

$$\begin{pmatrix} G^0 \\ A_1 \\ A_2 \\ A_3 \end{pmatrix} = \mathcal{O}_\gamma \mathcal{O}_\beta \begin{pmatrix} \chi_q \\ \chi_e \\ \chi_\mu \\ \chi_\tau \end{pmatrix}$$

$$\mathcal{O}_\gamma = \mathbf{P}_{34} \mathbf{P}_{24} \mathbf{P}_{23}$$
$$\mathbf{P}_{24} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & c_{\gamma_{24}} & 0 & s_{\gamma_{24}} \\ 0 & 0 & 1 & 0 \\ 0 & -s_{\gamma_{24}} & 0 & c_{\gamma_{24}} \end{pmatrix}$$

The model: scalar sector

Fixing notation...

Rotations to the mass basis:

CHARGED SECTOR

$$\begin{pmatrix} G^+ \\ H_1^+ \\ H_2^+ \\ H_3^+ \end{pmatrix} = \mathcal{O}_\delta \mathcal{O}_\beta \begin{pmatrix} \phi_q^+ \\ \phi_e^+ \\ \phi_\mu^+ \\ \phi_\tau^+ \end{pmatrix}$$

$$\mathcal{O}_\delta = \mathbf{Q}_{34} \mathbf{Q}_{24} \mathbf{Q}_{23}$$
$$\mathbf{Q}_{24} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & c_{\delta_{24}} & 0 & s_{\delta_{24}} \\ 0 & 0 & 1 & 0 \\ 0 & -s_{\delta_{24}} & 0 & c_{\delta_{24}} \end{pmatrix}$$

The model: gauge couplings

$$\mathcal{L}_k = \sum_{i=1}^4 |D_\mu \Phi_i|^2 \longrightarrow \left(\sum_{i=1}^4 C_i h_i \right) \left(\frac{g}{2c_W} m_Z Z_\mu Z^\mu + g m_W W_\mu^- W^{+\mu} \right)$$

$$\boxed{\alpha_{1j} = \beta_j} \longrightarrow \begin{aligned} C_1 &= 1 \\ C_k &= 0, \quad k \neq 1 \end{aligned}$$

$j = 2, 3, 4$

Alignment limit

The model: Yukawa couplings

$$\mathcal{L}_Y^S = - \sum_{f \in \{q, e, \mu, \tau\}} \frac{m_f}{v} (\xi_{h_1}^f \bar{f} f h_1 + \xi_{h_2}^f \bar{f} f h_2 + \xi_{h_3}^f \bar{f} f h_3 + \xi_{h_4}^f \bar{f} f h_4)$$

$$\mathcal{L}_Y^P = - \sum_{f \in \{q, e, \mu, \tau\}} \left(-i \frac{m_f}{v} \right) (\xi_{A_1}^f \bar{f} \gamma_5 f A_1 + \xi_{A_2}^f \bar{f} \gamma_5 f A_2 + \xi_{A_3}^f \bar{f} \gamma_5 f A_3)$$



$$\xi_{h_j}^q = \frac{\mathcal{O}_{\alpha j, 1}}{\hat{v}_1}, \quad \dots$$

$$\xi_{A_j}^q = \frac{(\mathcal{O}_\gamma \mathcal{O}_\beta)_{j, 1}}{\hat{v}_1}, \quad \dots$$

$$\hat{v}_i \equiv v_i / v$$

The model: Yukawa couplings

$$\mathcal{L}_Y^S = - \sum_{f \in \{q, e, \mu, \tau\}} \frac{m_f}{v} (\xi_{h_1}^f \bar{f} f h_1 + \xi_{h_2}^f \bar{f} f h_2 + \xi_{h_3}^f \bar{f} f h_3 + \xi_{h_4}^f \bar{f} f h_4)$$

$$\mathcal{L}_Y^P = - \sum_{f \in \{q, e, \mu, \tau\}} \left(-i \frac{m_f}{v} \right) (\xi_{A_1}^f \bar{f} \gamma_5 f A_1 + \xi_{A_2}^f \bar{f} \gamma_5 f A_2 + \xi_{A_3}^f \bar{f} \gamma_5 f A_3)$$



$$\xi_{h_j}^q = \frac{\mathcal{O}_{\alpha j(1)}}{\hat{v}_1}, \quad \dots$$

$$\xi_{A_j}^q = \frac{(\mathcal{O}_\gamma \mathcal{O}_\beta)_{j(1)}}{\hat{v}_1}, \quad \dots$$

$$\hat{v}_i \equiv v_i / v$$

The model: Yukawa couplings

$$\mathcal{L}_Y^C = -\sum_j \left[\sum_{u,d} \frac{\sqrt{2}V_{ud}}{v} \bar{u}(m_u \xi_{H_j^+}^{qL} \mathbf{P}_L + m_d \xi_{H_j^+}^{qR} \mathbf{P}_R) d H_j^+ + \sum_l \frac{\sqrt{2}m_l}{v} \xi_{H_j^+}^{lL} \bar{\nu}_L l_R H_j^+ \right] + \text{H.c.}$$



$$\xi_{H_j^+}^{qLR} = \frac{(\mathcal{O}_\delta \mathcal{O}_\beta)_{j,1}}{\hat{v}_1}, \quad \dots$$

$$\hat{v}_i \equiv v_i/v$$

The model: Yukawa couplings

$$\mathcal{L}_Y^C = -\sum_j \left[\sum_{u,d} \frac{\sqrt{2}V_{ud}}{v} \bar{u}(m_u \xi_{H_j^+}^{qL} \mathbf{P}_L + m_d \xi_{H_j^+}^{qR} \mathbf{P}_R) d H_j^+ + \sum_l \frac{\sqrt{2}m_l}{v} \xi_{H_j^+}^{lL} \bar{\nu}_L l_R H_j^+ \right] + \text{H.c.}$$



$$\xi_{H_j^+}^{qLR} = \frac{(\mathcal{O}_\delta \mathcal{O}_\beta)_{j,1}}{\hat{v}_1}, \quad \dots$$

$$\hat{v}_i \equiv v_i/v$$

General Yukawa couplings too cumbersome to be shown here

The model: theoretical constraints

- Boundedness from below criteria

4. CRITERIA FOR COPOSITIVE MATRICES OF ORDER FOUR

Let A be a matrix of the form

$$A = \begin{pmatrix} a_1 & a_{12} & a_{13} & a_{14} \\ a_{12} & a_2 & a_{23} & a_{24} \\ a_{13} & a_{23} & a_3 & a_{34} \\ a_{14} & a_{24} & a_{34} & a_4 \end{pmatrix}. \quad (4.1)$$

For all neutral directions

According to the signs of the off-diagonal elements of A , we consider eight different cases. Six of these cases are contained in the following theorem.

From Li Ping and Feng Yu Yu, *Criteria for copositive matrices of order four*, Linear Algebra and its Applications, Volume 194 (1993), doi.org/10.1016/0024-3795(93)90116-6.

The model: theoretical constraints

- Boundedness from below criteria
- Oblique parameters - arXiv:0802.4353 [hep-ph]
- Quartic couplings less than $\frac{1}{4}\pi$

Benchmark models

- The model without $(q\tau)-(\mu e)$ mixing
- The aligned model

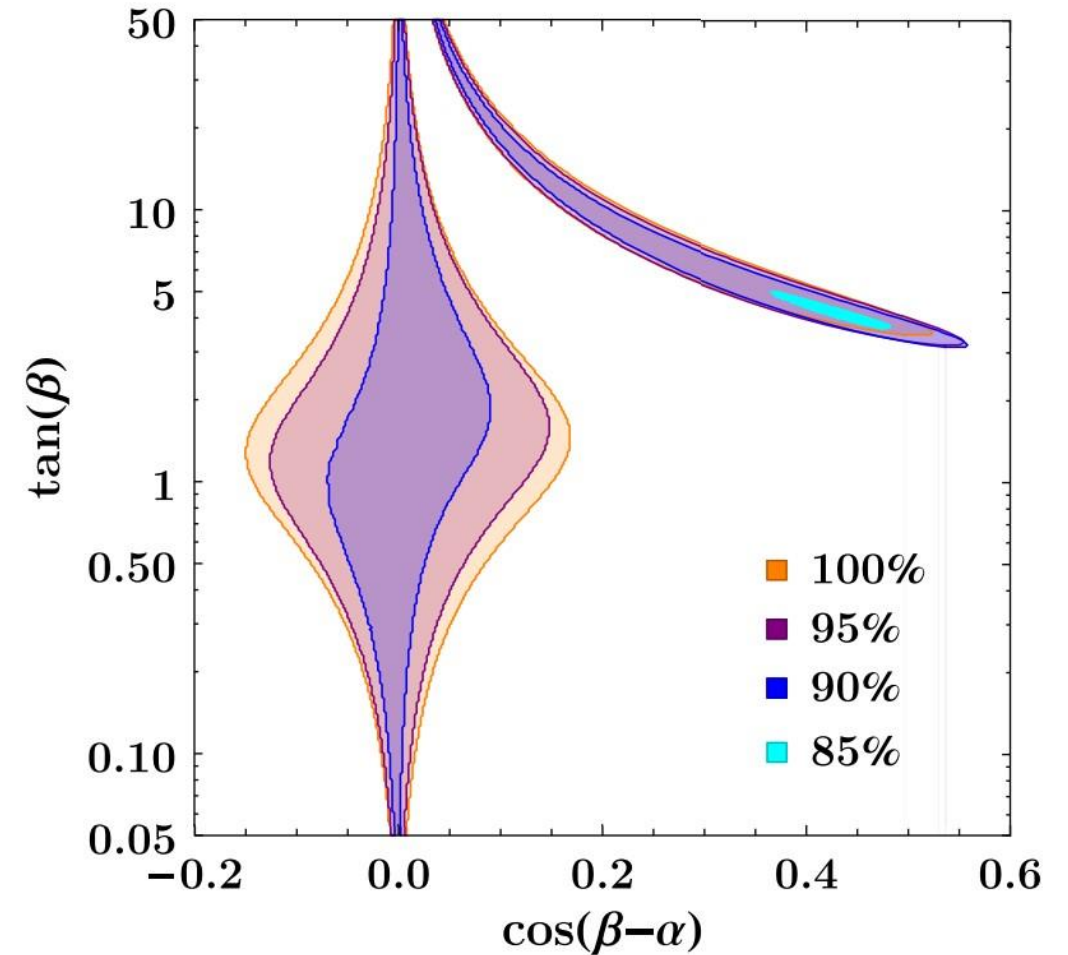
The model without $(q\tau)$ -(μe) mixing

4×4 is broken into two 2×2

Upper 2×2 very similar to lepton-specific 2HDM

$$\mu_X \equiv \frac{\sigma(pp \rightarrow H) \text{BR}(H \rightarrow X)}{\sigma(pp \rightarrow H)_{\text{SM}} \text{BR}(H \rightarrow X)_{\text{SM}}}$$

$$X = gg, \mu\mu, \tau\tau, \bar{c}c, \bar{b}b, \bar{t}t, \gamma\gamma, \gamma Z, WW, ZZ$$

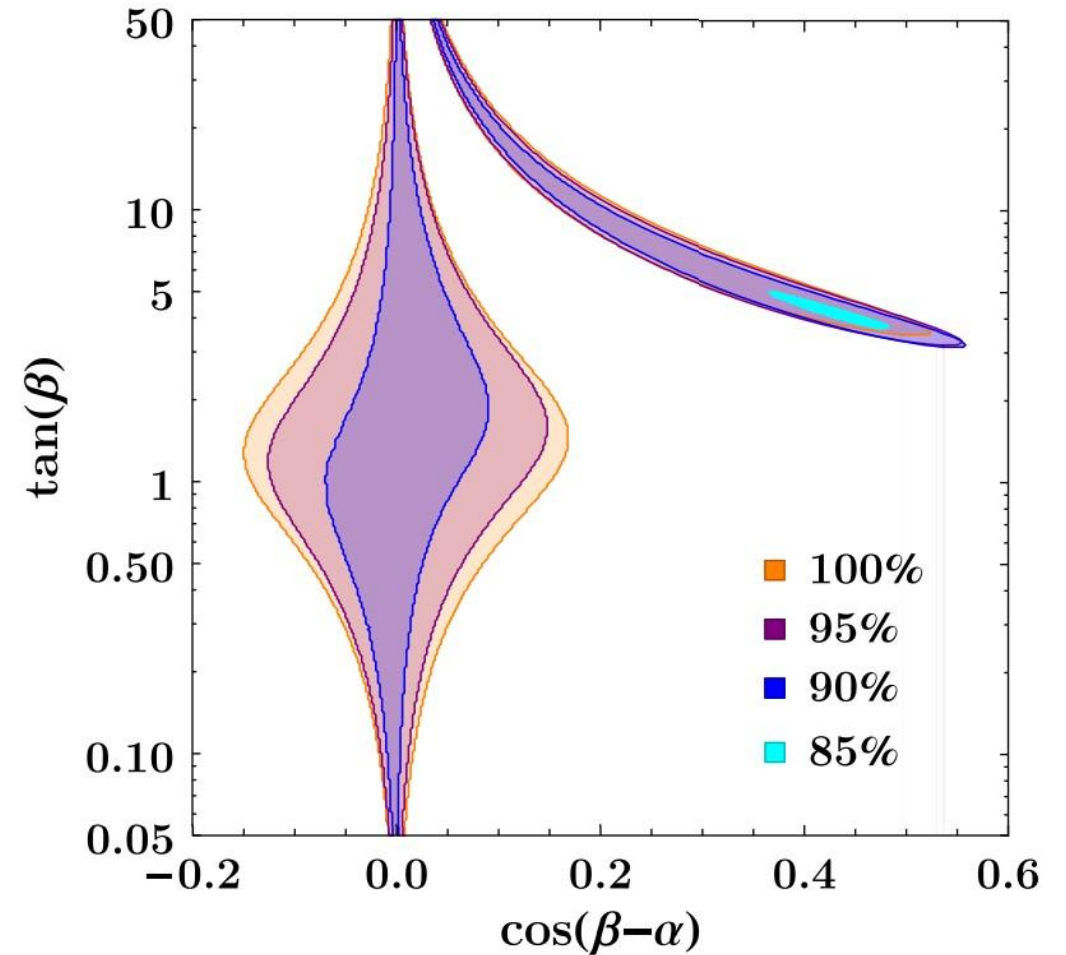


Allowed regions for different values of $(v_q^2 + v_\tau^2)^{1/2}/v$.

The model without $(q\tau)$ - (μe) mixing

Much of the VEV is saturated
by v_q and v_τ

Phenomenologically unacceptable
(additional massless scalars, the
coupling to the muon vanishes)



Allowed regions for different values of $(v_q^2 + v_\tau^2)^{1/2}/v$.

The aligned model

$$\alpha_{1j} = \beta_j$$

The aligned model

$$\lambda_1^i = \frac{1}{2v_i^3} \left(v_i M_{s,ii}^2 + \sum_{j \neq i} v_j m_{ij}^2 \right)$$

$$\lambda_3^{ij} = \frac{1}{v_i v_j} (M_{s,ij}^2 - 2M_{c,ij}^2 + m_{ij}^2)$$

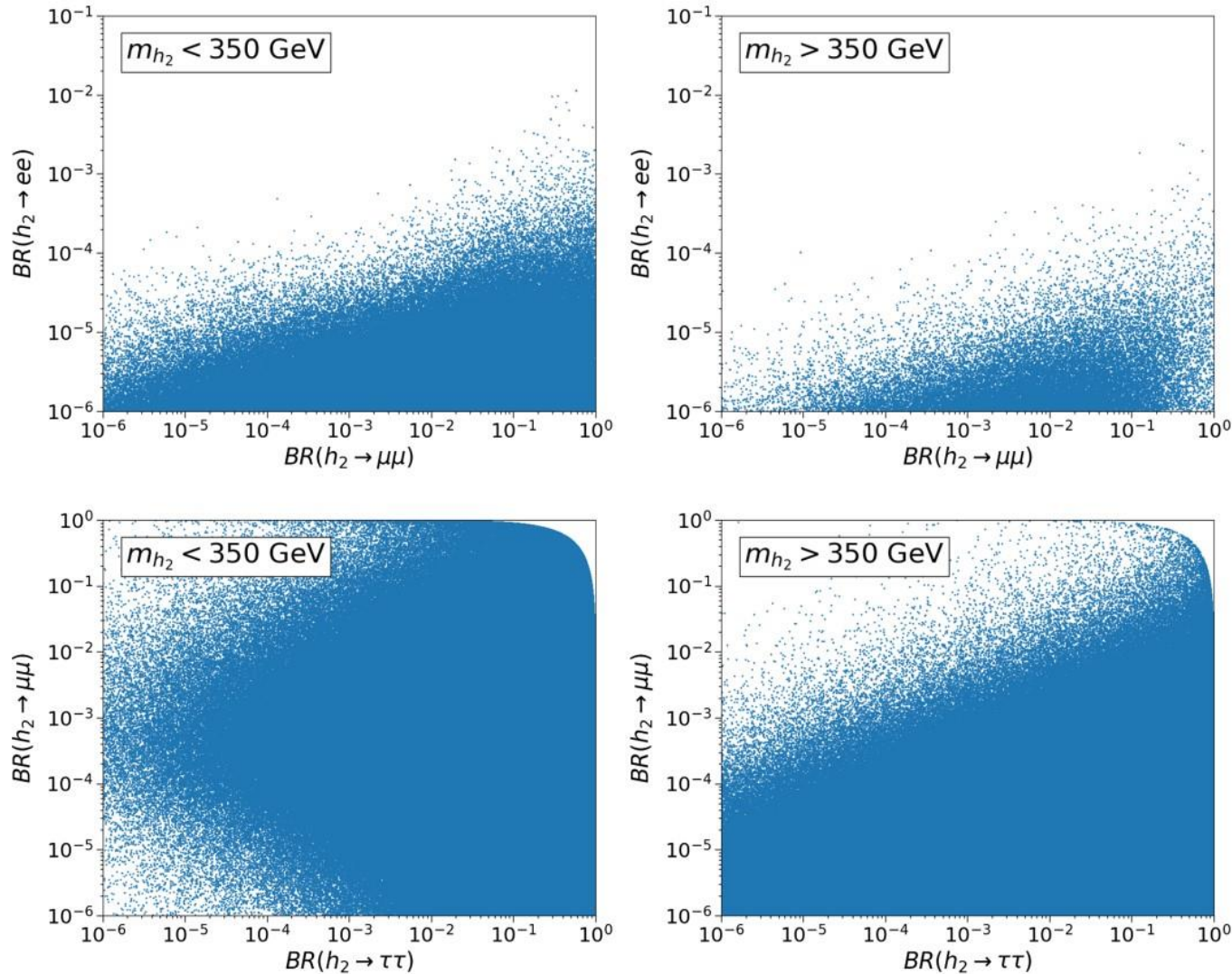
$$\lambda_4^{ij} = \frac{1}{v_i v_j} (2M_{c,ij}^2 - M_{p,ij}^2 - m_{ij}^2)$$

$$\lambda_5^{ij} = \frac{1}{v_i v_j} (M_{p,ij}^2 - m_{ij}^2)$$

The aligned model

- Bounded-from-below conditions
- Oblique parameters
- Quartic couplings and Yukawa couplings less than 4π
- Charged Higgs masses must exceed 80 GeV
- Higgs diphoton decay
- B and K meson oscillations
- $b \rightarrow s\gamma$ constraints
- Searches for heavy neutral and charged Higgs bosons at the LHC

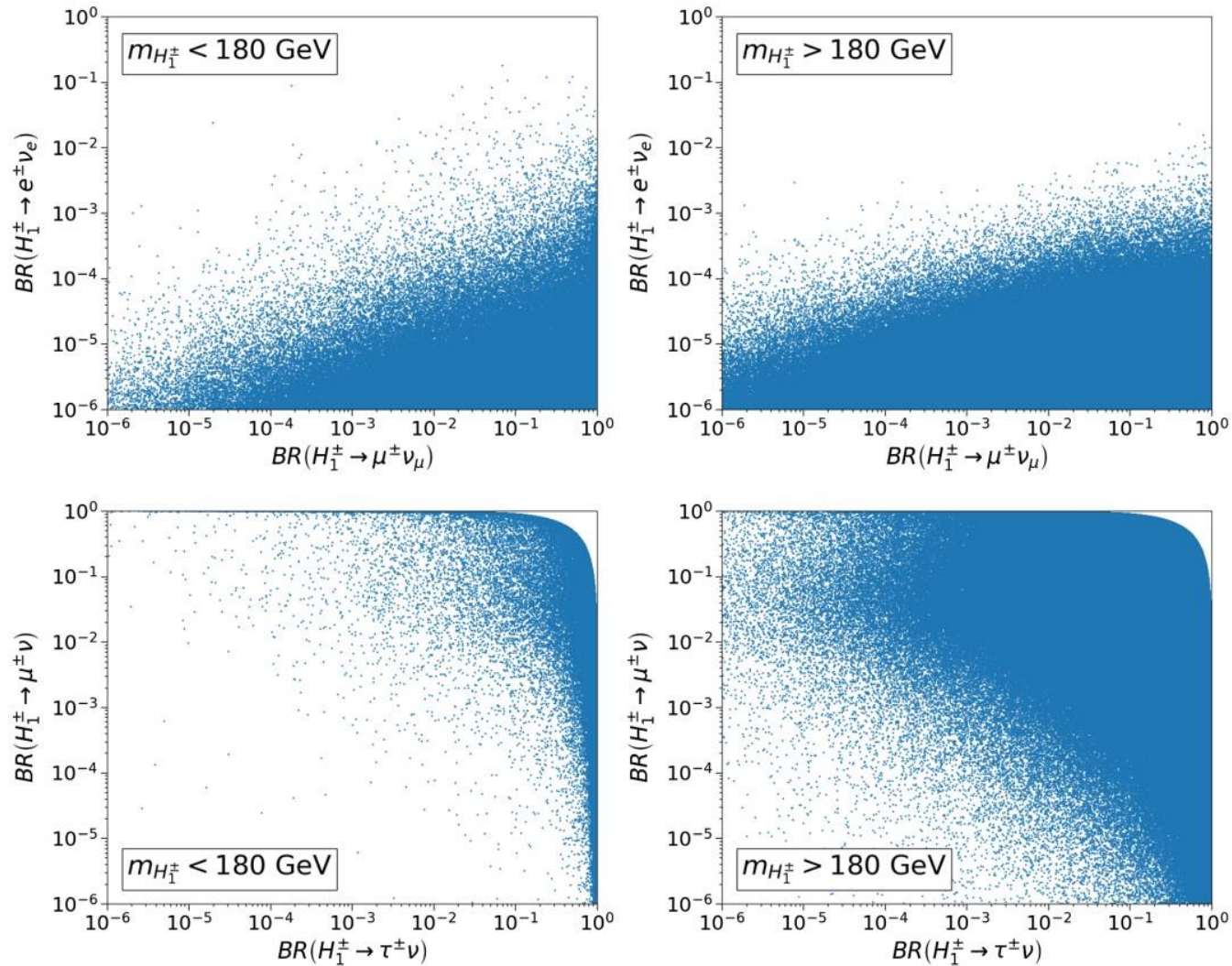
The aligned model



Masses > 350 GeV:
Opening of the top decay channel

Searches for heavy neutral Higgs bosons decaying into leptons, which generally focus on tauonic decays, should also study muonic and electronic decays

The aligned model



Masses > 180 GeV:
Opening of the top-bottom decay channel

There are more points in the region above 180 GeV since below that mass a much higher proportion of points are experimentally excluded

Concluding remarks

- We have studied a **4HDM** in which one scalar doublet couples to quarks and the other three couple to the electron, muon and tau families, respectively
- Dielectron and dimuon decays of the extra lightest neutral scalar can be much larger than expected
- An interesting signature arises from vector boson fusion into two Higgs bosons, each of which decays into an electron or muon pair

Concluding remarks

- We have studied a **4HDM** in which one scalar doublet couples to quarks and the other three couple to the electron, muon and tau families, respectively
- Dielectron and dimuon decays of the extra lightest neutral scalar can be much larger than expected
- An interesting signature arises from vector boson fusion into two Higgs bosons, each of which decays into an electron or muon pair

Funded through SFRH/BD/139165/2018 and CERN/FIS-PAR/0025/2021



Backup slides

Scalar benchmark points	S1	S2
$\beta_2/\pi, \beta_3/\pi, \beta_4/\pi$	0.05, 0.16, 0.18	0.04, 0.14, 0.21
$\alpha_{23}/\pi, \alpha_{24}/\pi, \alpha_{34}/\pi$	-0.09, -1.00, -0.70	-0.02, -0.05, 0.10
$\gamma_{23}/\pi, \gamma_{24}/\pi, \gamma_{34}/\pi$	0.50, 0.59, 0.80	0.16, 0.52, 0.39
$\delta_{23}/\pi, \delta_{24}/\pi, \delta_{34}/\pi$	0.08, -0.26, -0.96	0.62, -0.93, -0.95
$m_{h_2}, m_{h_3}, m_{h_4}$ (GeV)	269, 396, 483	175, 359, 360
$m_{A_1}, m_{A_2}, m_{A_3}$ (GeV)	439, 454, 484	265, 351, 369
$m_{H_1^\pm}, m_{H_2^\pm}, m_{H_3^\pm}$ (GeV)	438, 441, 443	289, 352, 370
$m_{qe}^2, m_{q\mu}^2, m_{q\tau}^2$ (GeV ²)	-17700, 71700, -340000	16000, -34600, -168000
$m_{e\mu}^2, m_{e\tau}^2, m_{\mu\tau}^2$ (GeV ²)	-18600, 20700, -53600	14000, -31200, -57400
$\text{BR}(h_2 \rightarrow ee)$	2.72×10^{-3}	1.63×10^{-4}
$\text{BR}(h_2 \rightarrow \mu\mu)$	4.68×10^{-1}	7.85×10^{-6}
$\text{BR}(h_2 \rightarrow \tau\tau)$	1.22×10^{-1}	7.42×10^{-1}

Backup slides

Charged benchmark points	C1	C2
$\beta_2/\pi, \beta_3/\pi, \beta_4/\pi$	0.05, 0.05, 0.09	0.10, 0.16, 0.11
$\alpha_{23}/\pi, \alpha_{24}/\pi, \alpha_{34}/\pi$	0.09, 0.54, 0.34	0.20, 0.88, 0.72
$\gamma_{23}/\pi, \gamma_{24}/\pi, \gamma_{34}/\pi$	-0.04, 0.66, 0.60	0.68, 0.50, -0.52
$\delta_{23}/\pi, \delta_{24}/\pi, \delta_{34}/\pi$	-0.98, 0.00, -0.36	1.00, 0.00, 0.77
$m_{h_2}, m_{h_3}, m_{h_4}$ (GeV)	127, 187, 208	180, 237, 240
$m_{A_1}, m_{A_2}, m_{A_3}$ (GeV)	131, 179, 244	161, 172, 173
$m_{H_1^\pm}, m_{H_2^\pm}, m_{H_3^\pm}$ (GeV)	164, 172, 229	158, 181, 234
$m_{qe}^2, m_{q\mu}^2, m_{q\tau}^2$ (GeV ²)	-14800, -17400, 6210	57000, -127000, -15100
$m_{e\mu}^2, m_{e\tau}^2, m_{\mu\tau}^2$ (GeV ²)	5880, 22100, 9060	-75600, -9570, 81300
$\text{BR}(H_1^\pm \rightarrow e^\pm \nu_e)$	2.24×10^{-3}	1.68×10^{-2}
$\text{BR}(H_1^\pm \rightarrow \mu^\pm \nu_\mu)$	5.36×10^{-1}	6.91×10^{-3}
$\text{BR}(H_1^\pm \rightarrow \tau^\pm \nu_\tau)$	4.55×10^{-1}	5.23×10^{-1}