

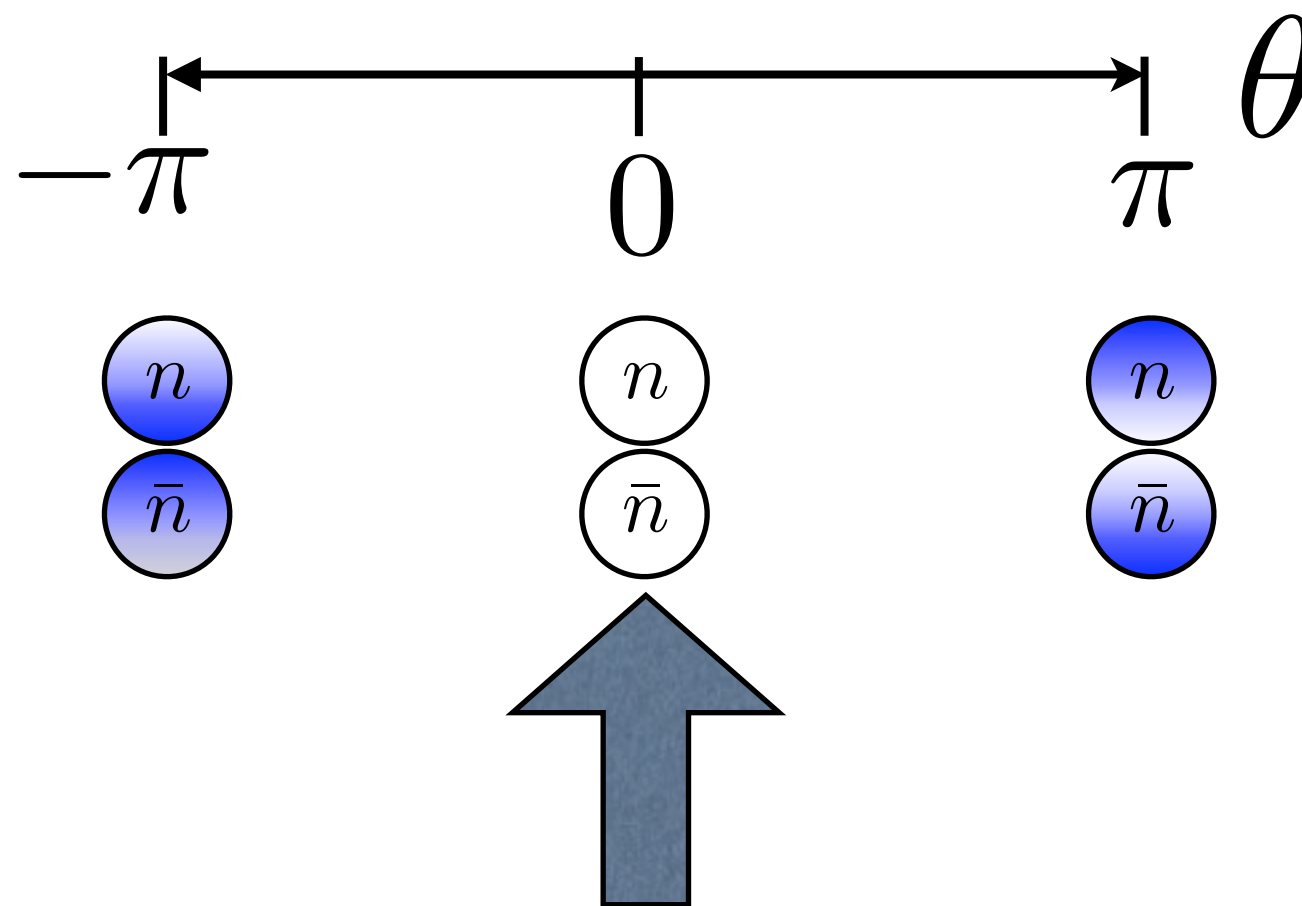
Axions, dark matter and all that MAD(MAX) stuff

**Javier Redondo
(Zaragoza U & MPP)**

**Warsaw Workshop on Non-standard (?)
dark matter: multicomponent scenarios and beyond
4th June 2016**

The theta angle of the strong interactions

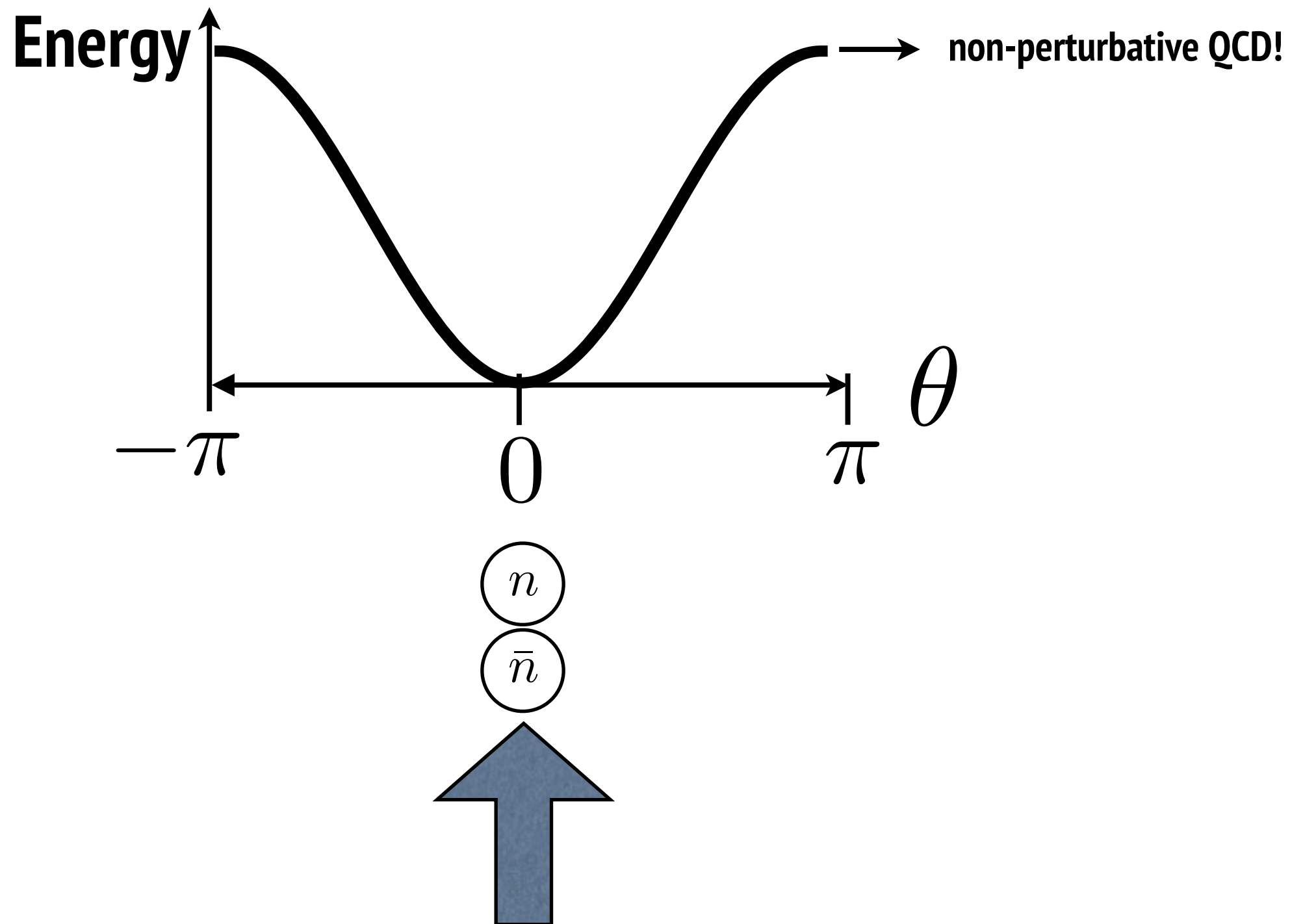
- The value of θ controls matter-antimatter differences in QCD



Measured today $|\theta| < 10^{-10}$ (strong CP problem)

Axions

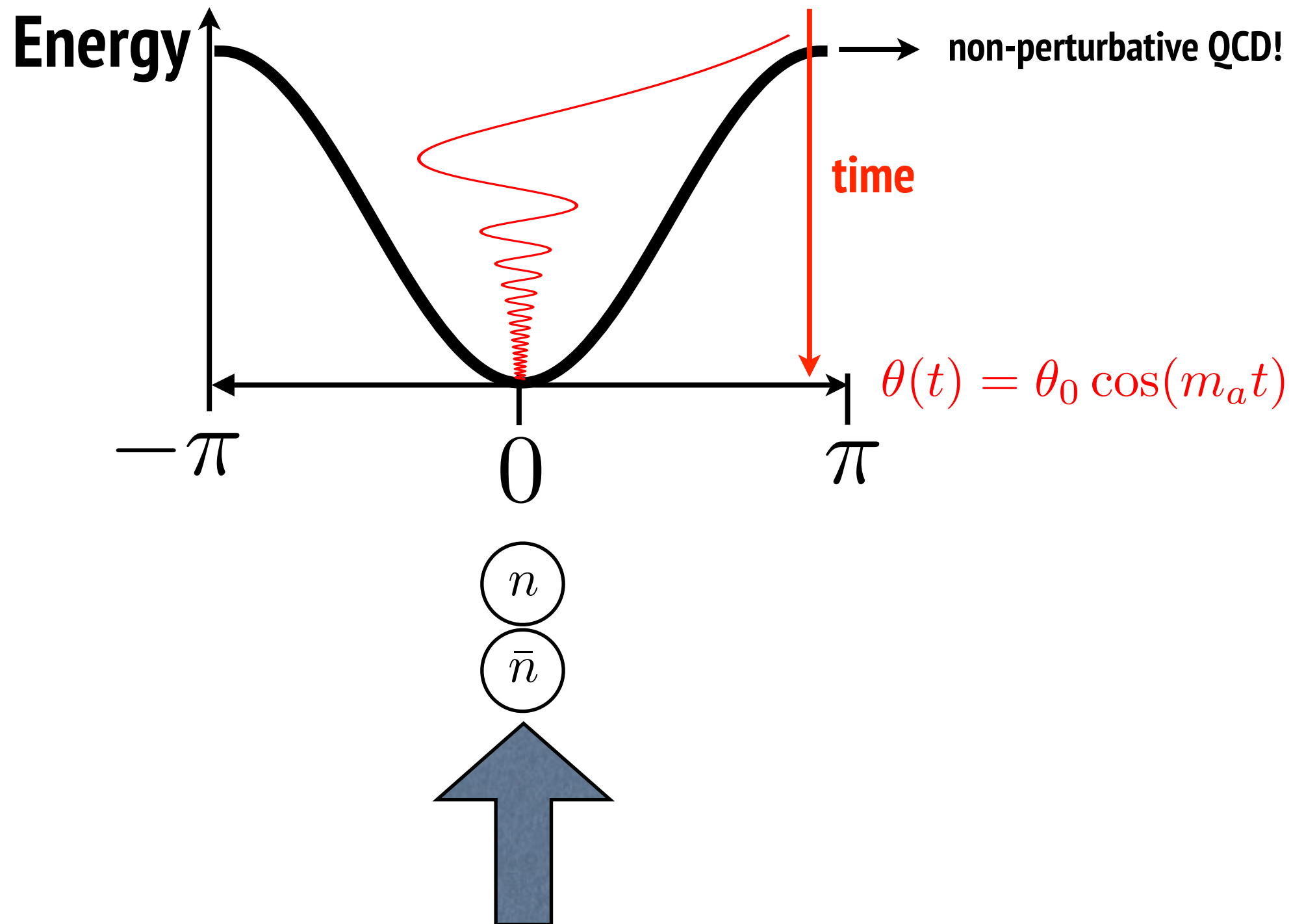
- is it a dynamical field? $\theta(t, \mathbf{x})$



Measured today $|\theta| < 10^{-10}$ (strong CP problem)

Axions are necessarily dark matter

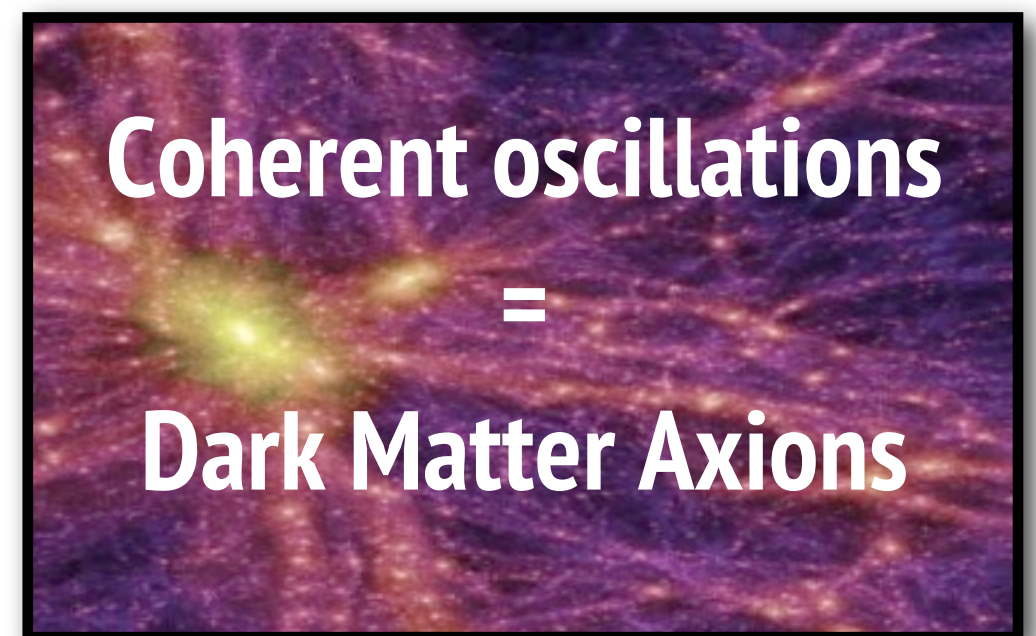
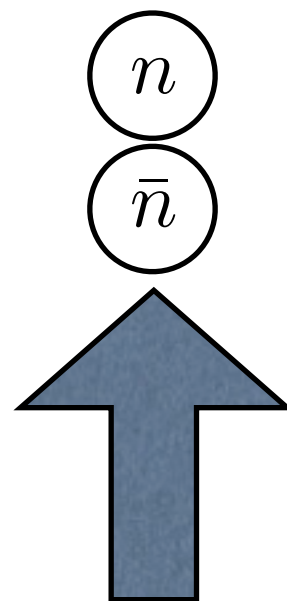
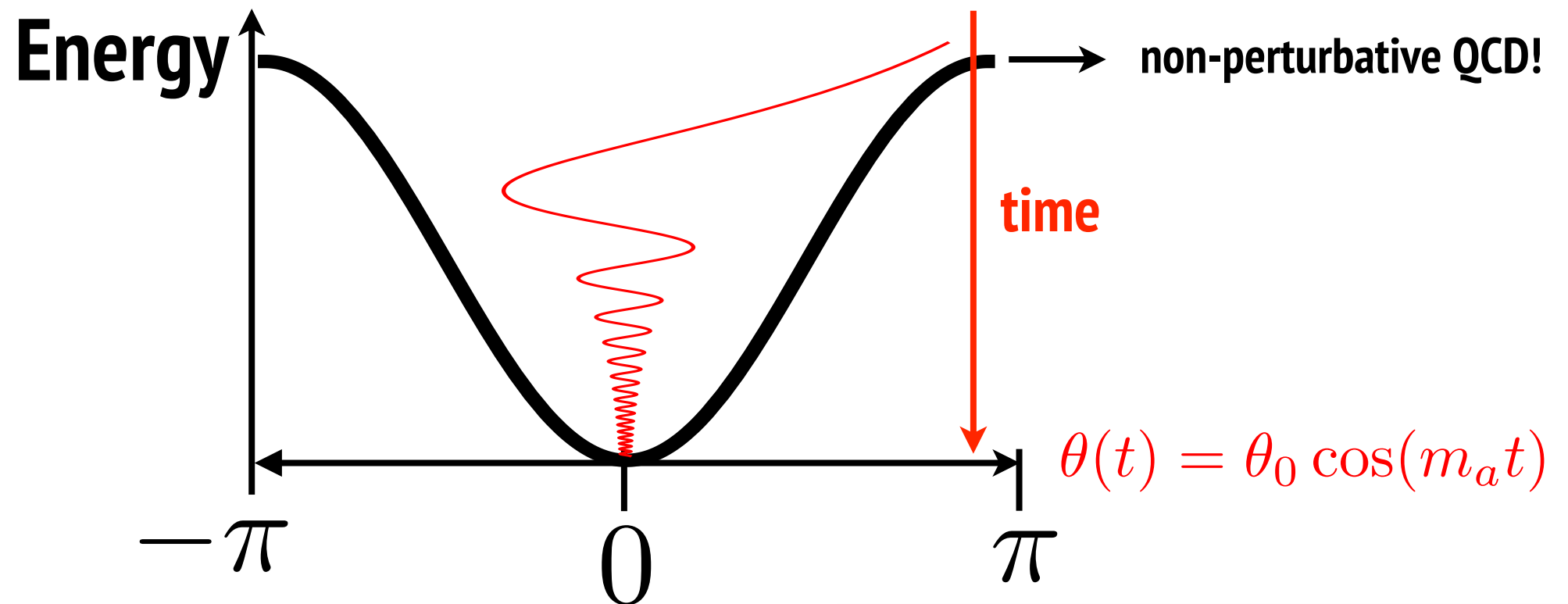
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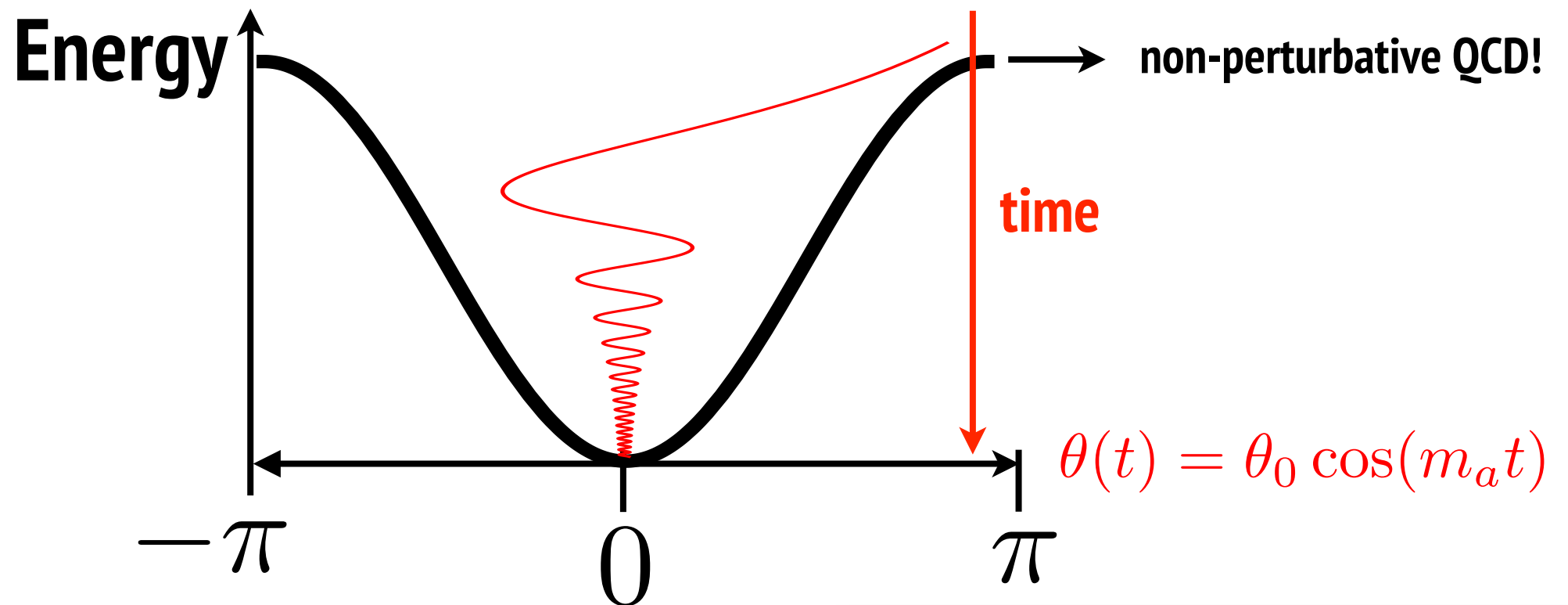
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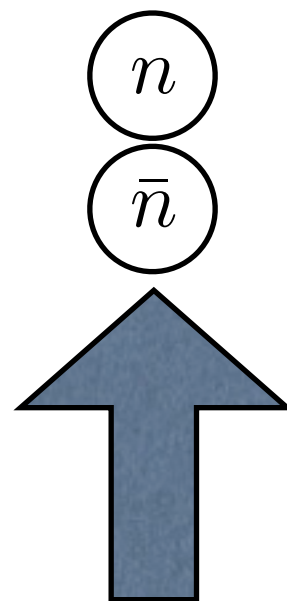


~ One parameter theory

$$\theta(t, x) = a(t, x)/f_a$$

axion mass

$$m_a = 6 \text{ meV} \frac{10^9 \text{ GeV}}{f_a}$$



Coherent oscillations

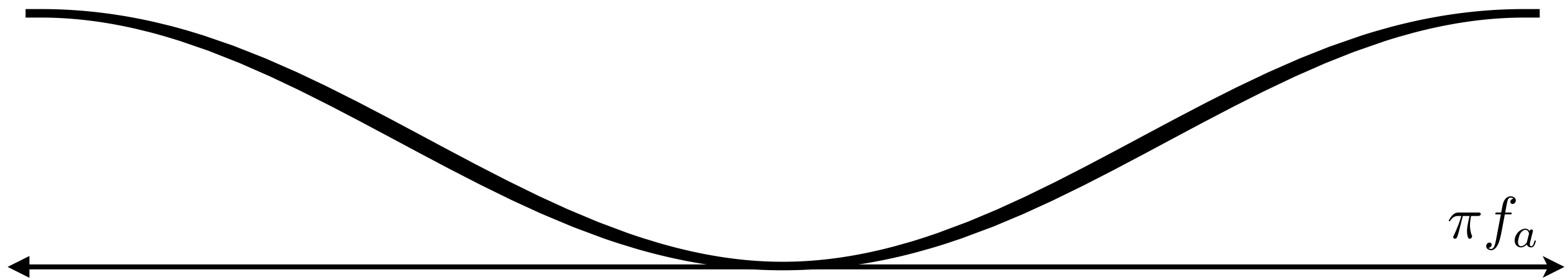
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Dark Matter Axions

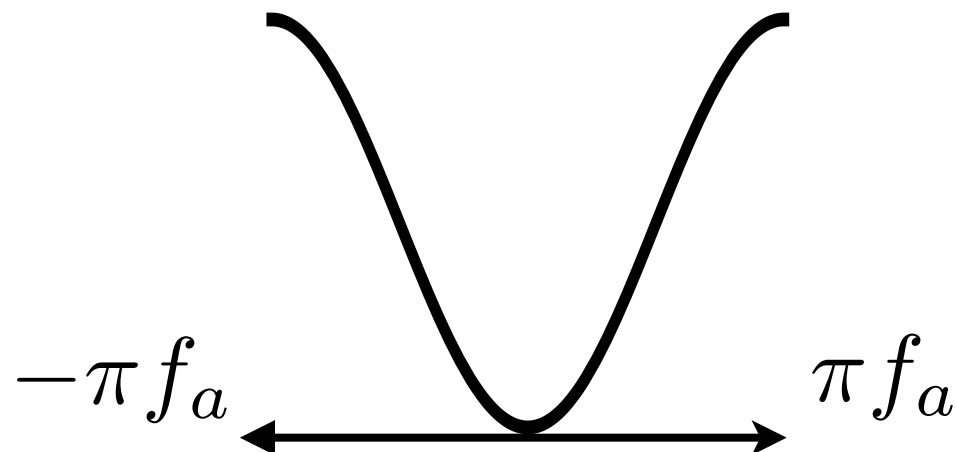
Measured today $|\theta| < 10^{-10}$ (strong CP problem)

Axion dark matter

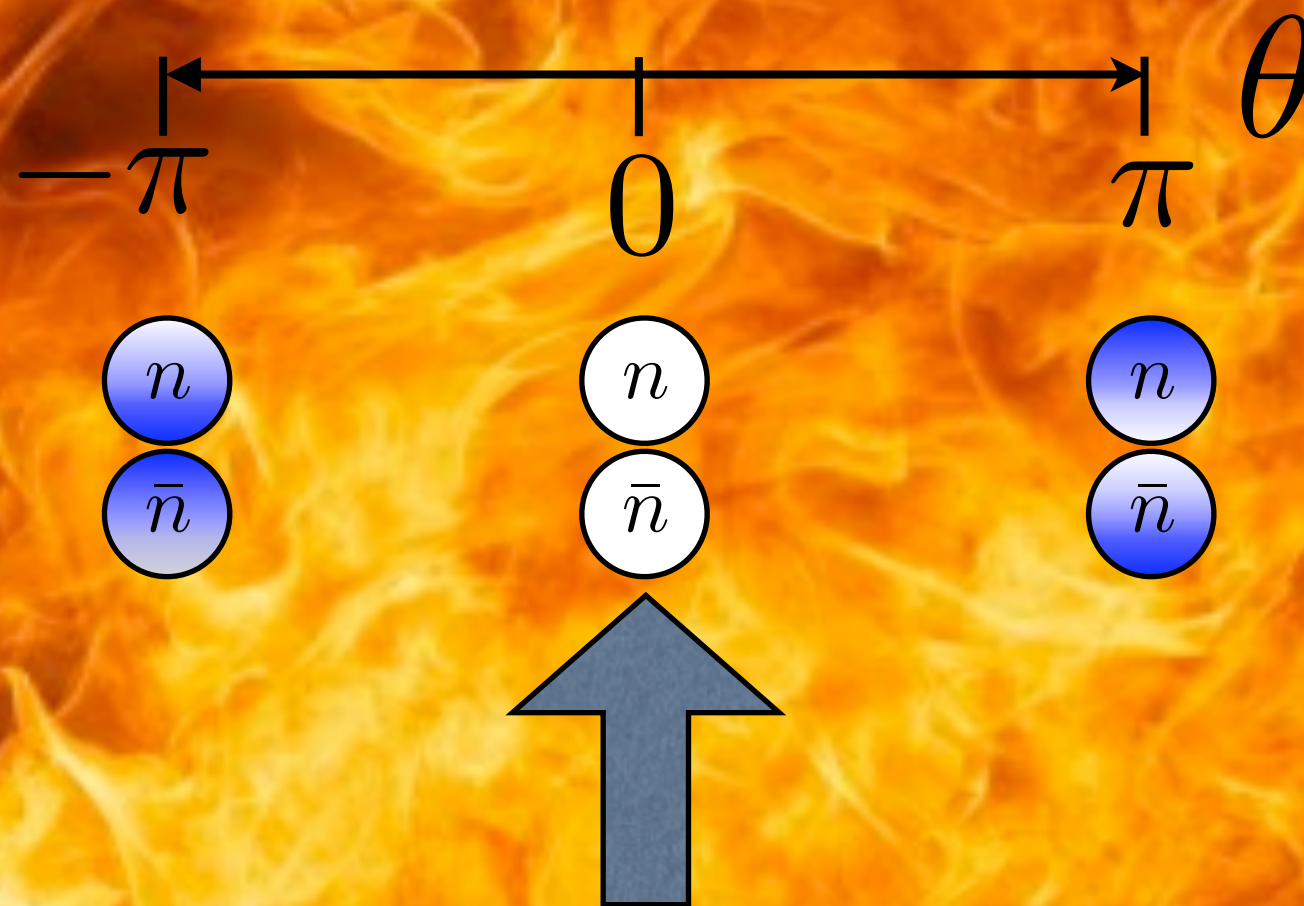
- The amount of axion DM produced depends on f_a
- large f_a , small curvature, oscillations start later $\rightarrow$ more DM



- small f_a , large curvature, oscillations start earlier $\rightarrow$ less DM

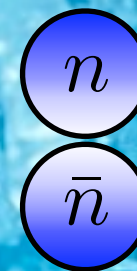
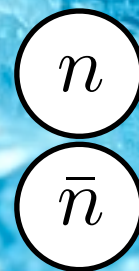
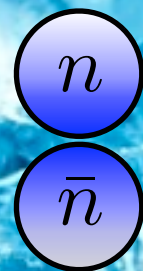
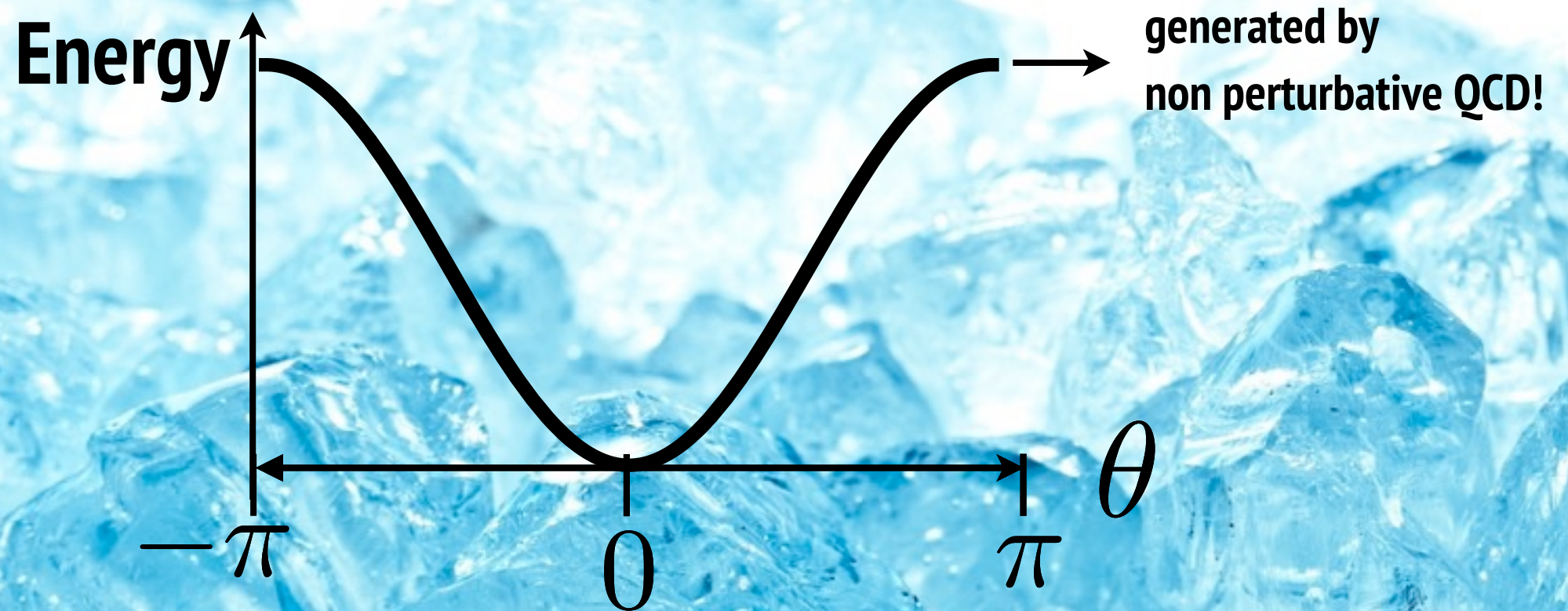


no preferred value at high Temperature ($T > \Lambda_{\text{QCD}}$)



Measured today $|\theta| < 10^{-10}$ (strong CP problem)

below confinement, $\theta = 0$ minimises vacuum energy!



Measured today $|\theta| < 10^{-10}$ (strong CP problem)

Simple model KSVZ

- Peccei-Quinn symmetry, color anomalous, spontaneously broken at f_a

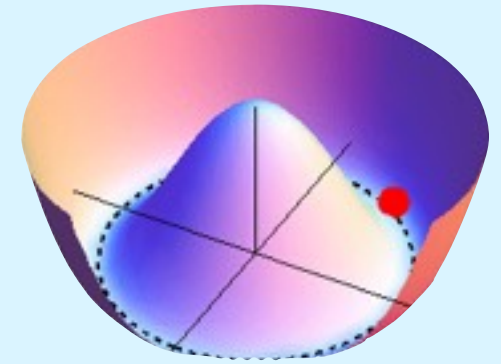
↑
ENERGY

Simple model KSVZ

- Peccei-Quinn symmetry, color anomalous, spontaneously broken at f_a

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + i\bar{Q}DQ - (y\bar{Q}_L Q_R \Phi + \text{h.c.}) - \lambda|\Phi|^4 + \mu^2|\Phi|^2$$

$$\Phi(x) = \rho(x)e^{i\frac{a(x)}{f_a}}$$



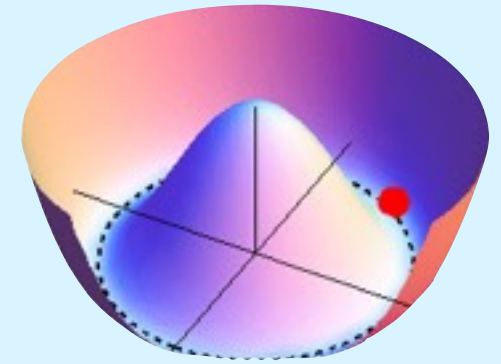
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- At energies below f_a (SSB)

$$\mathcal{L} \in \frac{1}{2}(\partial a)^2 + \frac{\alpha_s}{8\pi} G\tilde{G} \frac{a}{f_a}$$

$\sim f_a$

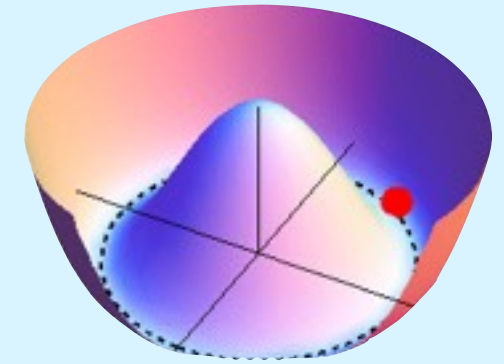
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- At energies below f_a (SSB)

$$\mathcal{L} \in \frac{1}{2}(\partial a)^2 + \frac{\alpha_s}{8\pi} G\tilde{G} \frac{a}{f_a}$$

- At energies below Λ_{QCD} , $a \rightarrow \eta' \rightarrow \pi^0 \rightarrow \eta \rightarrow \dots$ mixing

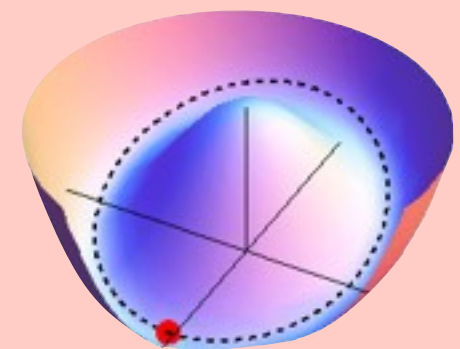
axion mass $m_a \simeq \frac{m_\pi f_\pi}{f_a} \sim 6\text{meV} \frac{10^9\text{GeV}}{f_a}$

couplings $\mathcal{L}_{a,I} = \sum_N c_{N,a} \bar{N} \gamma^\mu \gamma_5 N \frac{a}{f_a} + c_{a\gamma} \frac{\alpha}{2\pi} F_{\mu\nu} \tilde{F}^{\mu\nu} \frac{a}{f_a} + \dots$

nucleons ...

photons ...

mesons ...



ENERGY $\sim f_a$ $\sim \text{GeV}$

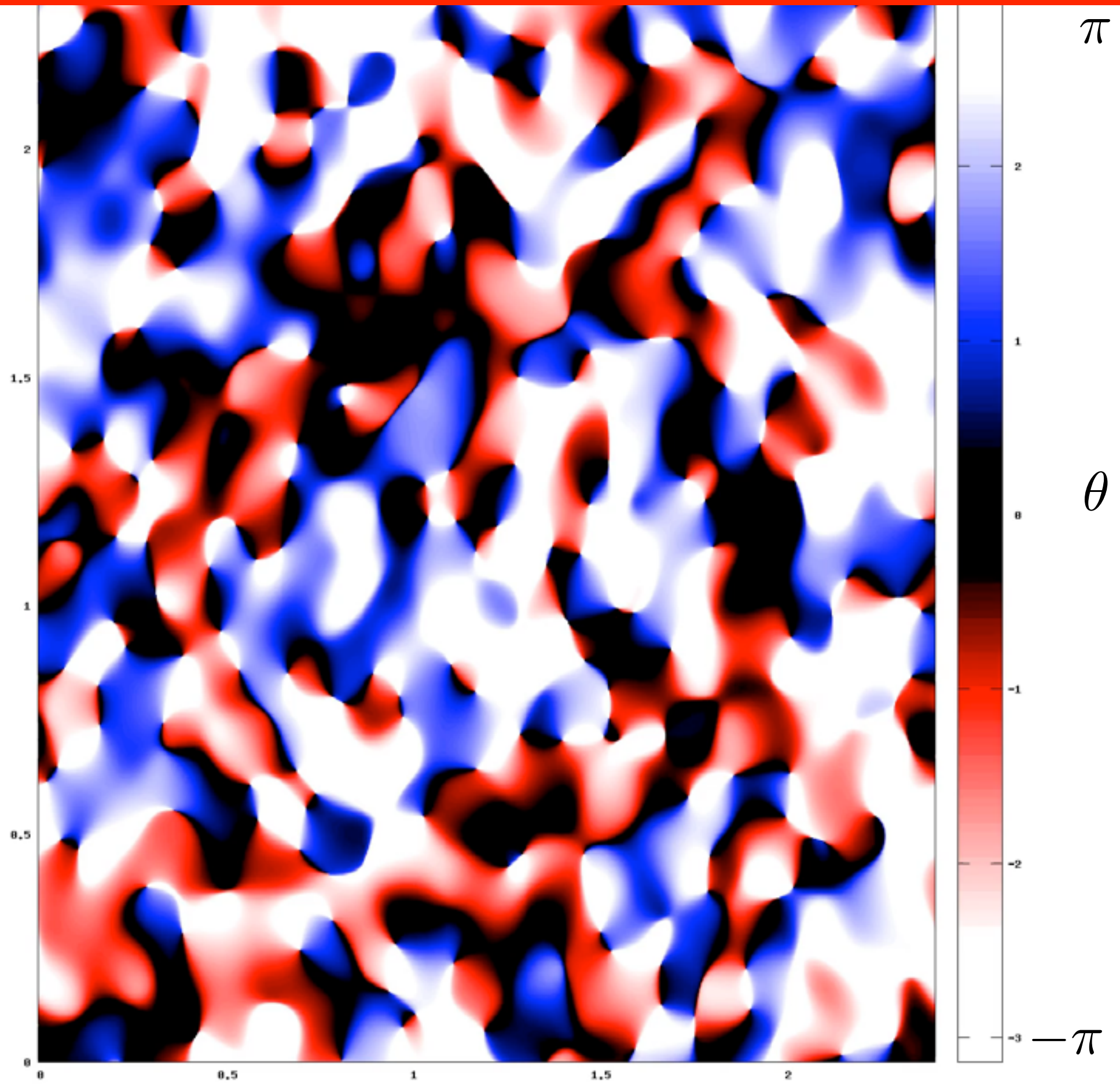
Theta evolution, Averaged SCENARIO I

π

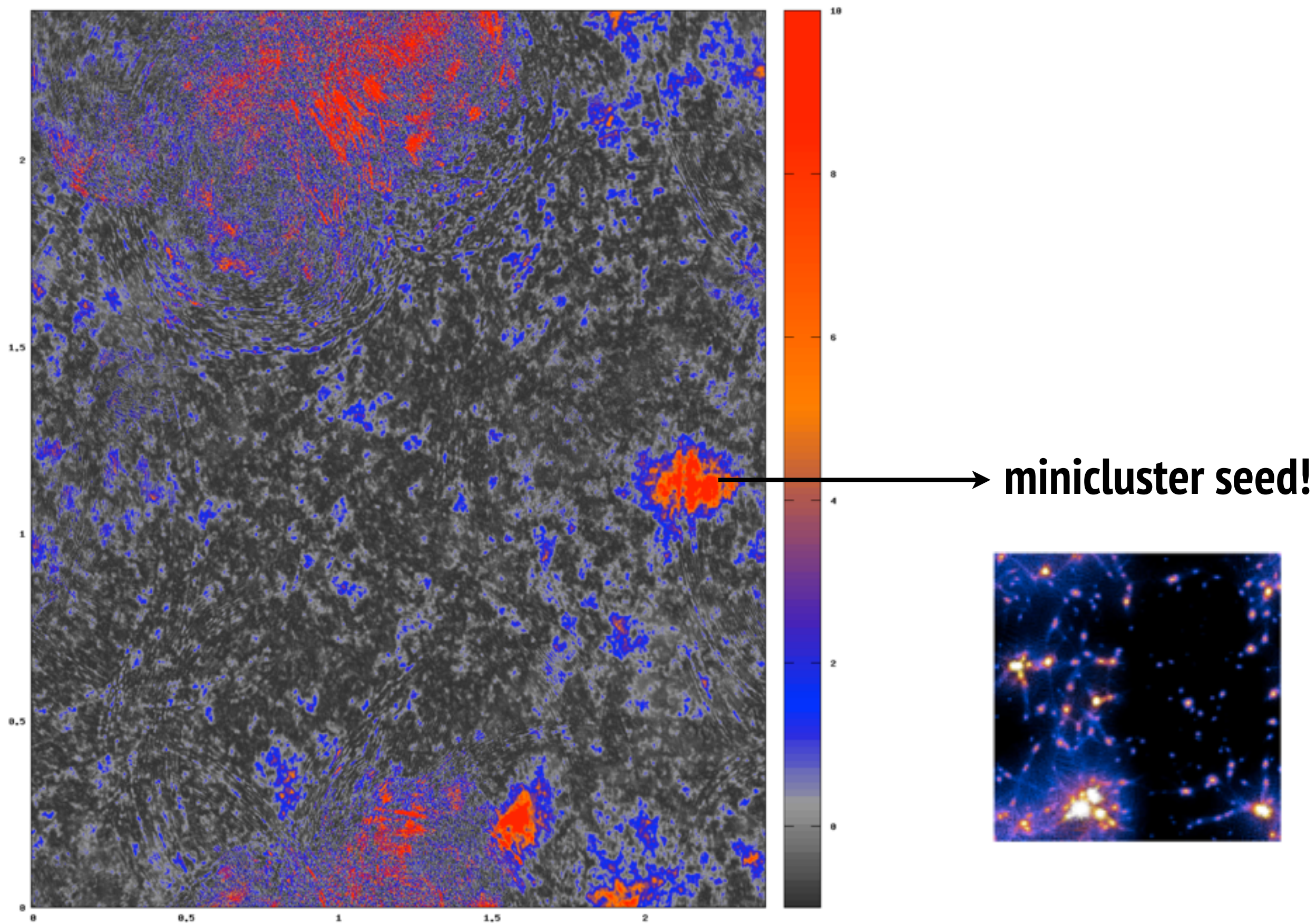
θ

$-\pi$

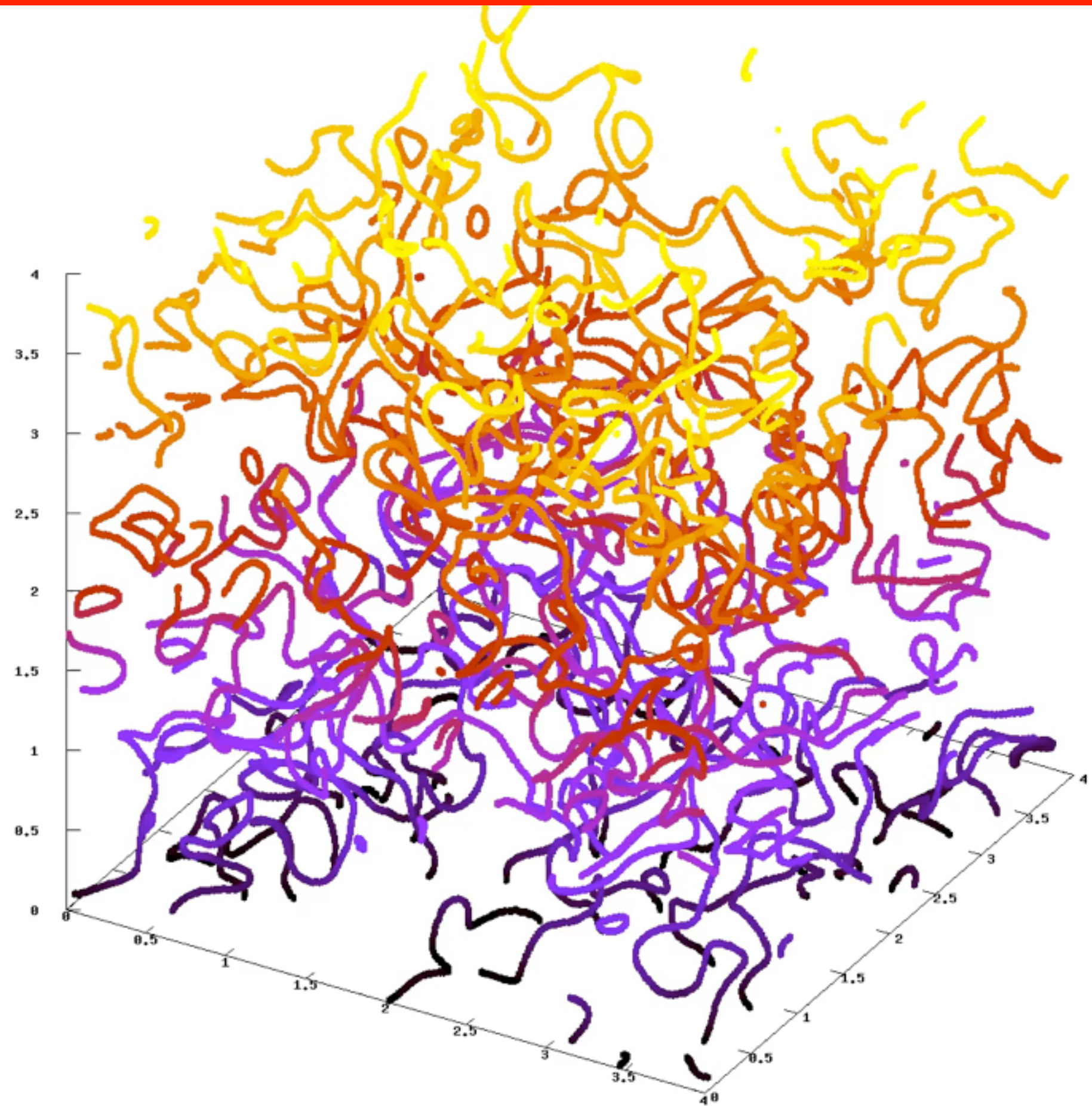
Theta evolution, Averaged SCENARIO I



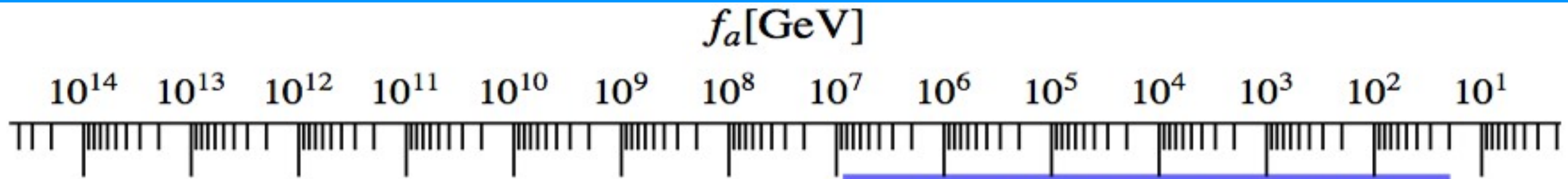
Dark matter density, inhomogeneous at comoving mpc scales



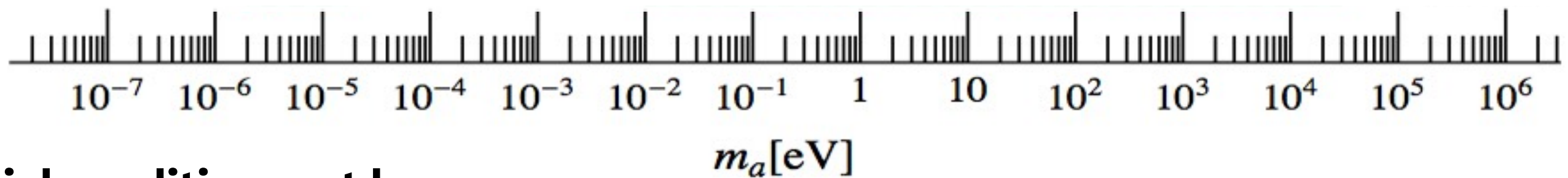
Strings



Axion dark matter (Scenario I)

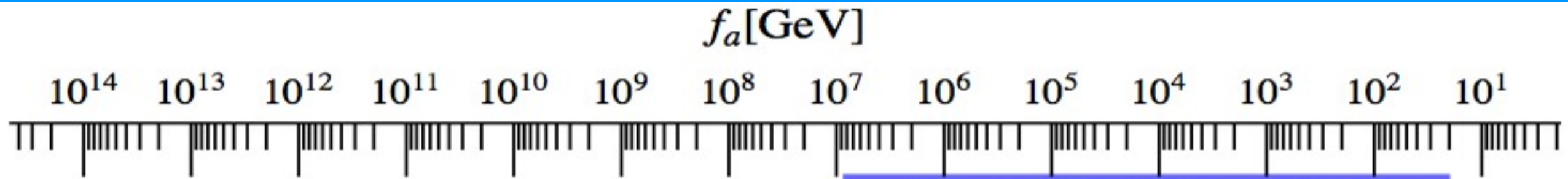


- Axion DM scenarios



Initial conditions set by :

Axion dark matter (Scenario I)

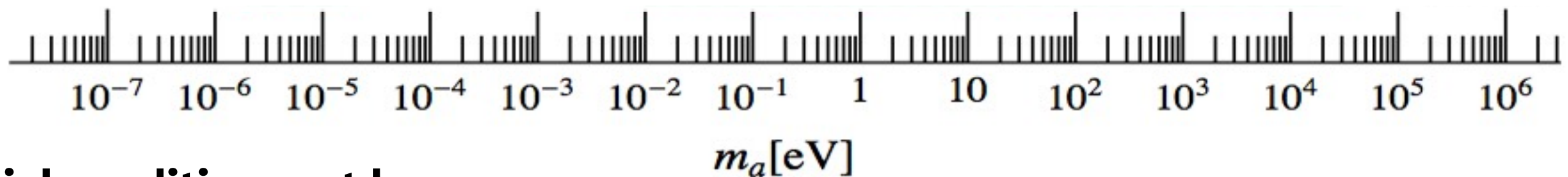


- Axion DM scenarios

Excluded (too much DM)

ok

sub

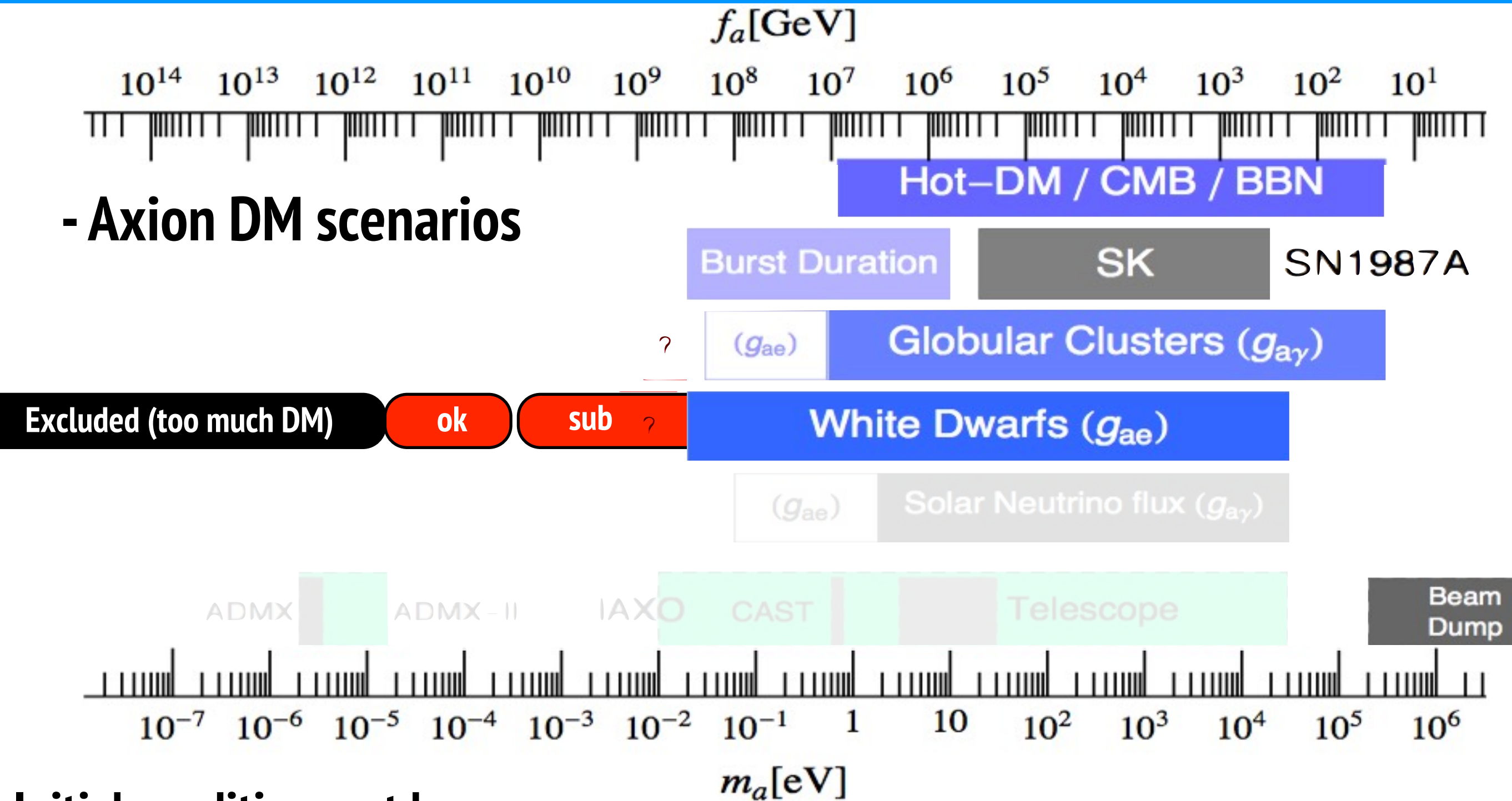


Initial conditions set by :

Phase transition (N=1)
strings+unstable DW's

Axion dark matter (Scenario I)

- Axion DM scenarios

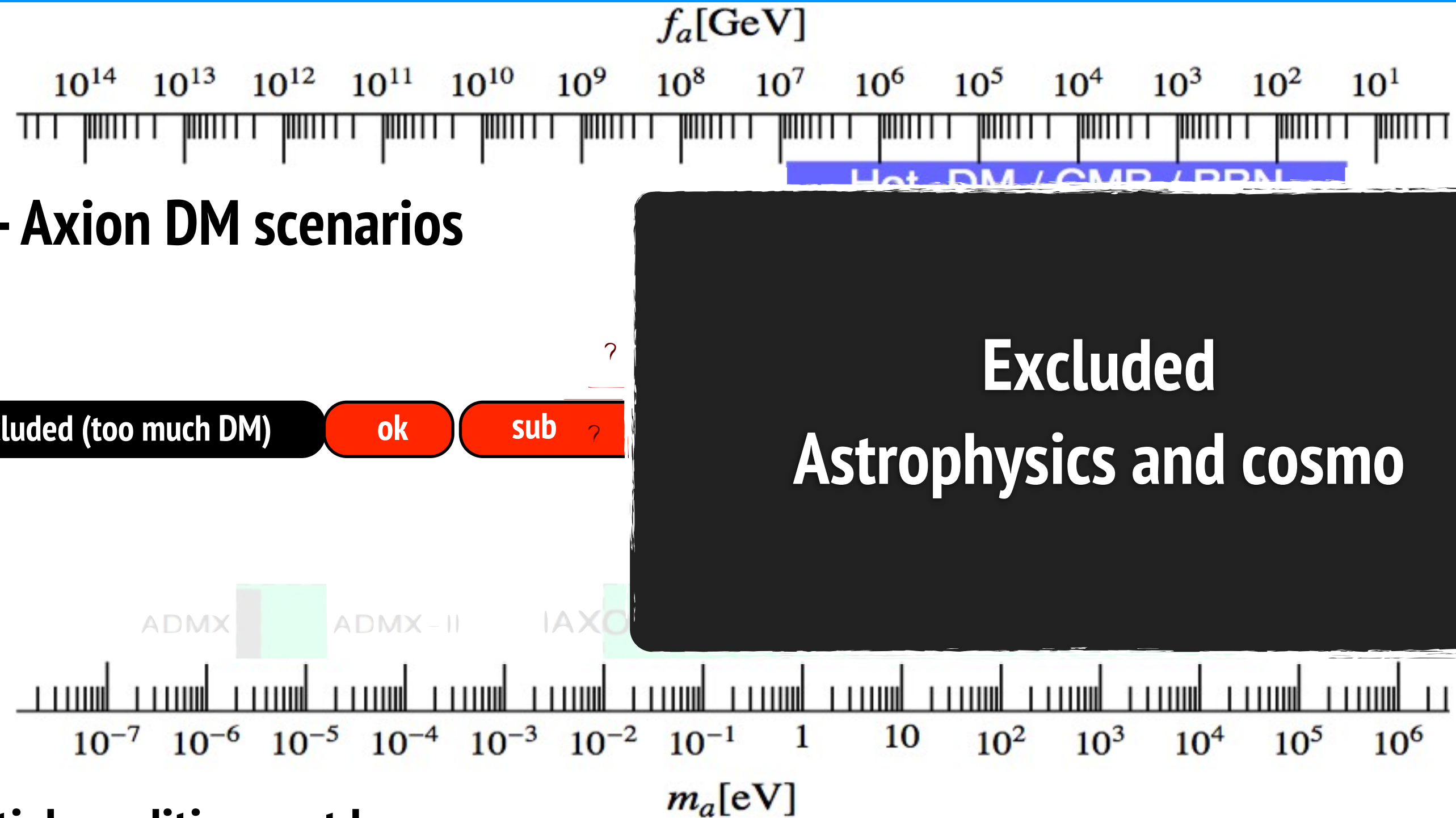


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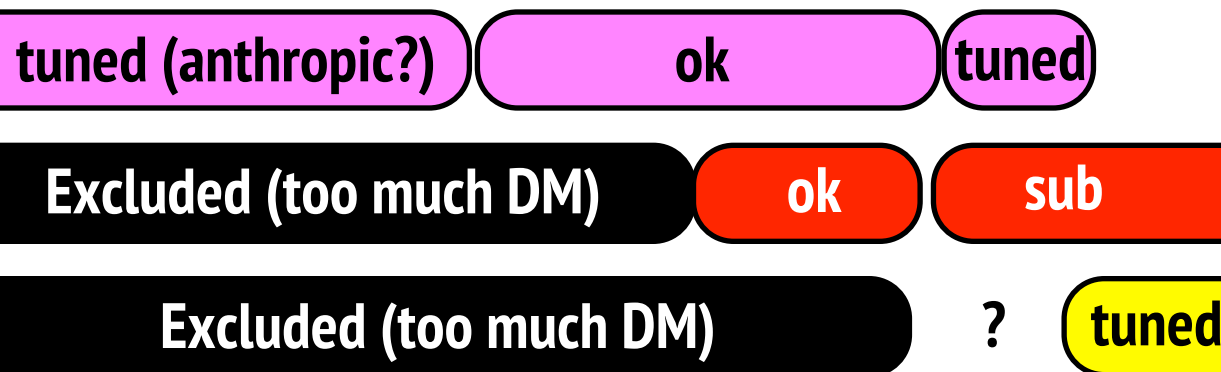
**Phase transition (N=1)
strings+unstable DW's**

Axion dark matter

$f_a[\text{GeV}]$

$10^{14} \quad 10^{13} \quad 10^{12} \quad 10^{11} \quad 10^{10} \quad 10^9 \quad 10^8 \quad 10^7 \quad 10^6 \quad 10^5 \quad 10^4 \quad 10^3 \quad 10^2 \quad 10^1$

- Axion DM scenarios



Excluded

$10^{-7} \quad 10^{-6} \quad 10^{-5} \quad 10^{-4} \quad 10^{-3} \quad 10^{-2} \quad 10^{-1} \quad 1 \quad 10 \quad 10^2 \quad 10^3 \quad 10^4 \quad 10^5 \quad 10^6$

$m_a[\text{eV}]$

Initial conditions set by :

Inflation smooth

$$\Omega_{\text{aDM}} h^2 \simeq \theta_I^2 \left(\frac{80 \mu\text{eV}}{m_a} \right)^{1.19}$$

Phase transition (N=1)
strings+unstable DW's

Phase transition (N>1)
strings+long-lived DWs

Axion dark matter

**Dark Matter
huge parameter space!**

$f_a[\text{GeV}]$

10^8 10^7 10^6 10^5 10^4 10^3 10^2 10^1

tuned (anthropic?)

ok

tuned

Excluded (too much DM)

ok

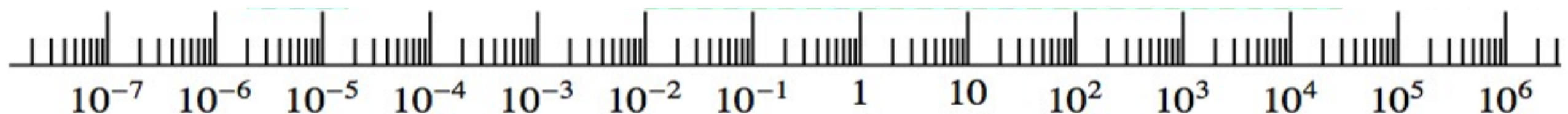
sub

Excluded (too much DM)

?

tuned

Excluded



$m_a[\text{eV}]$

Initial conditions set by :

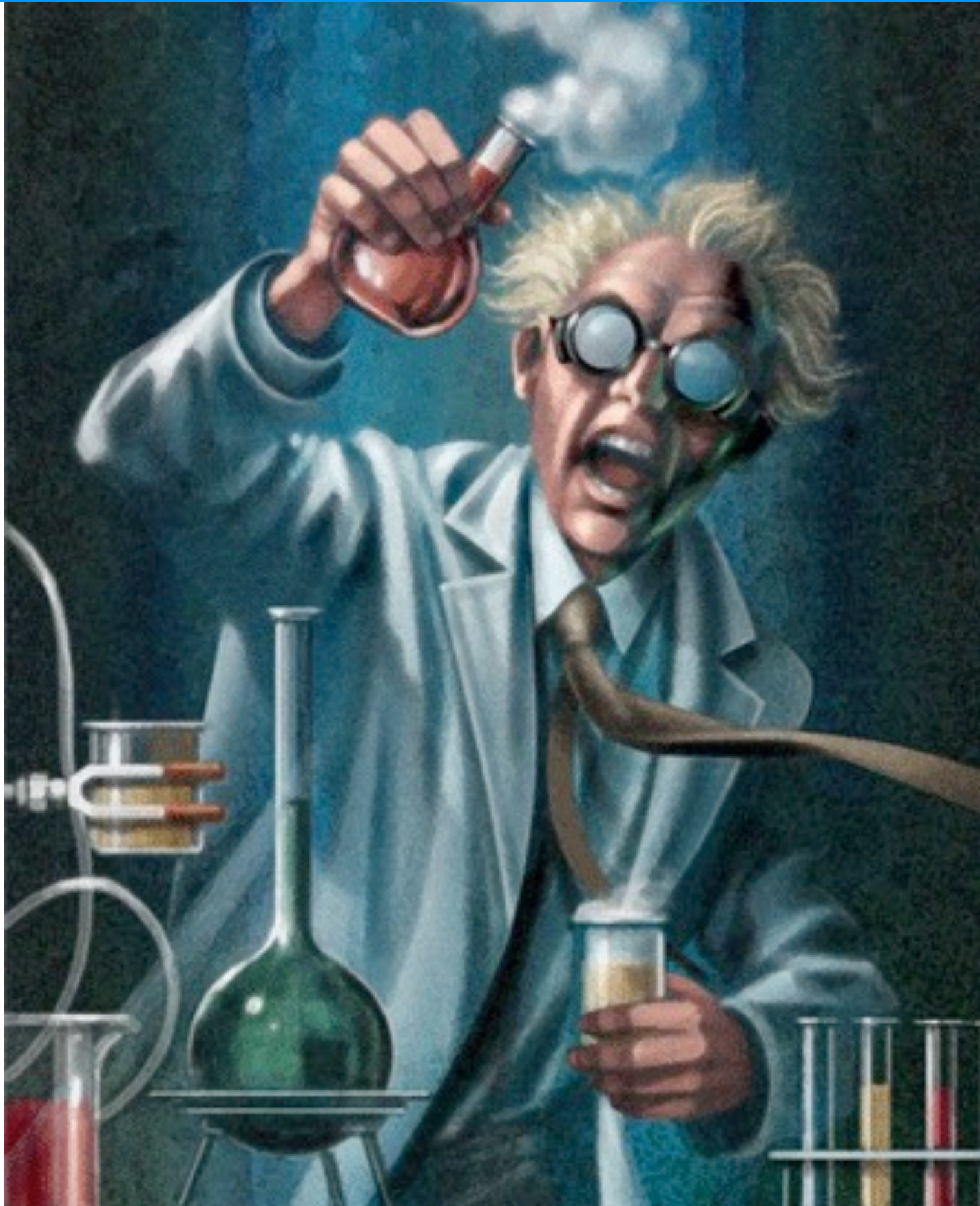
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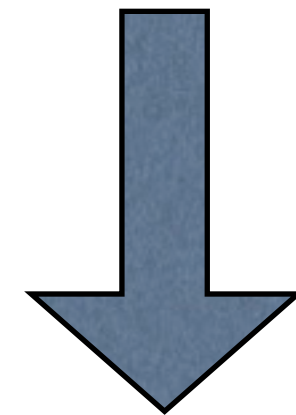
**Phase transition (N=1)
strings+unstable DW's**

**Phase transition (N>1)
strings+long-lived DWs**

Detecting SCL Axions



$$\rho_{\text{aDM}} = 0.3 \frac{\text{GeV}}{\text{cm}^3}$$



$$\theta_0 = 3.6 \times 10^{-19}$$

Detecting Axion (Dark Matter) in the lab

$$\rho_{\text{CDM}} \simeq 0.3 \frac{\text{GeV}}{\text{cm}^3} = m_a n_a \simeq \frac{1}{2} m_a^2 f_a^2 \theta^2 \longrightarrow \theta \sim O(10^{-19})$$

velocities in the galaxy

$$v \lesssim 300 \text{ km/s} \sim 10^{-3} c$$

phase space density

$$\frac{n_a}{\frac{4\pi p^3}{3}} \sim 10^{29} \left(\frac{\mu\text{eV}}{m_a} \right)^4$$

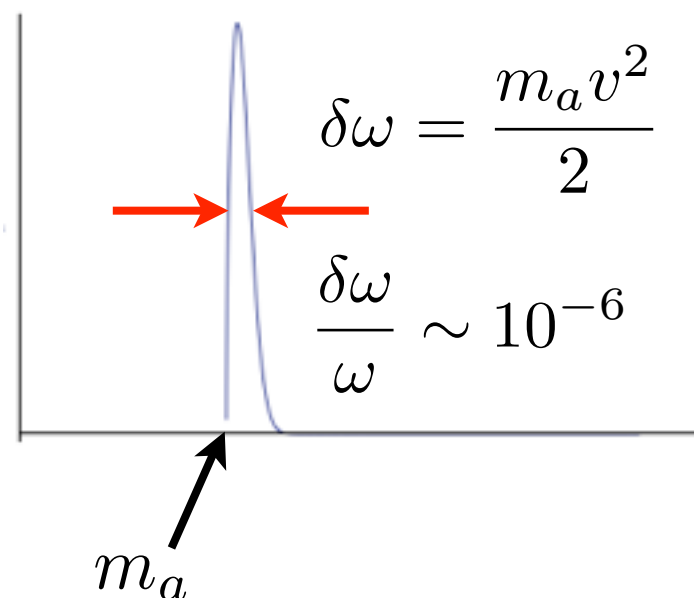
occupation number is HUGE! $\longrightarrow$ treat it like a classical coherent (NR) field

Roughly...

$$a(t) = a_0 \cos(m_a t)$$

Fourier-transform $a(x)$

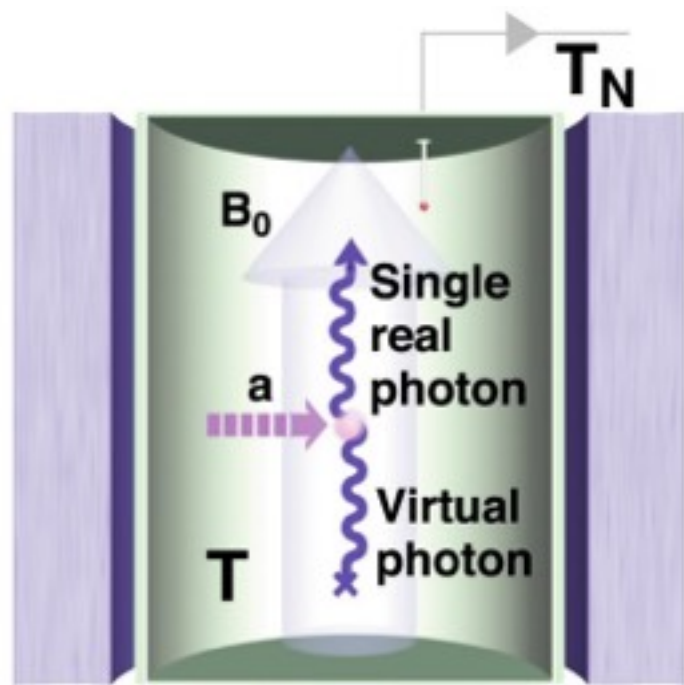
$$\omega \simeq m_a (1 + v^2/2 + \dots)$$



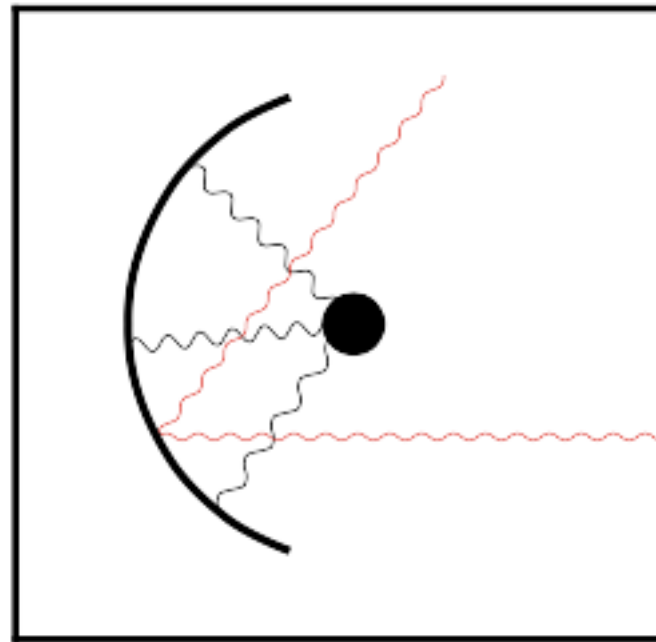
$$\delta t \sim \frac{1}{\delta\omega} \sim 0.13 \text{ms} \left(\frac{10^{-5} \text{eV}}{m_a} \right)$$

$$\delta L \sim \frac{1}{\delta p} \sim 20 \text{m} \left(\frac{10^{-5} \text{eV}}{m_a} \right)$$

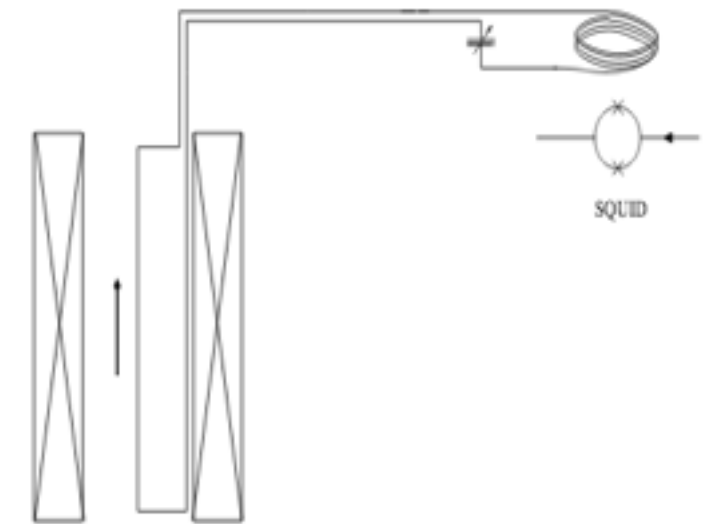
Cavities



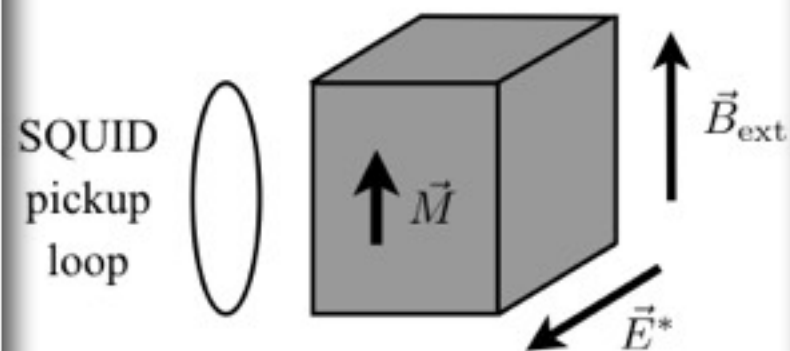
Mirrors



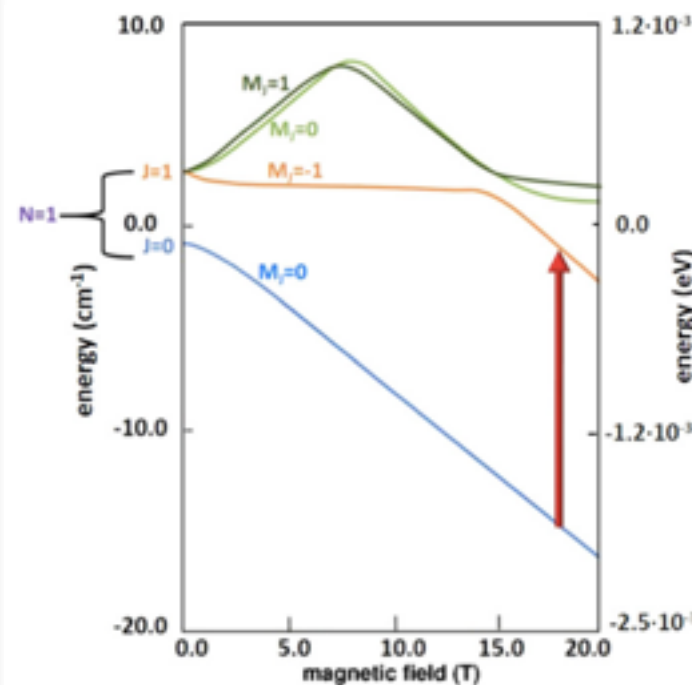
LC-circuit



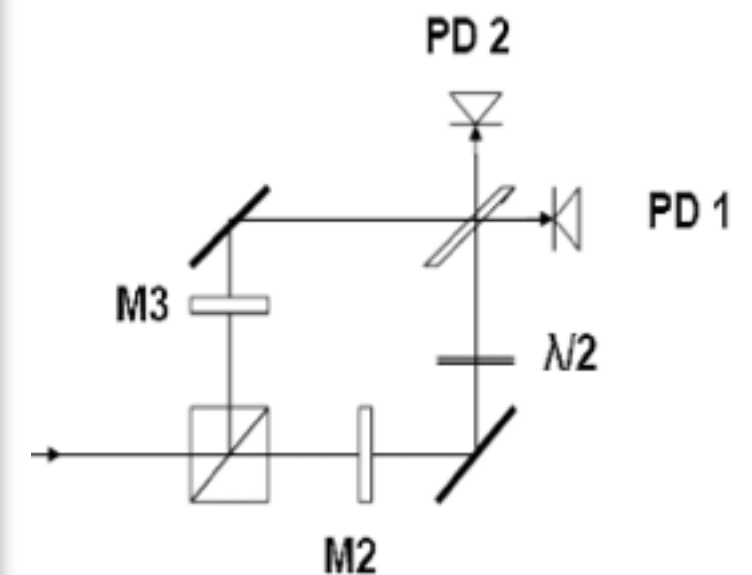
Spin precession



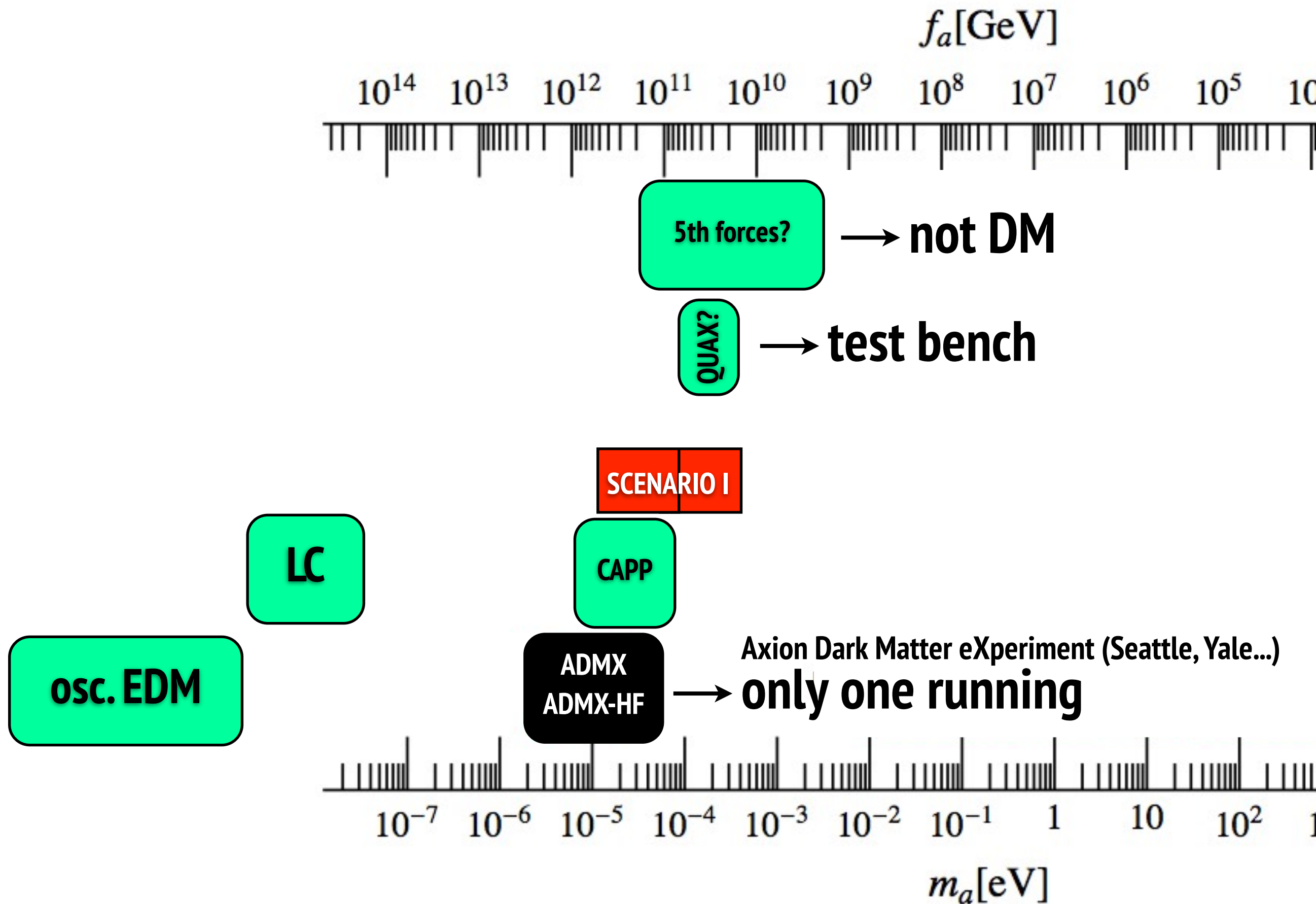
Atomic transitions



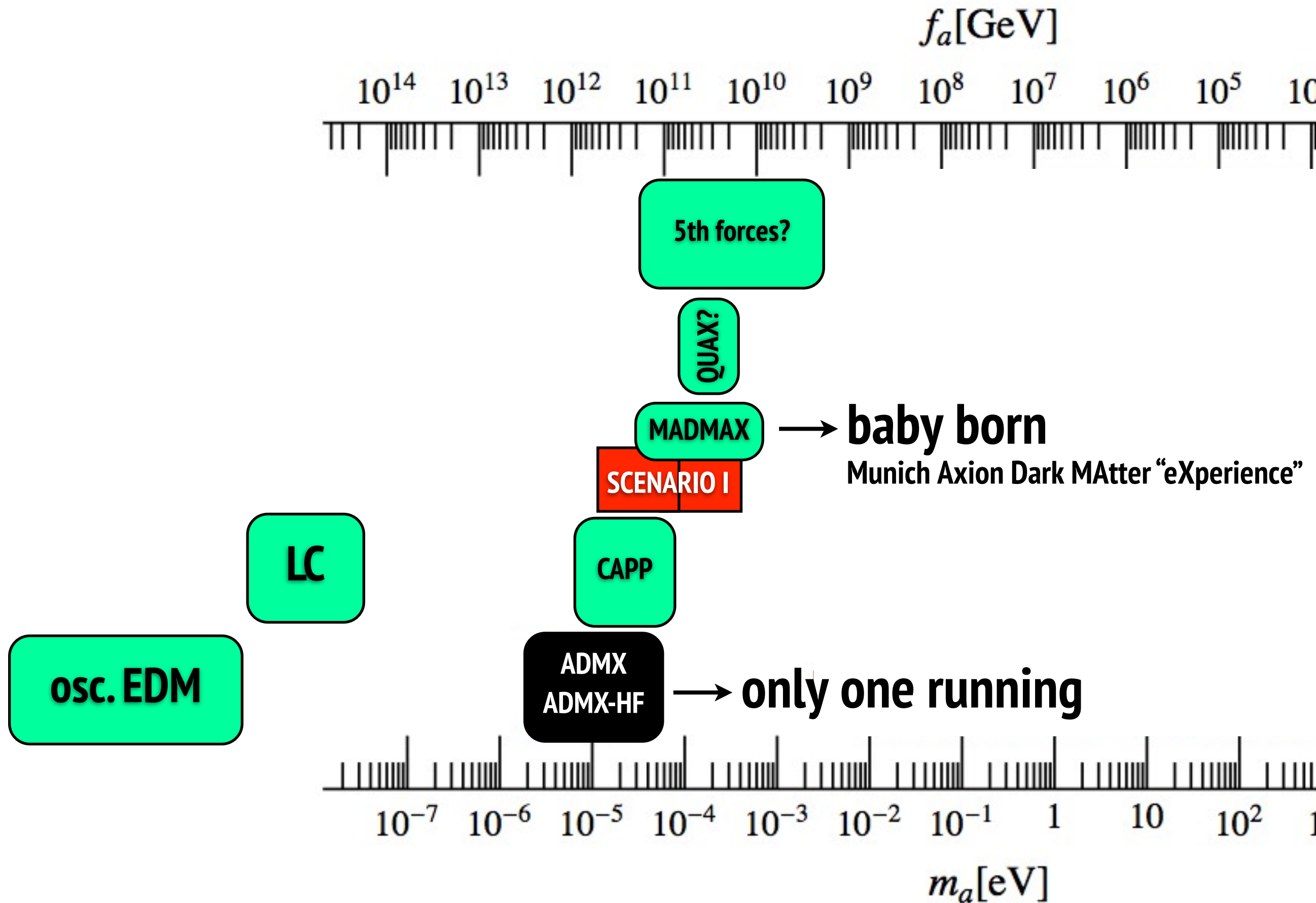
Optical



Axion Dark matter experiments (target areas)



Axion Dark matter experiments (target areas)



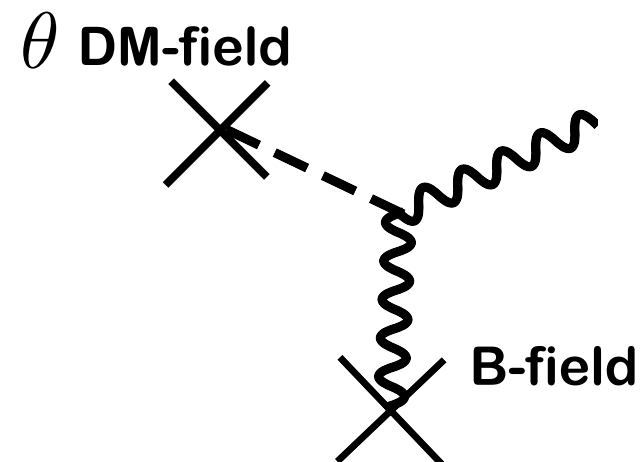
Axion DM in a B-field : two photon coupling

$$\mathcal{L}_I = -C_{a\gamma} \frac{\alpha}{2\pi} \frac{a}{f_a} \mathbf{B} \cdot \mathbf{E}$$

- In a static magnetic field, the oscillating axion field generates EM-fields

$$\mathcal{L}_I = -C_{a\gamma} \frac{\alpha}{2\pi} \theta(t) \mathbf{B}_{\text{ext}} \cdot \mathbf{E}$$

source



Detecting axion DM

- **Axion DM**, $\theta = \theta_0 \cos(m_a t)$, in a B-field is a source in Maxwell's eq.

$$\begin{aligned} \nabla \cdot \epsilon \mathbf{E} &= \rho_f \\ \nabla \times \mathbf{H} - \frac{\partial \epsilon \mathbf{E}}{\partial t} &= \mathbf{J}_f - C_{a\gamma} \frac{\alpha}{2\pi} \mathbf{B} \frac{\partial \theta}{\partial t} \\ \nabla \cdot \mathbf{B} &= 0 \\ \frac{\partial \mathbf{B}}{\partial t} + \nabla \times \mathbf{E} &= 0 \end{aligned} \quad \longrightarrow \quad \begin{array}{l} \text{In a magnetised medium} \\ \mathbf{E}(t) = \frac{c_\gamma \alpha \theta_0 \mathbf{B}}{2\pi \epsilon} \cos(m_a t) \end{array}$$

- **Electric fields** $E = 1.3 \times 10^{-12} \text{ V/m} \frac{B_e}{10 \text{ T}} \frac{C_{a\gamma}}{\epsilon}$. (amp independent of mass!)

- **Oscillating at a frequency** $\omega \simeq m_a$

Radiation from a dielectric interface ...

$$\mathbf{E}(t) = \frac{c_\gamma \alpha \theta_0 \mathbf{B}}{2\pi\epsilon} \cos(m_a t)$$

$$\mathbf{E}(t) = \frac{c_\gamma \alpha \theta_0 \mathbf{B}}{2\pi} \cos(m_a t)$$

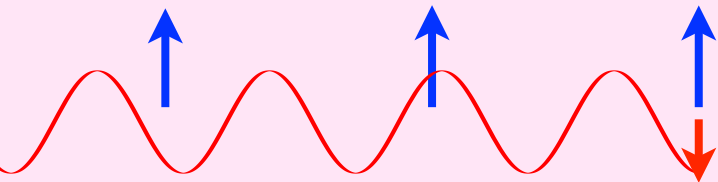


← **Boundary conditions!**

$$\mathbf{E}_{||1} = \mathbf{E}_{||2}$$

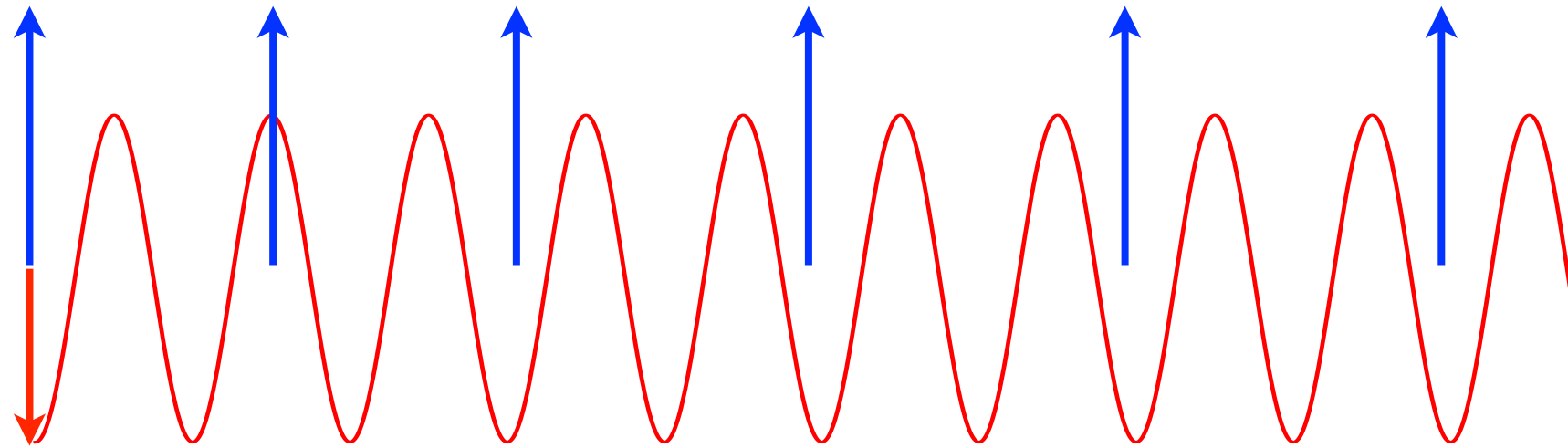
Radiation from a dielectric interface ...

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Emitted EM-wave

$$\mathbf{E}(t) = \frac{c_\gamma \alpha \theta_0 \mathbf{B}}{2\pi} \cos(m_a t)$$



← **Boundary conditions!**

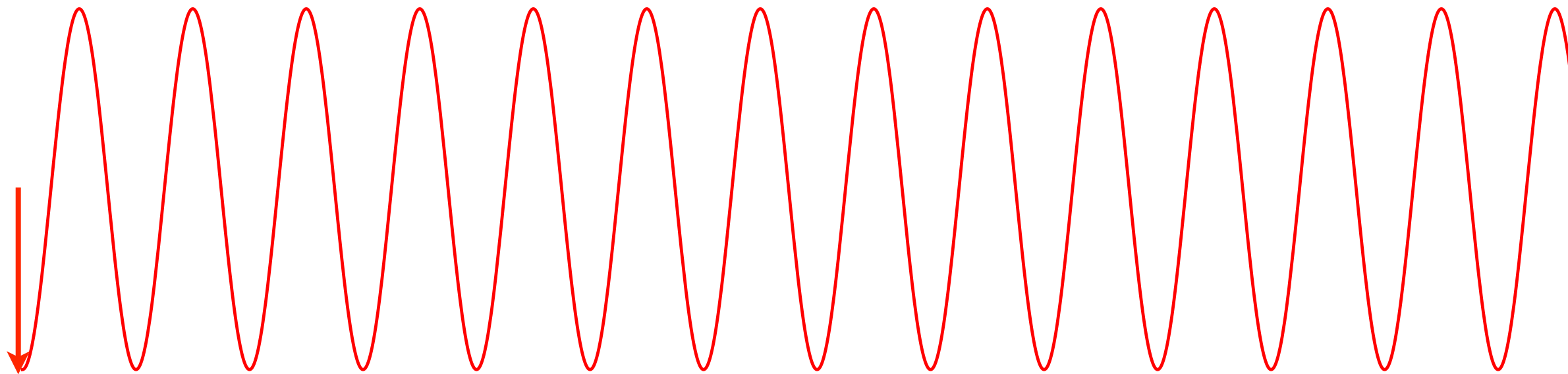
$$\mathbf{E}_{||1} = \mathbf{E}_{||2}$$



Emitted EM-wave

Radiation from a magnetised mirror : Power

MIRROR



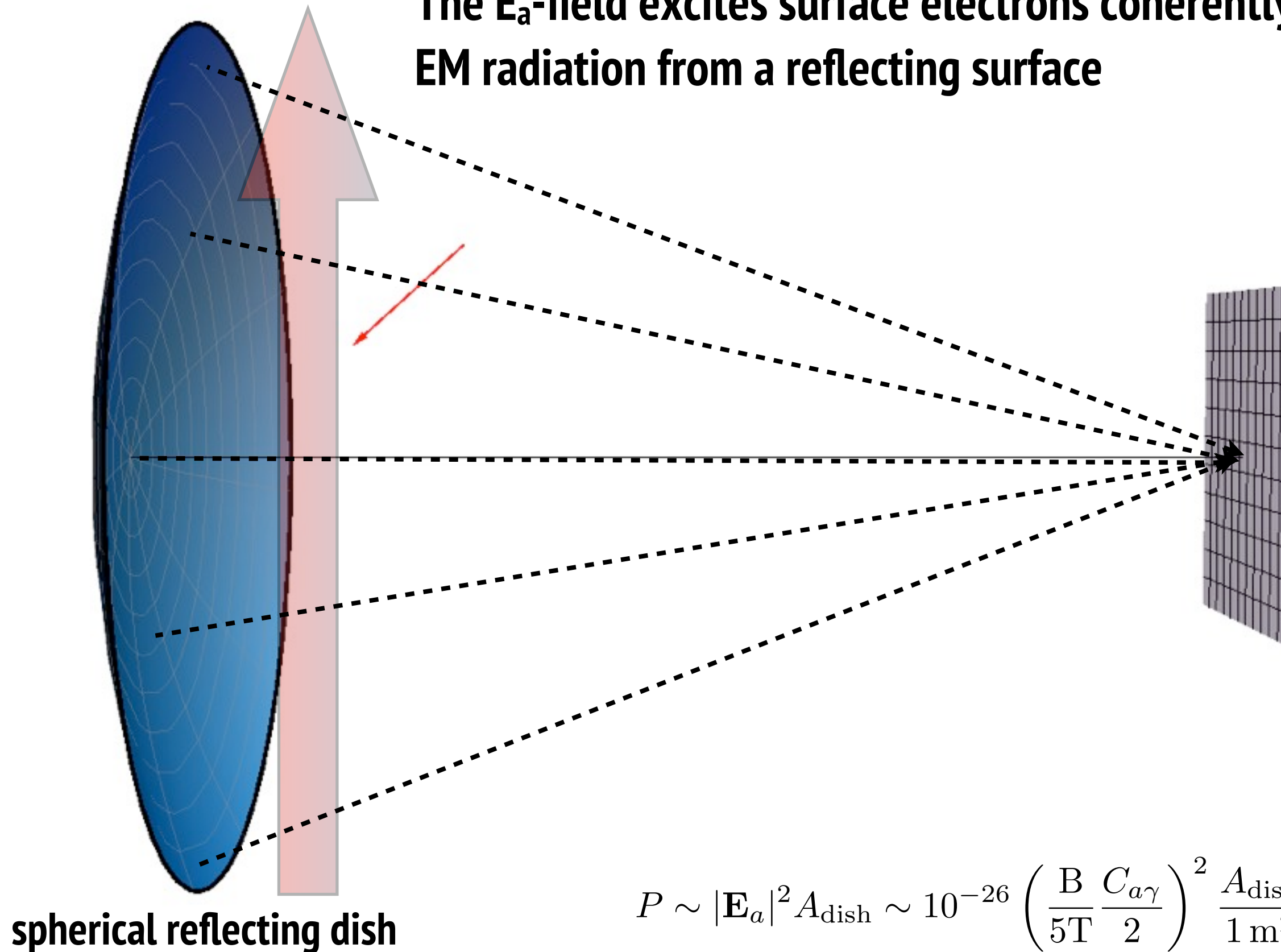
Emitted EM-wave

$$\frac{\text{Power}}{\text{Area}} \sim 2.2 \times 10^{-27} \frac{\text{Watt}}{\text{m}^2} \left(\frac{C_{a\gamma}}{2} \frac{B_{||}}{5\text{T}} \right)^2$$

Dish antenna experiment?

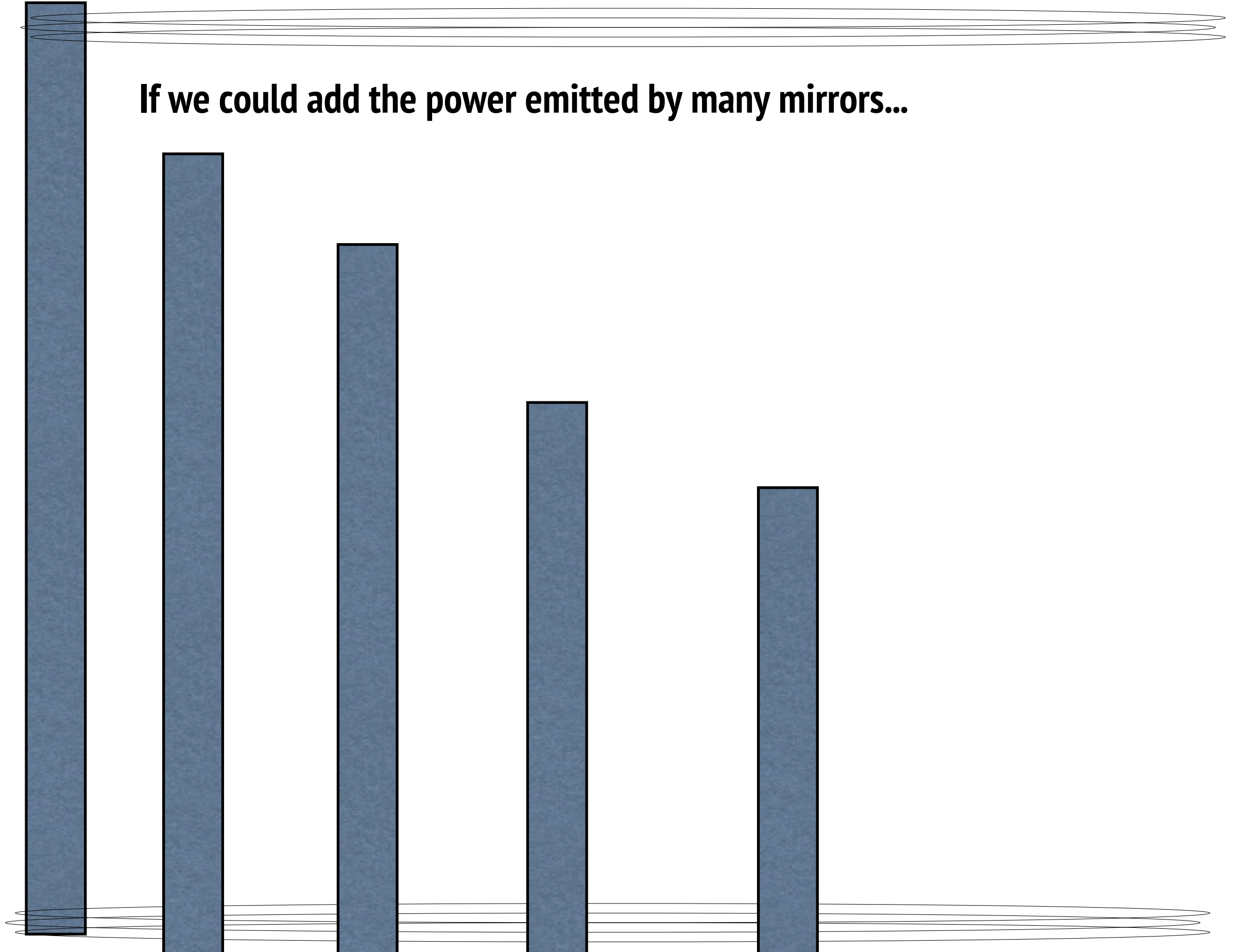
Horns 2012

The E_a -field excites surface electrons coherently
EM radiation from a reflecting surface

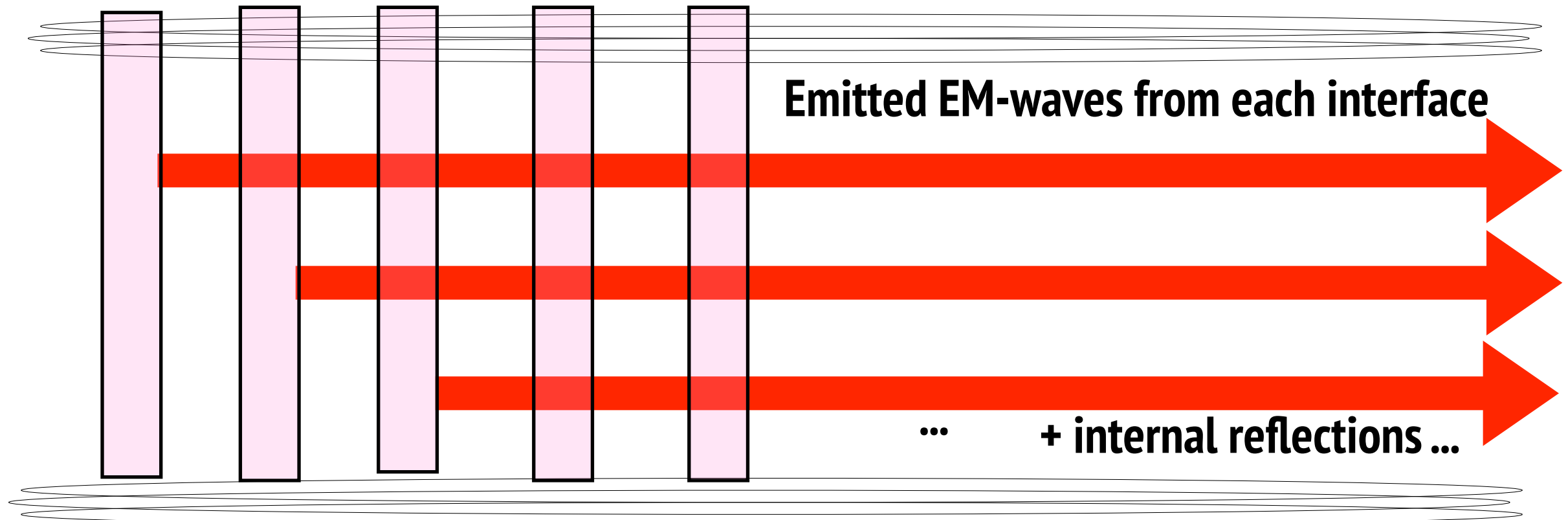


Mixed scheme?

If we could add the power emitted by many mirrors...



Many dielectrics : MADMAX at MPP Munich

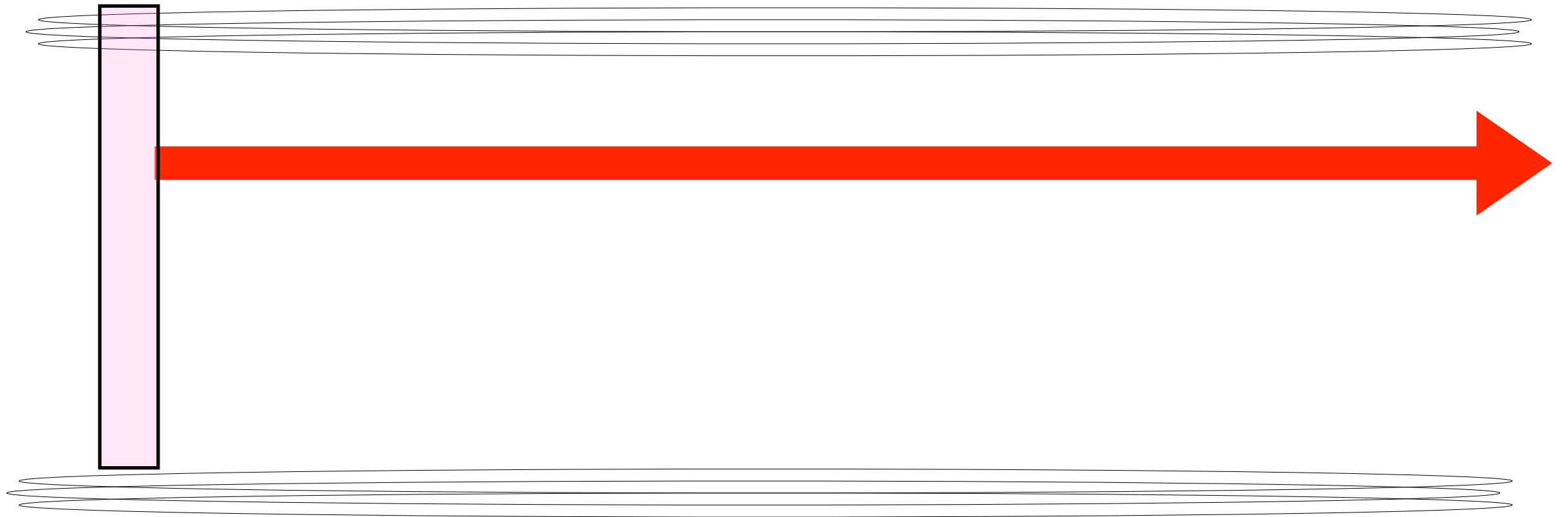


- Emission has large spatial coherence; adjusting plate separation -> coherence

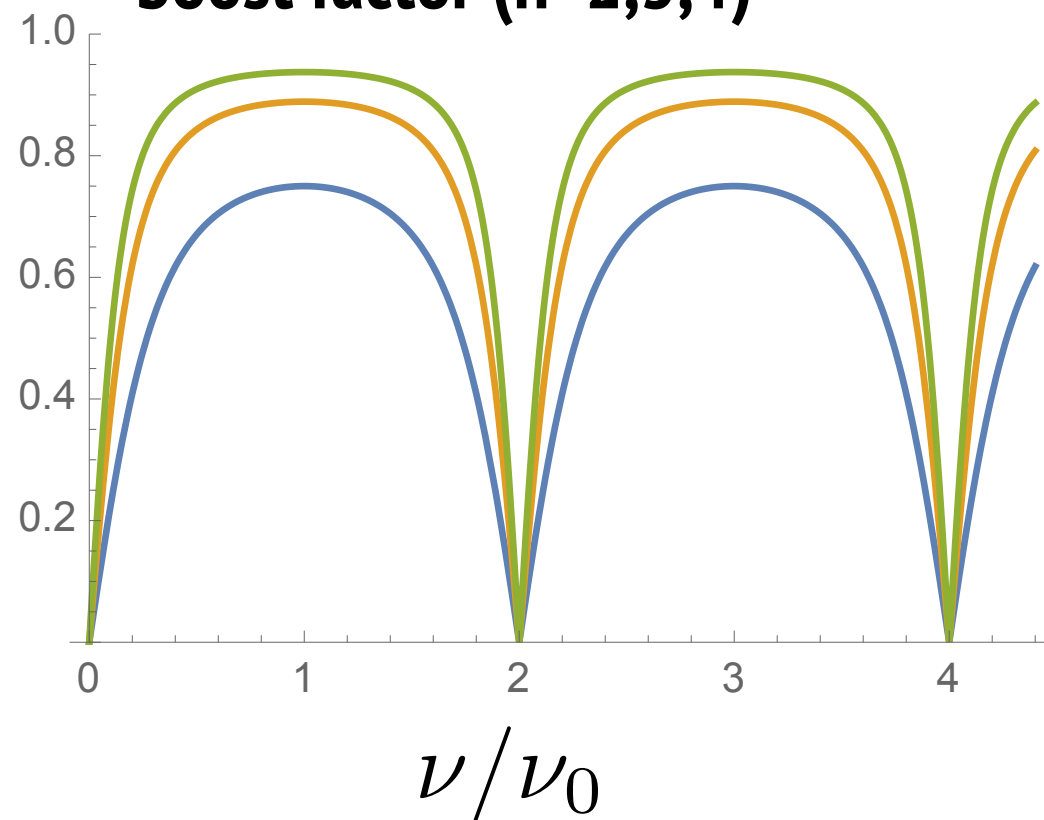
$$\frac{P}{Area} \sim 2 \times 10^{-27} \frac{W}{m^2} \left(c_\gamma \frac{B_{||}}{10T} \right)^2 \times \beta^2(\omega) \quad \text{boost factor}$$

- Work in progress at Max Planck Institute fur Physik (Conceptual design)

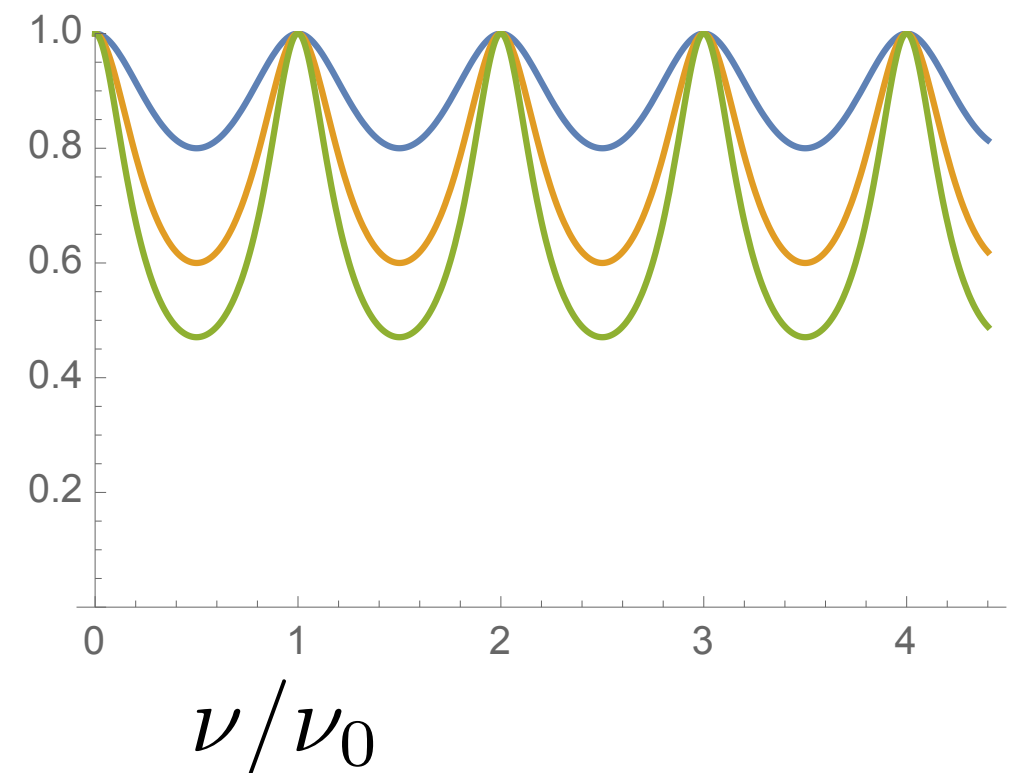
One dielectric



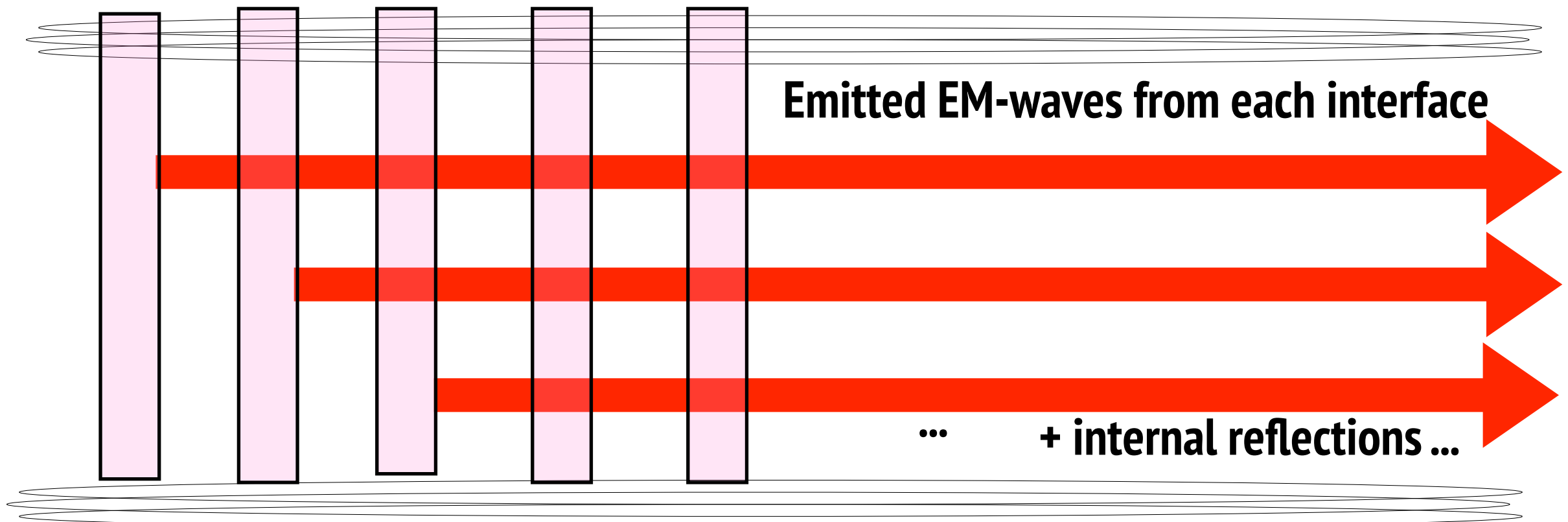
boost factor ($n=2,3,4$)



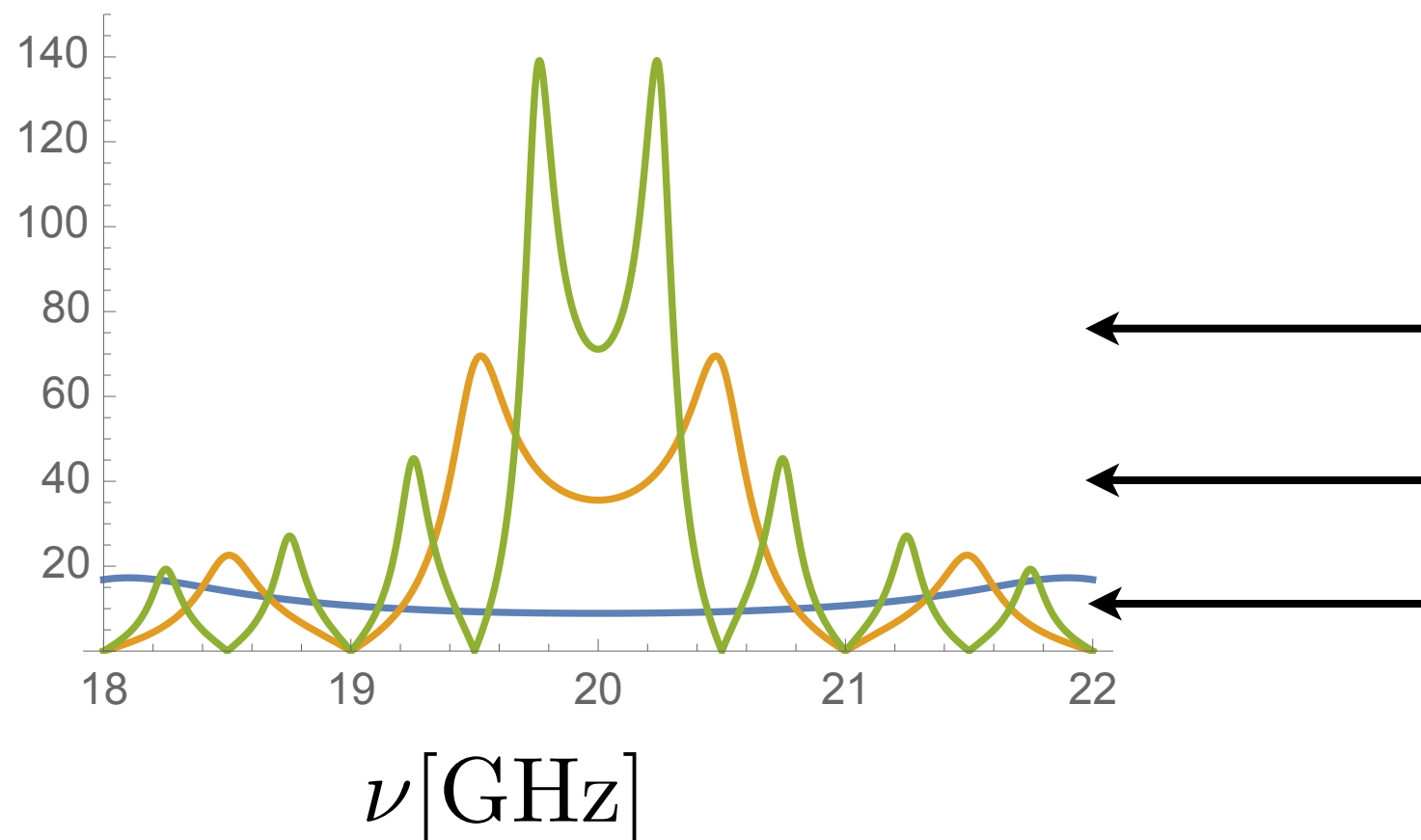
transmission coefficient



Close to ν_0 , many layers



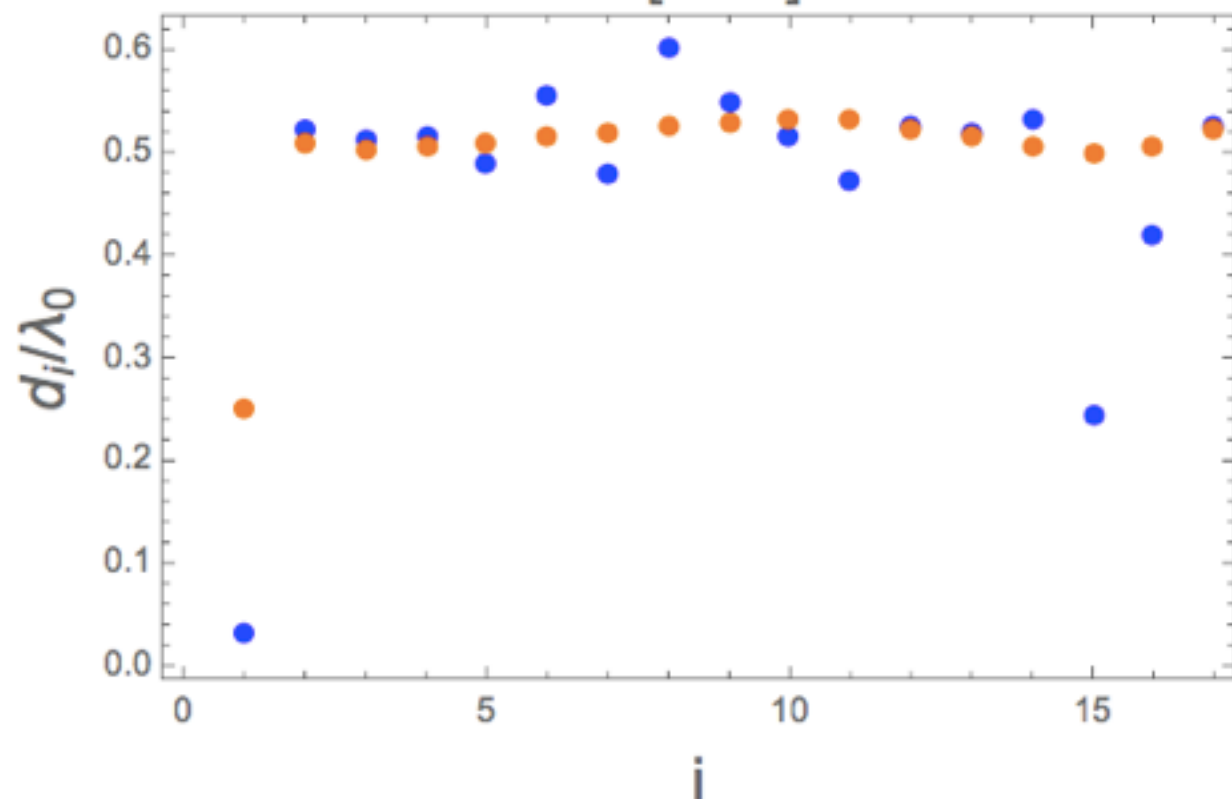
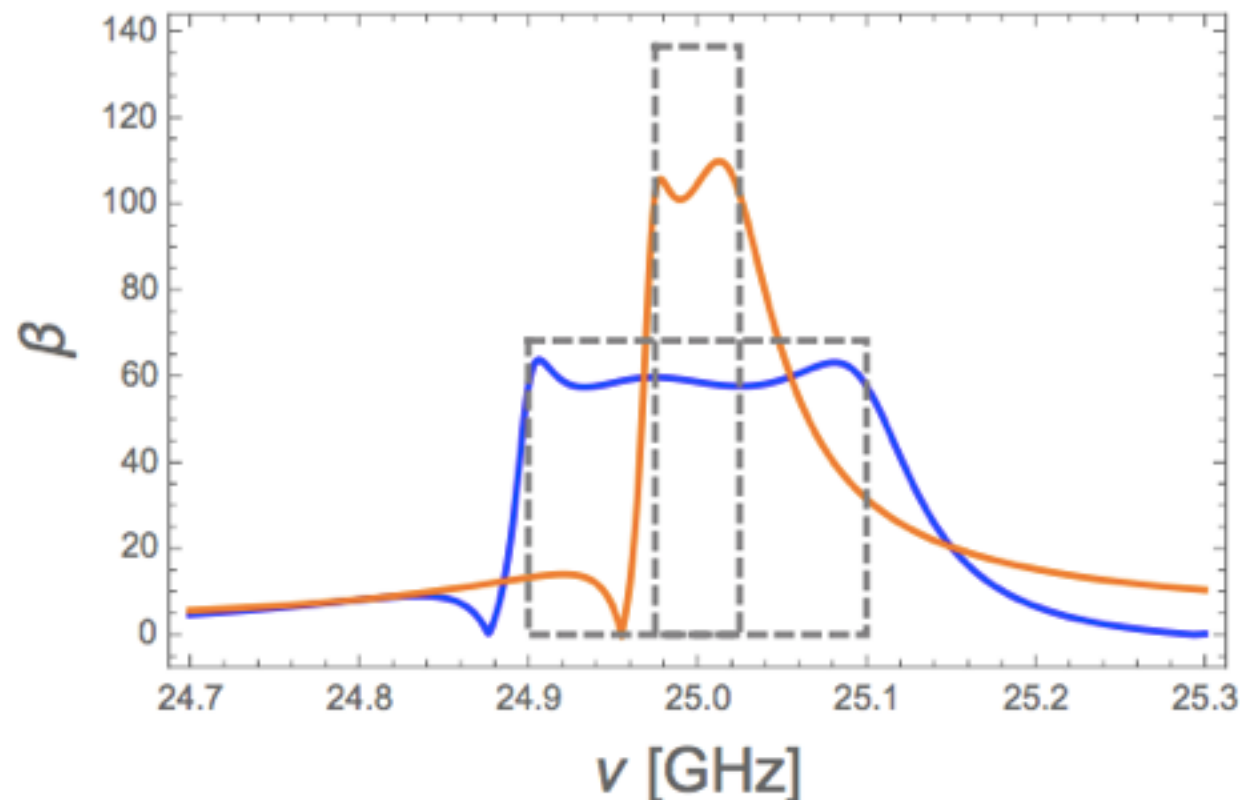
boost factor ($N=10,40,80$; $n=3, \nu_0=20$ GHz)



$$\beta_N \sim N \times \beta_1$$

Even larger boosts are possible (small resonant enhancement)

Numerical optimisation of distance between 17 layers $n=5$ (flat response)



Conceptual paper in preparation:

PREPARED FOR SUBMISSION TO JCAP (ALMOST)

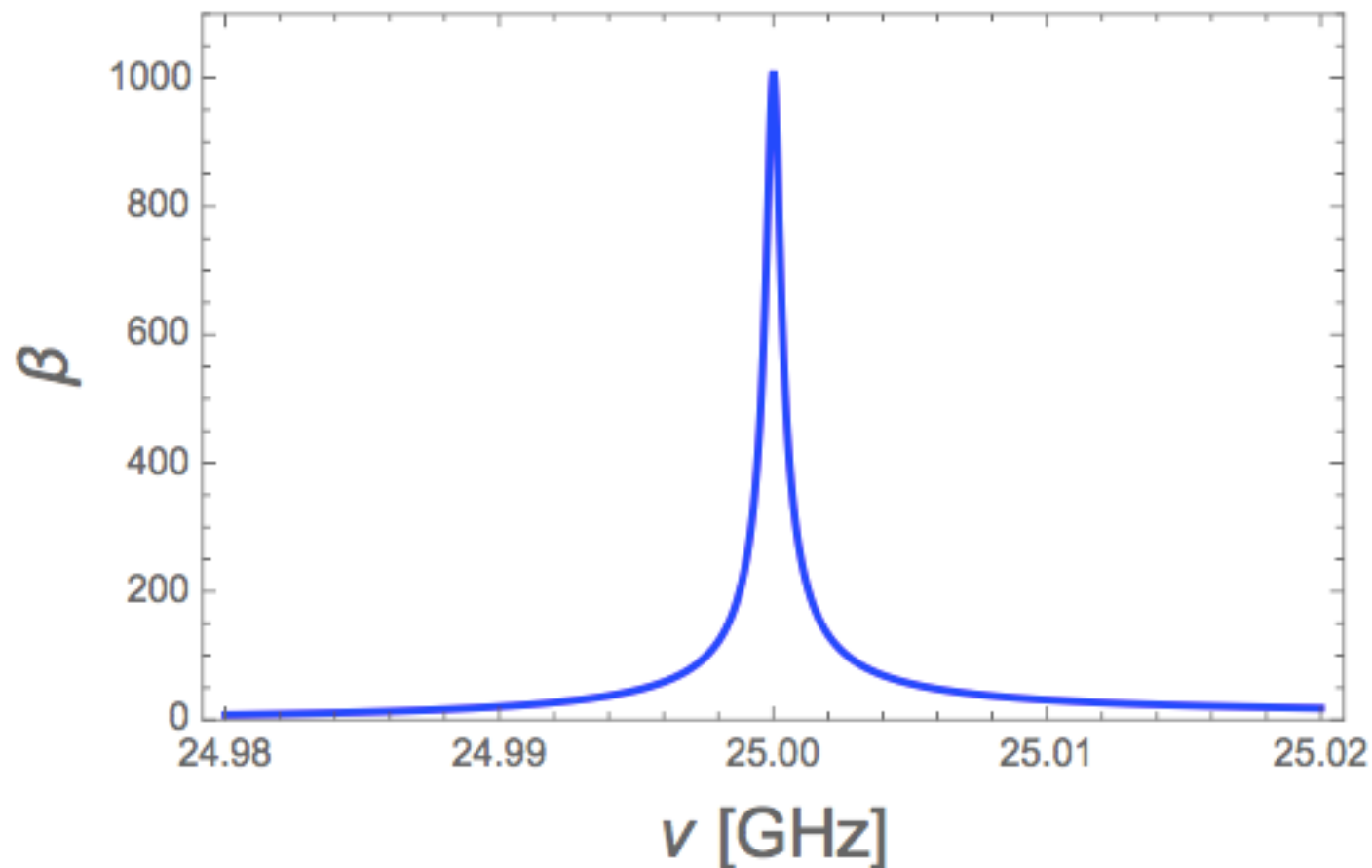
MPP-2016-XXX

Layered dielectric haloscopes: a new way to detect axion dark matter

Alexander J. Millar,^a Georg G. Raffelt,^a Javier Redondo,^{a,b}
Frank D. Steffen^a

and if a candidate is found ...

Numerical optimisation of distance between 17 layers $n=5$ (max response)



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Experimental idea

~80 high dielectric plates spacing ~mm to cm range for boost in the frequency band 10 to 100 GHz

< 200cm

Metallic disc
($\epsilon=\infty$)

Disc
positioning
motors

Disc suspension

10 Tesla dipole magnet

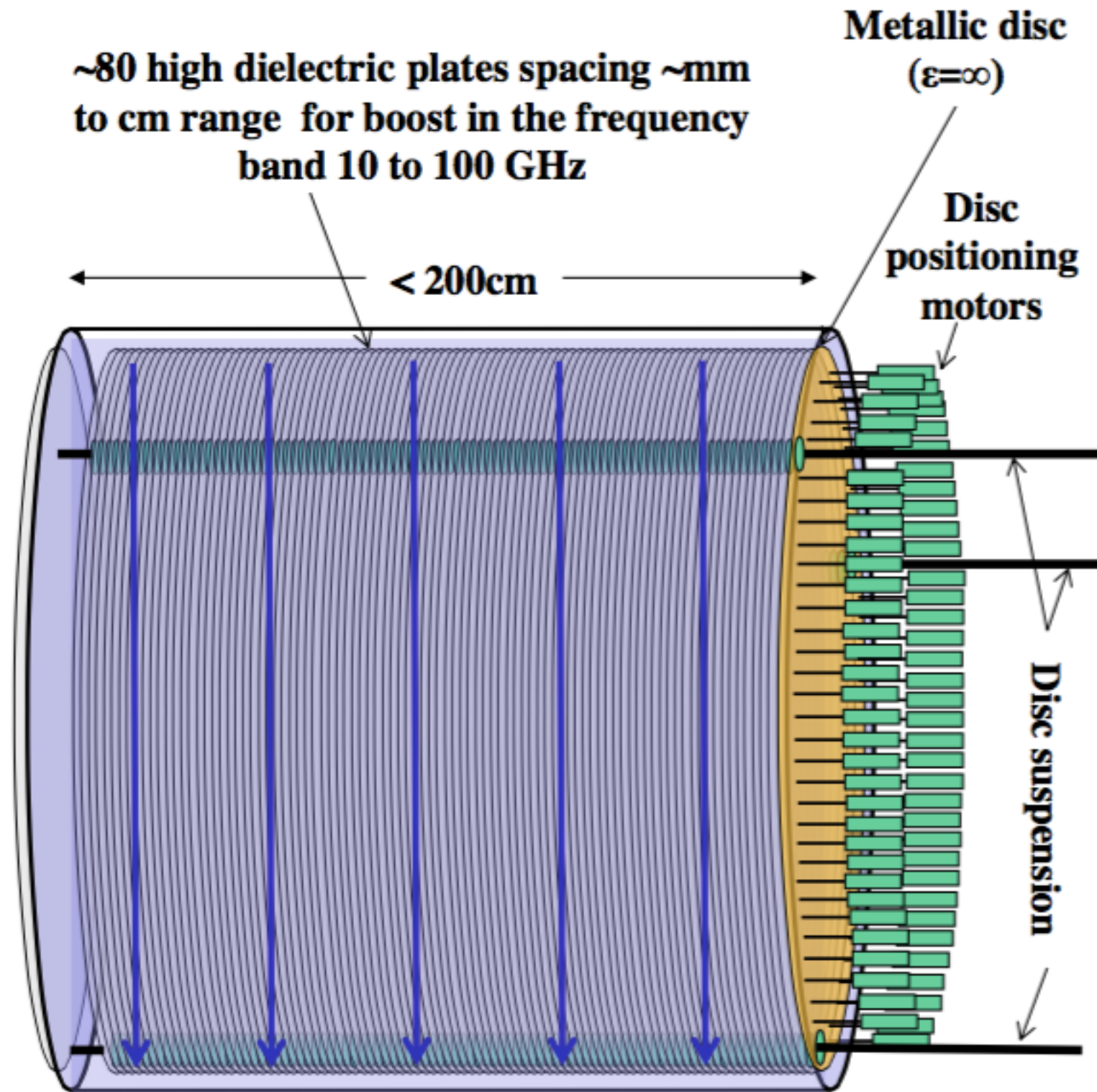
4 K cryostat

Cold
preamp

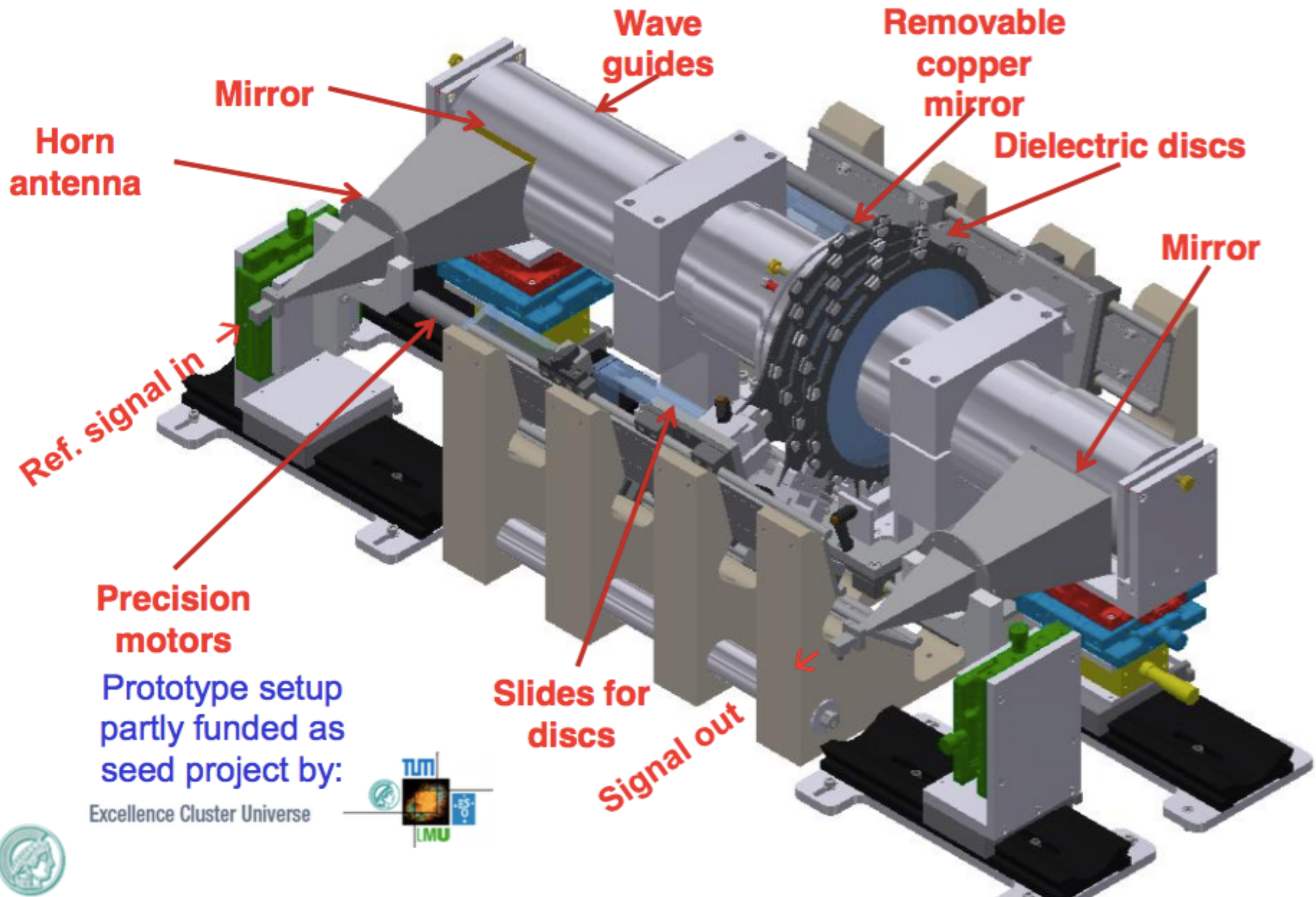
Feedthrough
to 4K

Horn antenna

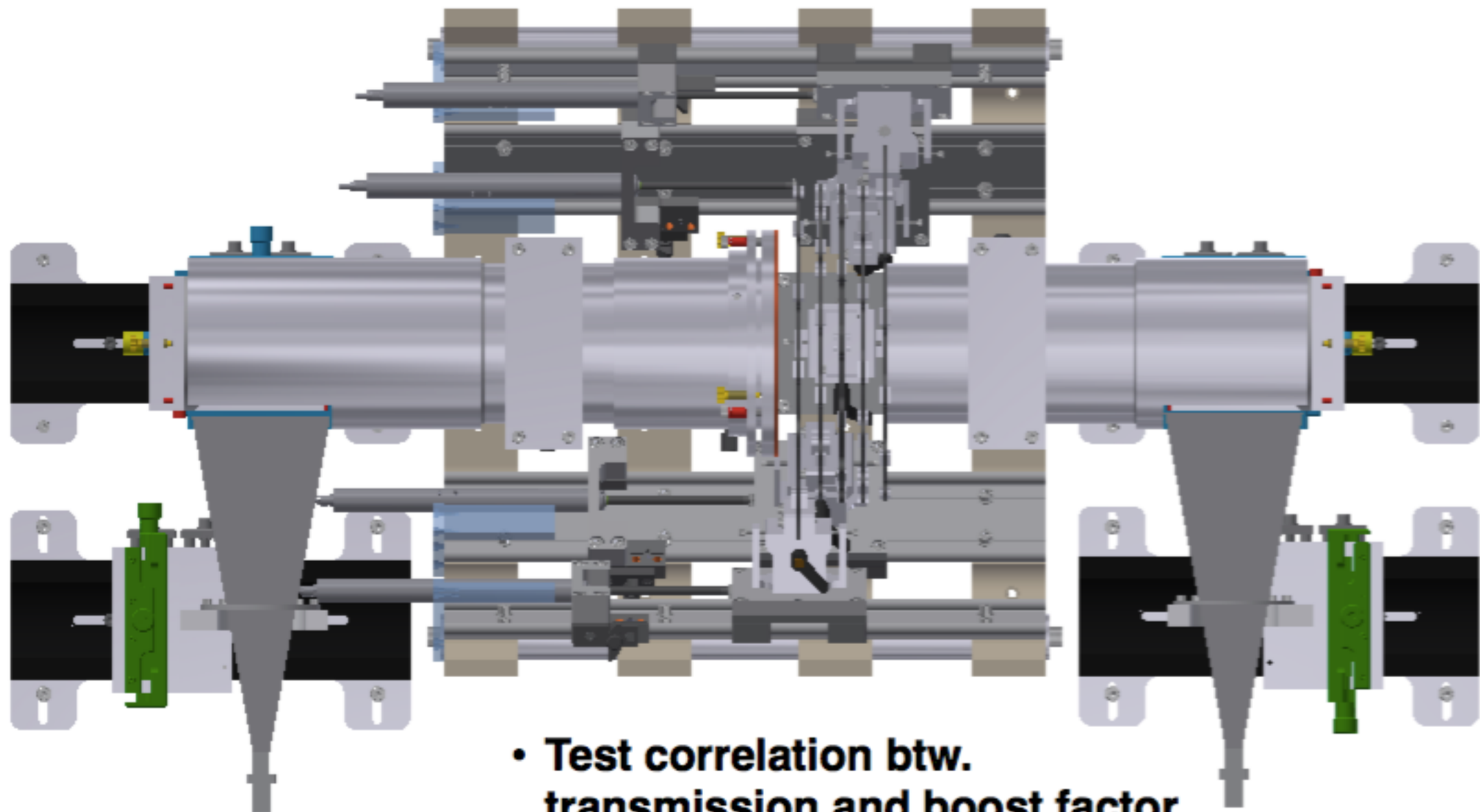
Parabolic mirror



First prototype setup at MPI

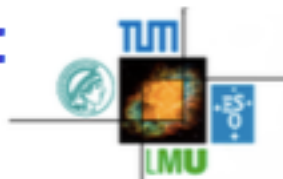


First prototype setup at MPI



Prototype setup
partly funded as
seed project by:

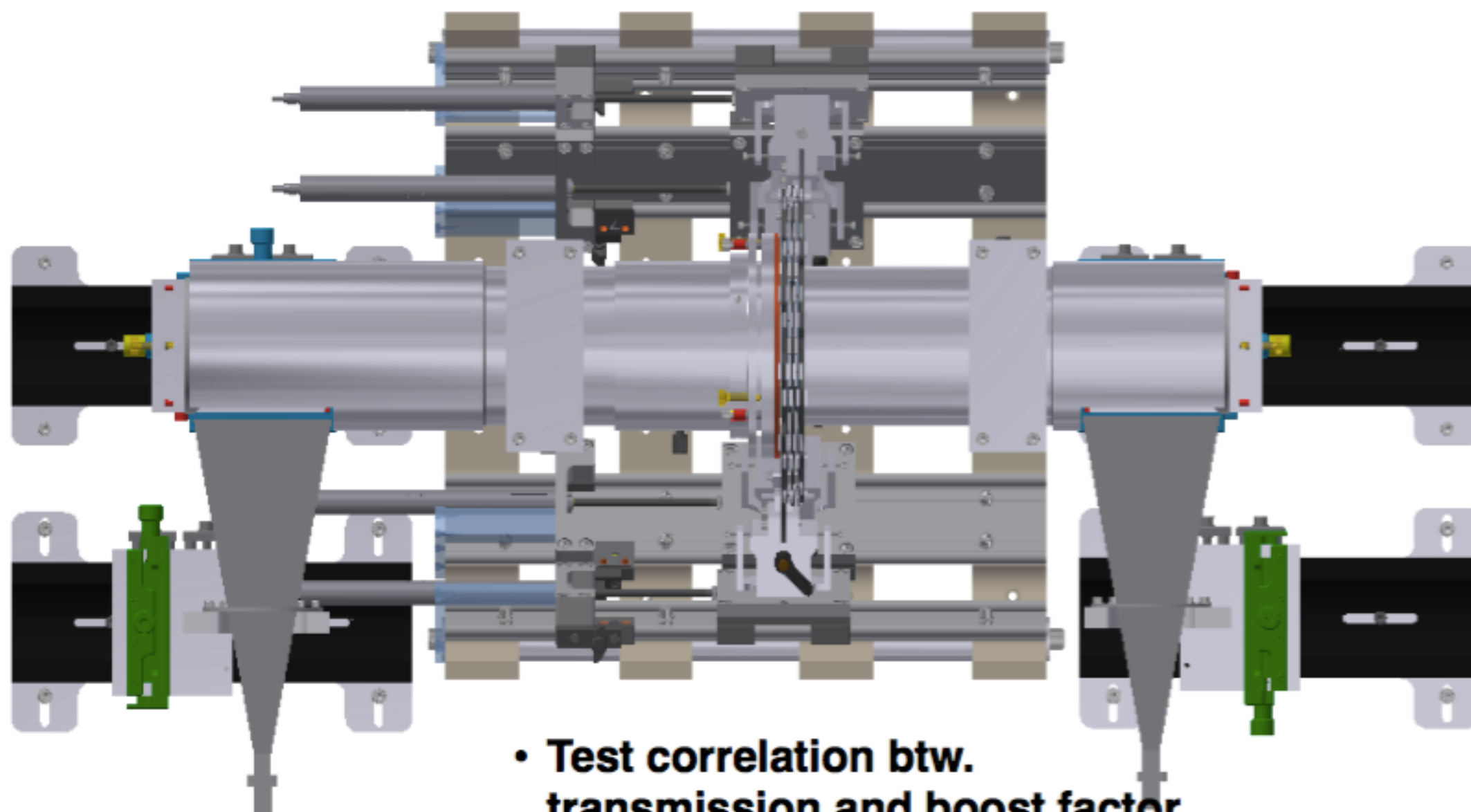
Excellence Cluster Universe



- Test correlation btw. transmission and boost factor
- Test needed disc precision
- Evaluate uncertainties
- R&D on tiling

Phone Conference with Saclay Magnet Group, Feb. 23 2016

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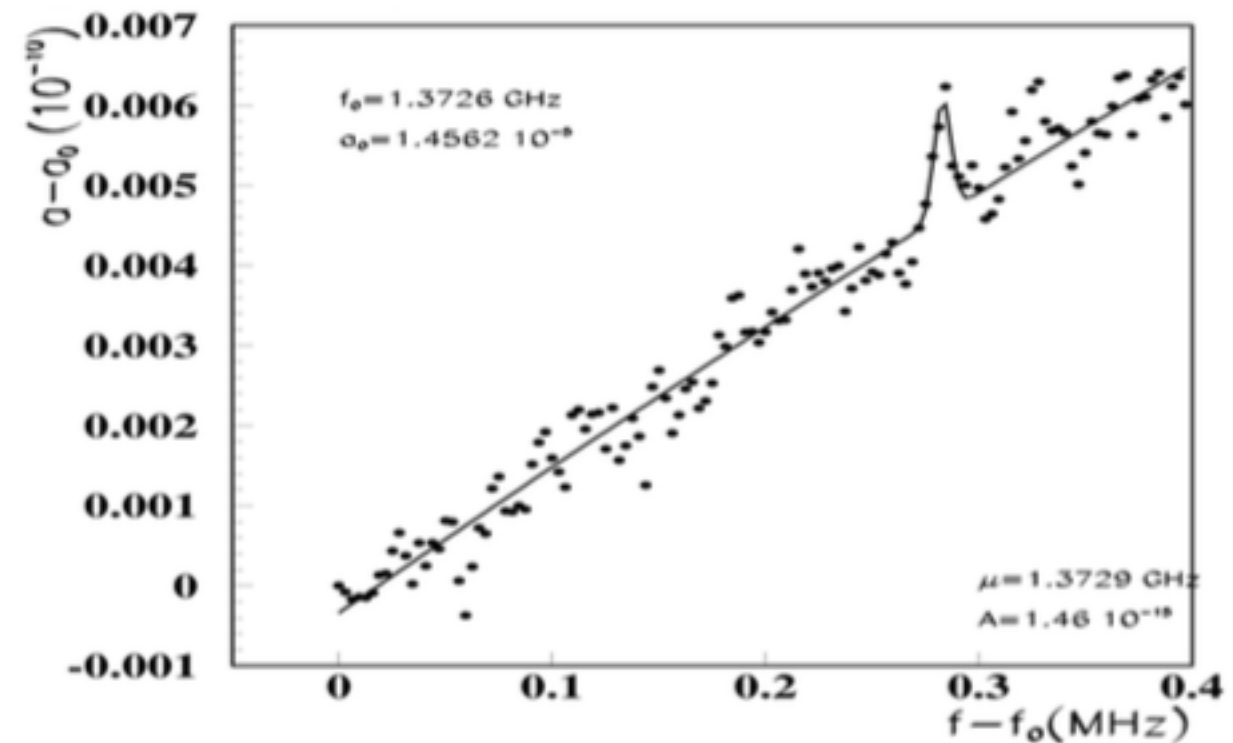
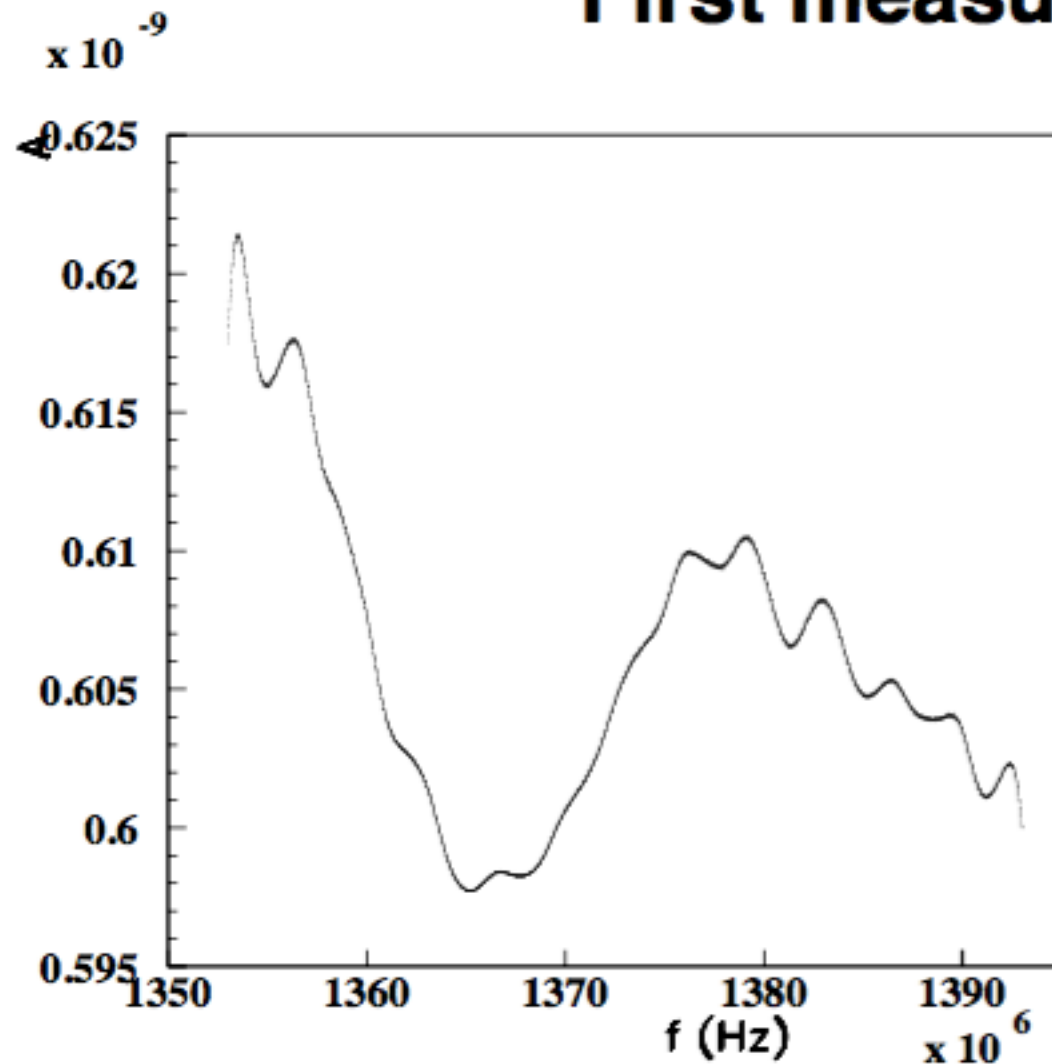
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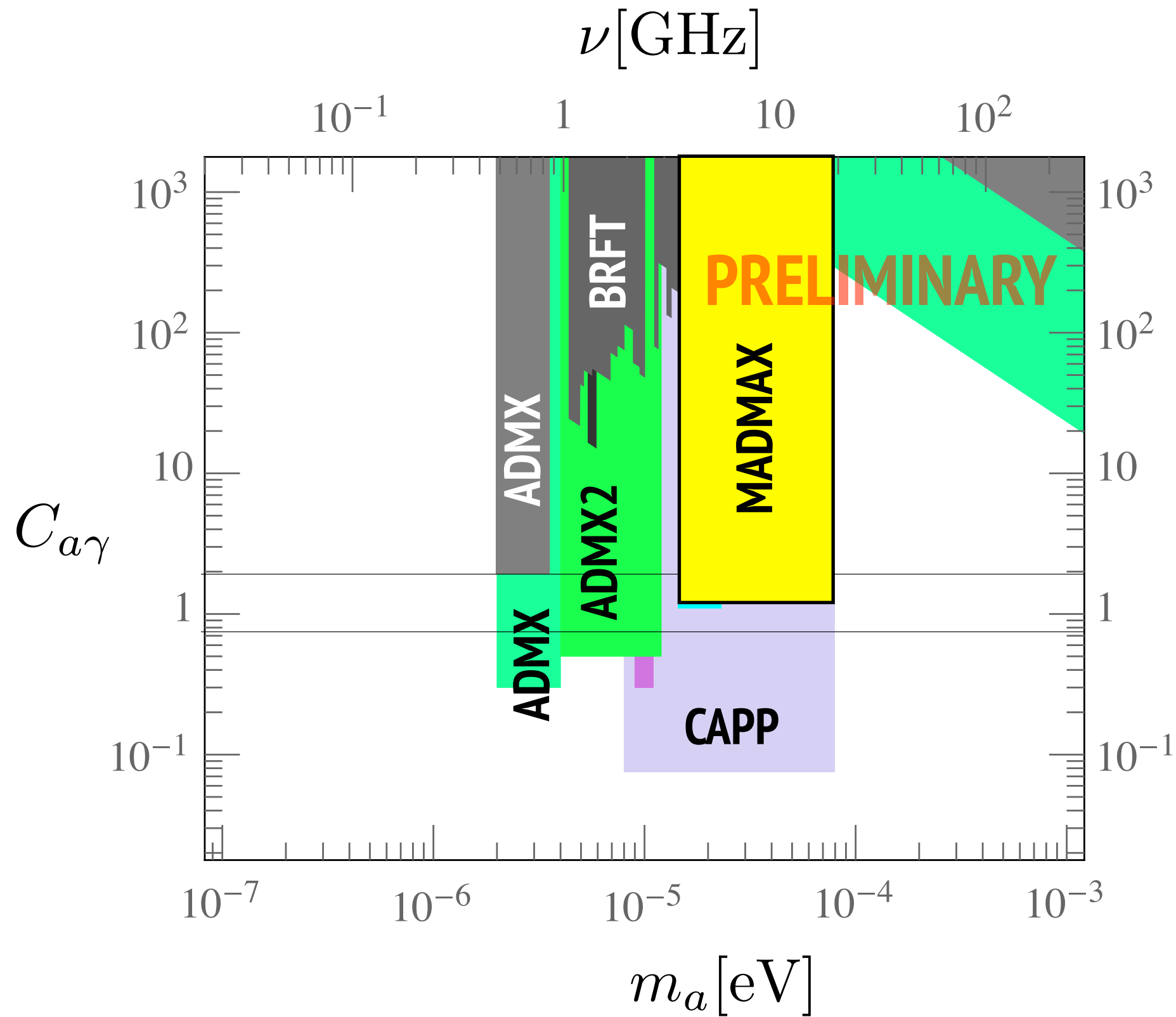
Phone Conference with Saclay Magnet Group, Feb. 23 2016

First measurements: sensitivity



- Inject fake axion signal with $3 \cdot 10^{-21} \text{ W}$ power
- Measurement for one week (integrate signal): Receiver at Room Temp.
 - Independent „blind“ analysis
 - found $> 6\sigma$ signal successfully
 - **At LHe: noise level factor 100 better**
 - **Sensitivity at the level of 10^{-23} W expected**

Sensitivity (10 T, 1 m², 5K, 5 years, boost=100)



Further plans

2016:

- Finish first test measurements at room temperature at MPI
- Test noise of preamplifier at LHe temperature
- Find additional collaborators for specific parts of project
- Start design of 10T magnet
- Develop technique to cover frequencies above 30 GHz
- R&D on production of large diameter high- ϵ discs

2017-2020:

- Demonstrate low noise performance, operation with many discs, scalability to 1m diameter, work in ~ 10 T environment
- Build prototype with preamp in LHe in cryostat and resonator in magnetic field

2020 :

- Start building full scale experiment

Conclusions

- Strong CP problem and dark matter motivate Axions
- Most predictive model (N=1) mass~ 0.1 meV ($f_a \sim 10^{11}$ GeV)
- Many experimental efforts, solid player missing in that range
- MW emission from interfaces is weak, make layered haloscope
- Munich Axion Dark MATter eXperiment

SMASH : Standard Model Axion See-saw Hidden scalar inflation