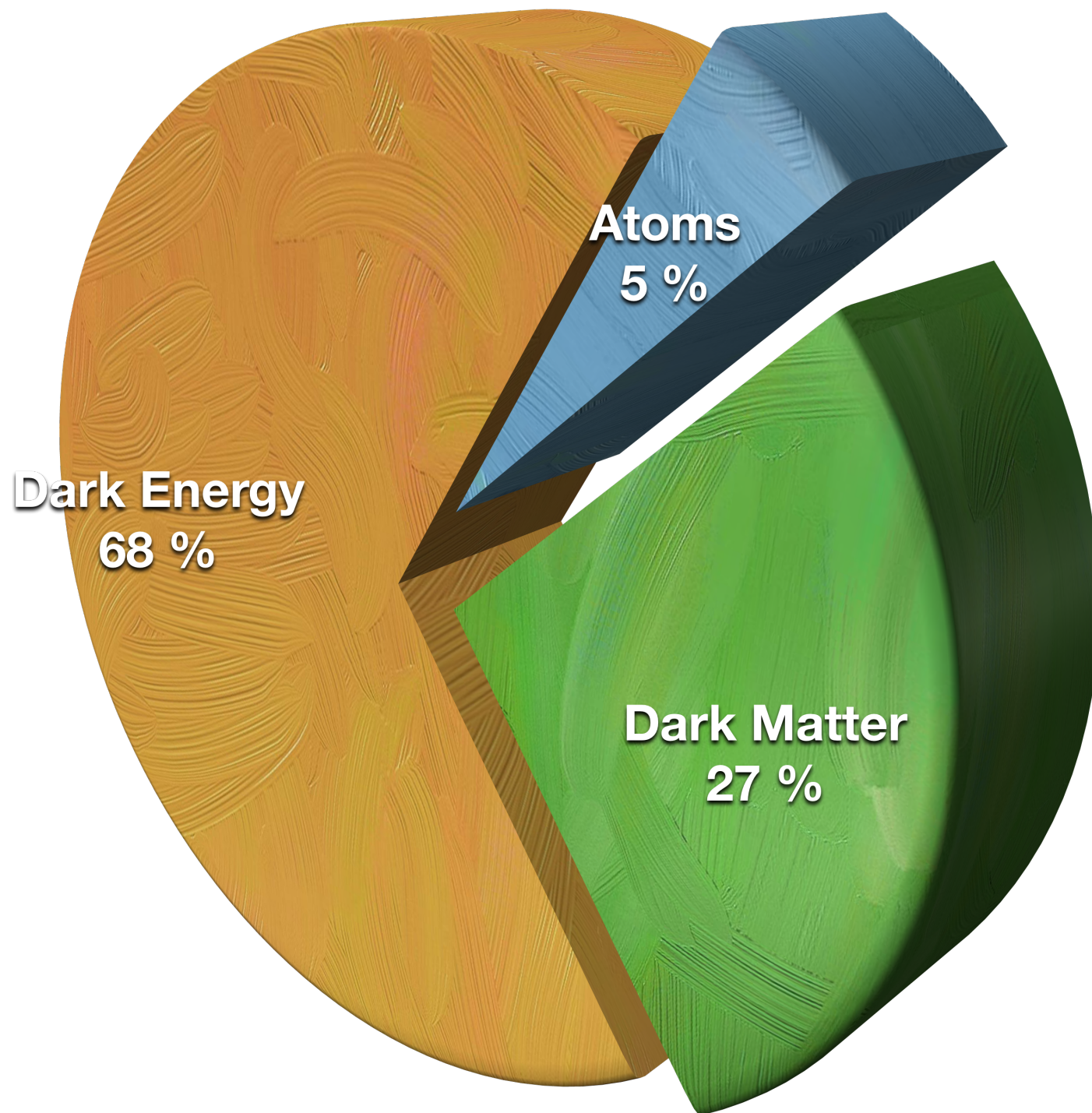


Fundamental Composite Dynamics

Francesco Sannino

Much ado for 5%



95% is unknown!

Richer than 5%? Likely

Minimal Composite Dynamics

Minimal Composite Dynamics

Minimal = 4D minimal matter and simplest gauge-groups

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- ◆ $SU(\mathbf{2})$ or $SU(\mathbf{3})$ New Gauge Group
- ◆ At most 2 New Dirac Flavours
- ◆ Either Fund., Symmetric or Adj matter rep.

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What is the dynamics and spectrum of these theories ?

Bright side

Composite Higgs dynamics

$$DH^\dagger DH - V(H) + \overline{\Psi}_L H \psi_R$$

Composite Higgs dynamics

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$$m_W^2 WW$$

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TC/Fund Comp Dyn

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TC/Fund Comp Dyn

Extended TC (ETC)

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Extended TC (ETC)

Minimal Technicolor

Higgs is the lightest scalar excitation of the condensate

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Inside the box

- ◆ Break EW
- ◆ Theories available/unexplored
- ◆ Vacuum stable
- ◆ Natural

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- ◆ Fermion masses vs FCNC
- ◆ Electroweak precision data
- ◆ Light Higgs

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TC can be conformal if ETC is strong

If ETC scales differ for each generation, walking is not needed..

Composite Goldstone Higgs

D.B. Kaplan & H. Georgi, 84

Higgs is a composite pseudo goldstone

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D.B. Kaplan & H. Georgi, 84

Higgs is a composite pseudo goldstone

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- ◆ Higgs is massless
- ◆ Gauge boson couplings
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Work in 4 dimensions

Fundamental Composite Dynamics

- ◆ Unified TC and CH framework
- ◆ Fund 4D underlying theory
- ◆ Spectrum via lattice

(Mostly) Effective Theories

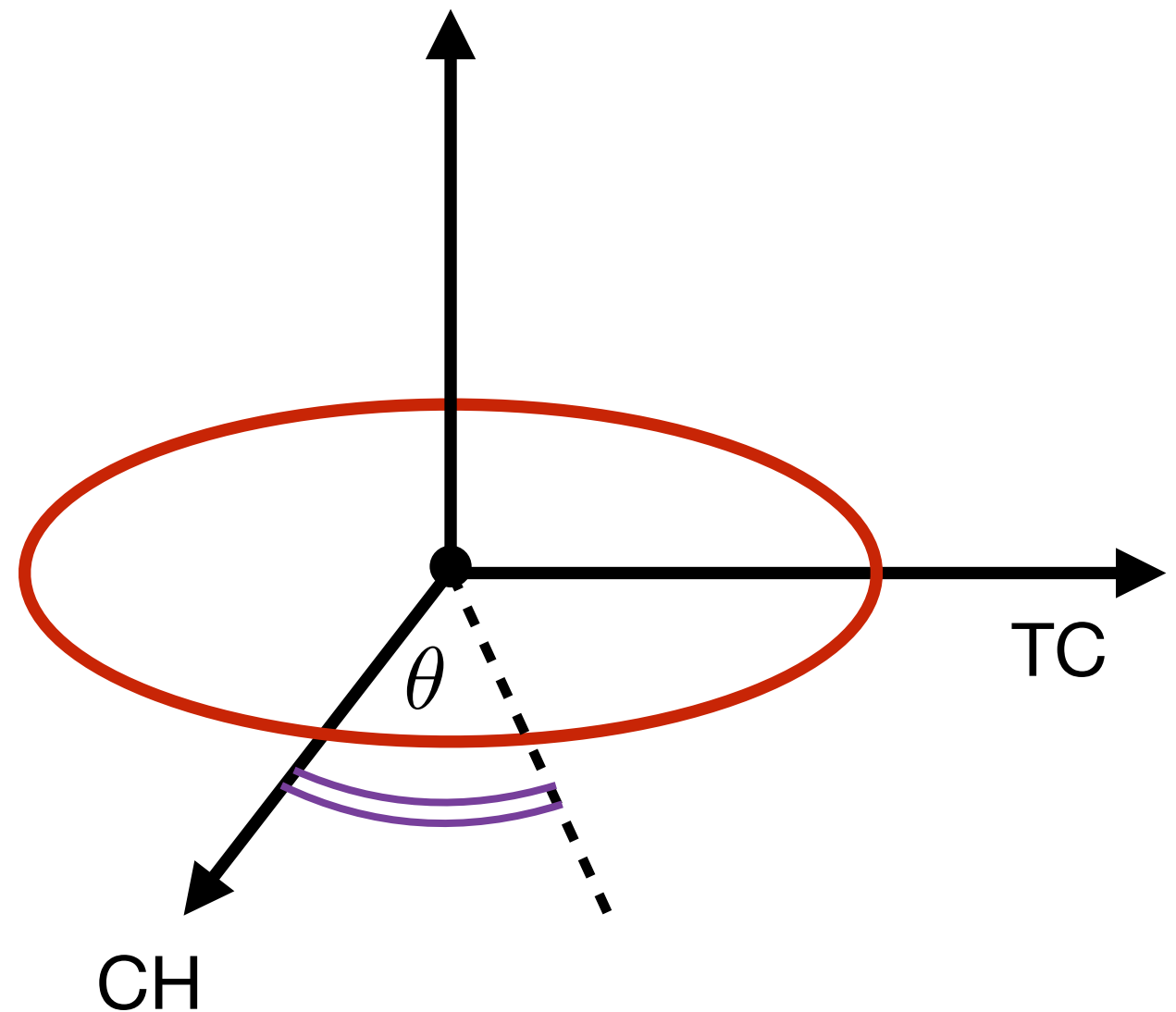
Appelquist, Sannino, 98, 99

Ryttov, Sannino, 2008

Katz, Nelson Walker, 2005

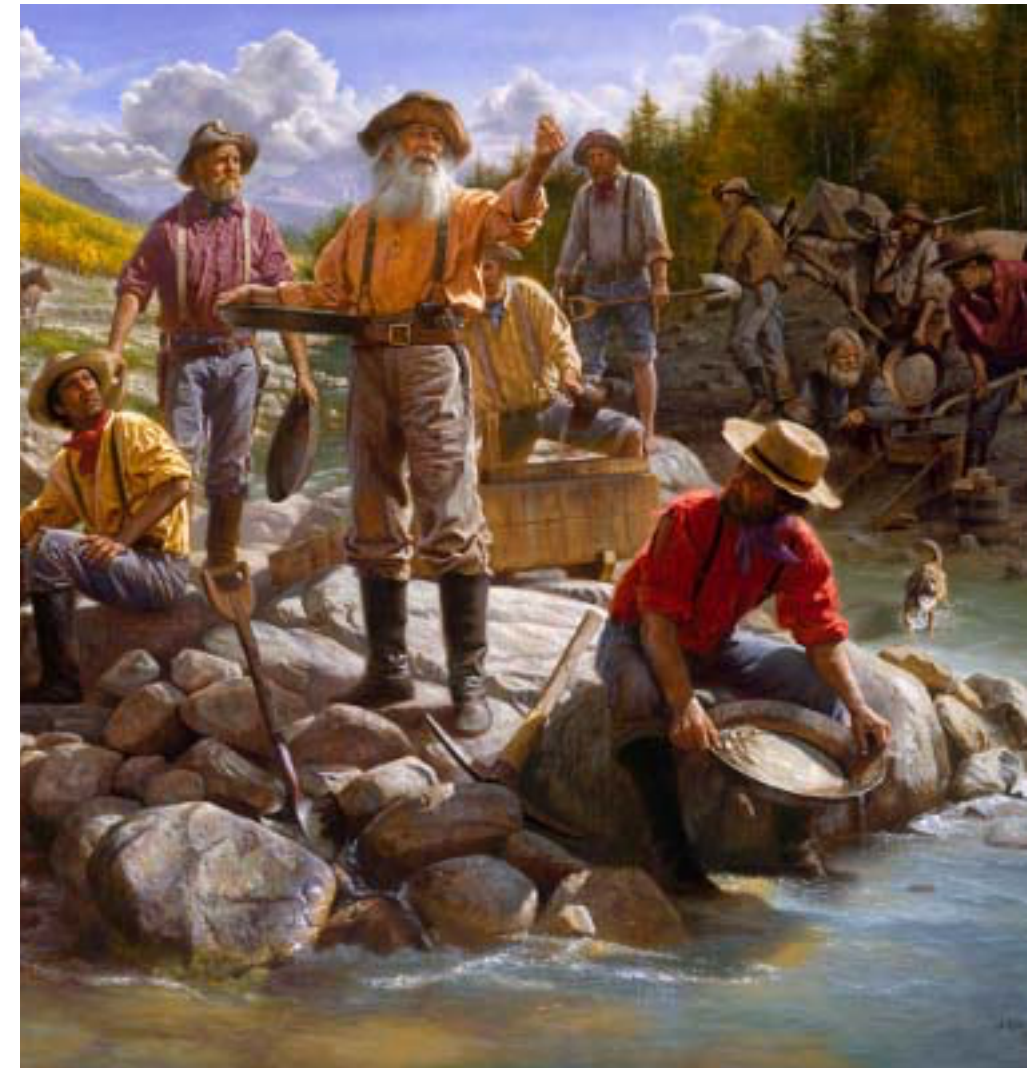
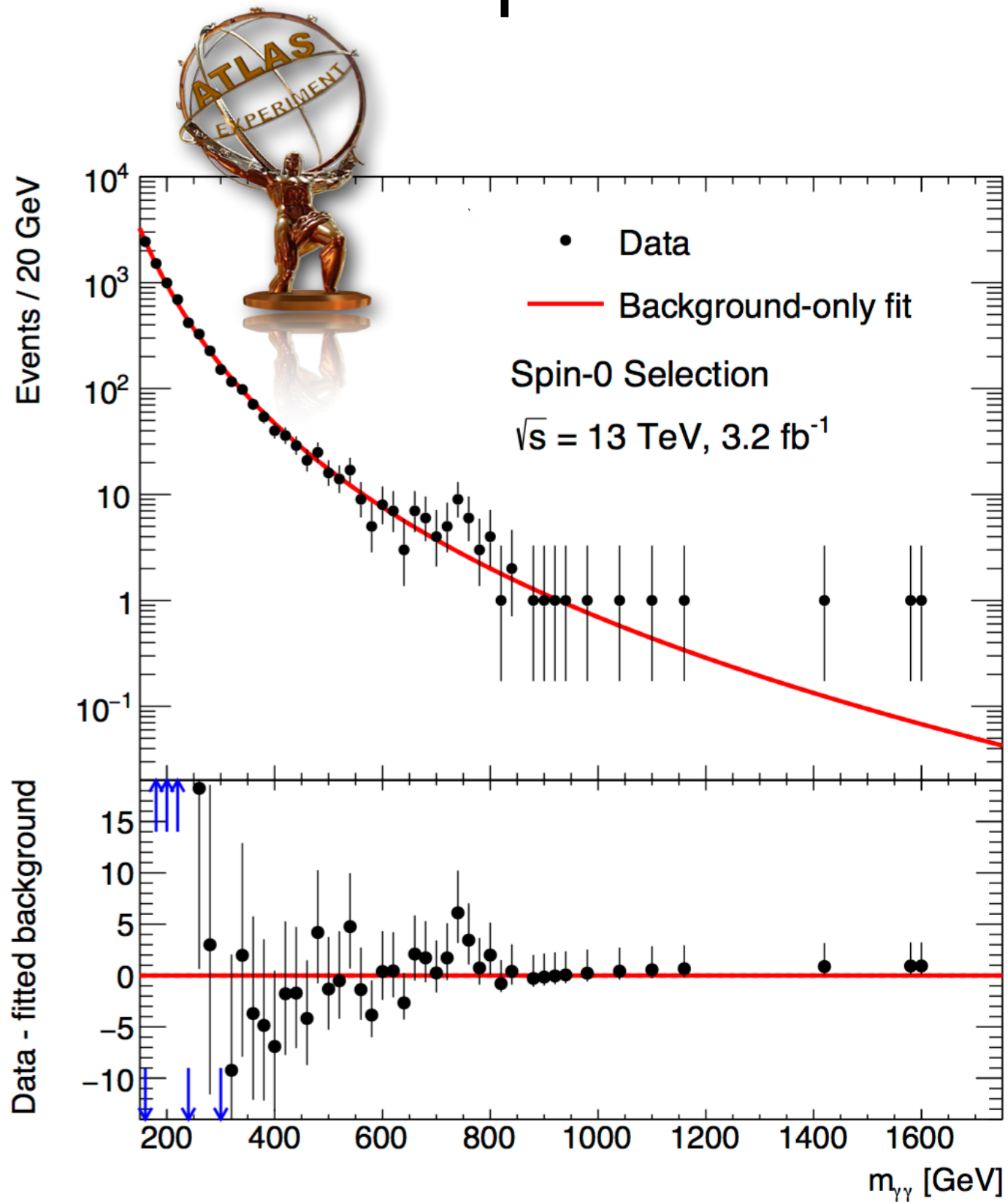
Gripaios, Pomarol, Riva, Serra, 2009

Galloway, Evans, Luty, Tacchi, 2010



Cacciapaglia and Sannino 1402.0233 JHEP

Diphoton Gold Rush



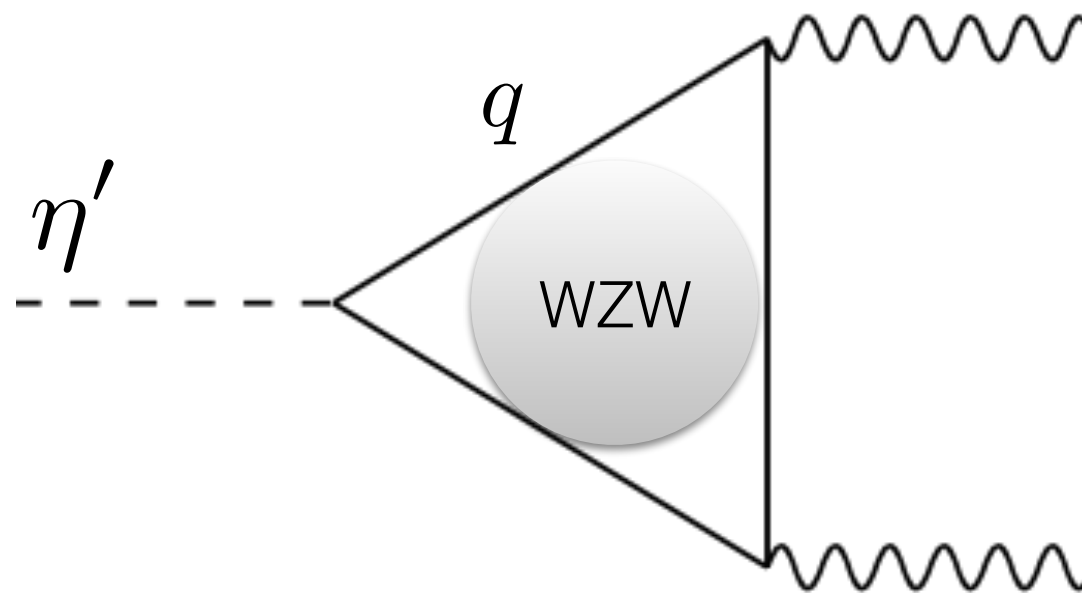
Diphoton explained minimally and naturally

Molinaro, Vignaroli, Sannino.1512.05334,1602.07574

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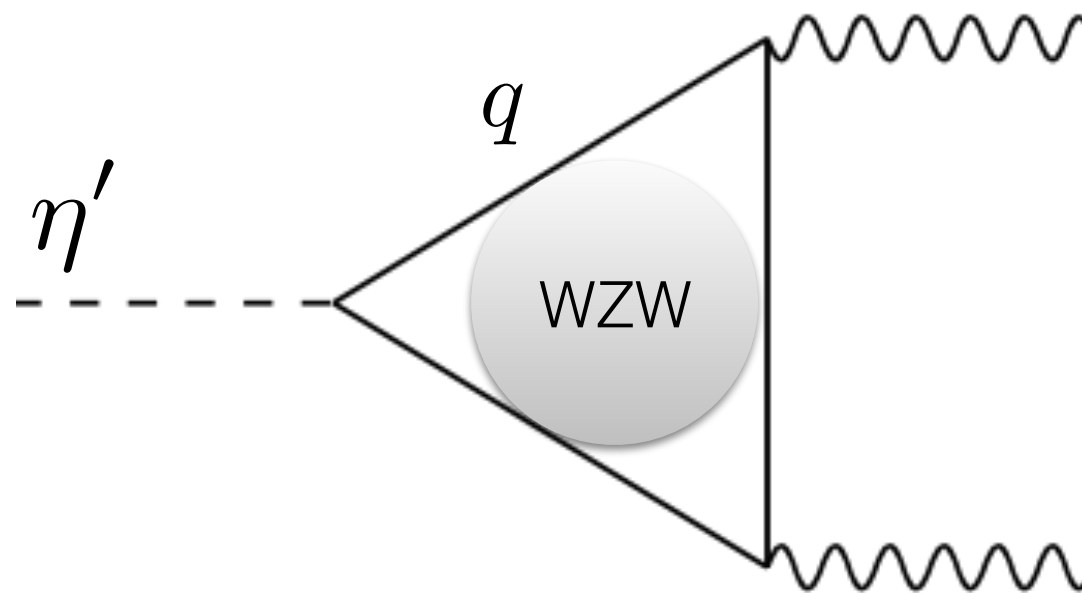
QCD axial anomaly template



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QCD axial anomaly template

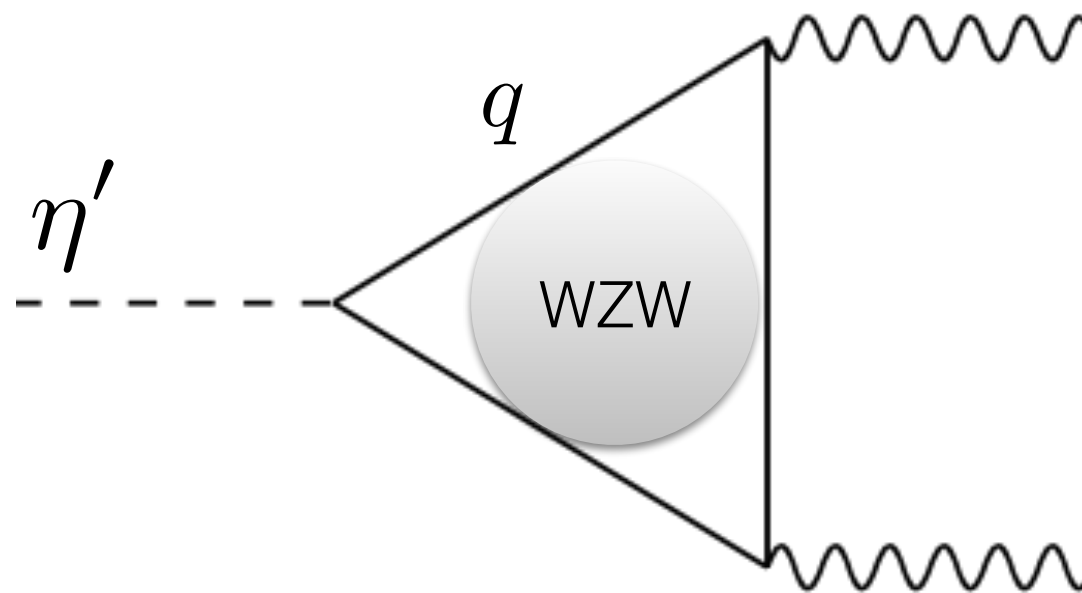


Related to the topological susceptibility

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Related to the topological susceptibility

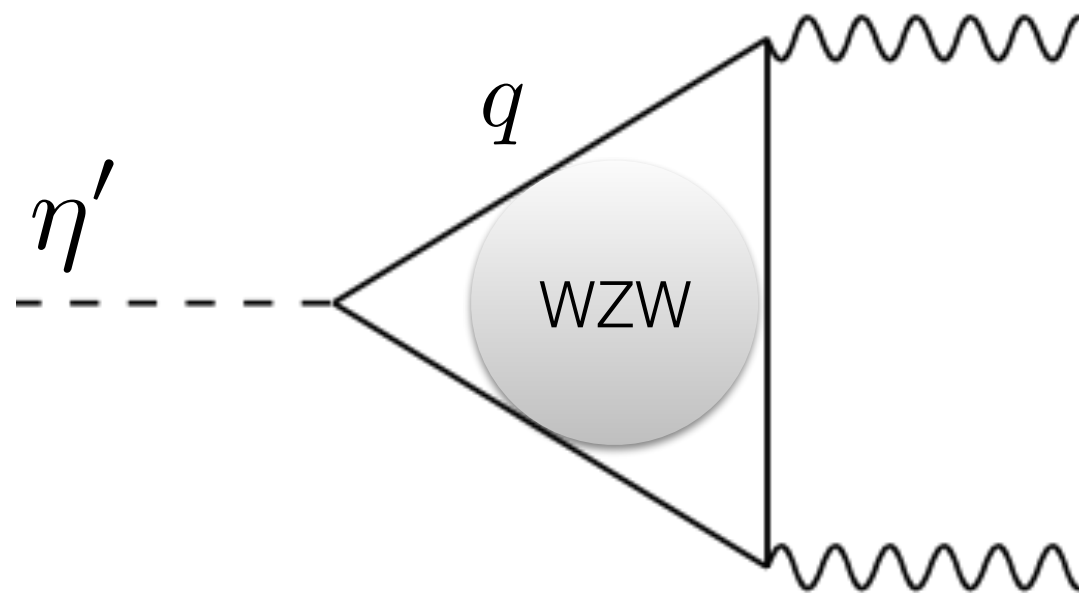
Generalization to non-fund. representations and multiple QCDs

Di Vecchia and Sannino, 1310.0954

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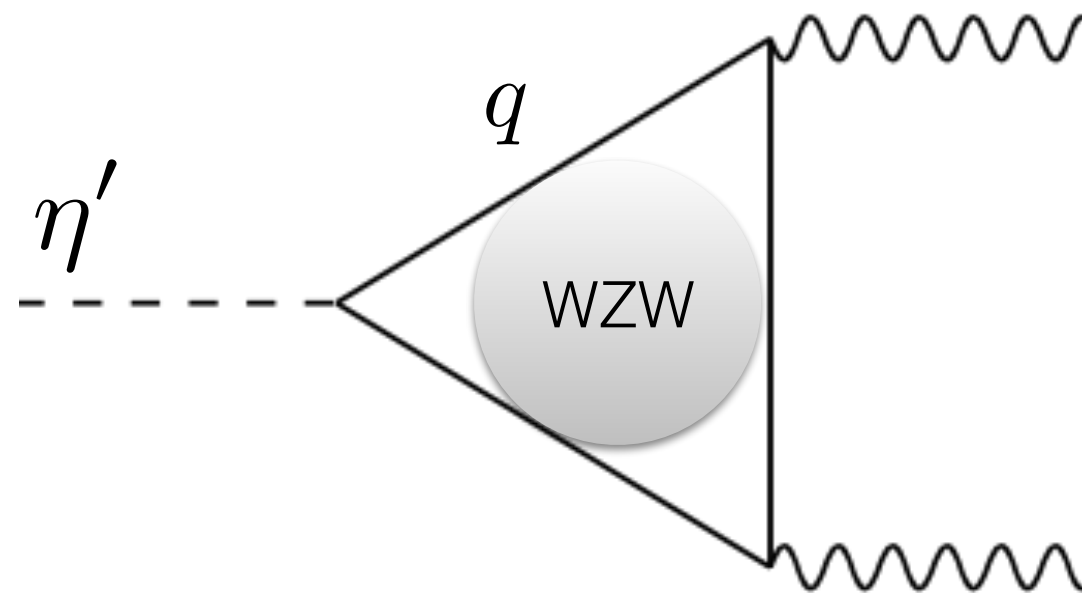
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(QCD axion might be replaced by new colored gapped dynamics,
Hsu & Sannino hep-ph/0408319 in PLB, Wilczek and Moore 1601.02937)



Minimal Composite Dynamics

Molinaro, Vignaroli, Sannino.1512.05334,1602.07574

Minimal Composite Dynamics

$$SU(2) \times SU(2) \rightarrow SU(2)$$

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- ◆ Natural mass scale
- ◆ Littlest matter required
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$$F_T = 246 \text{ GeV}$$

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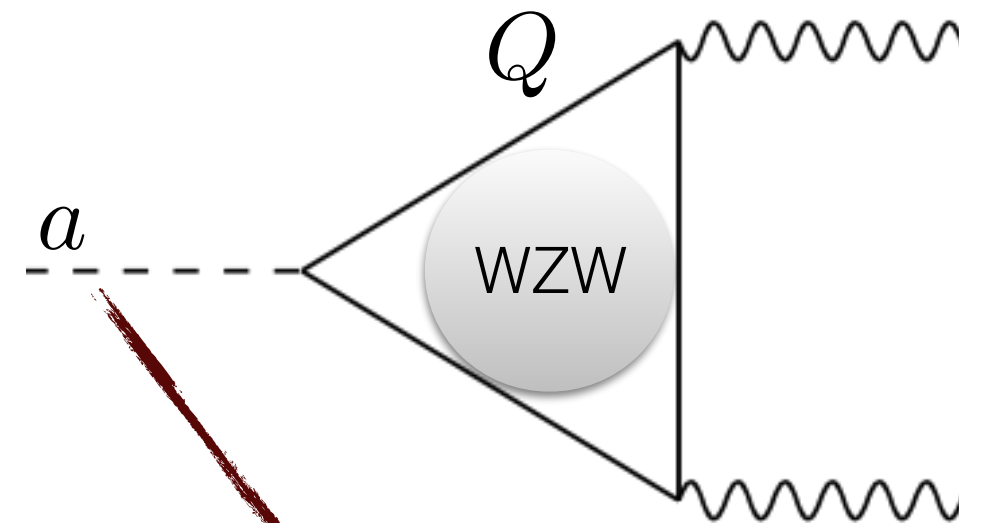
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Production

Molinaro, Vignaroli, Sannino.1512.05334,1602.07574

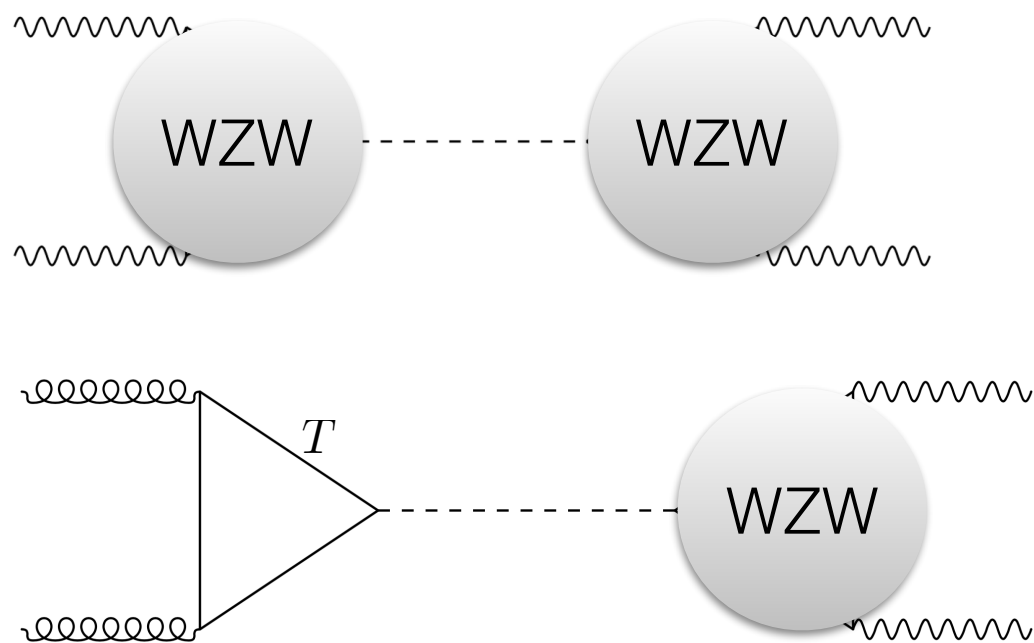
Talk by Emiliano Molinaro this afternoon

Production

Molinaro, Vignaroli, Sannino.1512.05334,1602.07574

Narrow width

- ◆ photon fusion
- ◆ top prime induced gluon fusion



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Production

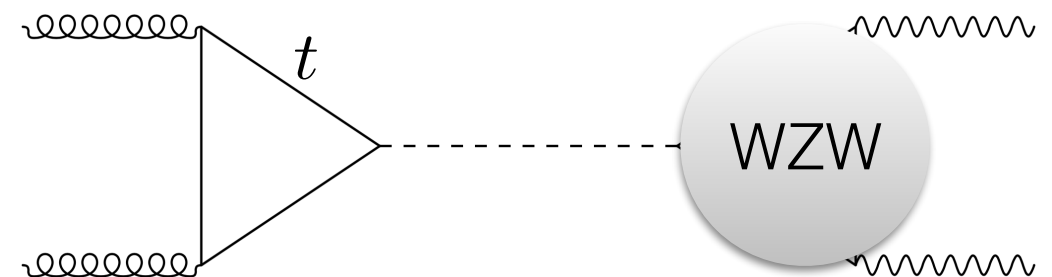
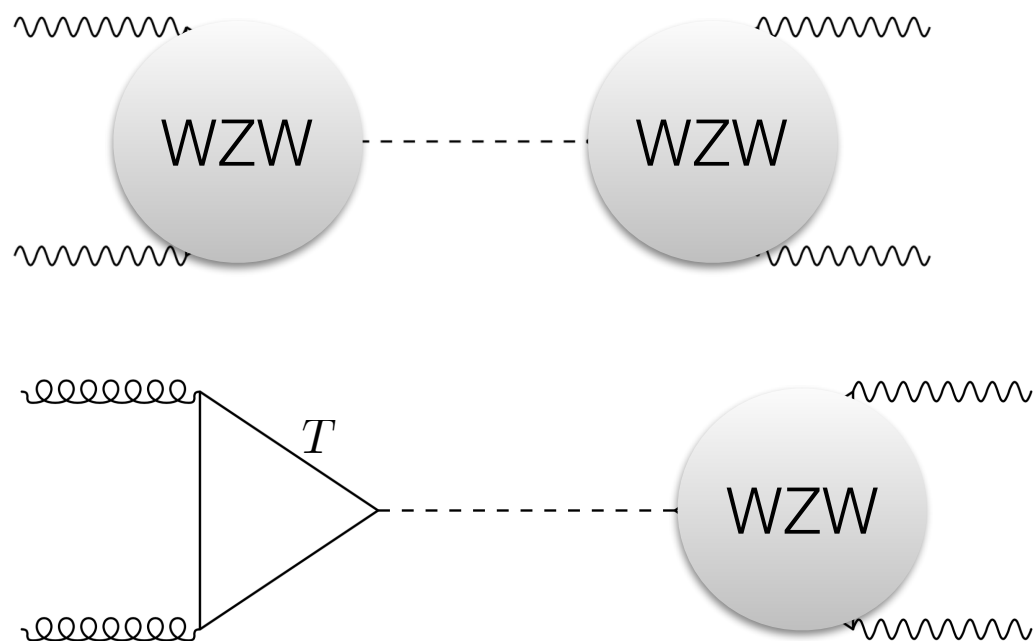
Molinaro, Vignaroli, Sannino.1512.05334,1602.07574

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- ◆ photon fusion
- ◆ top prime induced gluon fusion

ATLAS width ~ 40 GeV

- ◆ Coupling with top via mass operator

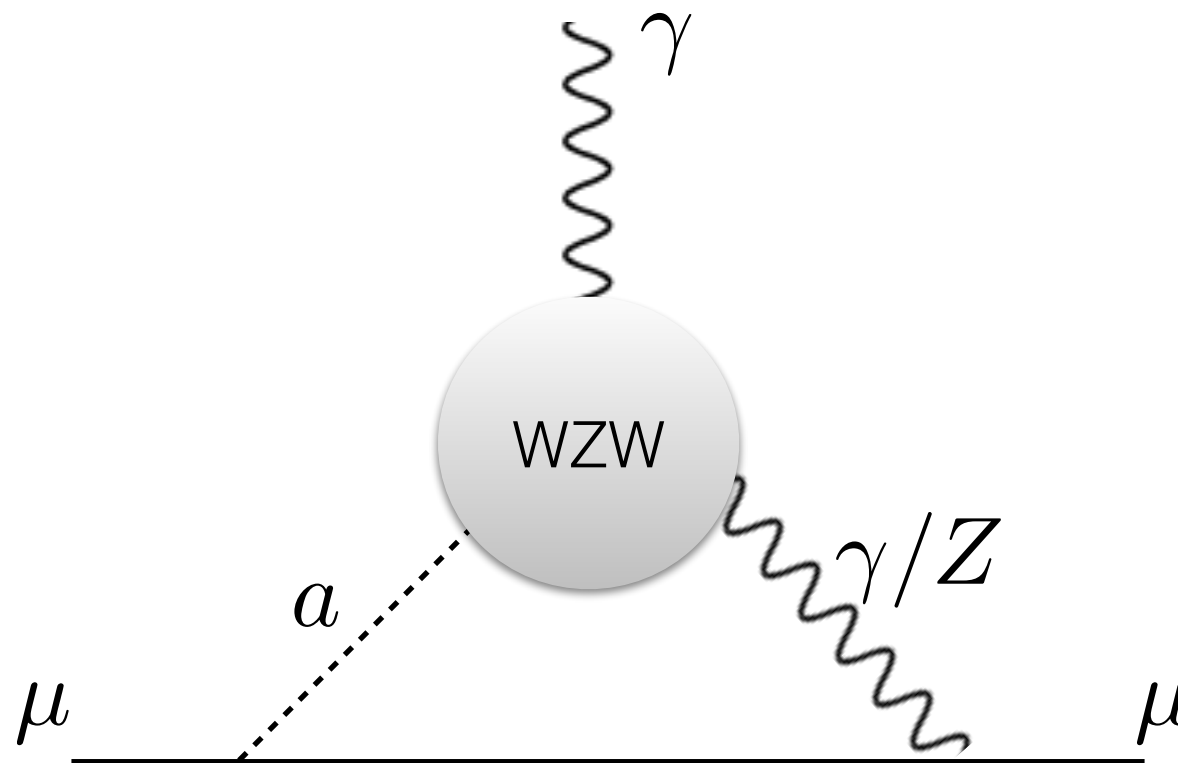


$g - 2$

about 3.2 sigma deviations (BNL) 2006

Naive dimensional analysis

Deog Ki Hong, Du Hwan Kim 1602.06628

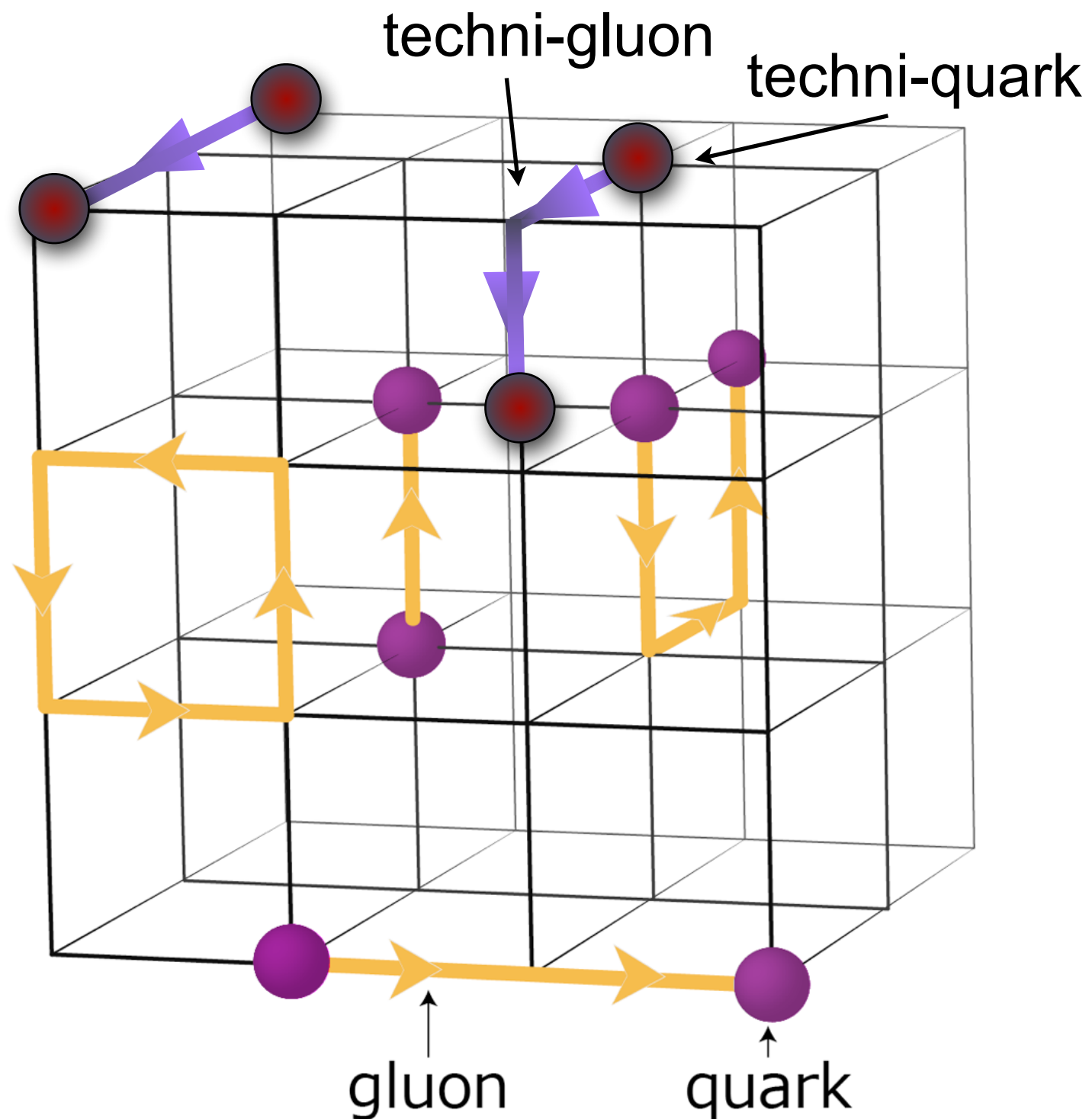


What will LHC see next?

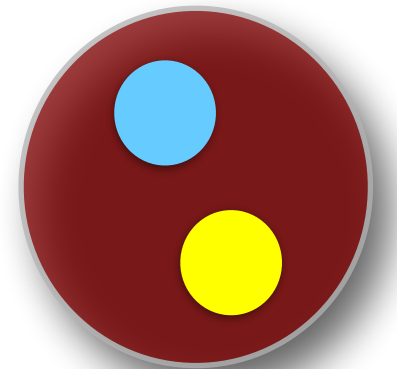
What will LHC see next?

- ◆ Related TC-eta processes
- ◆ Spin-1 resonances in Drell-Yan (2 - 4) TeV
- ◆ Diboson resonances (2-4) TeV
- ◆ New lepton/color states needed to fix anomalies and top mass
- ◆ Direct tests of Minimal TC via diphotons
- ◆

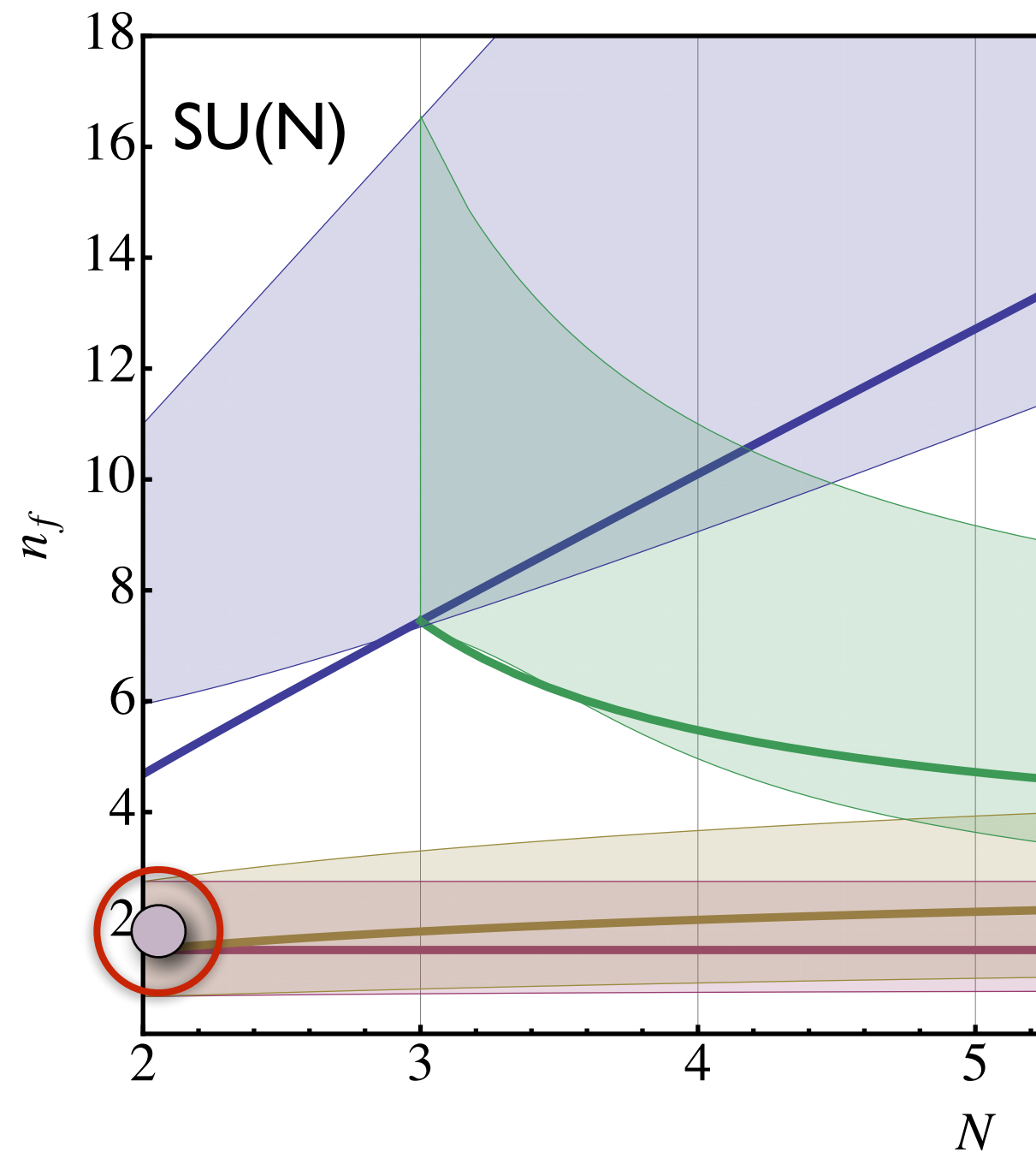
Composite Dynamics on the Lattice



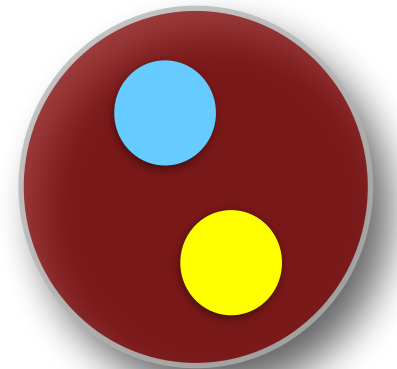
$SU(2) = Sp(2)$ with 2 Flavors



Minimal Fund. Template

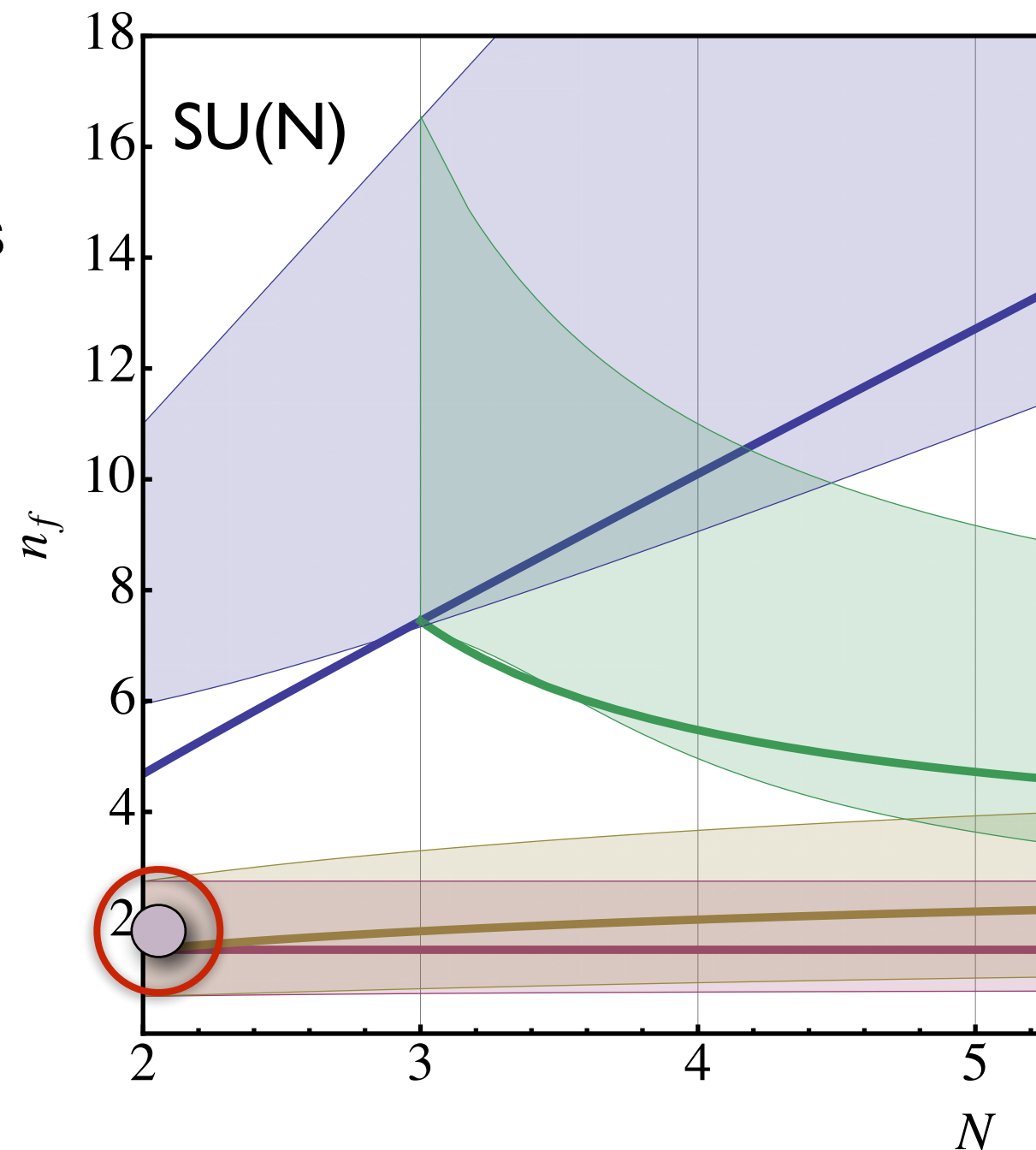


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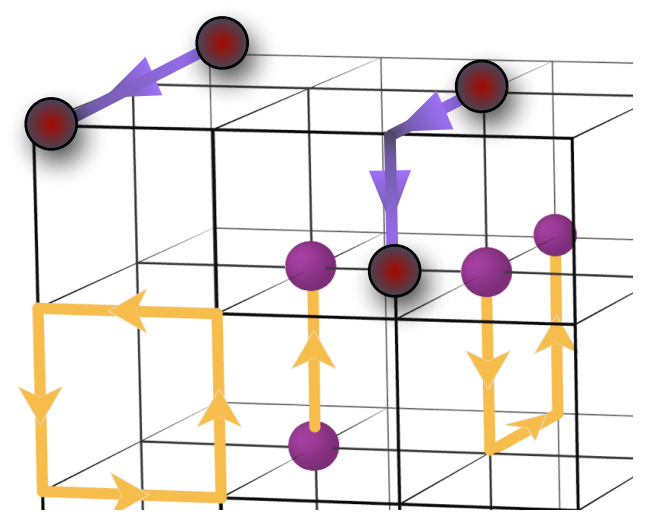


Minimal Fund. Template

- ◆ Unified TC & Comp. Goldstone Higgs
- ◆ TC Meson DM
- ◆ Stealth DM
- ◆ Dark Nuclei
- ◆ SIMPlest Miracle
- ◆ ...



$SU(\mathbf{2}) + 2$ Dirac Flavors



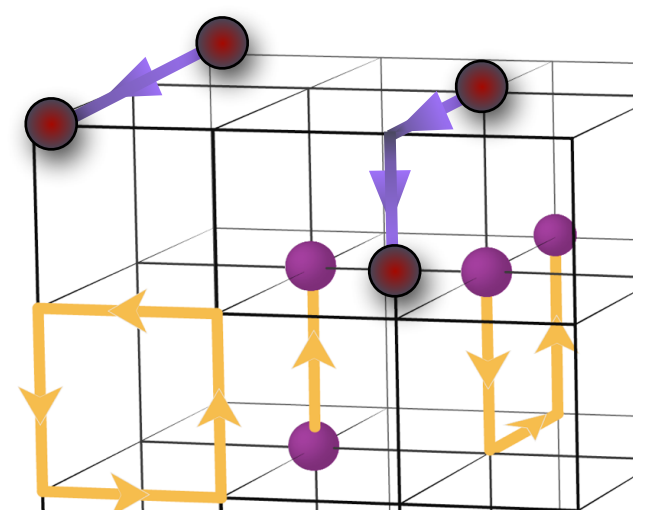
$SU(\mathbf{2}) + 2$ Dirac Flavors

- ◆ $SU(4)$ global symmetry breaks to $Sp(4)$
- ◆ 5 Goldstone bosons
- ◆ Goldstone form factors

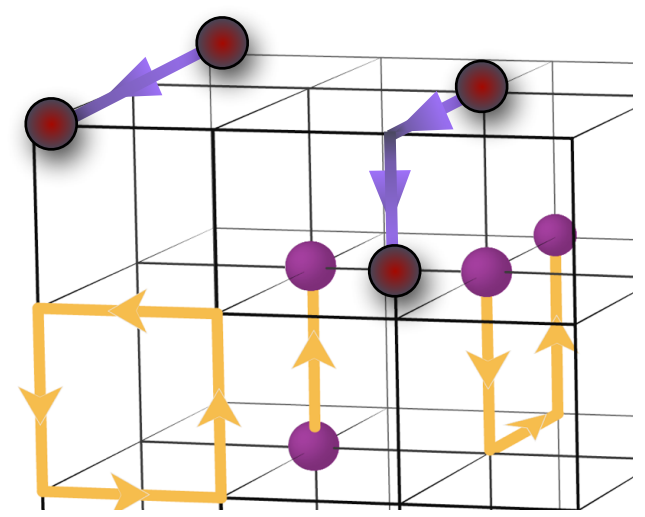
Lewis, Pica, Sannino, 1109.3513

Hietanen, Lewis, Pica, Sannino, 1308.4130

Hietanen, Lewis, Pica, Sannino, 1404.2794



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Lewis, Pica, Sannino, 1109.3513

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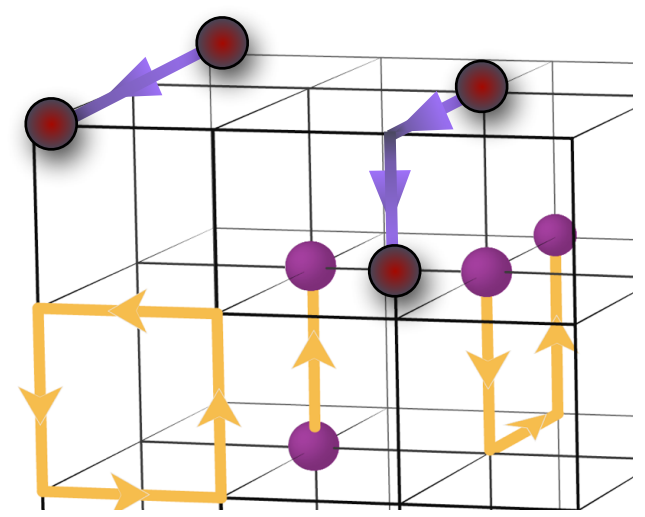
Lattice predictions for TC & CH Spin-One states

$$m_V = \frac{3.2(5)}{\sin \theta} \text{ TeV}$$

$$m_A = \frac{3.6(9)}{\sin \theta} \text{ TeV}$$

Arthur, Drach, Hansen, Hietanen, Pica, Sannino, 1602.06559

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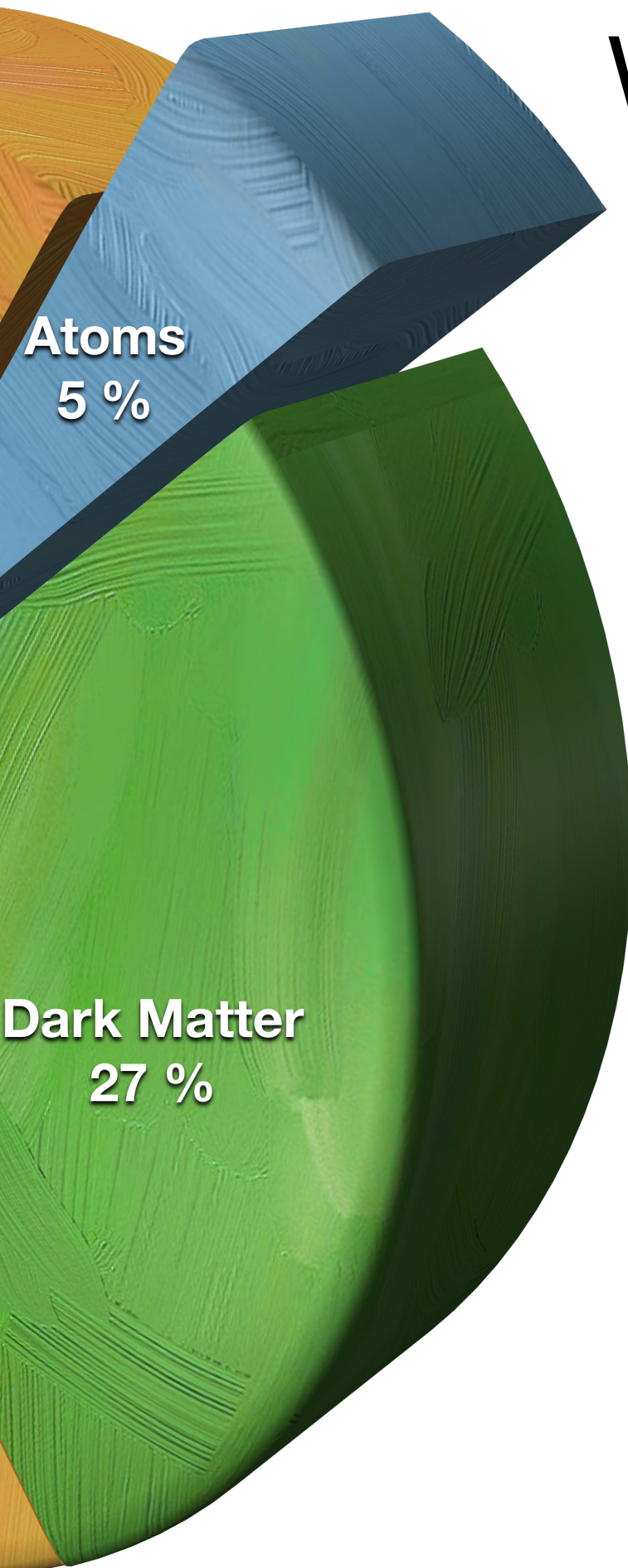
Arthur, Drach, Hansen, Hietanen, Pica, Sannino, 1602.06559

In progress:

- ◆ Scalar spectrum
- ◆ Scattering amplitudes

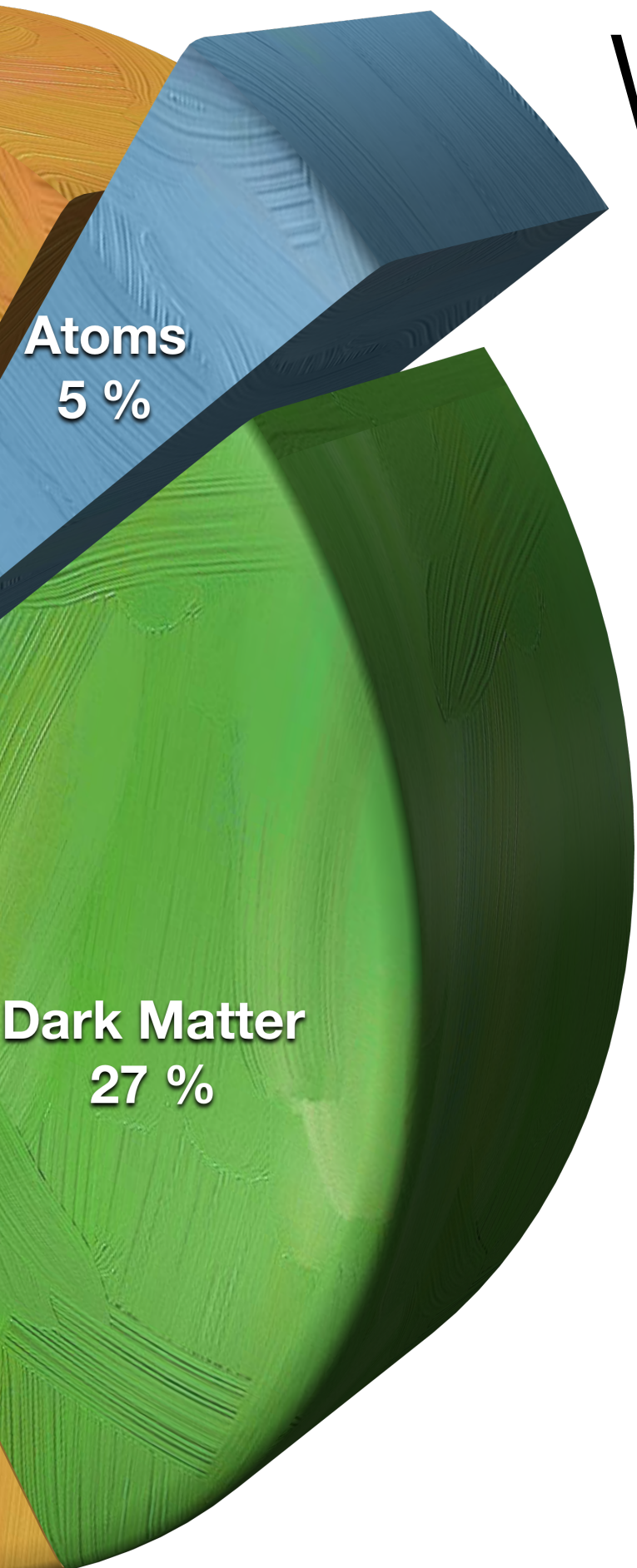
Dark side

What makes dark matter ?



Atoms: 3 forces and many fund. particles

What makes dark matter ?



Atoms
5 %

Atoms: 3 forces and many fund. particles

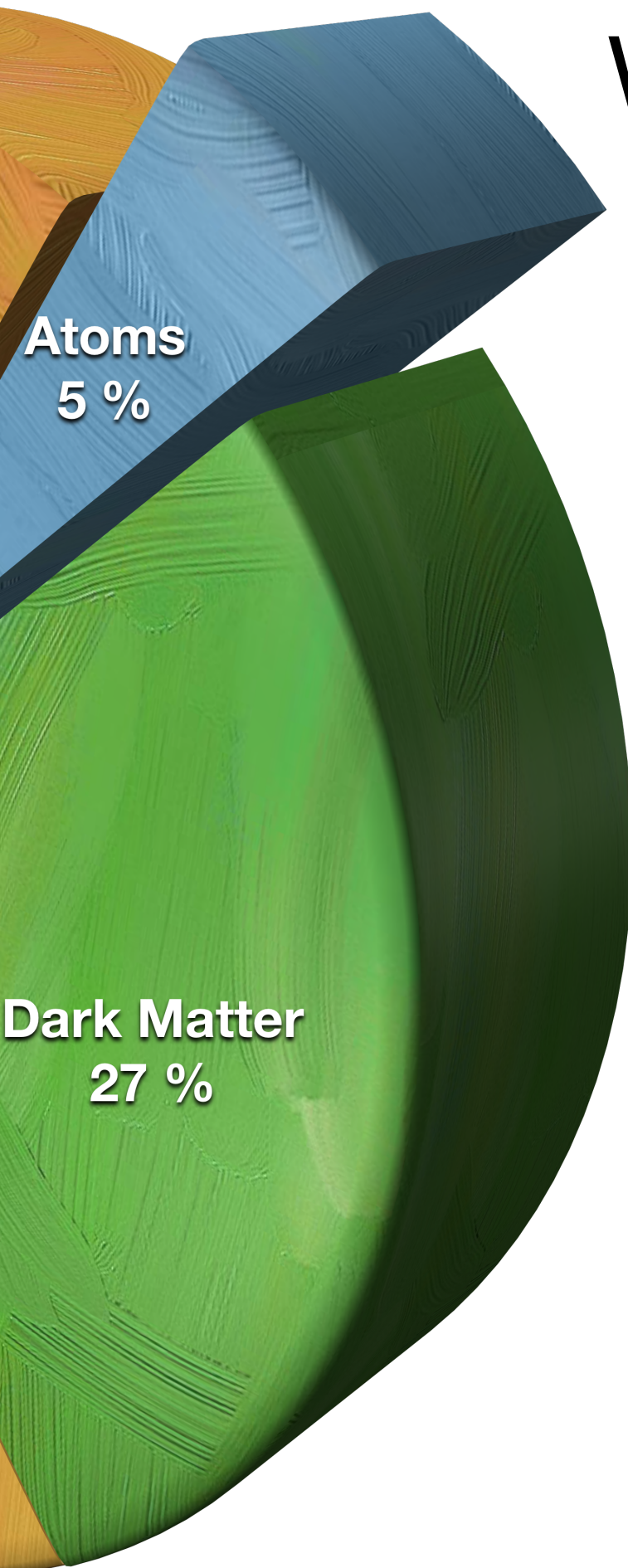
DM oversimplification

DM Particle



Dark Matter
27 %

What makes dark matter ?



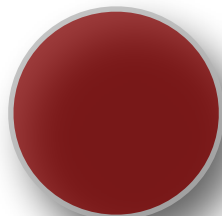
Atoms: 3 forces and many fund. particles

DM oversimplification

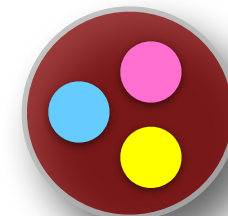
DM Particle

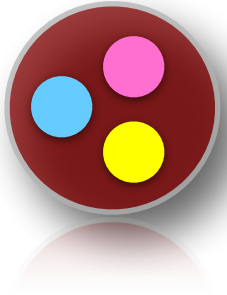


Elementary

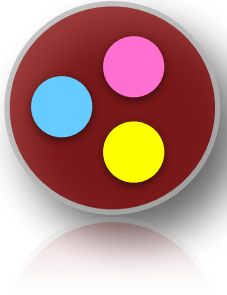


Composite



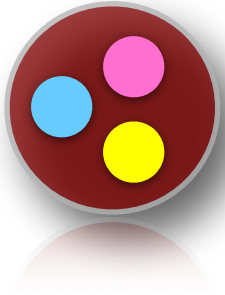


Composite Dark Matter



Composite Dark Matter

Building Blocks

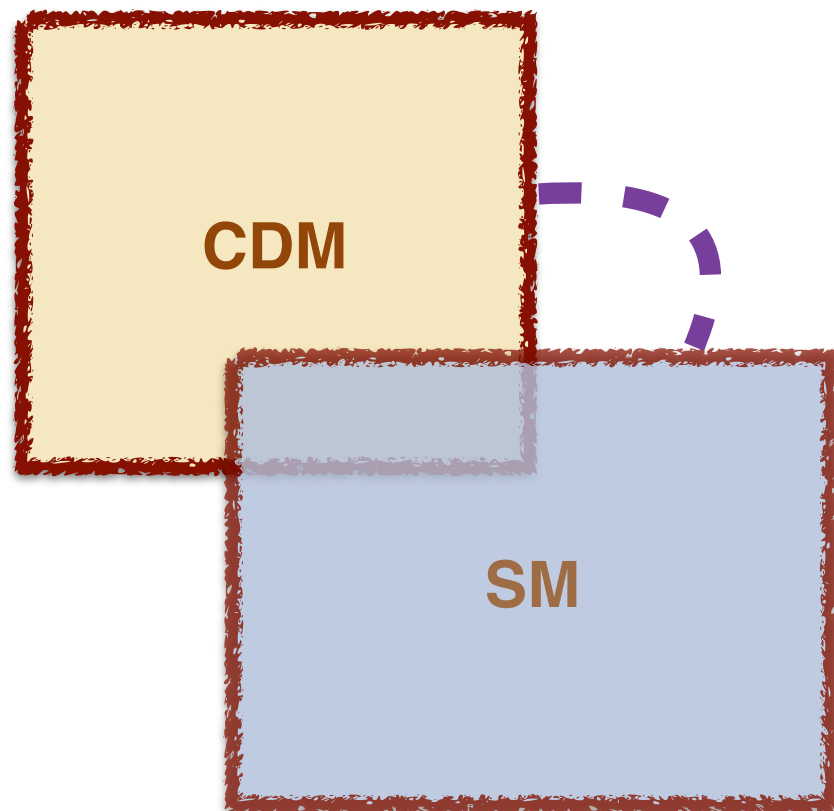


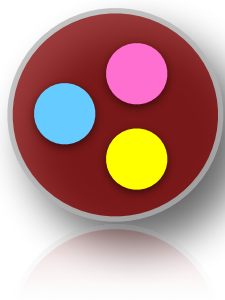
Composite Dark Matter

Building Blocks

SM charged

Type I





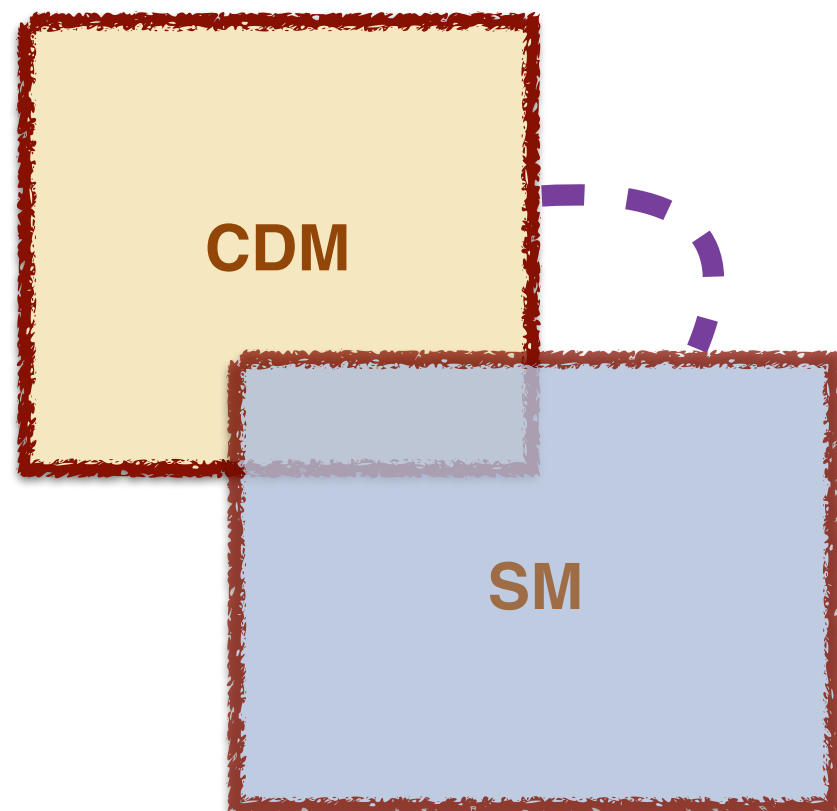
Composite Dark Matter

Building Blocks

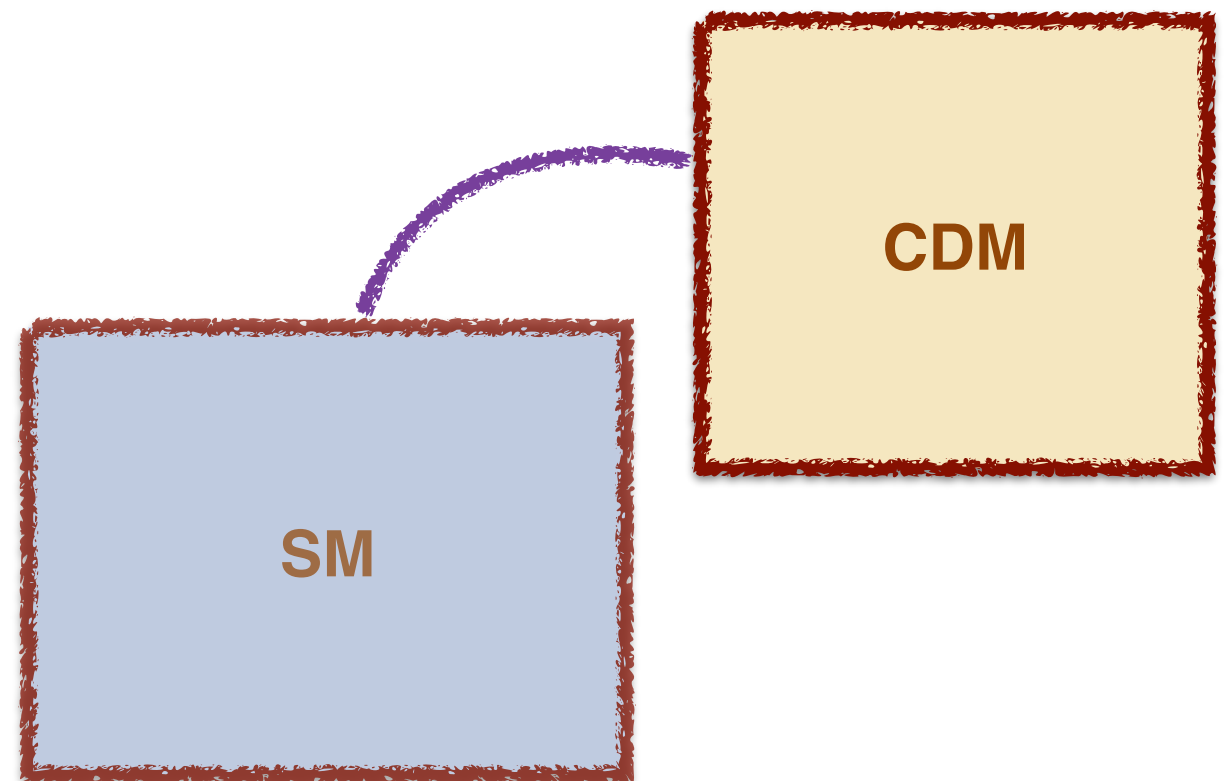
SM charged

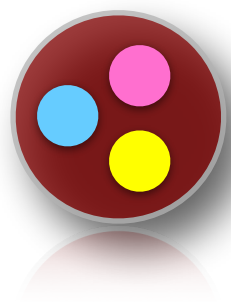
SM singlets

Type I



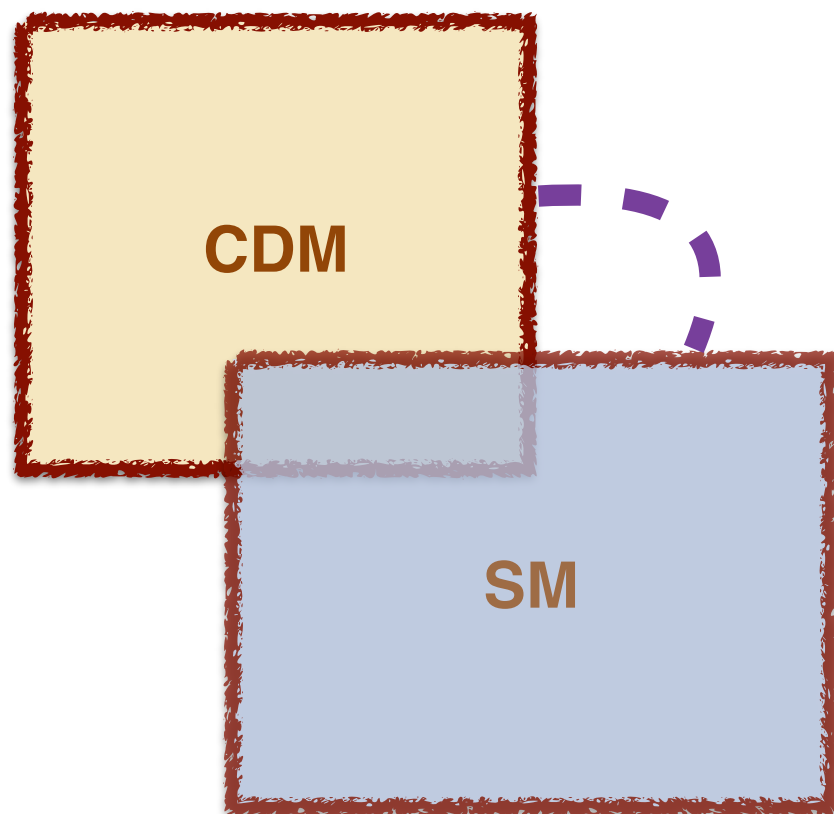
Type II

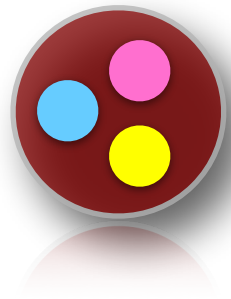




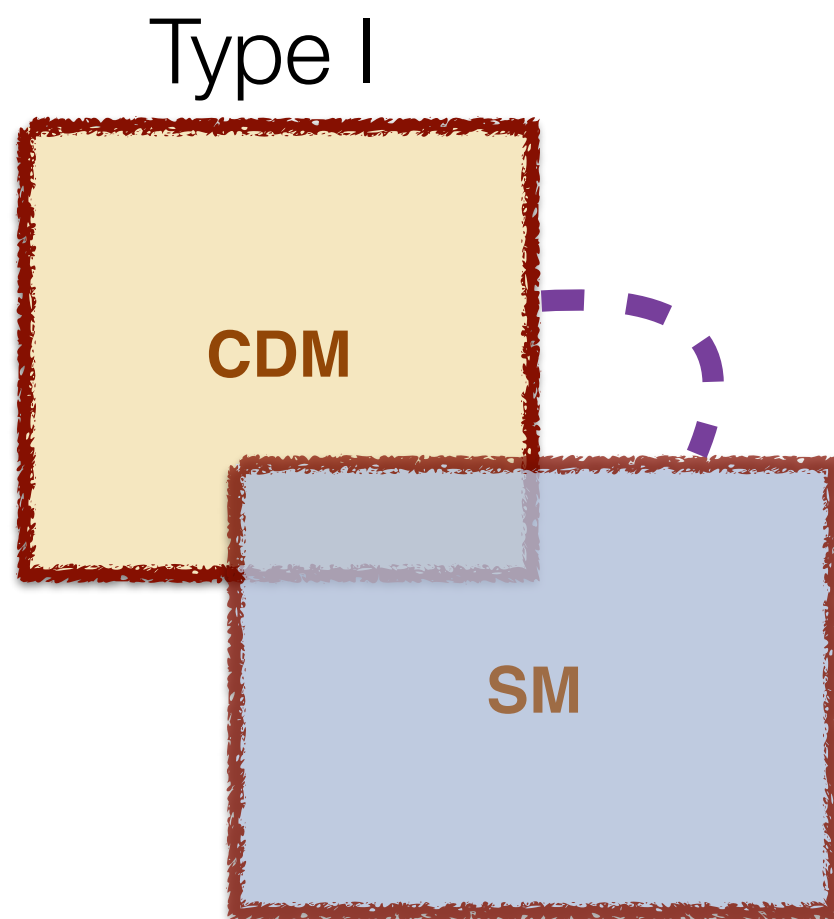
CDM Type I

Type I





CDM Type I



- TC Baryon¹
- TC Meson²
- Millicharged Comp. DM³
- Stealth DM⁴
- Solitons/Little Higgs⁵
-

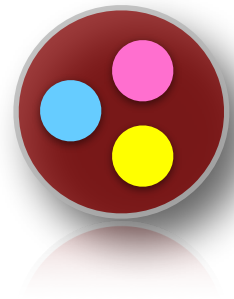
¹Nussinov 85 & Barr, Chivukula, Farhi 90

²Gudnason, Kouvaris, Sannino ph-0603014, 0608055

³Kouvaris 1304.7476

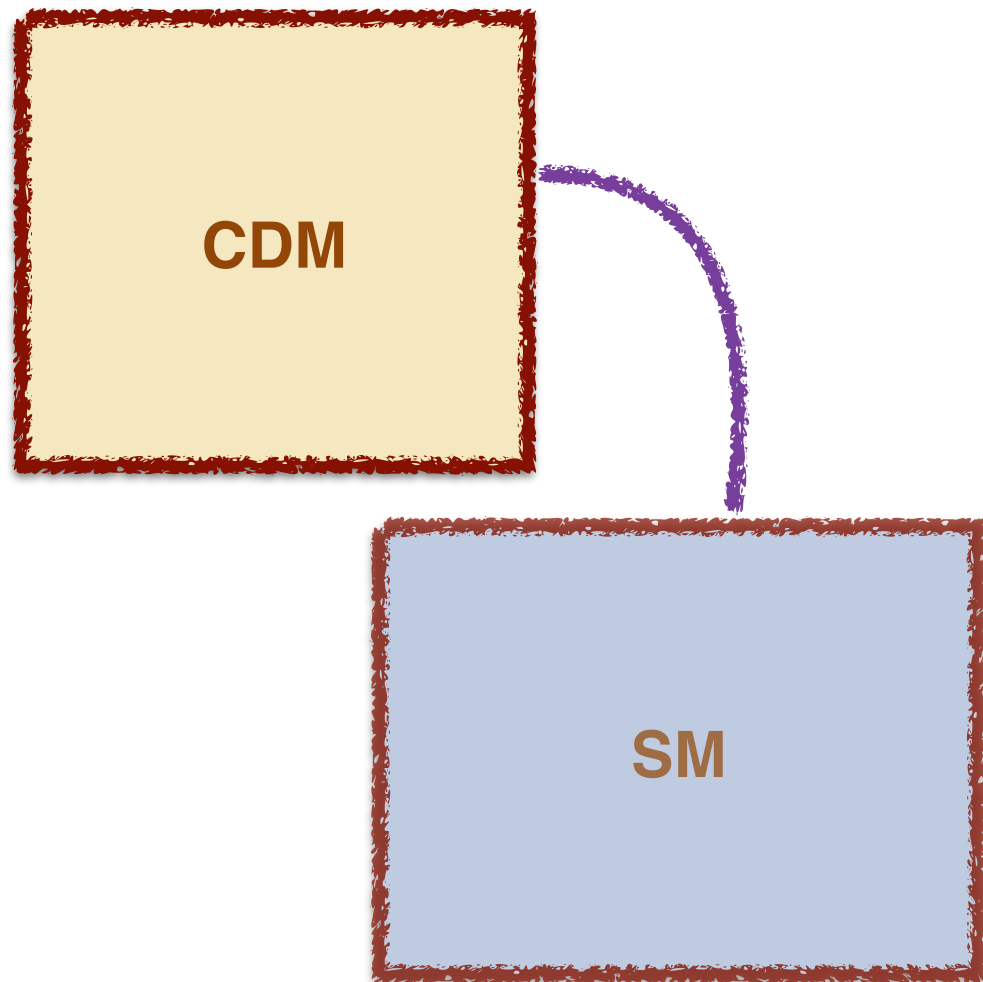
⁴Appelquist et al. 1503.04203

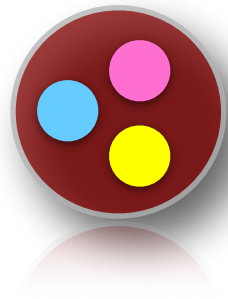
⁵Gillioz, 1103.5990



CDM Type II

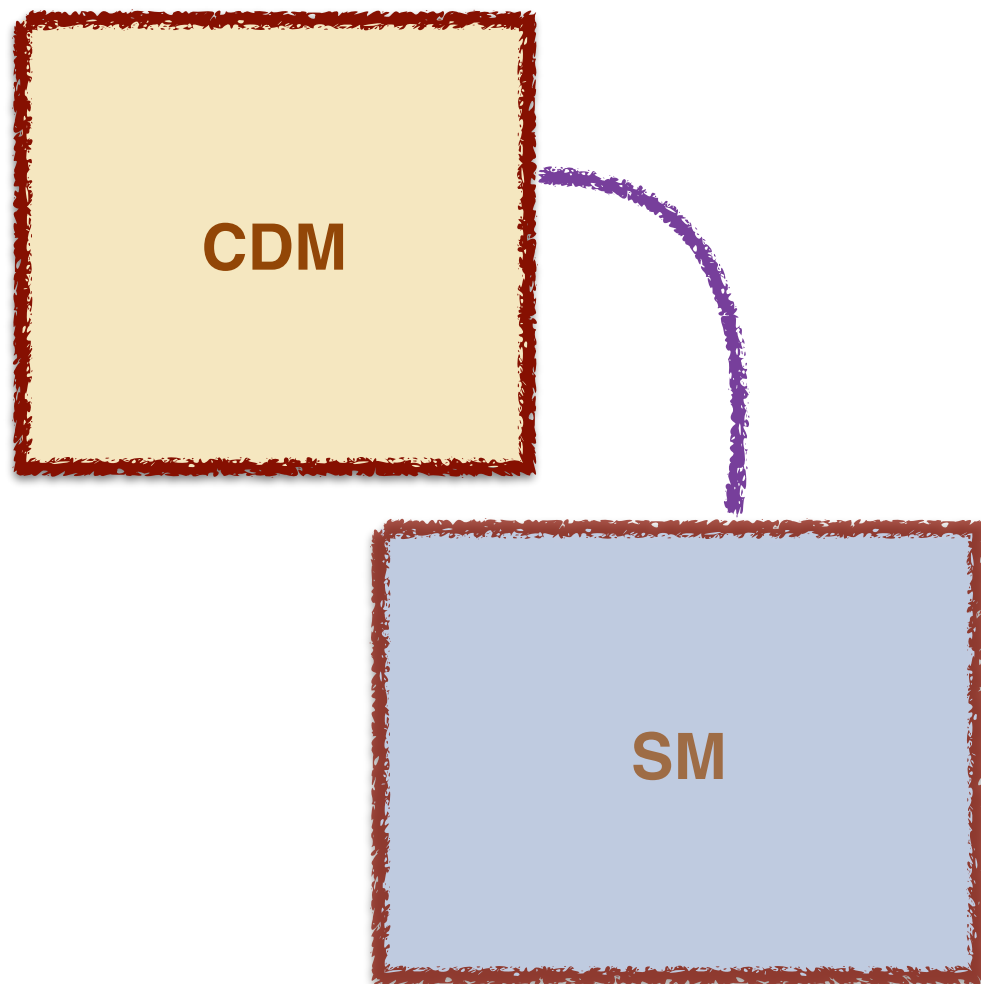
Type II





CDM Type II

Type II



- Dark Nuclei¹
- SIMPllest Miracle^{2,3}
- Solitonic
-

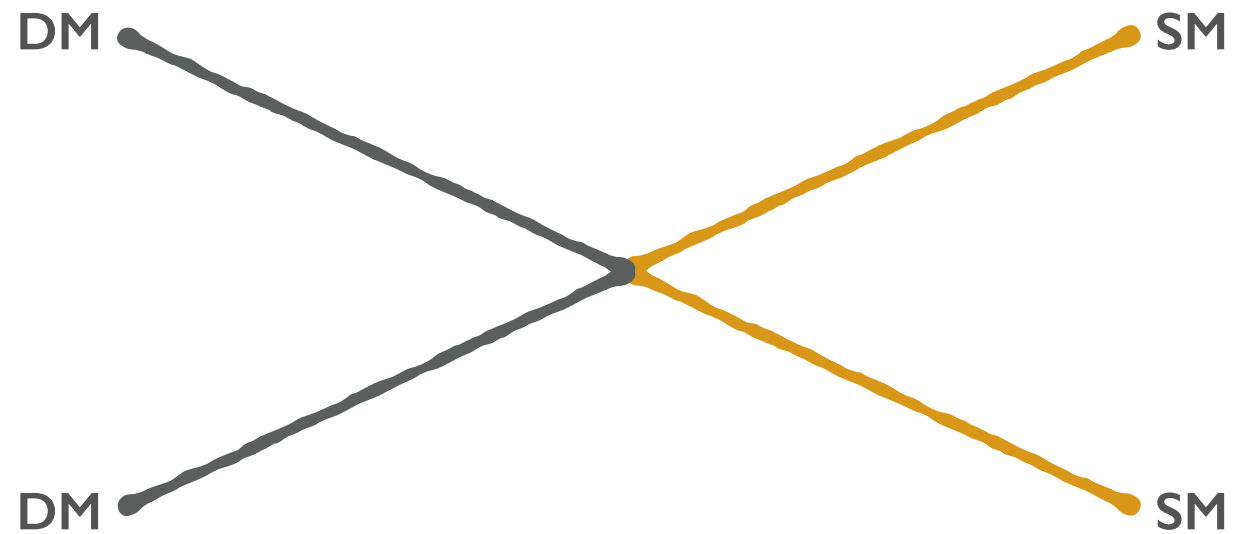
¹Detmold, McCullough, Pochinsky 1406.2276

²Hochberg, Kuflik, Murayama, Volansky, Wacker, 1411.3727

³Hansen, Langaebler, Sannino, 1507.01590

(Not) the SIMPlest miracle

The SIMP Mechanism



$2 \rightarrow 2$ annihilation

The SIMP Mechanism

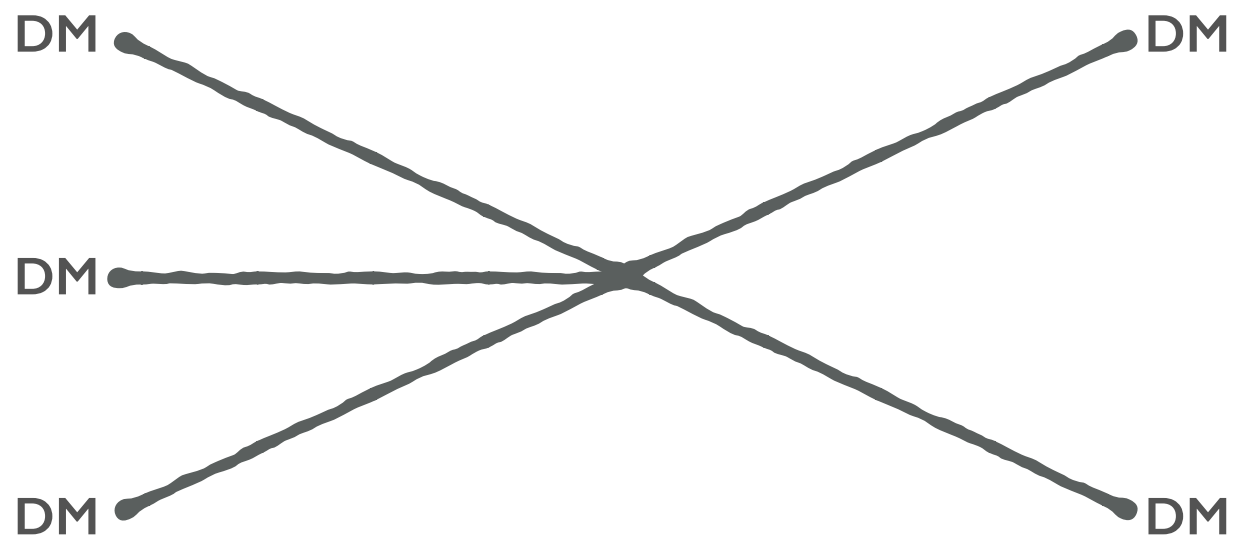


$2 \rightarrow 2$ annihilation

The SIMP Mechanism



$2 \rightarrow 2$ annihilation

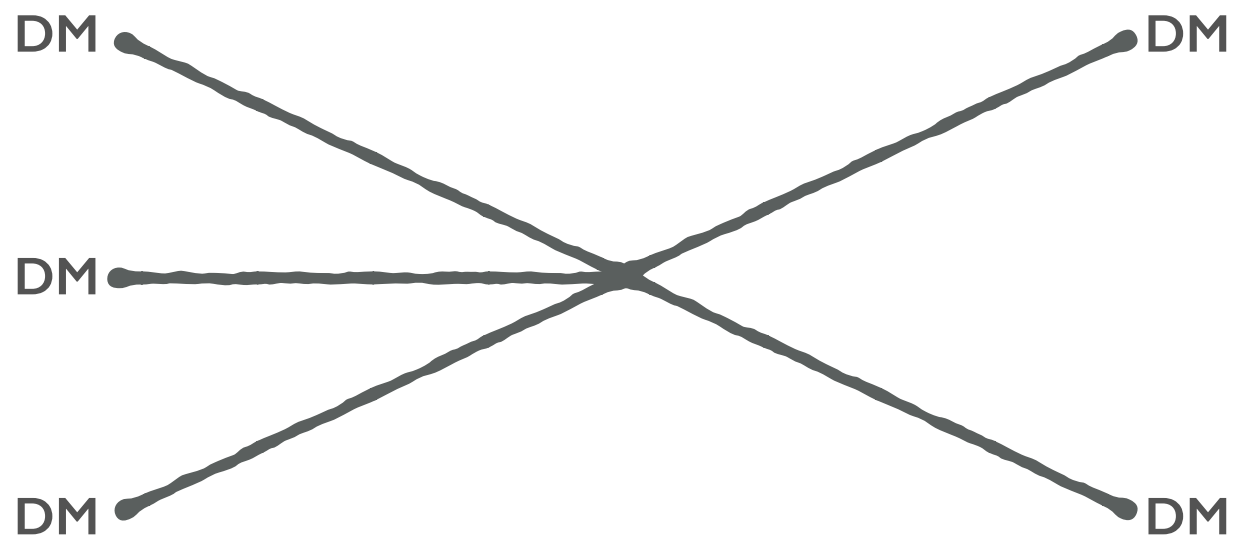


$3 \rightarrow 2$ annihilation

The SIMP Mechanism



2 → 2 annihilation



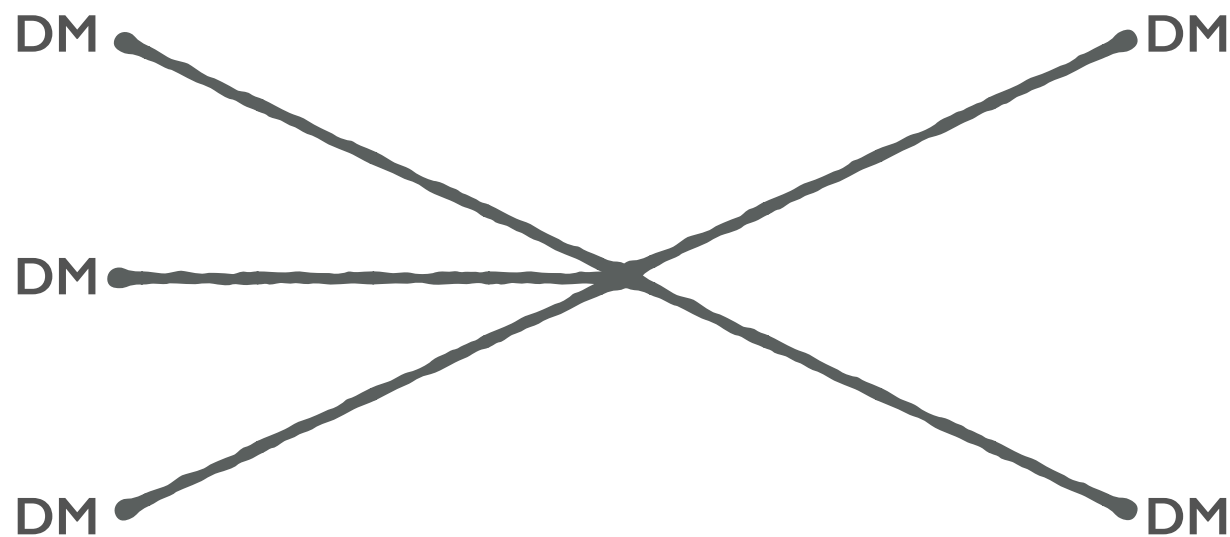
3 → 2 annihilation

Relevant DM - DM # changing operators

The SIMP Mechanism



$2 \rightarrow 2$ annihilation



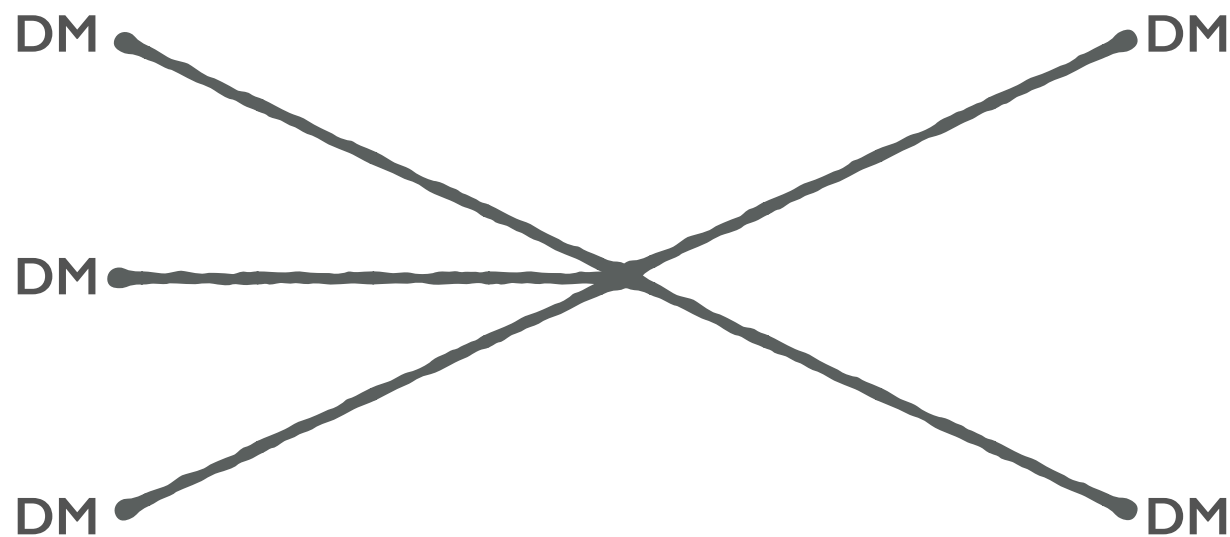
$3 \rightarrow 2$ annihilation

Relevant DM - DM # changing operators

The SIMP Mechanism



2 → 2 annihilation



3 → 2 annihilation

Relevant DM - DM # changing operators

Hochberg, Kuflik, Murayama, Volansky, Wacker, 1411.3727, PRL

Hansen, Langaebler, Sannino, 1507.01590, PRD

Original idea

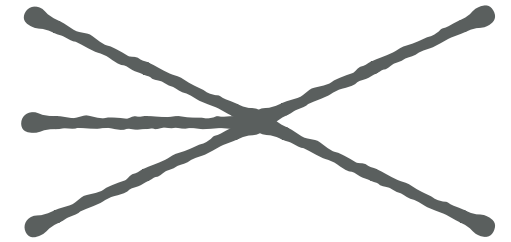
E. Carlson et al: Astrophys.J. 398 (1992) 43-52

A. de Laix et al: Astrophys.J. 452 (1995) 495

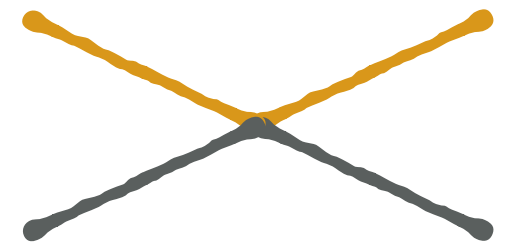
Relevant processes

- The $3 \rightarrow 2$ process constrains DM via Boltzmann equation/
relic-density.

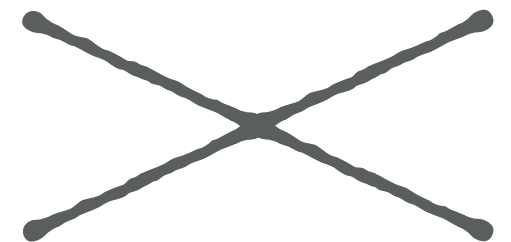
$$\dot{n} + 3Hn = -(n^3 - n^2 n_{eq}) \langle \sigma v^2 \rangle_{3 \rightarrow 2}$$



- @ Freeze-out, thermal equilibrium with SM via e.g. $2 \rightarrow 2$
scattering between DM - SM



- The $2 \rightarrow 2$ scattering among DM constrained by observations



Dark SU(**2**) + 2 Dirac Flavors

Dark $SU(2)$ + 2 Dirac Flavors

- ◆ $SU(4)$ global symmetry breaks to $Sp(4)$
- ◆ 5 Goldstone bosons

ChPT based on $SU(4)$ to $Sp(4)$

$$u = \exp\left(\frac{i\alpha}{\sqrt{2}f} X^a \phi^a\right)$$

$$u_a = i(u^\dagger \partial_a u - u \partial_a u^\dagger)$$

ChPT based on $SU(4)$ to $Sp(4)$

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The topological WZW term leads to a 5-point interaction

$$\mathcal{L}_{WZW}^{(4)} = \frac{N_c}{240\pi^2} \int_0^1 d\alpha \int d^4x \epsilon^{abcde} \langle u_a u_b u_c u_d u_e \rangle$$

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(Inconsistent) $2 \rightarrow 2$ analysis to lowest non-vanishing order

$$\mathcal{L}^{(2)} = \frac{f^2}{4} \langle u^\mu u_\mu + \chi_+ \rangle$$

Consistent ChPT SIMP corrections

$2 \rightarrow 2$ evaluated at the same $3 \rightarrow 2$ order

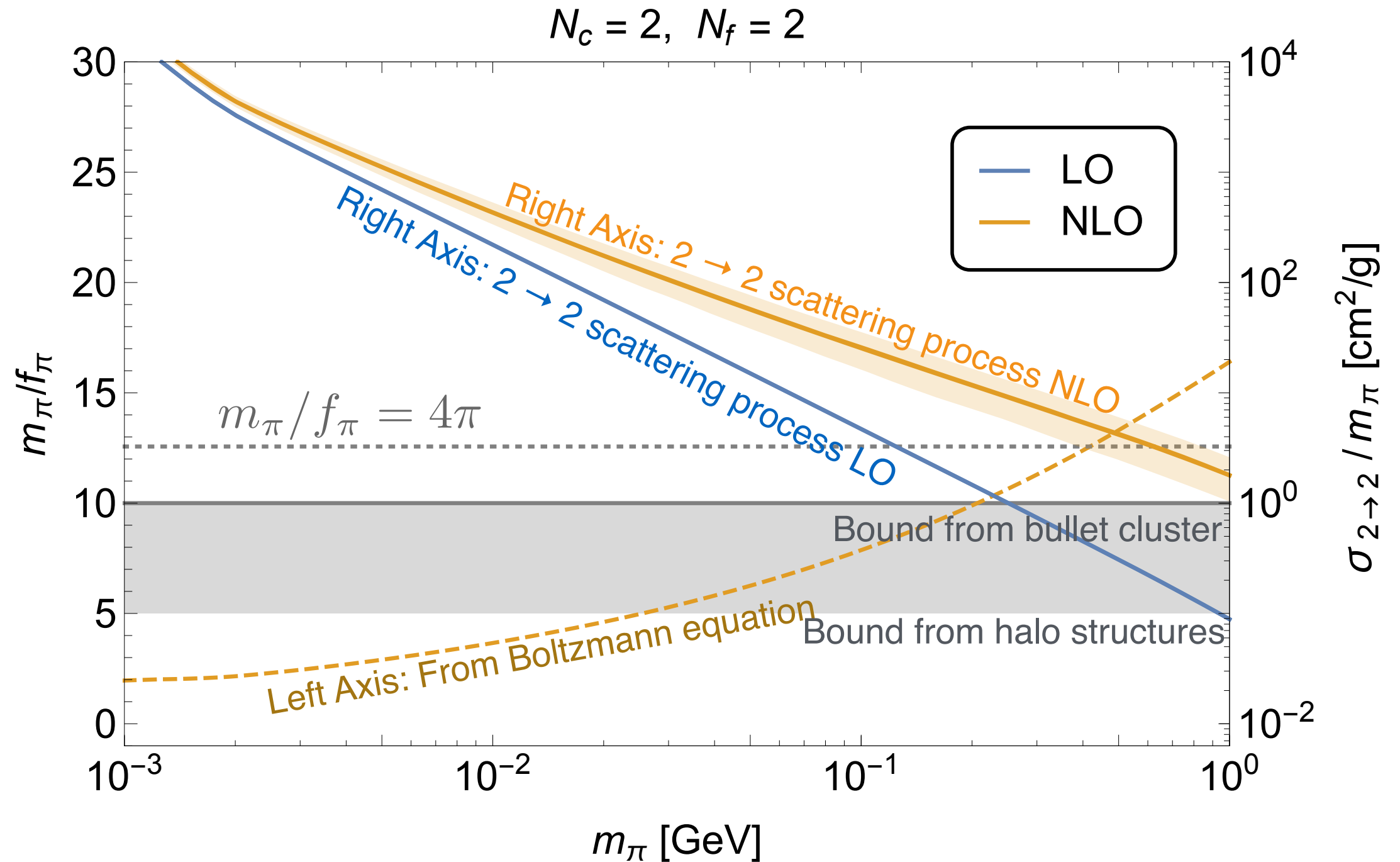
Physical values for the mass and decay constant.

$$f_\pi = f \left[1 + \frac{m^2}{f^2} (a_f L + b_f) \right] \quad m_\pi^2 = m^2 \left[1 + \frac{m^2}{f^2} (a_m L + b_m) \right]$$

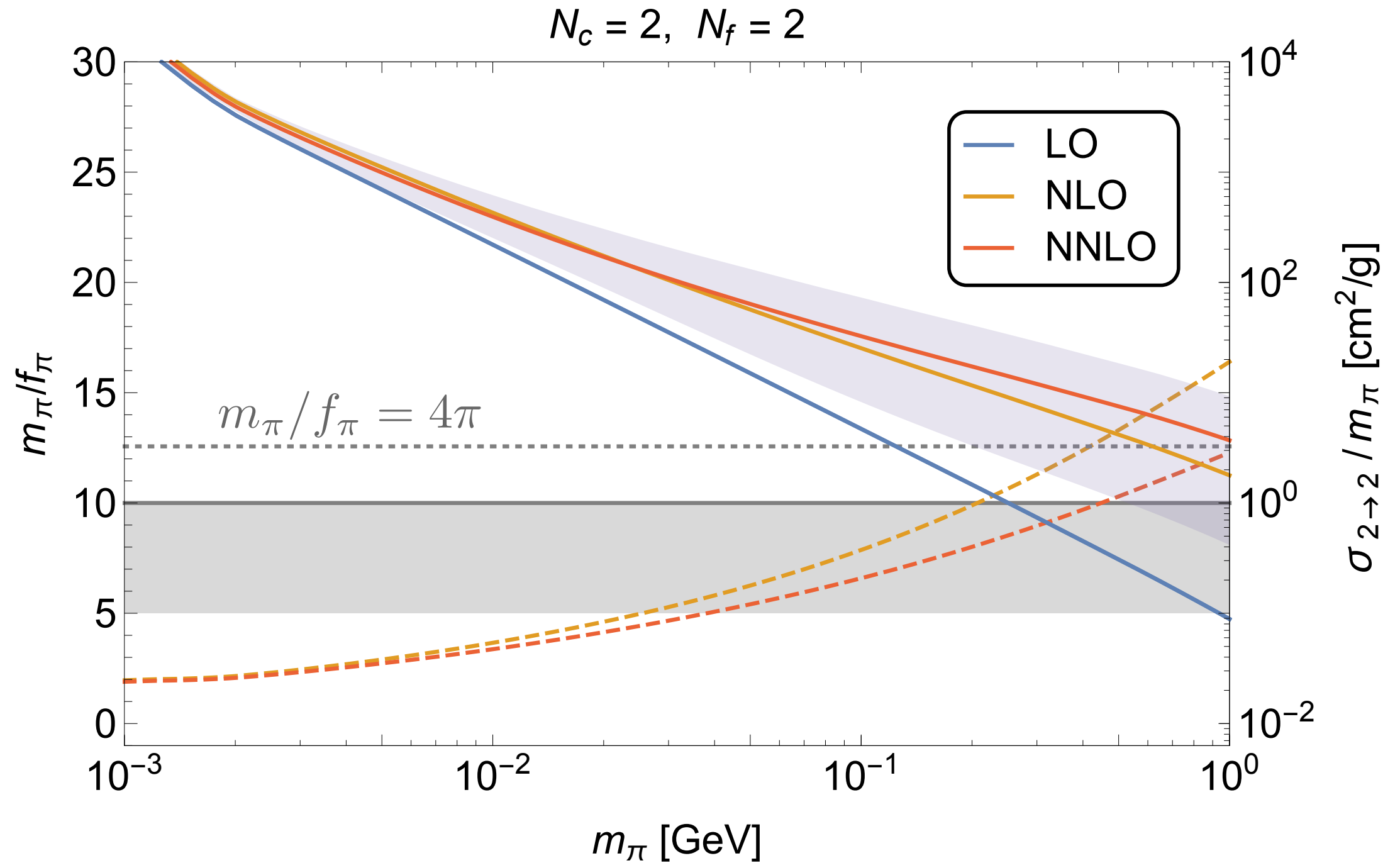
DM relic density relates mass and decay constant

DM $2 \rightarrow 2$ scattering process (constrained)

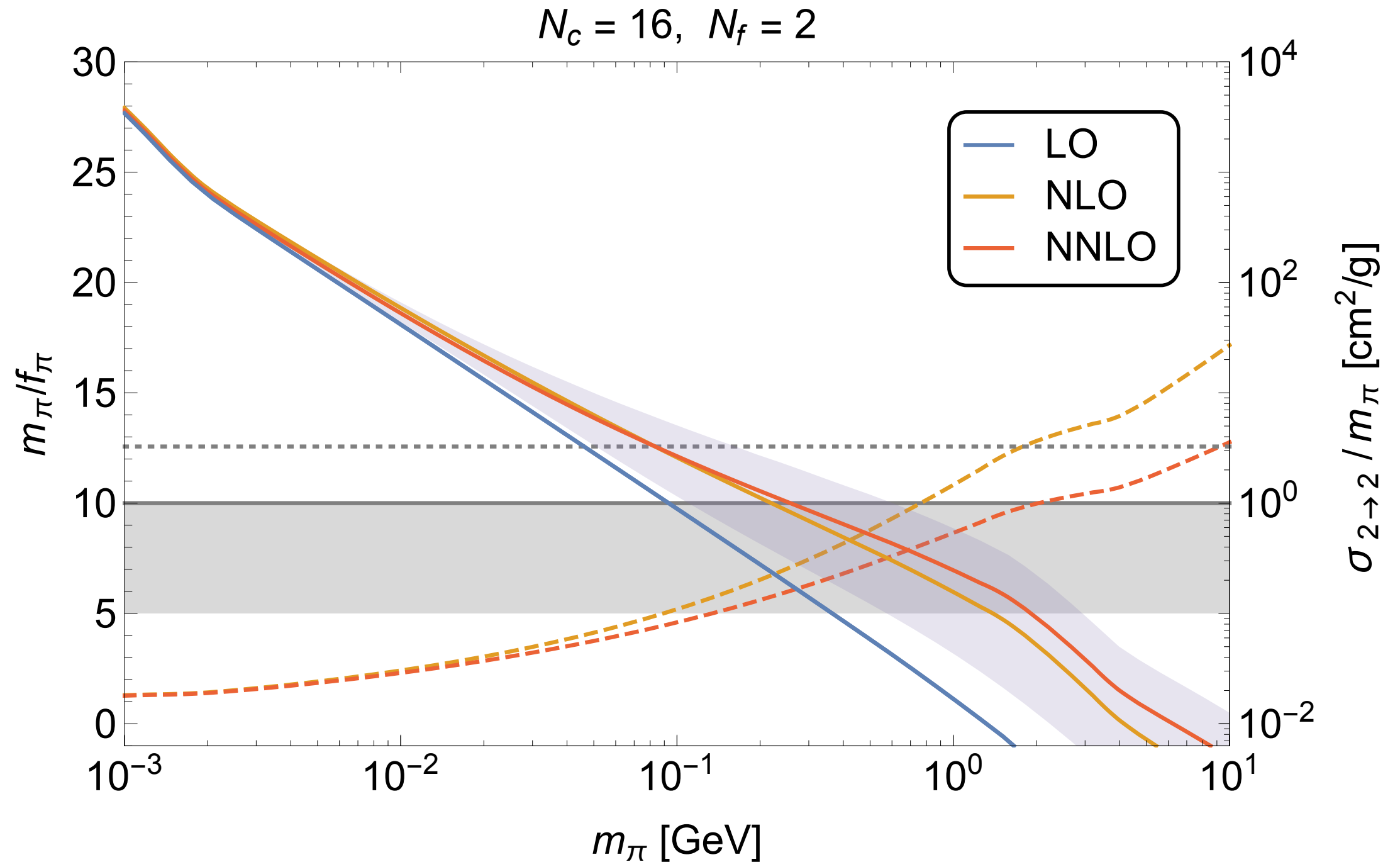
ChPT SU(2) with 2 Dirac Flavours



ChPT SU(2) with 2 Dirac Flavours



ChPT Sp(**16**) with 2 Dirac Flavours



(Not) the SIMPllest Miracle

- Consistent (N)NLO corrections challenge the minimal model
- Large (dark) pion masses vs decay constant needed
- Lattice results | 602.06559: compressed dark spin-one resonance spectrum for large dark quark masses
- Large number of dark colors help

Summary

Bright

- Minimal underlying composite template for TC and CH
- Lattice predictions for composite spin-one resonances
- TC-eta prime is a natural/testable candidate for the 750 GeV state

Molinaro, Vignaroli, Sannino. [1512.05334](#), [1602.07574](#)

Di Vecchia, Veneziano, (1980)

Dark

- Presented several more or less natural composite realisations of DM
- Introduced the SIMP paradigm and its underlying template theory
- (N)NLO ChPT for SIMPlest miracle makes it less miraculous
- (N)NLO must be taken into account when SIMPs is coupled to SM fields

Charting strong dynamics is key to concrete composite extensions of the SM

Backup slides

Composite theory space

Knobs

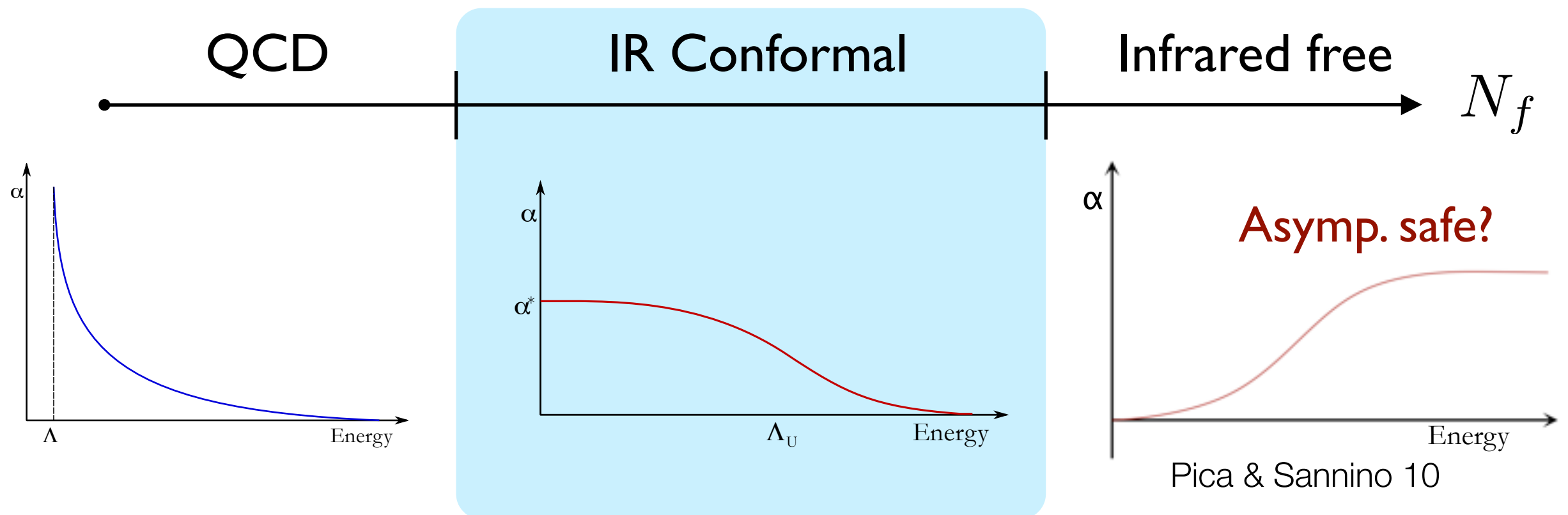


Gauge Group: SU, SO, SP, Exceptional

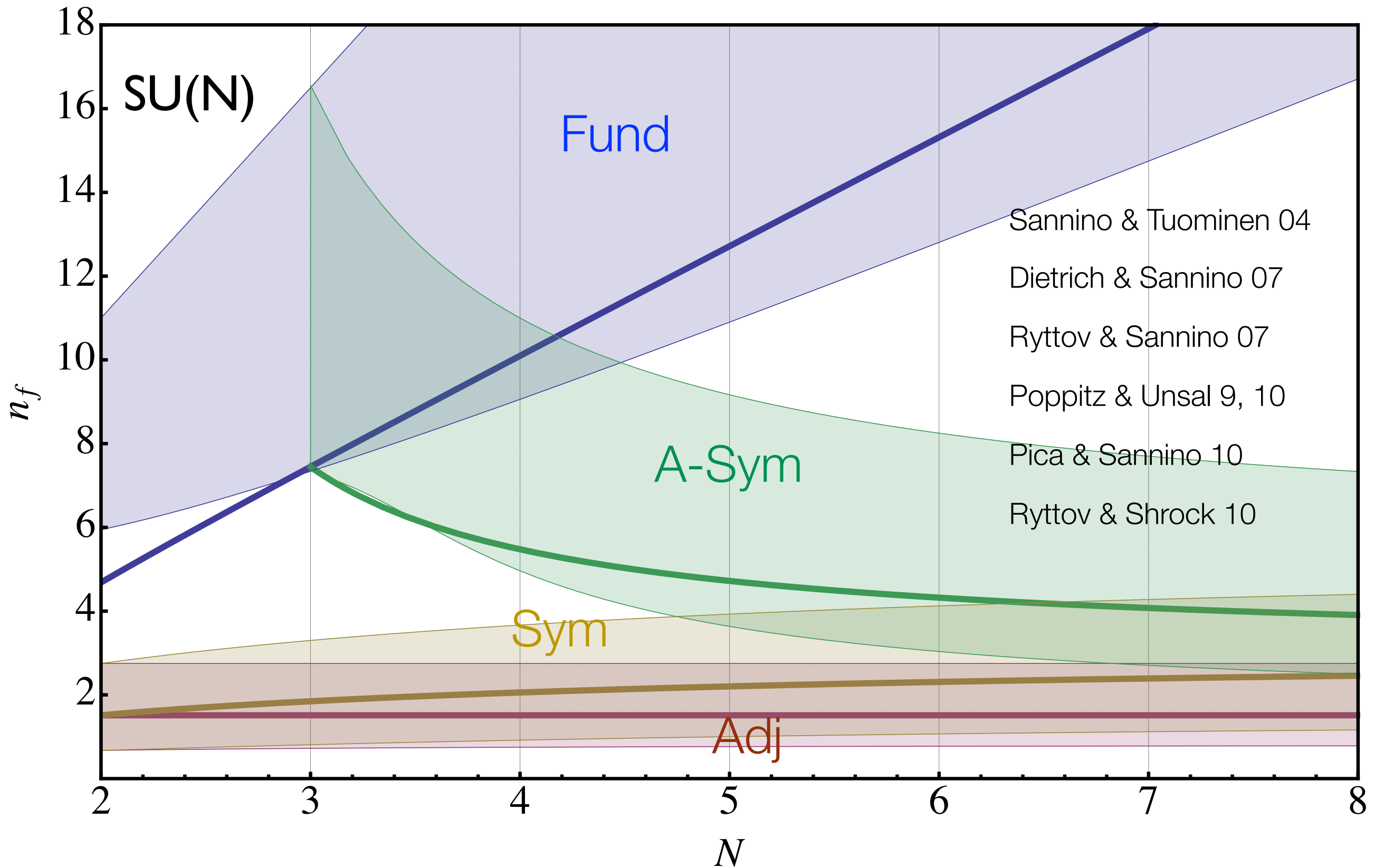
Matter Representation

of Flavours per Representation

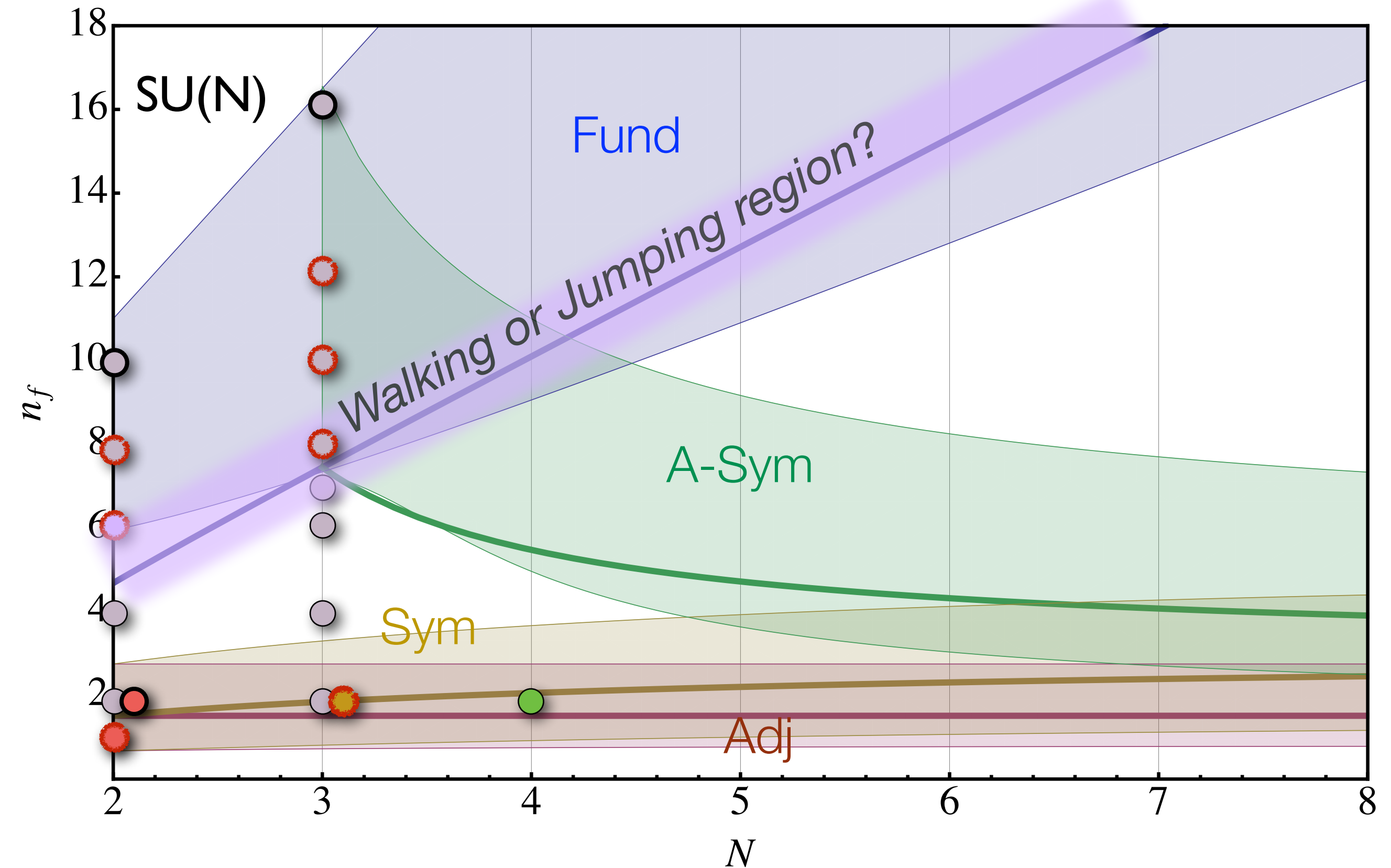
4 Fermi interactions / ETC



SU(N) Phase Diagram



Lattice SU(N) Phase Diagram

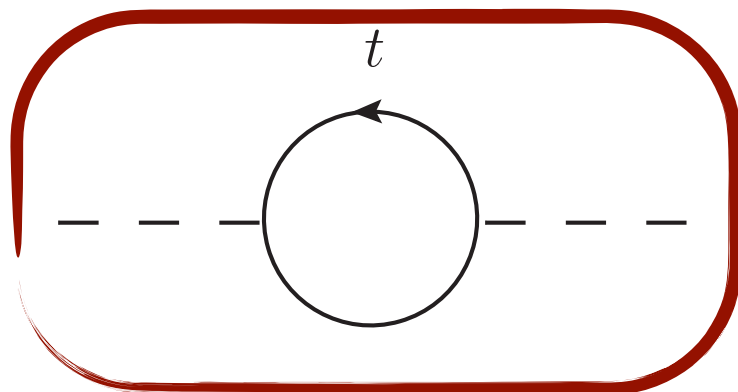


TC Higgs

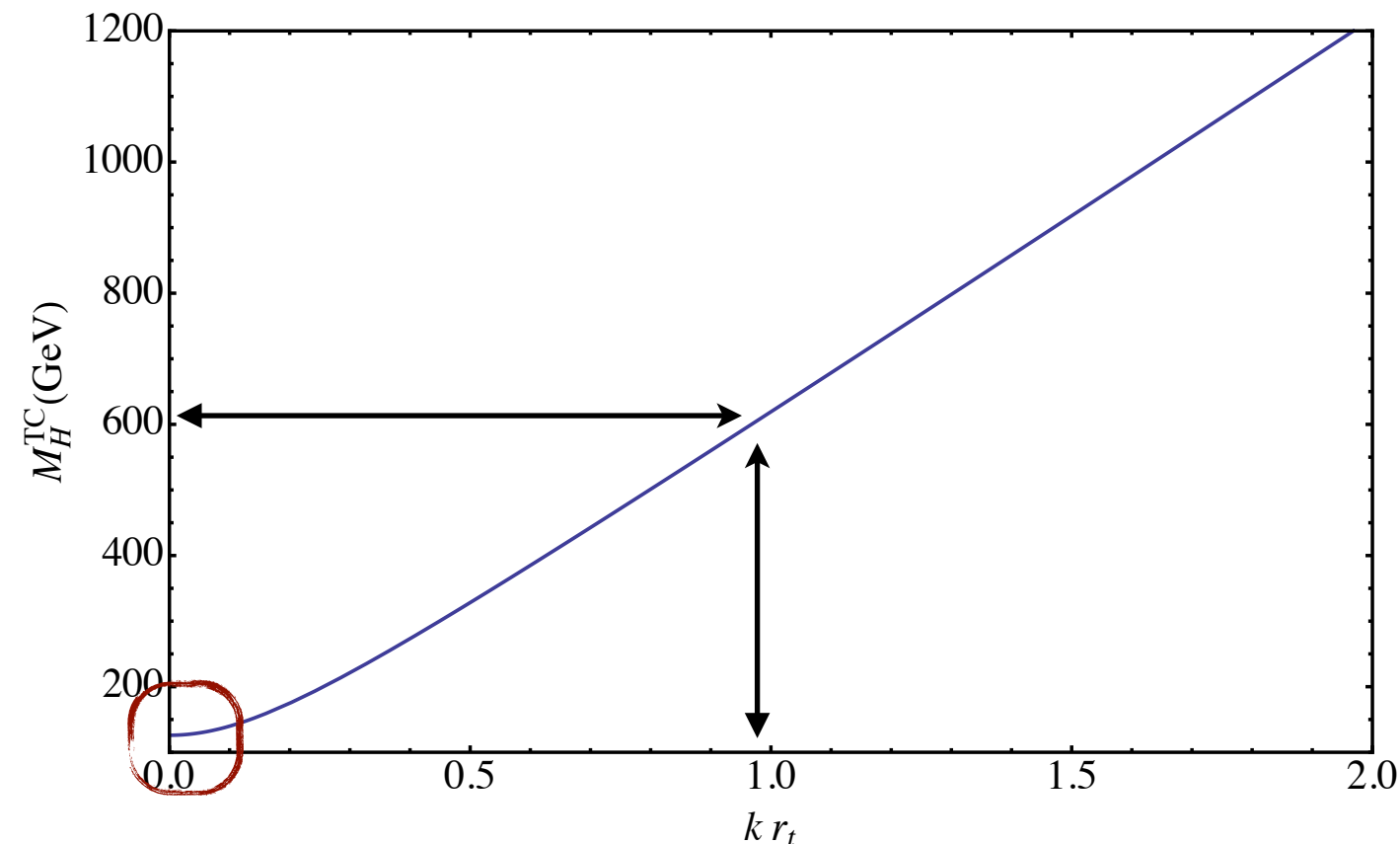
TC - Higgs is the lightest spin-0 scalar made of TC-fermions

$$H \sim c_1 \bar{Q}Q + c_2 \bar{Q}Q\bar{Q}Q + \dots$$

Top corrections



$$(M_H^{\text{TC}})^2 \simeq M_H^2 + 12 \kappa^2 r_t^2 m_t^2$$



Foadi, Frandsen, Sannino, 1211.1083 PRD
Cacciapaglia, Sannino 1402.0233 JHEP

TC Higgs can be heavy

Minimal Composite Dynamics

2 Dirac flavours in a given underlying rep.

Complex: $SU(2) \times SU(2) \times U(1) \rightarrow SU(2) \times U(1)$

QCD with 2 Dirac flavours

Pseudoreal: $SU(4) \rightarrow Sp(4)$

$SU(2)$ gauge with 2 fund. Dirac flavours

Real: $SU(4) \rightarrow SO(4)$

$SU(2)$ gauge with 2 adj. Dirac flavours