

# GRAVITATIONAL-WAVE SIGNALS FROM A SUPERCOOLED PHASE TRANSITION AND HOW TO COMPUTE THEM

---

*Bogumiła Świeżewska*

*University of Warsaw*

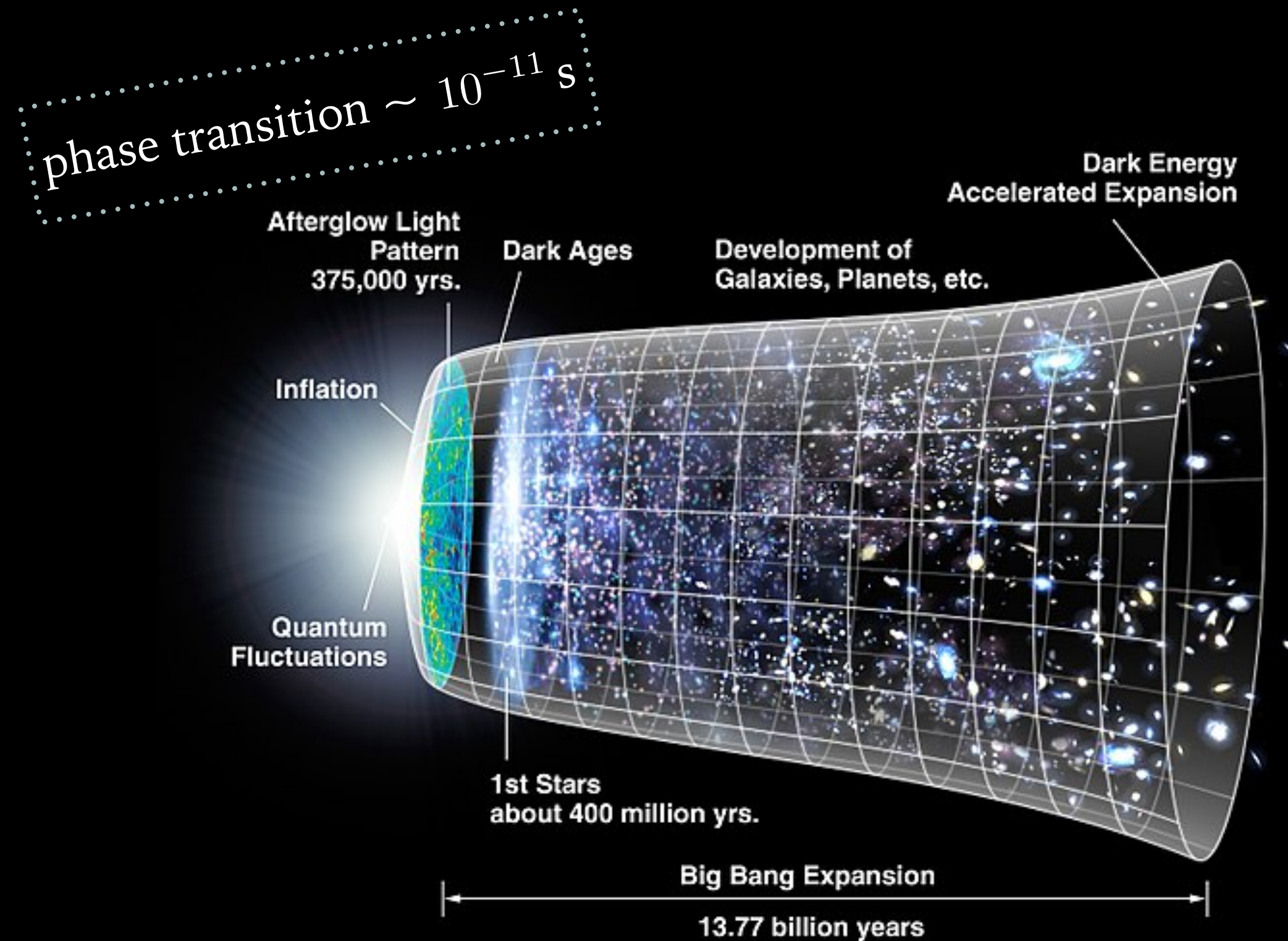
*in collaboration with  
Maciej Kierkla, Alexandros Karam,  
Jorinde van de Vis, Tuomas Tenkanen*

*based on  
JHEP 03 (2023) 007  
and work in progress*

---

*SCALARS 2023, Warsaw, 15.09.2023*

# PHASE TRANSITION IN THE VERY EARLY UNIVERSE

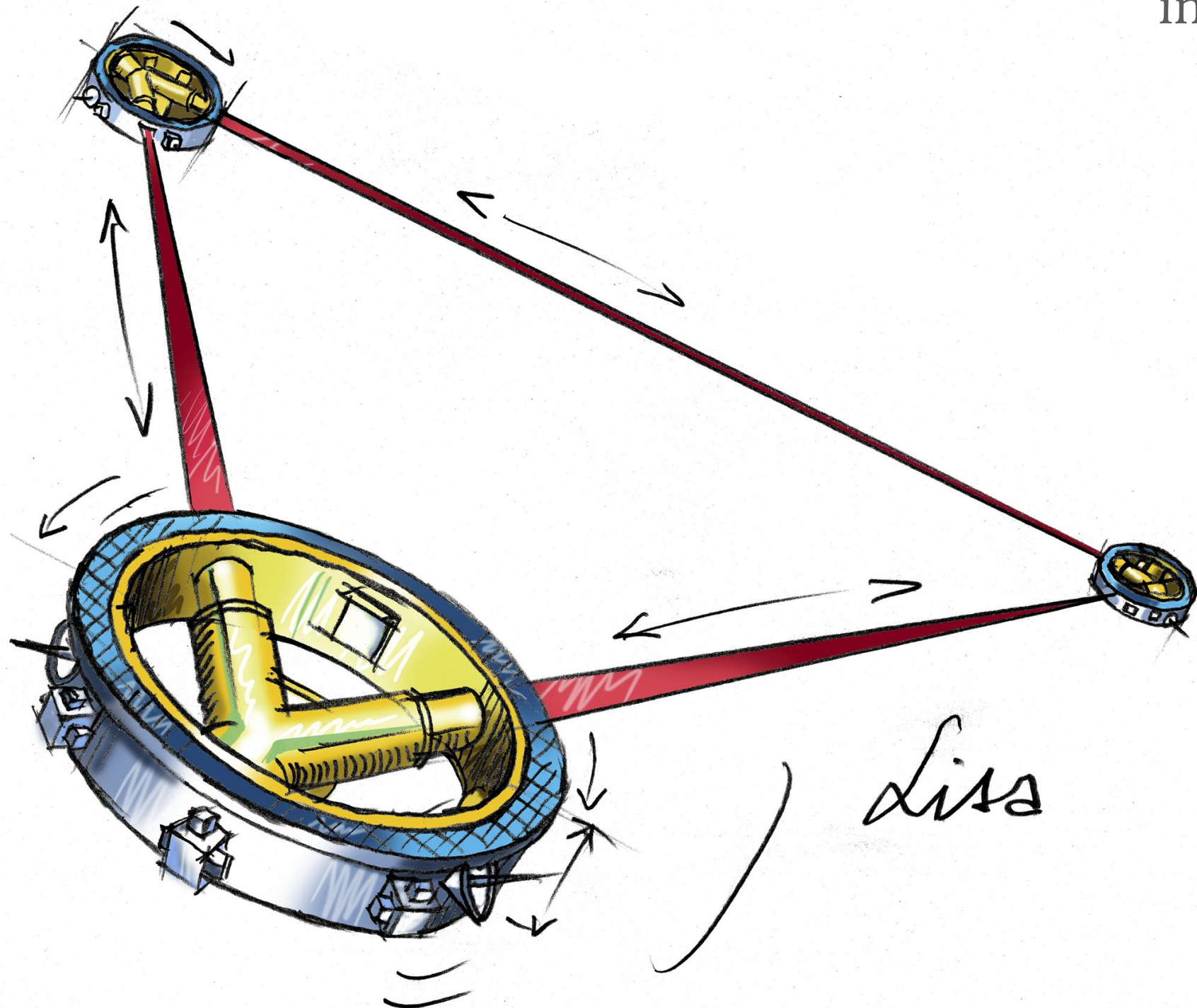


[Image Credit: NASA]

# LISA IS COMING!

---

in the 2030's



[Image credit: ESA-C. Vijoux]

---

Bogumiła Świeżewska

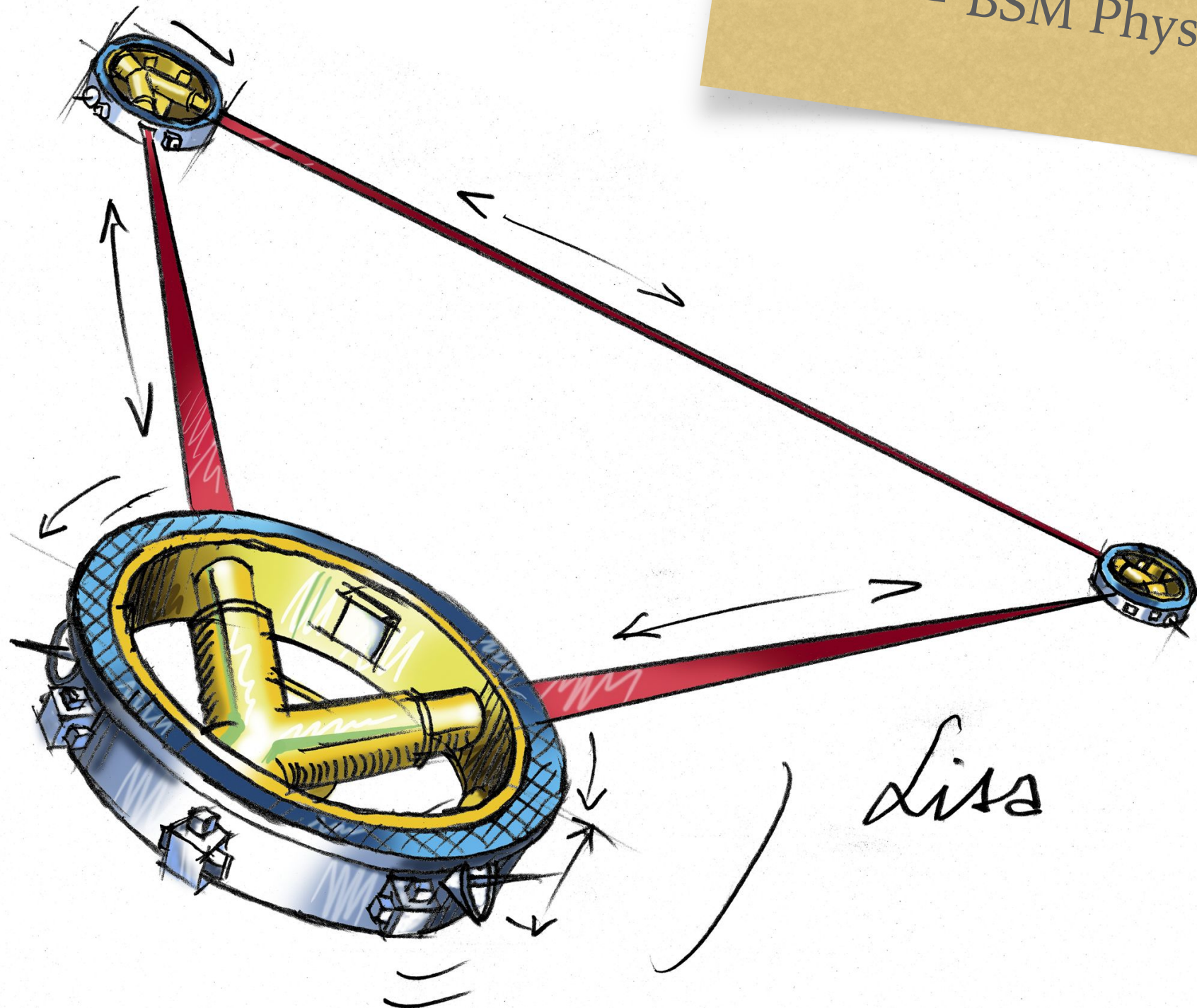
GW from supercooled PTs and how to compute them



# LISA IS COMING!

---

First-order phase transition  
= BSM Physics!



[Image credit: ESA-C. Vijoux]

---



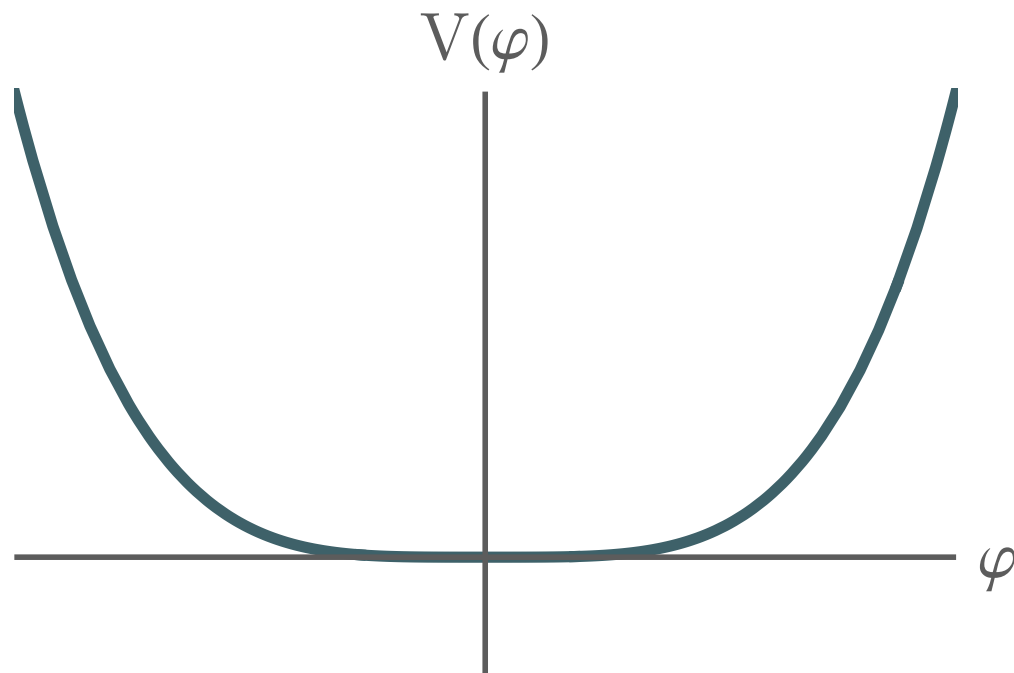
# CLASSICAL CONFORMAL SYMMETRY

---

# CLASSICAL CONFORMAL SYMMETRY

---

No dimensionful parameters at tree level



---

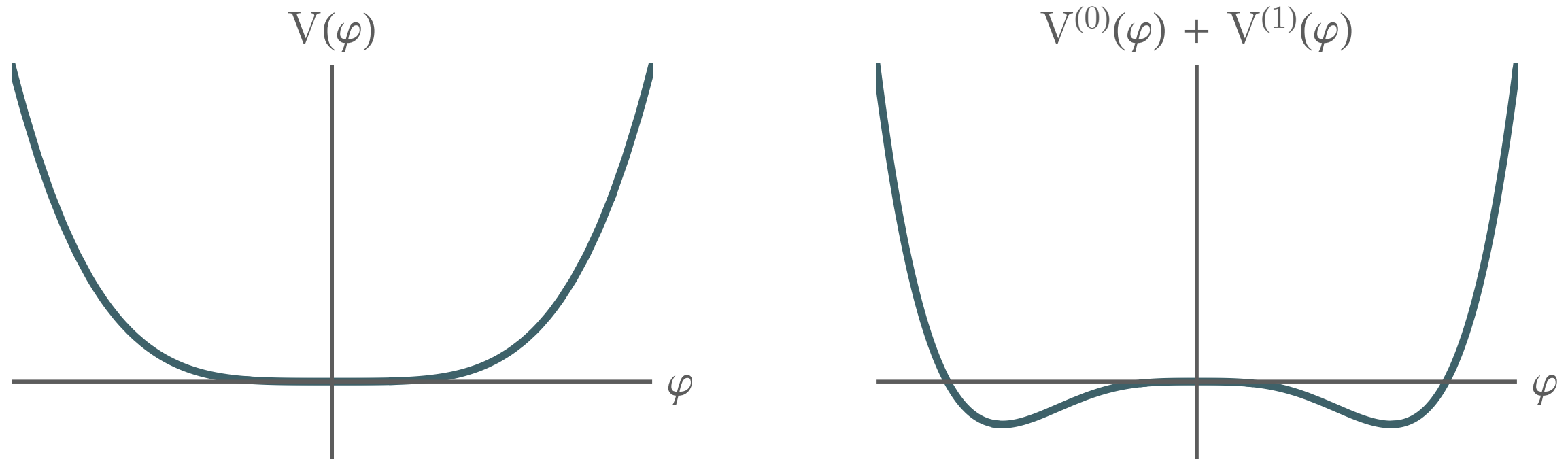
[S. R. Coleman, E. J. Weinberg, *Phys.Rev. D*7 (1973) 1888]



# CLASSICAL CONFORMAL SYMMETRY

---

No dimensionful parameters at tree level



Symmetry broken by loop corrections (dimensional transmutation)

[S. R. Coleman, E. J. Weinberg, *Phys.Rev. D*7 (1973) 1888]

# WHY CLASSICAL CONFORMAL SYMMETRY?

---

dynamical  
generation of all  
mass scales

predictivity -  
few free  
parameters

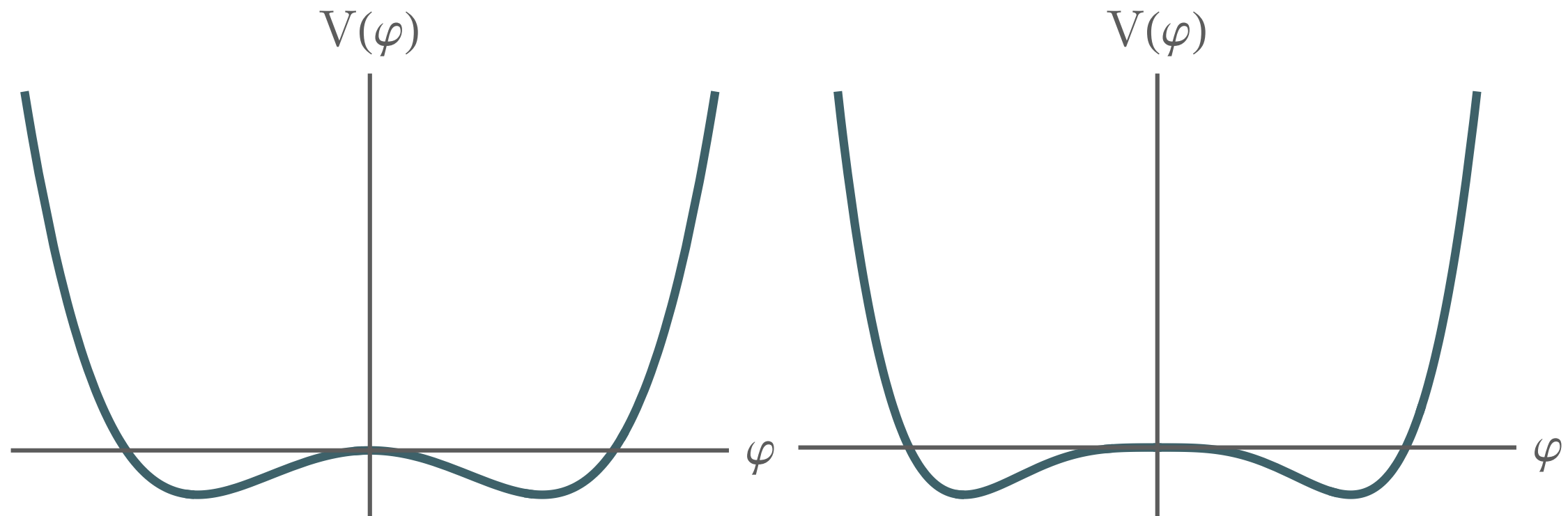
generically strong  
GW signal testable  
with LISA

+ DM candidate



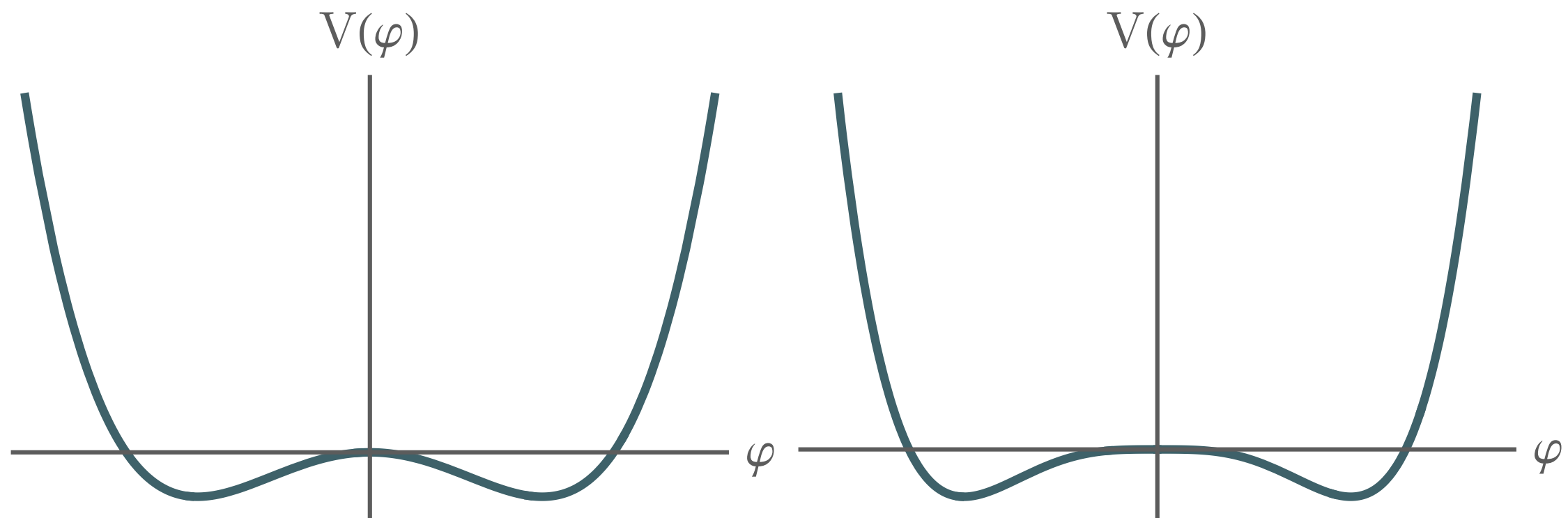
# CONFORMAL VS “NORMAL” POTENTIAL

---



# CONFORMAL VS “NORMAL” POTENTIAL

---

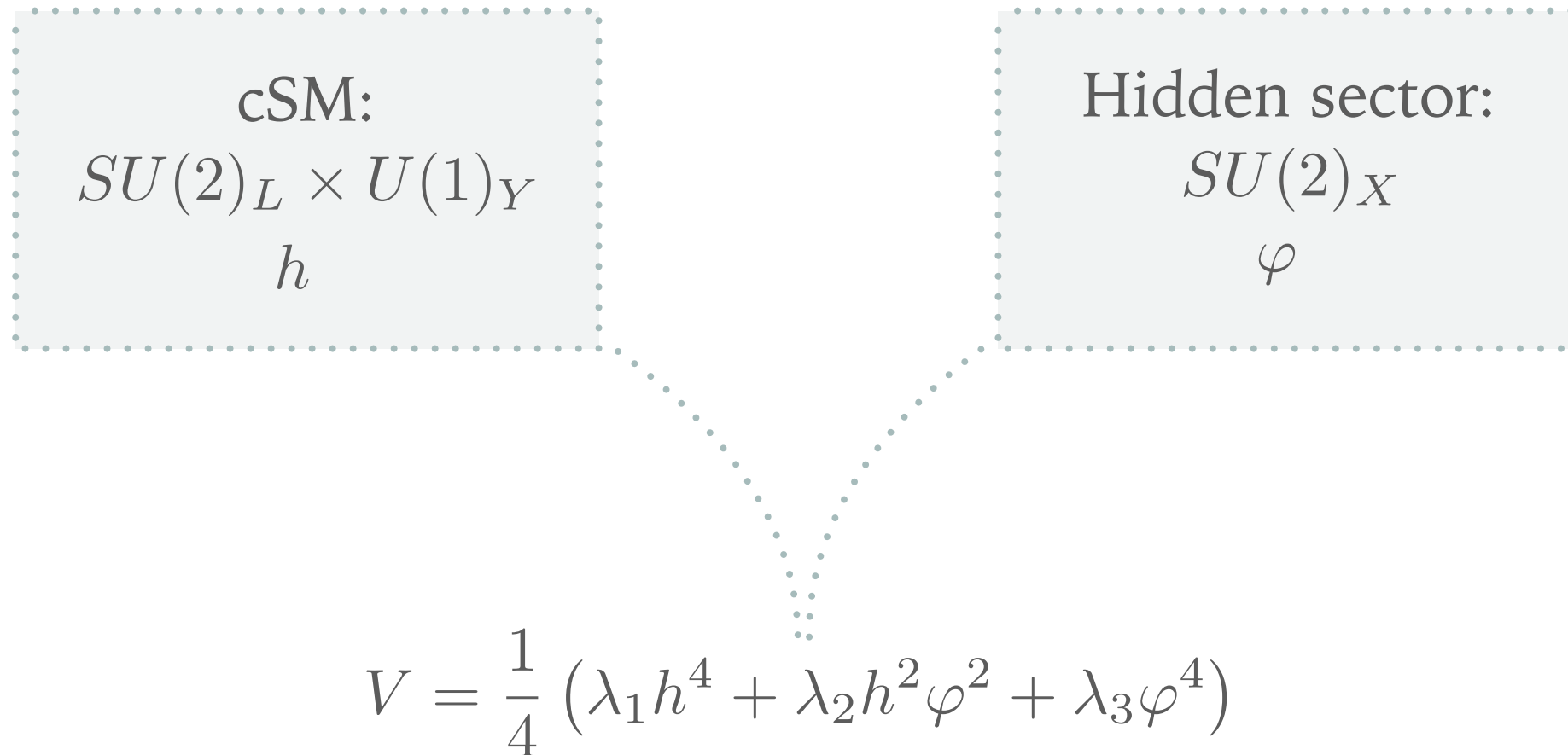


The thermal barrier can last until low temperatures  
↓  
Potential for supercooling and strong transition



# THE MODEL: SU(2)CSM

.....



[See also: T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, T.Prokopec, J.Rezacek, BS, JCAP02(2019)009, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

.....

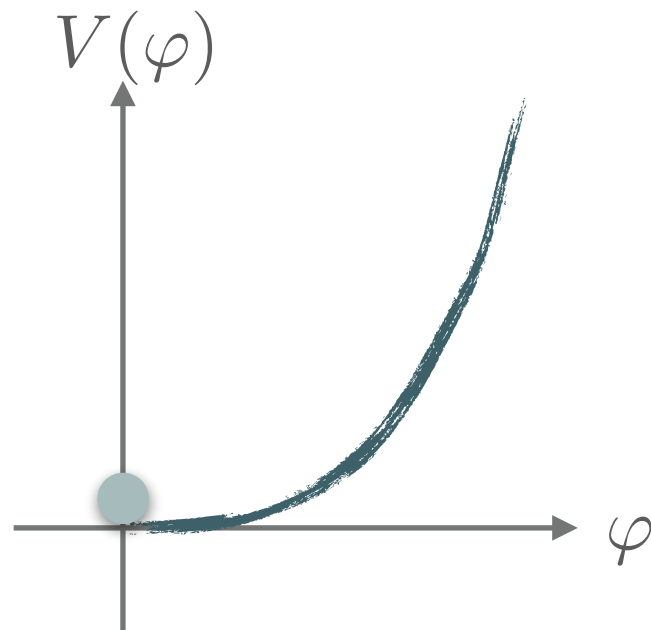
# SUPERCOOLED PHASE TRANSITION IN THE EARLY UNIVERSE

---



# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$

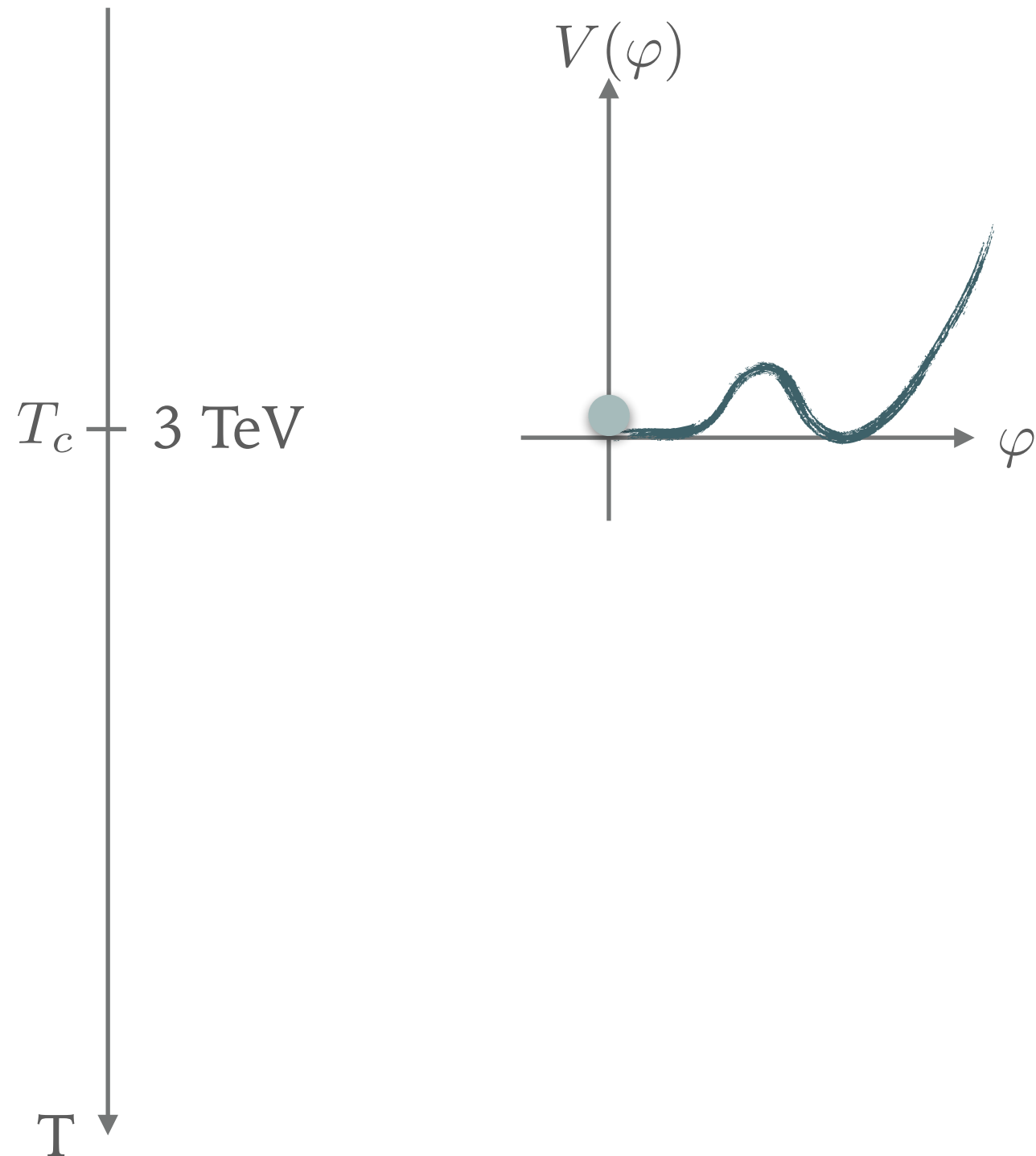


high temperature:  
EW and conformal  
symmetry restored

T

# TEMPERATURE EVOLUTION

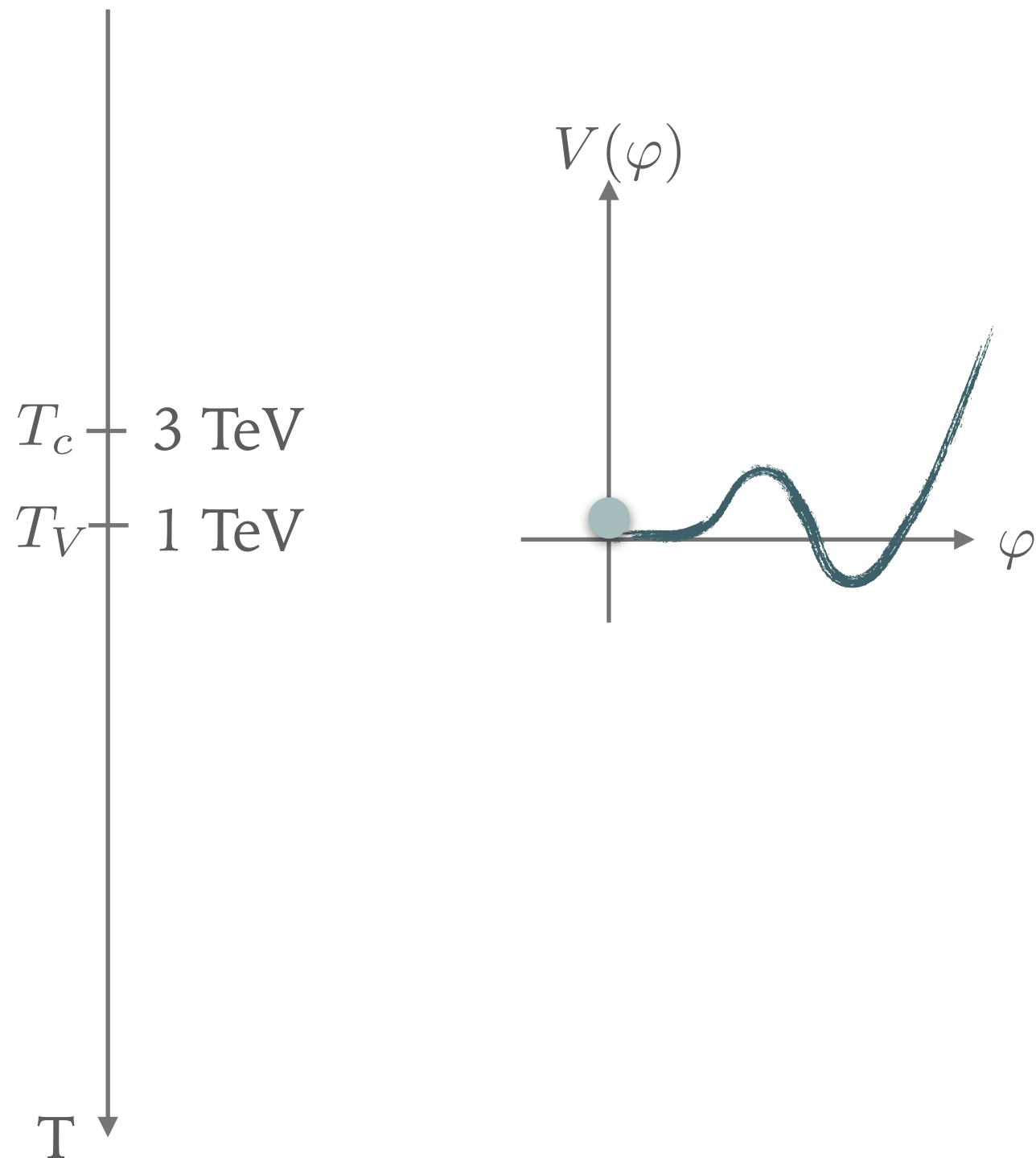
$$M_X = 9 \text{ TeV}, g_X = 0.9$$



critical temperature:  
two degenerate  
minima

# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$

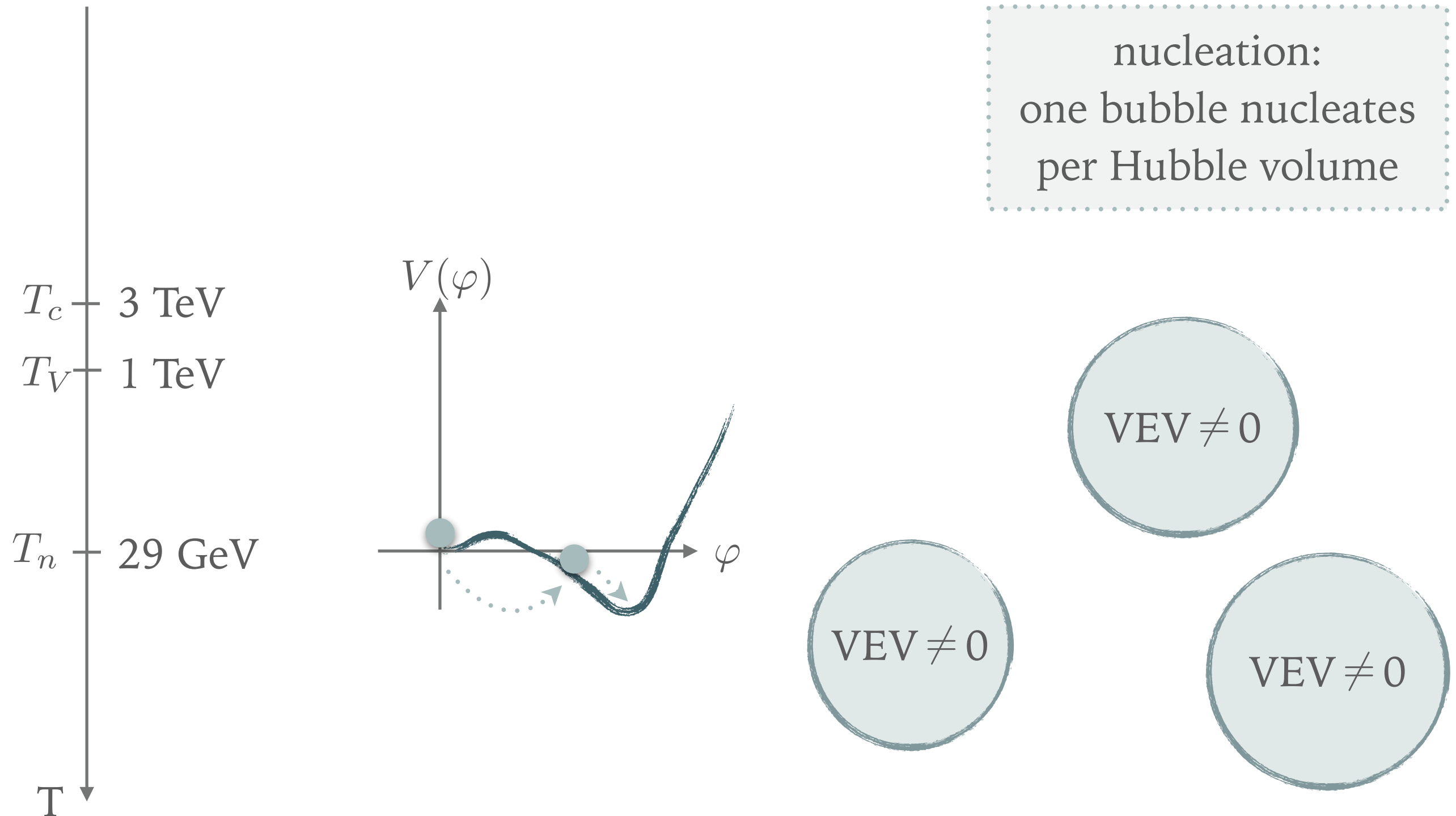


vacuum domination  
begins



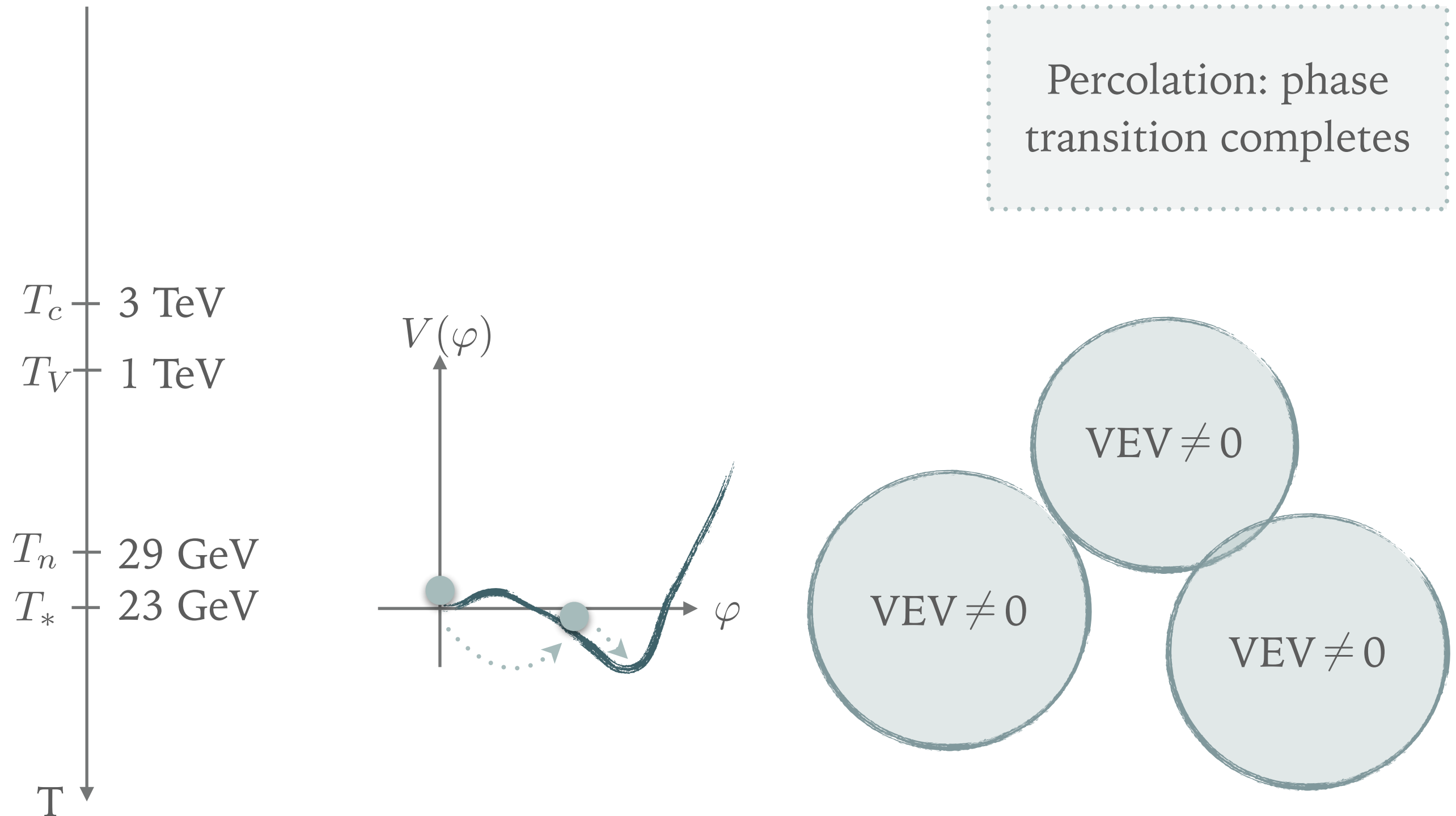
# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$



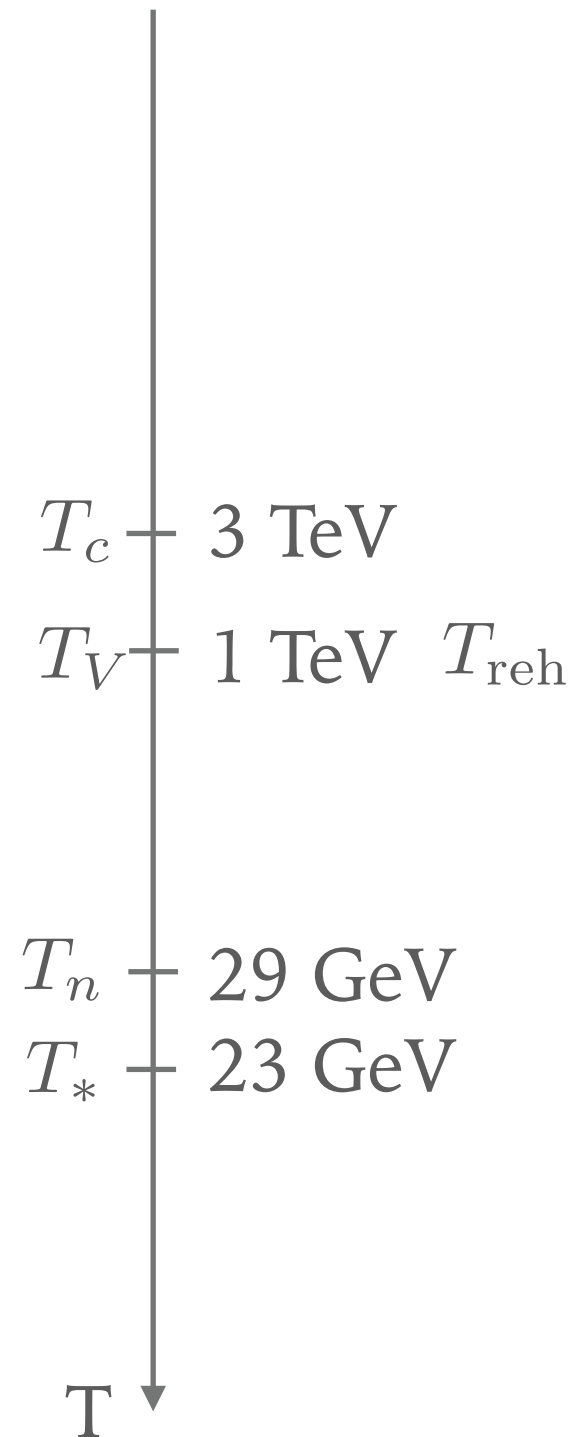
# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$



# TEMPERATURE EVOLUTION

$$M_X = 9 \text{ TeV}, g_X = 0.9$$



reheating: vacuum  
energy  $\rightarrow$  radiation

$$\alpha = \frac{\Delta V}{\text{energy of radiation}} \approx 4 \cdot 10^6$$

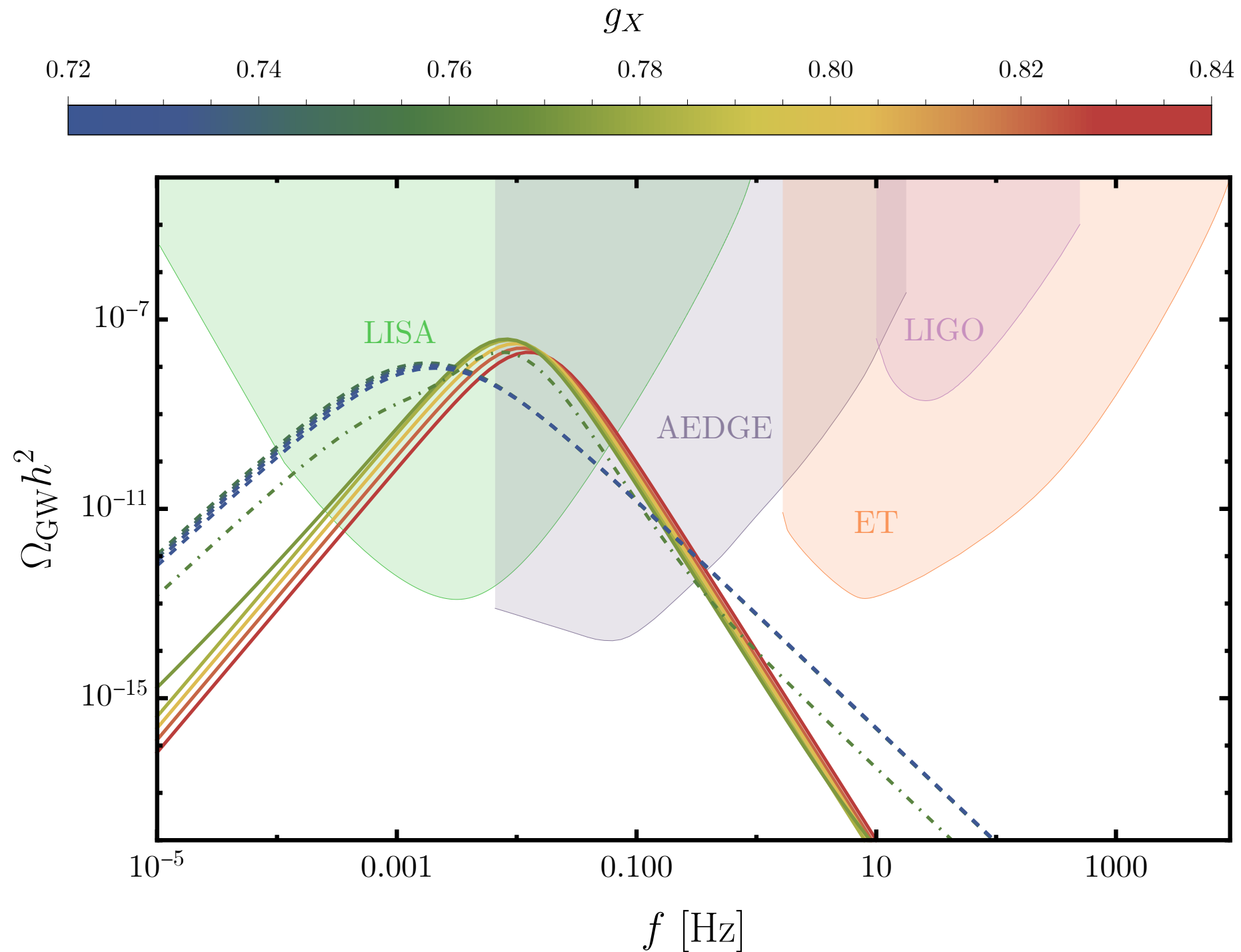
# GRAVITATIONAL WAVES IN $SU(2)$ CSM

---



# GRAVITATIONAL WAVE SPECTRA

---



$$M_X = 10^5 \text{ GeV}$$

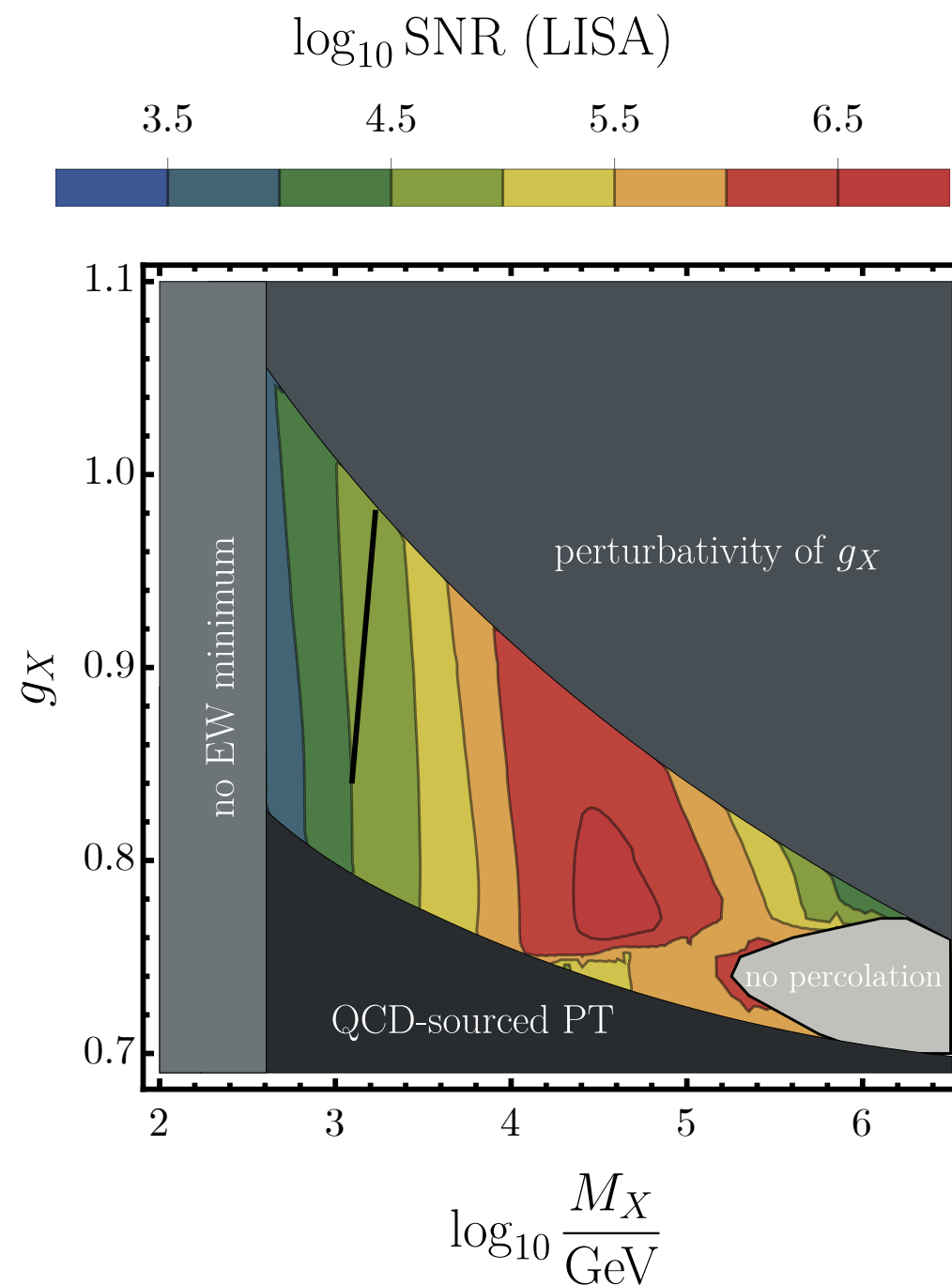
Bogumiła Świeżewska

[M.Kierkla, A.Karam, BS, JHEP 03 (2023) 007]

GW from supercooled PTs and how to compute them

# SIGNAL-TO-NOISE RATIO

---



[M.Kierkla, A.Karam, BS, JHEP 03 (2023) 007]

# TAKE-HOME MESSAGE

---

First-order phase transition in  $SU(2)_c$ SM  
falsifiable through GW!

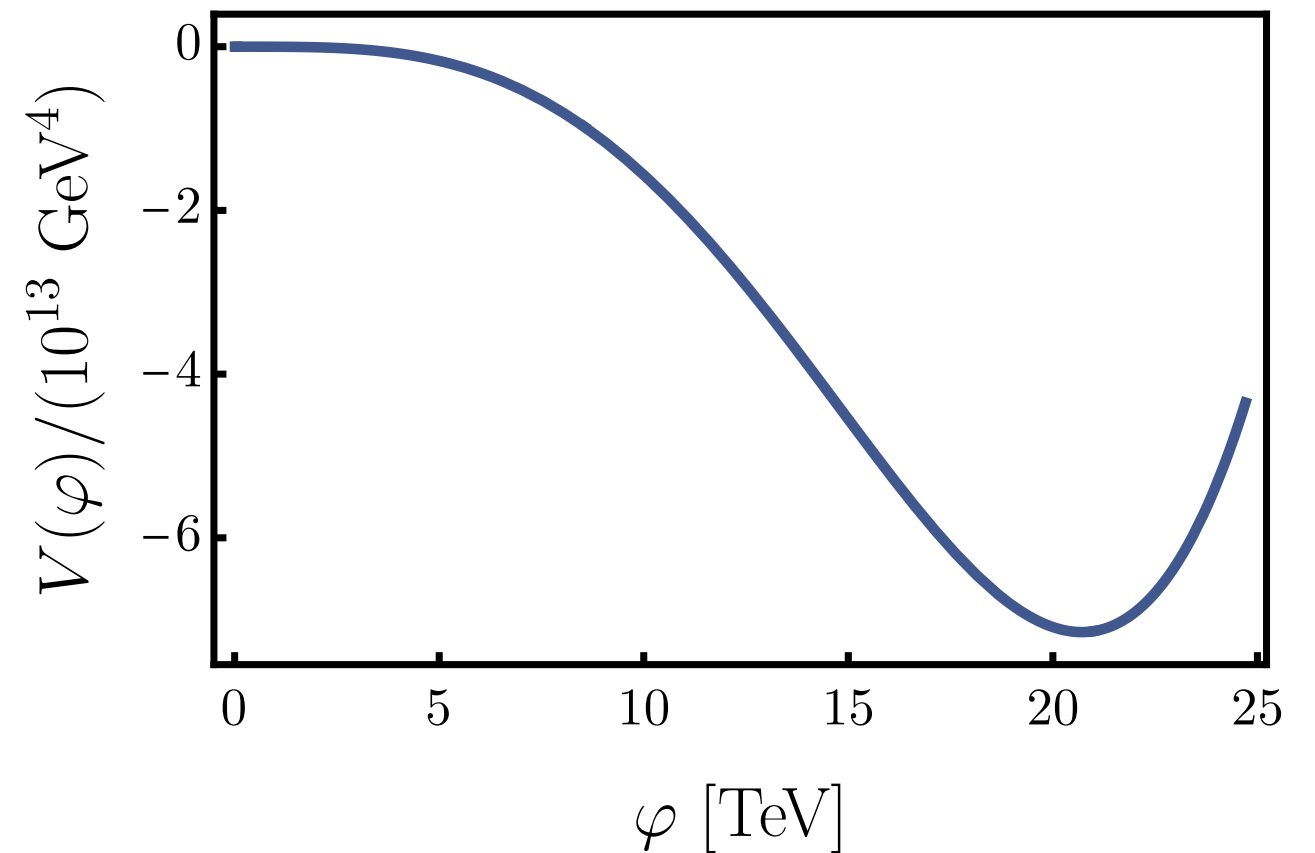
# ... AND HOW TO COMPUTE THEM

---



# DIFFERENT SCALES INVOLVED

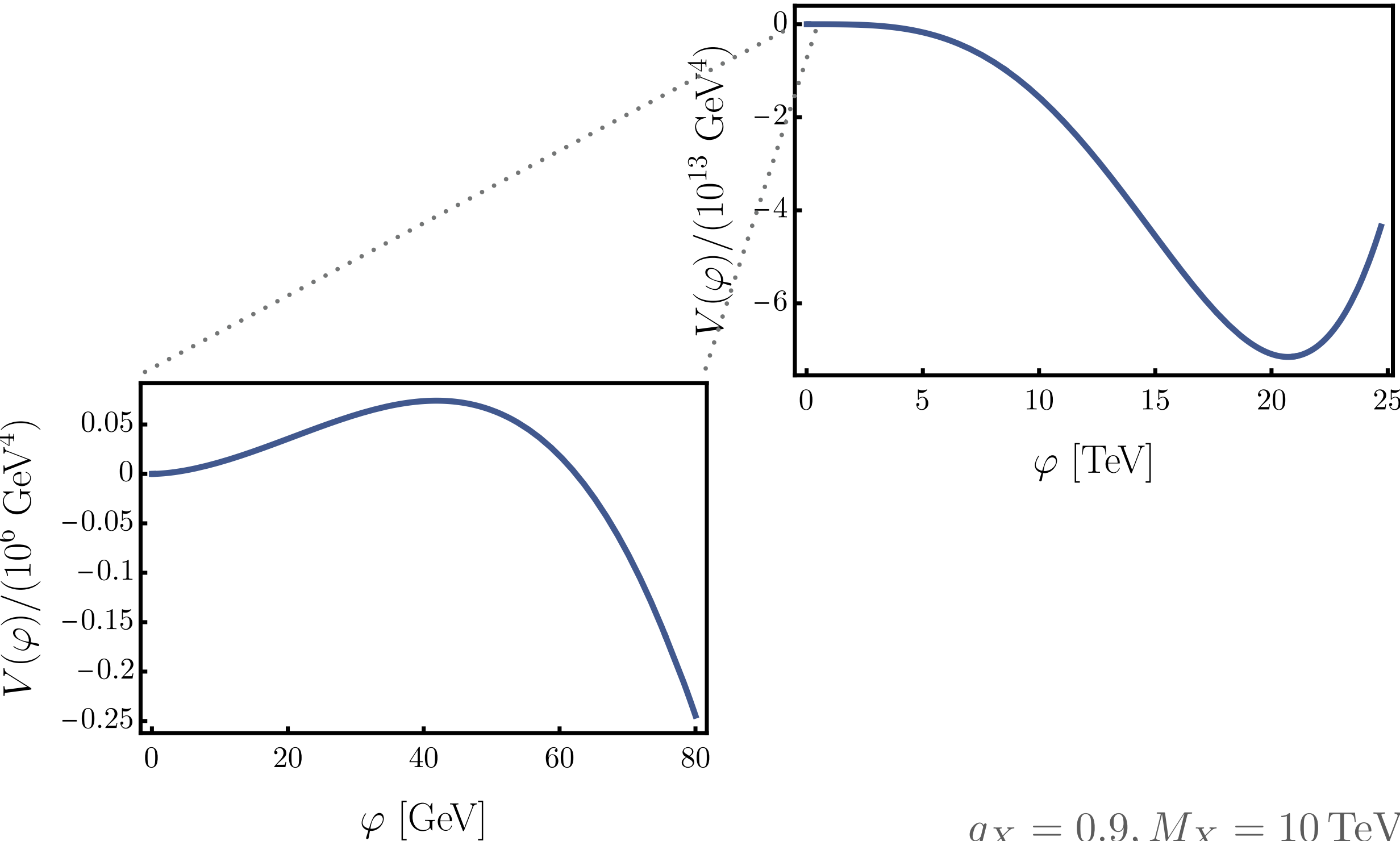
---



---

$$g_X = 0.9, M_X = 10 \text{ TeV}$$

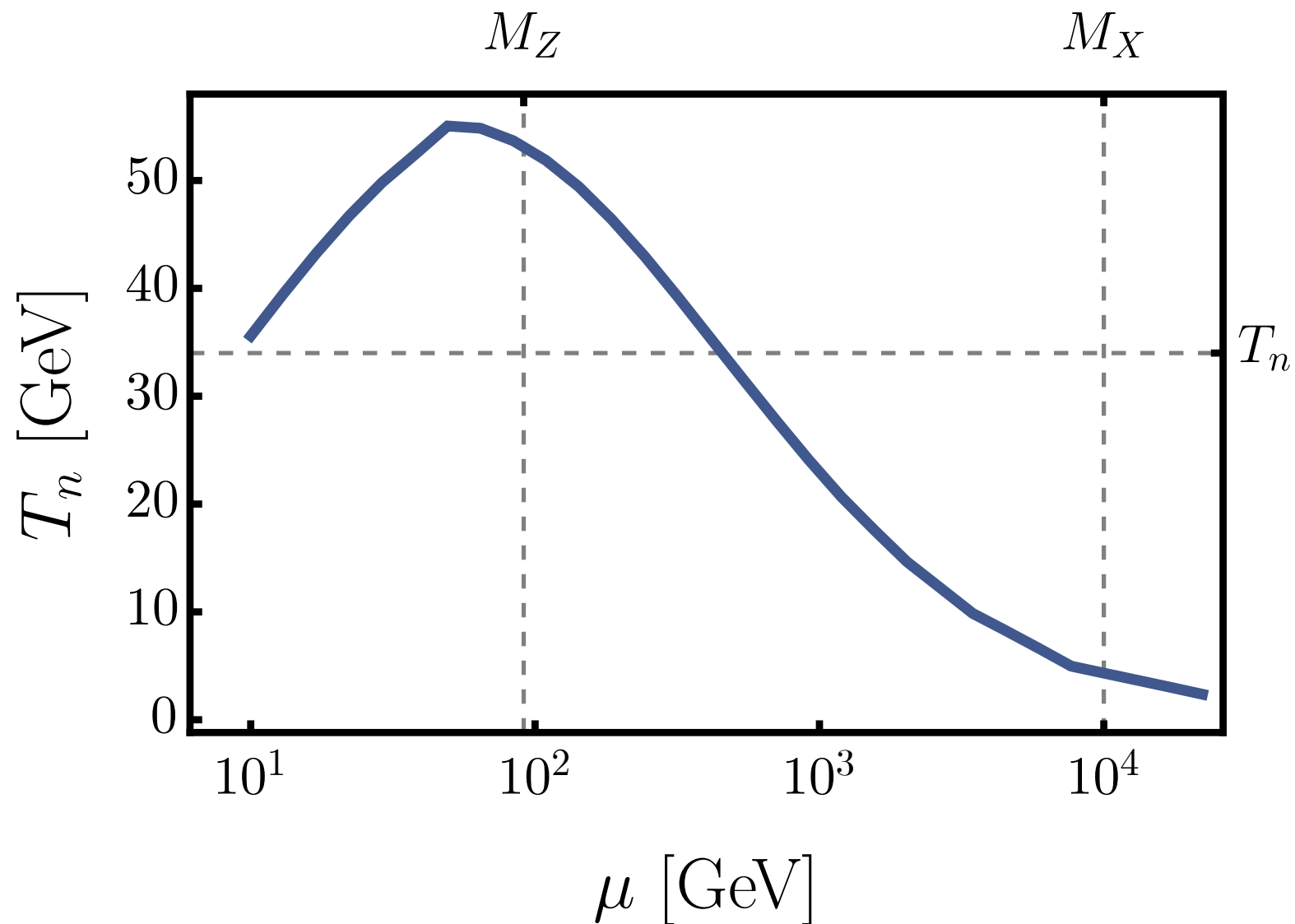
# DIFFERENT SCALES INVOLVED



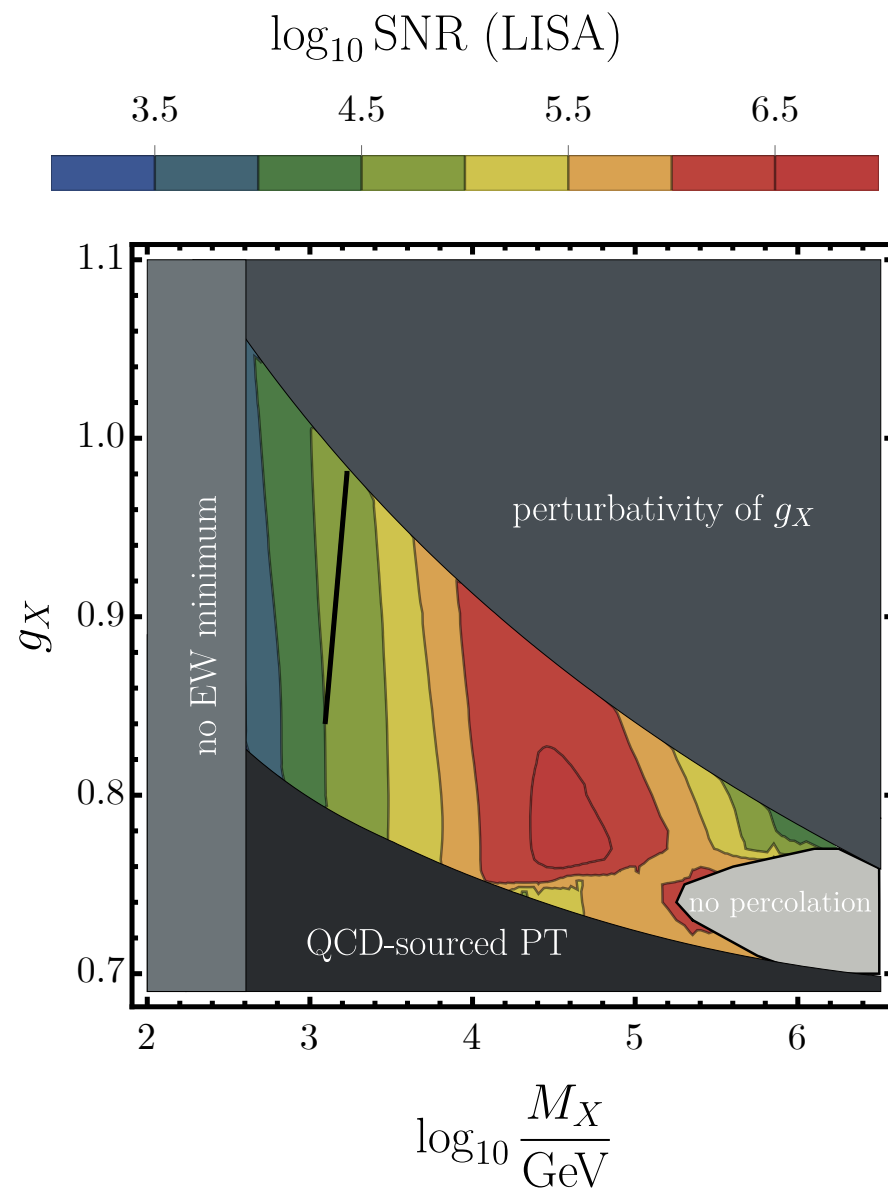
$$g_X = 0.9, M_X = 10 \text{ TeV}$$

# SCALE DEPENDENCE OF NUCLEATION

---

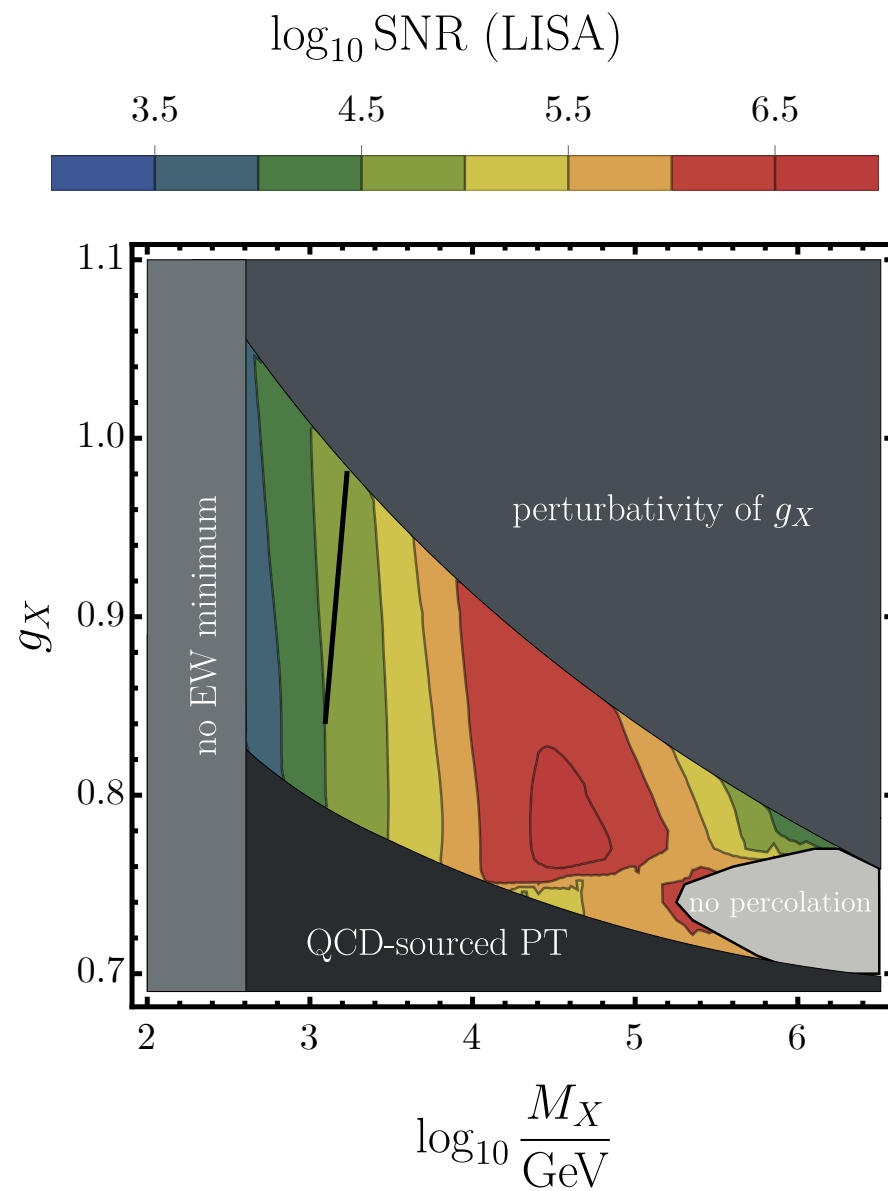


# SCALE DEPENDENCE OF SNR



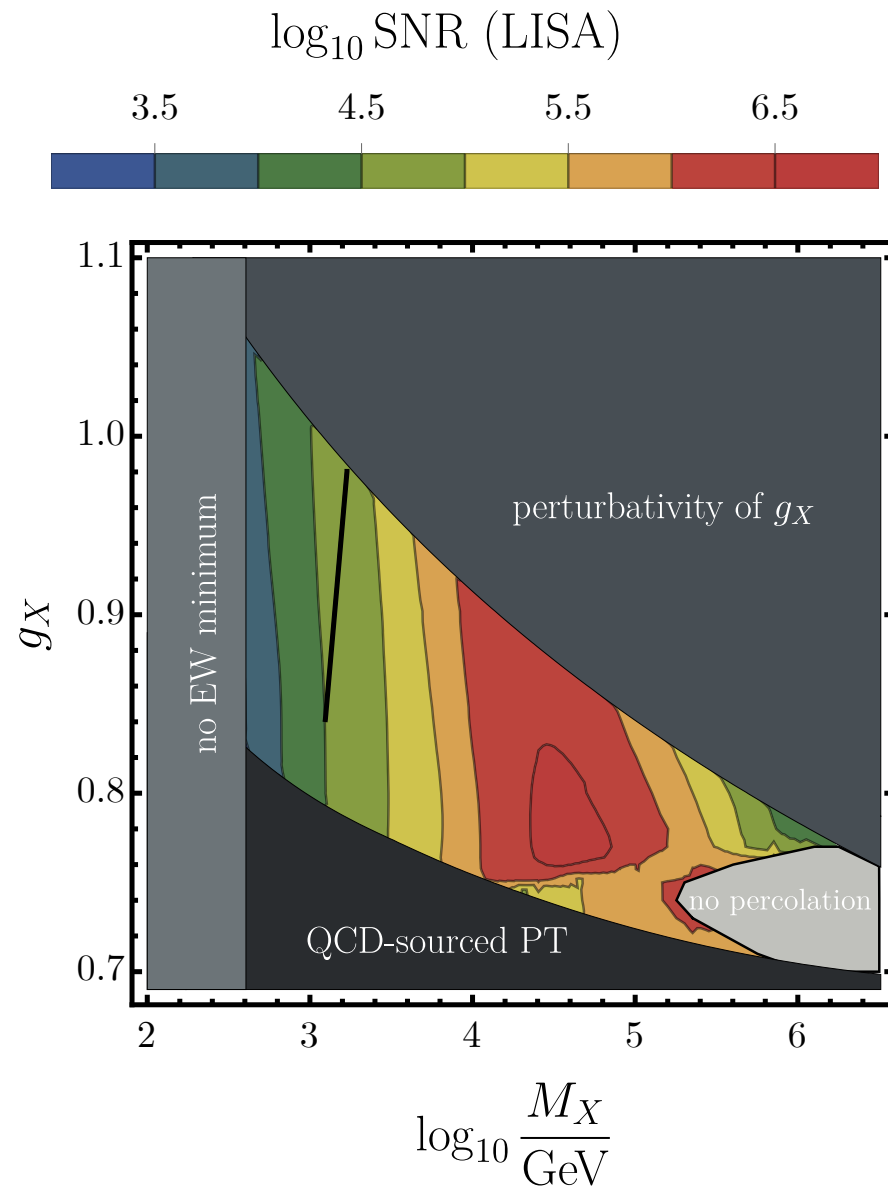


# SCALE DEPENDENCE OF SNR

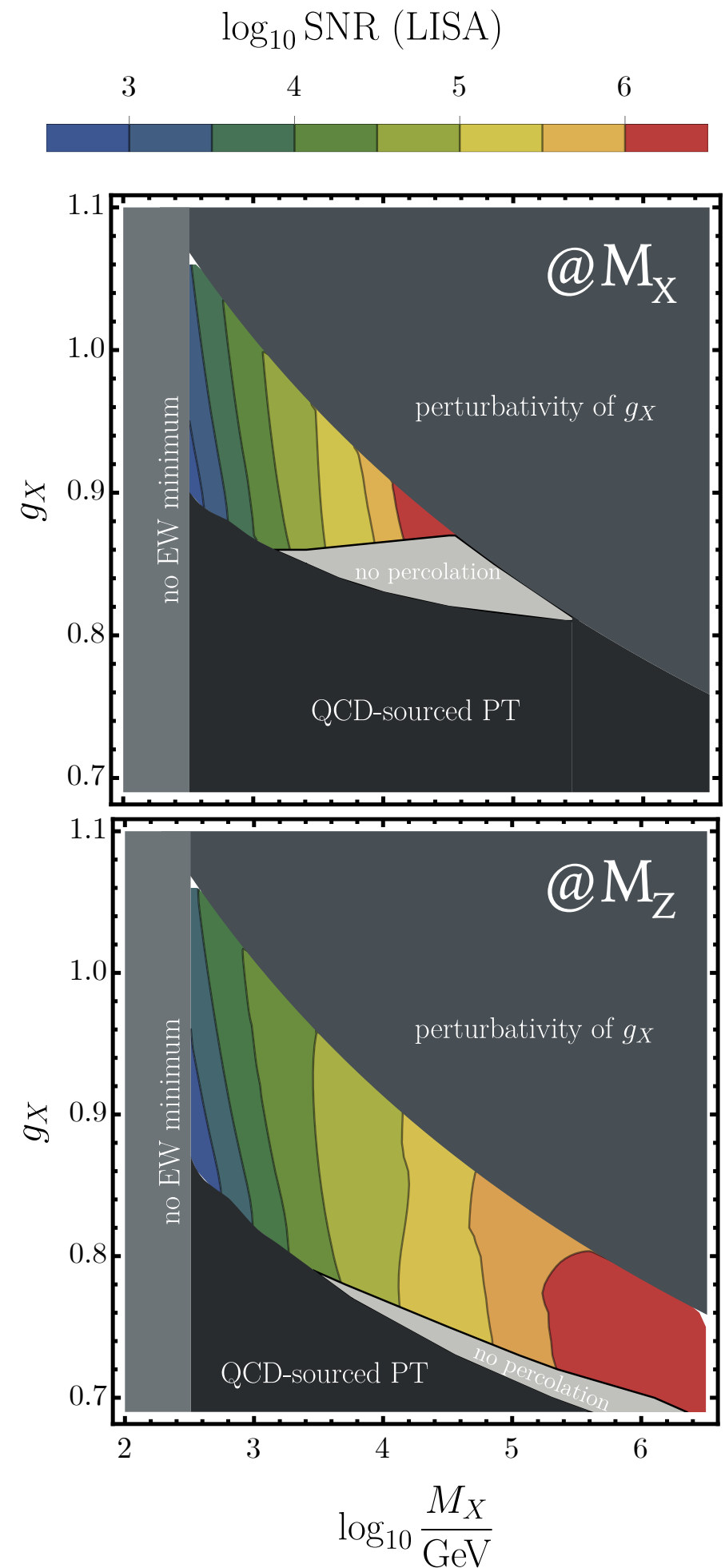


- RG-improvement
- Careful expansion in  $g_X$

# SCALE DEPENDENCE OF SNR

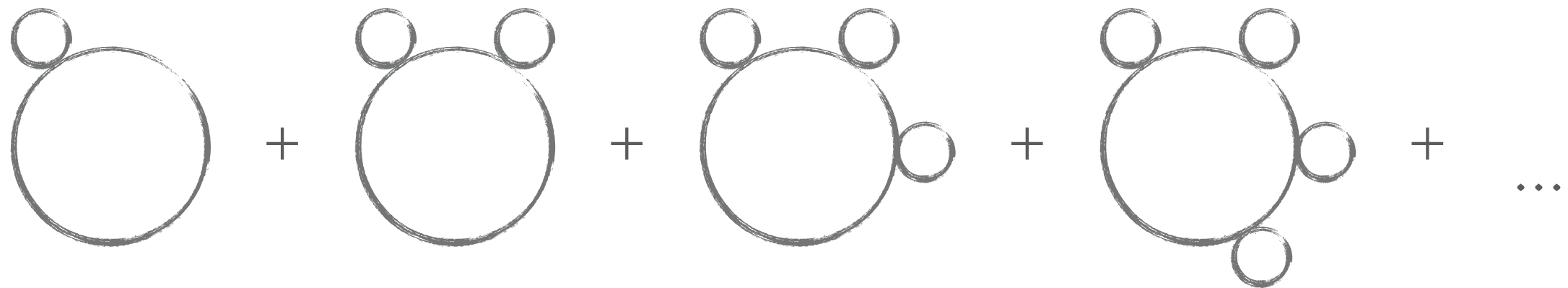


- RG-improvement
- Careful expansion in  $g_X$



# DIMENSIONAL REDUCTION (DR)

---



Systematic way of organizing  
resummations

Dimensional reduction:  
effective field theory in the presence  
of temperature-related energy scales

# DIMENSIONAL REDUCTION FOR SUPERCOOLED TRANSITIONS

---



DRalgo can do DR for us



DR requires high-  
temperature expansion

---

[A. Ekstedt, P. Schicho, T. V.I. Tenkanen, *Comput.Phys.Commun.* 288 (2023) 108725]

# DIMENSIONAL REDUCTION FOR SUPERCOOLED TRANSITIONS

---



DRalgo can do DR for us



DR requires high-  
temperature expansion

**STAY TUNED**

---

[A. Ekstedt, P. Schicho, T. V.I. Tenkanen, *Comput.Phys.Commun.* 288 (2023) 108725]



# SUMMARY



# SUMMARY

---

LISA will be able to  
probe models of  
fundamental  
interactions

Theoretical  
uncertainties are still  
sizable: improvements  
needed before LISA

THANK YOU FOR YOUR ATTENTION

---



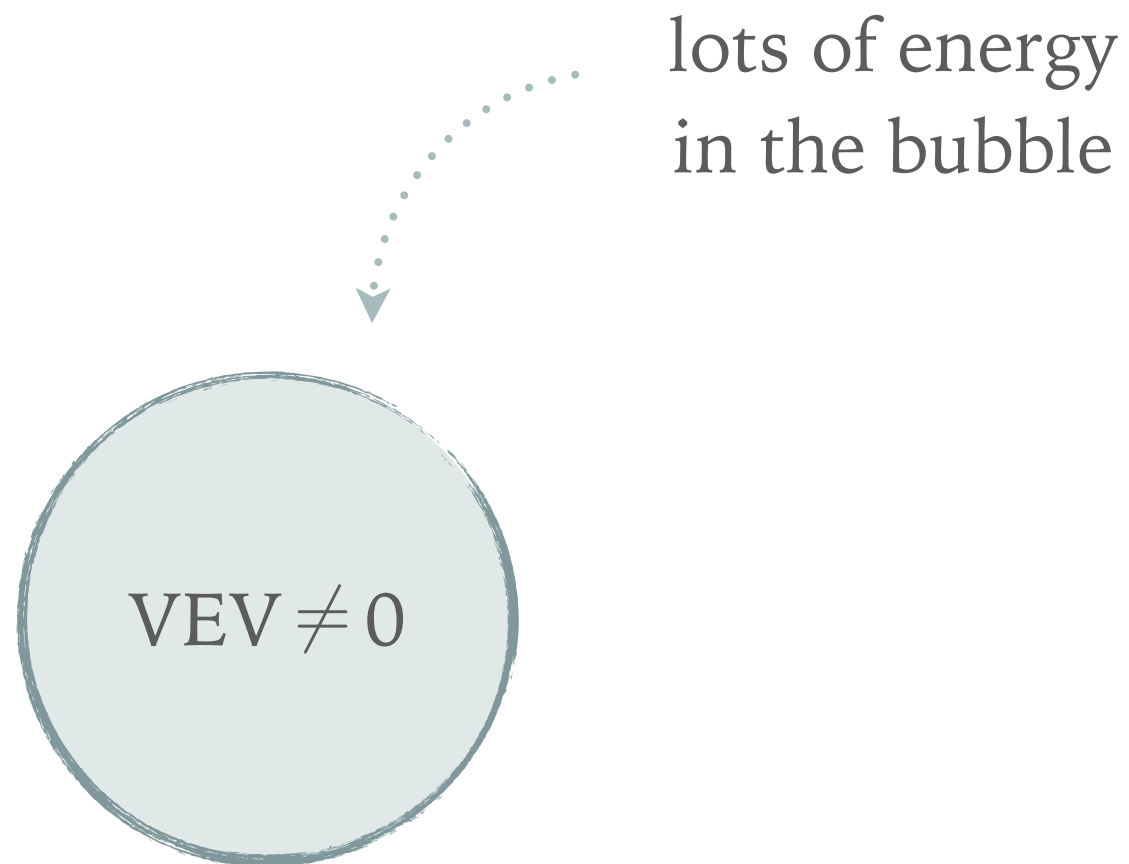
NATIONAL SCIENCE CENTRE  
POLAND

# GRAVITATIONAL-WAVE GENERATION DURING PT

---

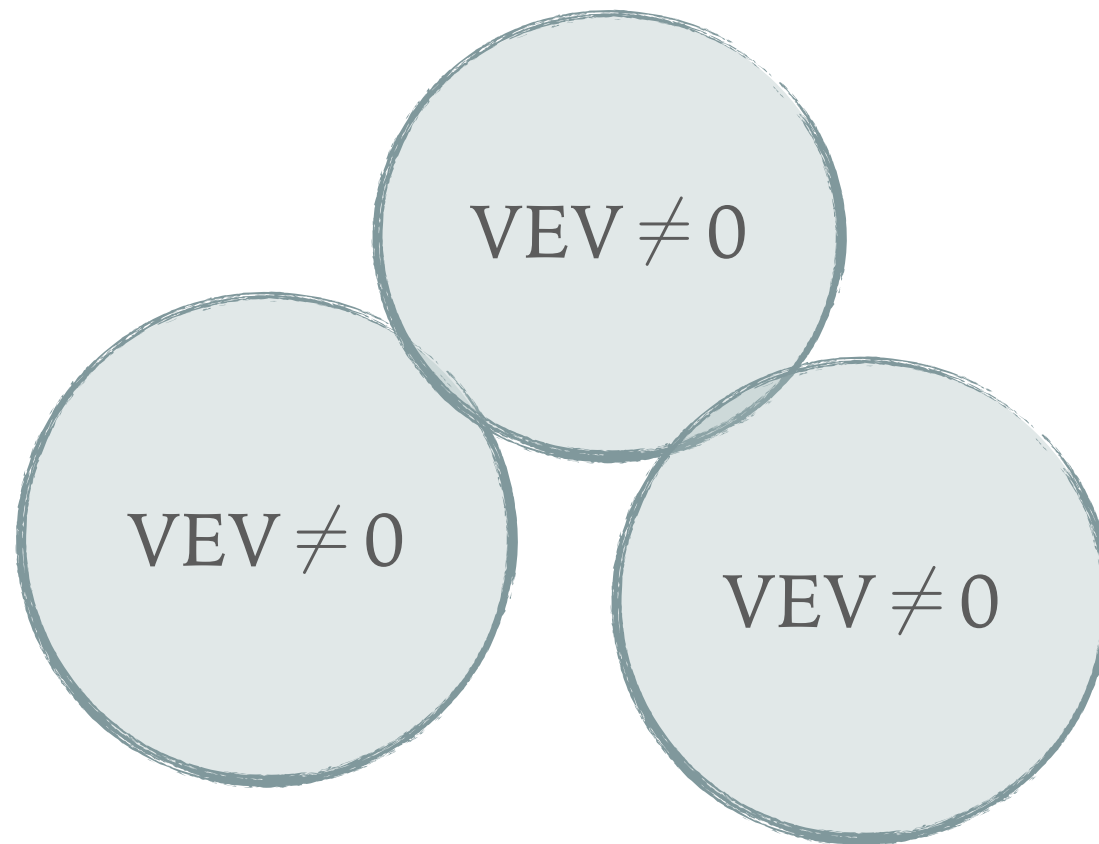
# SOURCES OF GRAVITATIONAL WAVES

---



# SOURCES OF GRAVITATIONAL WAVES

---

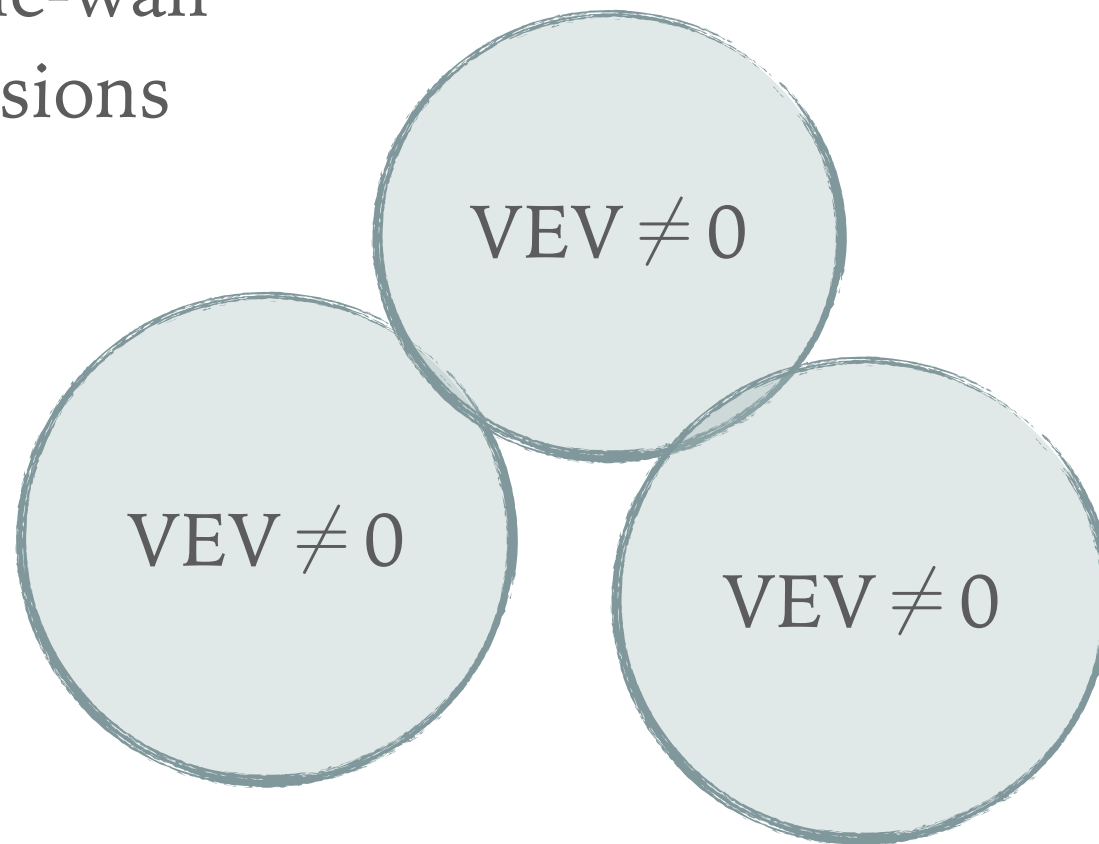




# SOURCES OF GRAVITATIONAL WAVES

---

bubble-wall  
collisions

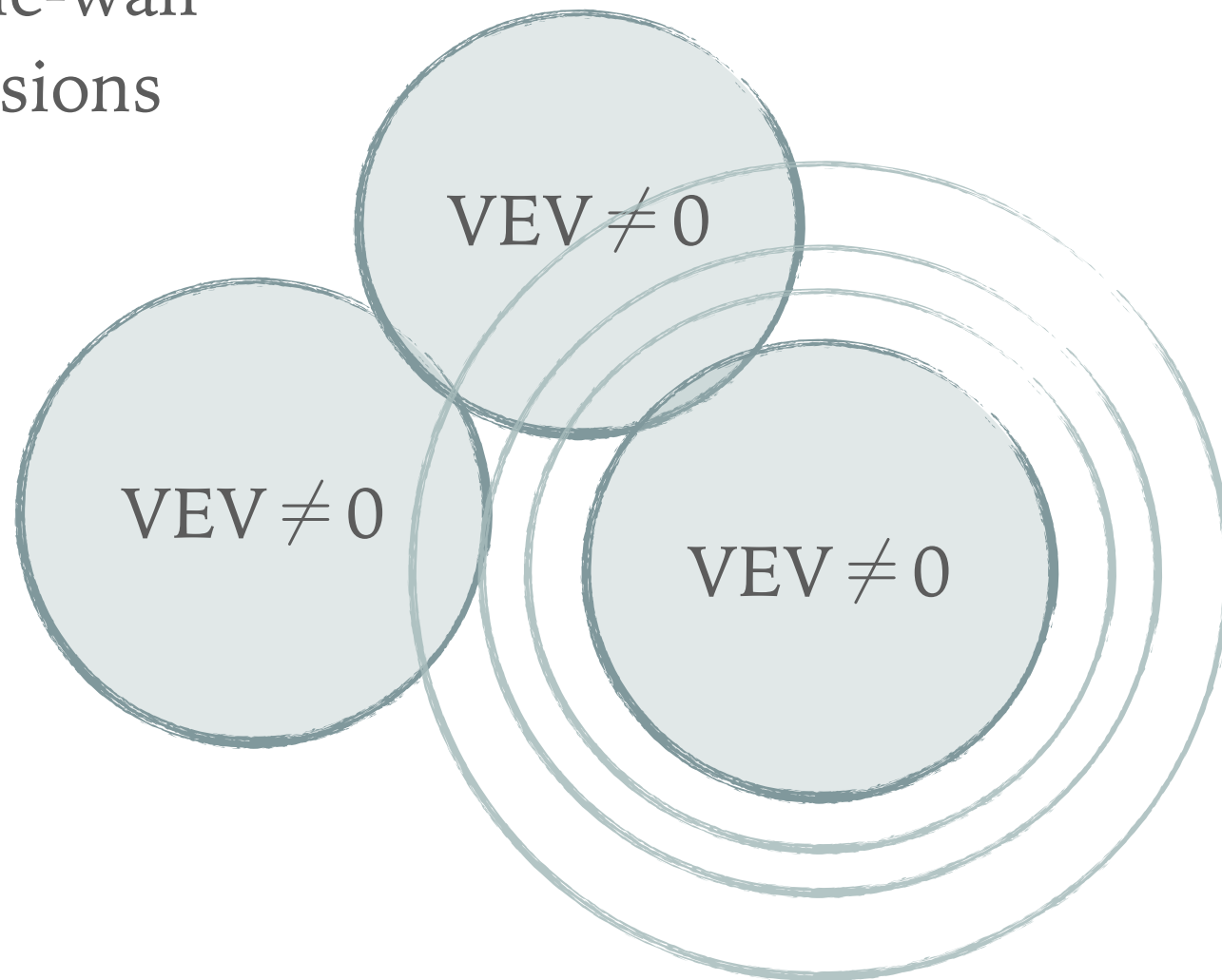


# SOURCES OF GRAVITATIONAL WAVES

---

bubble-wall  
collisions

sound waves  
in the plasma

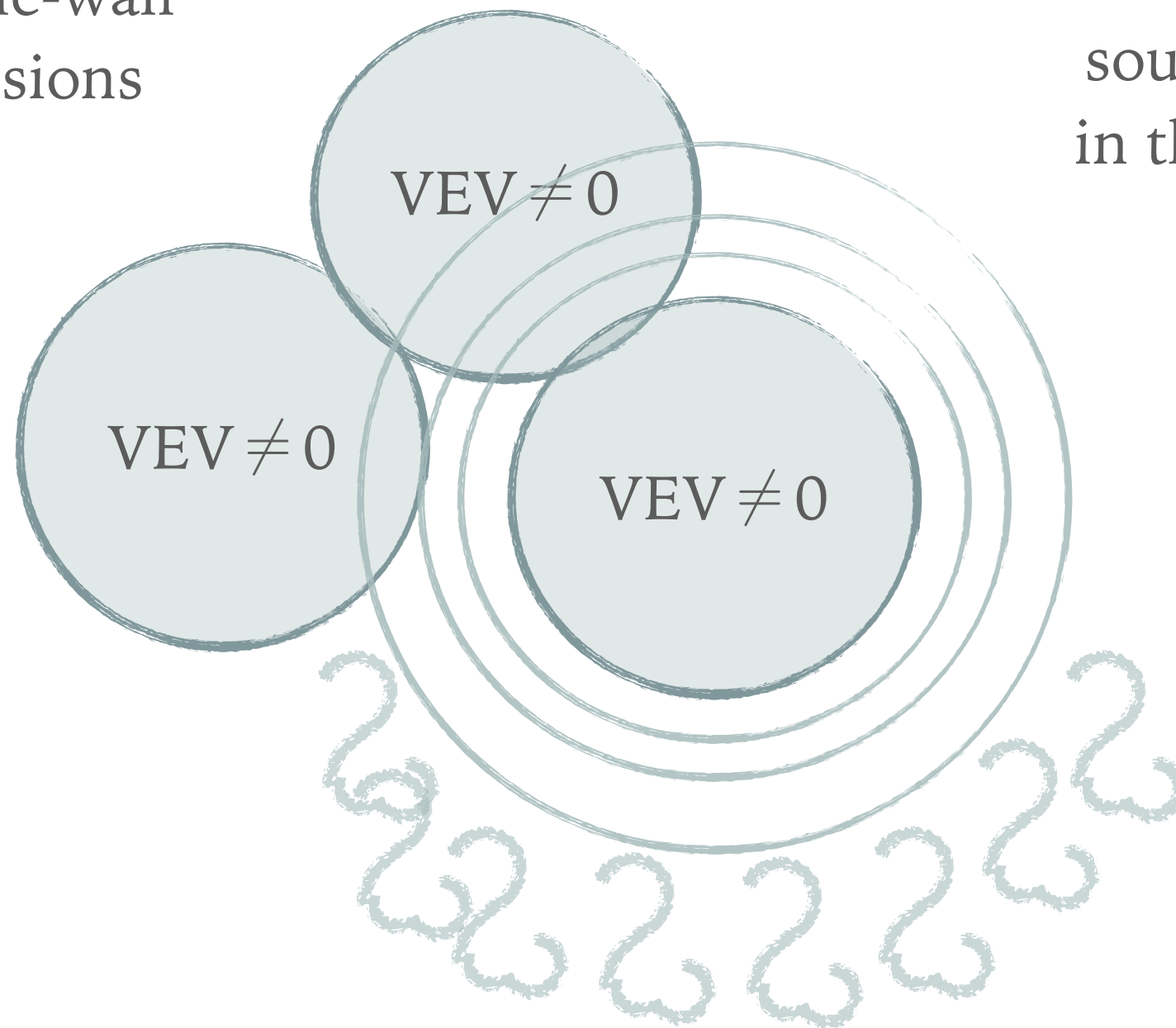


# SOURCES OF GRAVITATIONAL WAVES

---

bubble-wall  
collisions

sound waves  
in the plasma



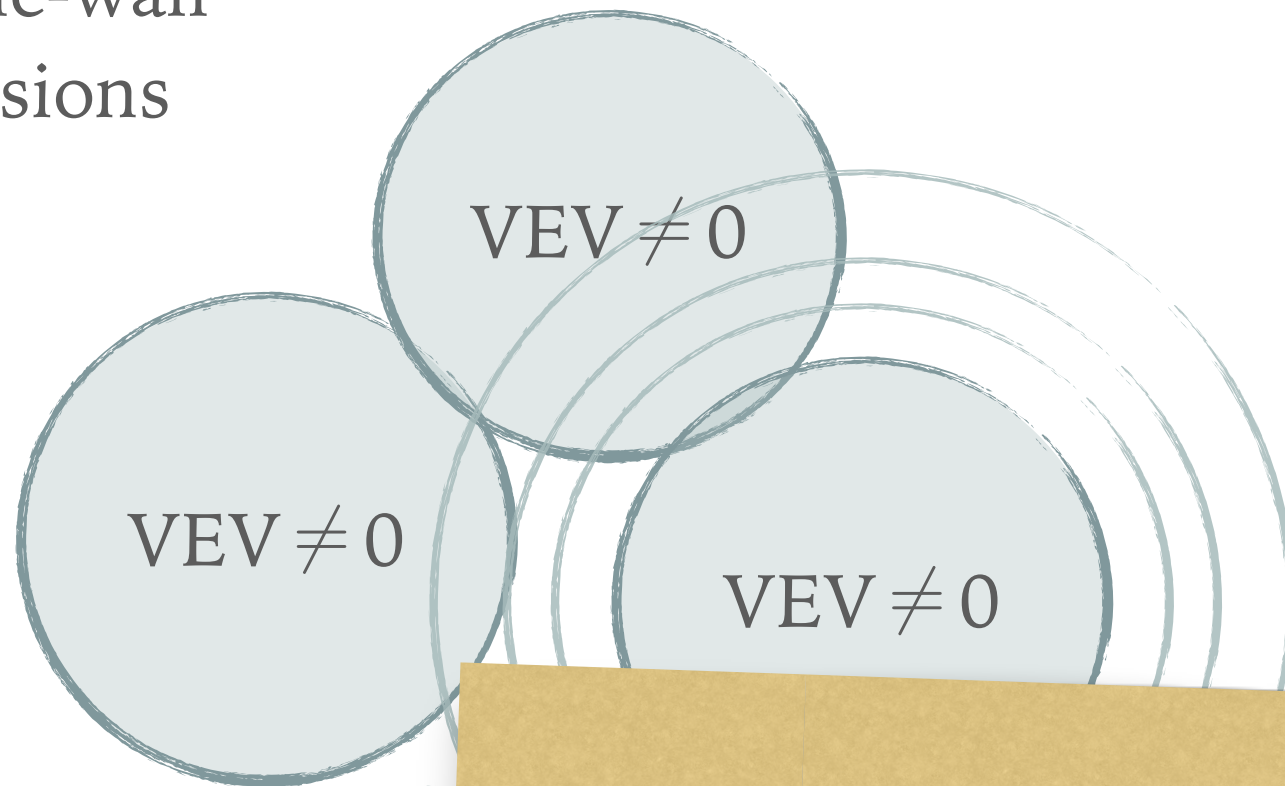
turbulence in  
the plasma

# SOURCES OF GRAVITATIONAL WAVES

---

bubble-wall  
collisions

sound waves  
in the plasma



Simulations of bubbles and plasma motion  
→ predictions for GW spectra

# GRAVITATIONAL WAVES IN PULSAR TIMING ARRAYS?

.....

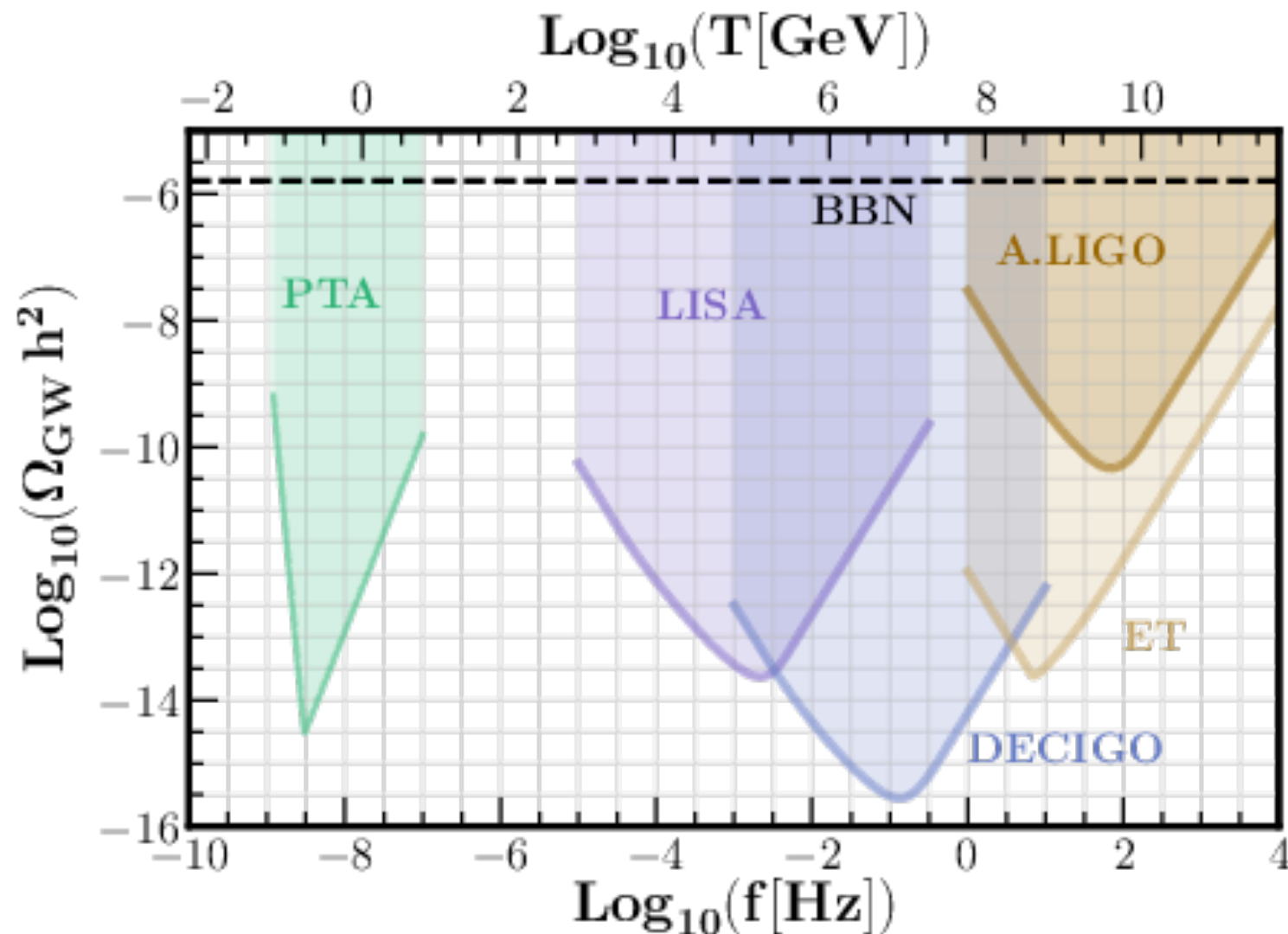
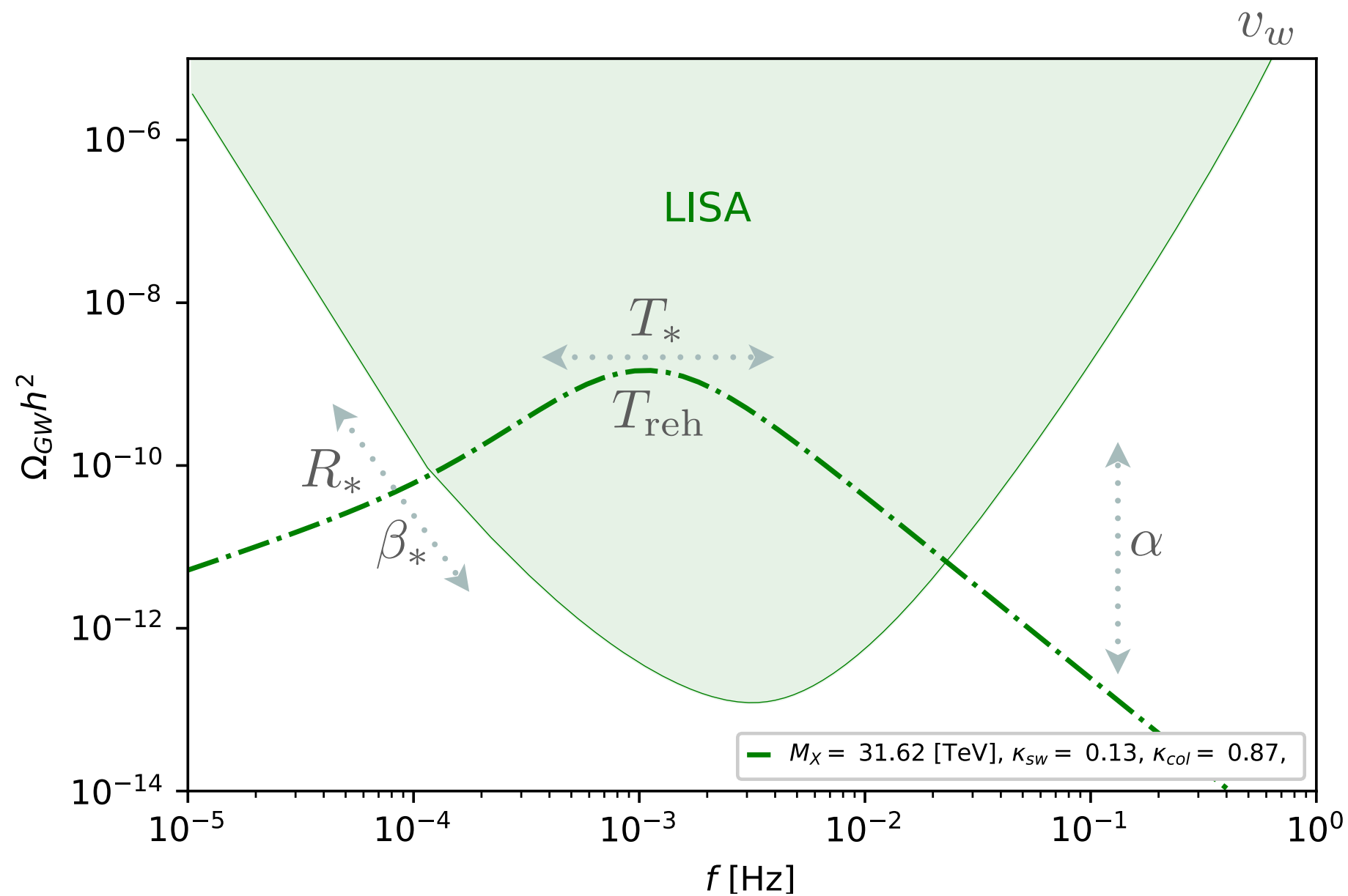


Figure from: G. Domenech, Universe 7 (2021) 11, 398

.....  
[See e.g. J. Ellis et al, 2308.08546 and references therein]

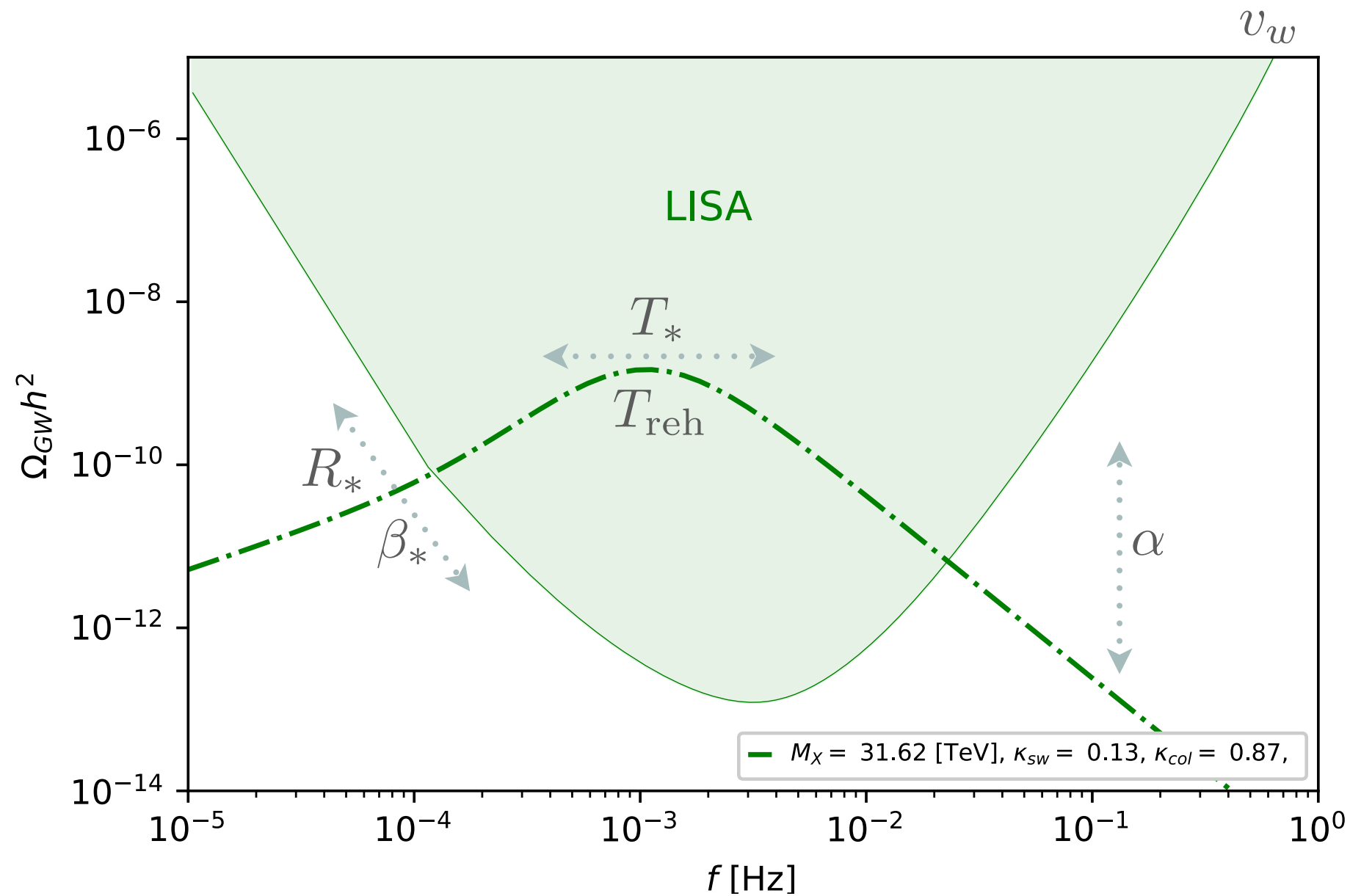
# RELEVANT PARAMETERS

---



*[Inspired by a talk by Pedro Schwaller]*

# RELEVANT PARAMETERS



[Inspired by a talk by Pedro Schwaller]

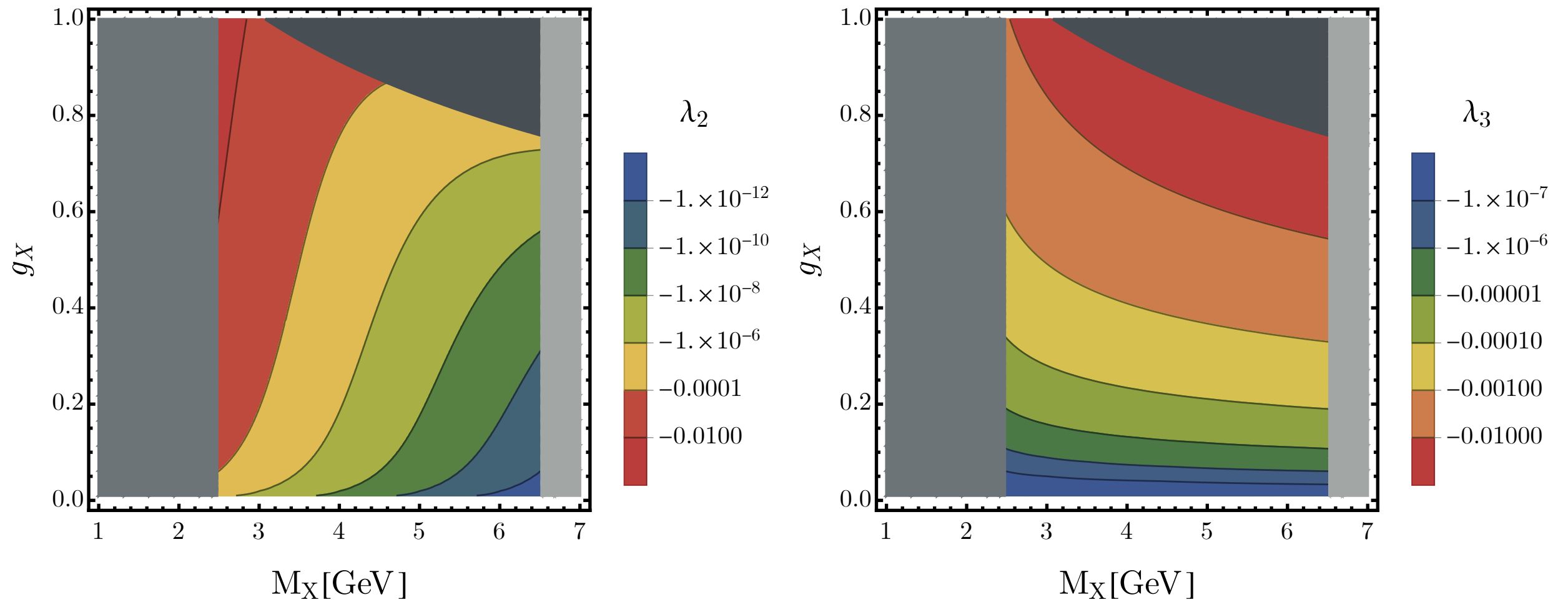


# RSB IN SU(2)CSM

---

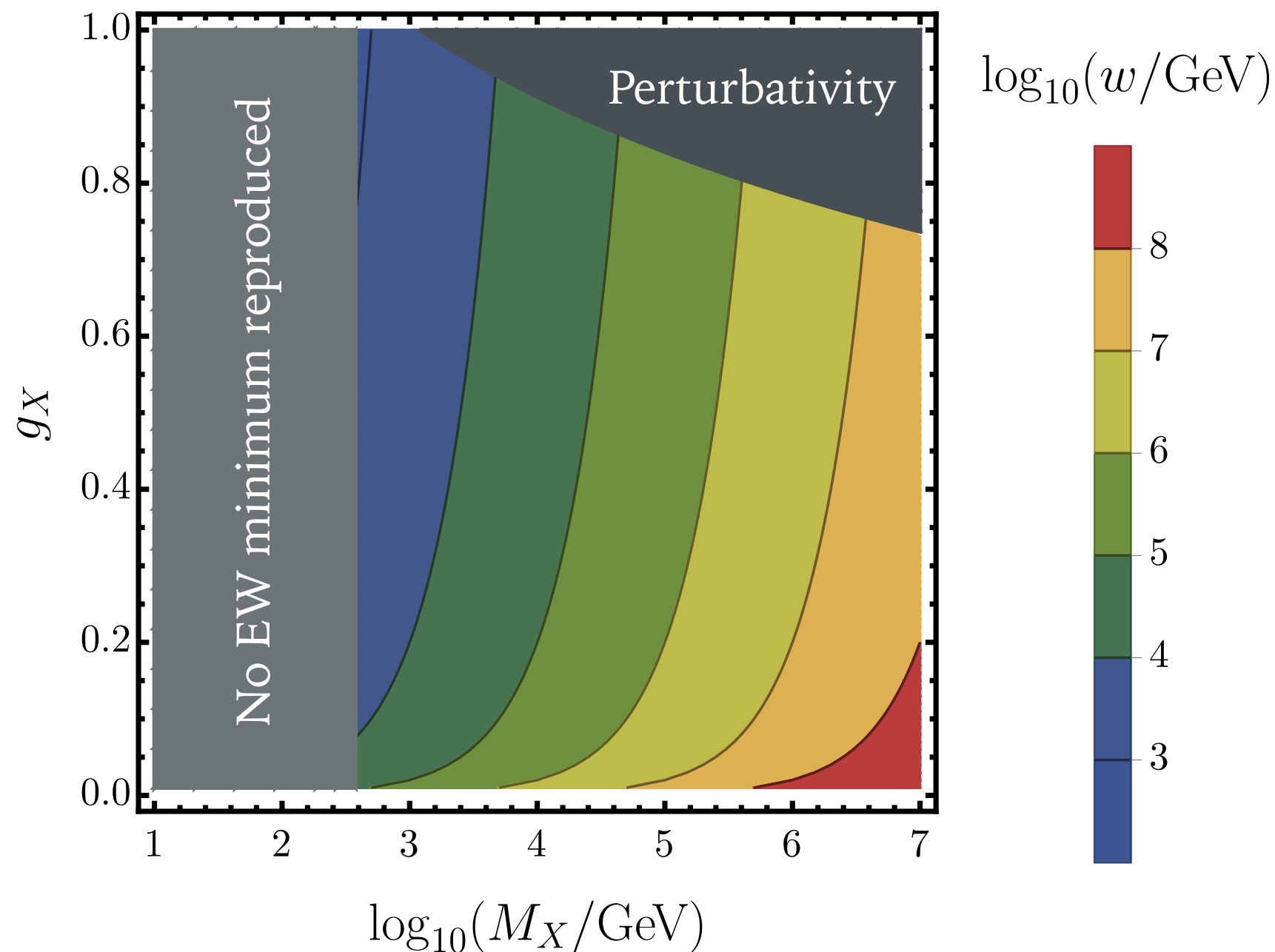
# SCALAR COUPLINGS

---



# RADIATIVE SYMMETRY BREAKING IN SU(2)CSM

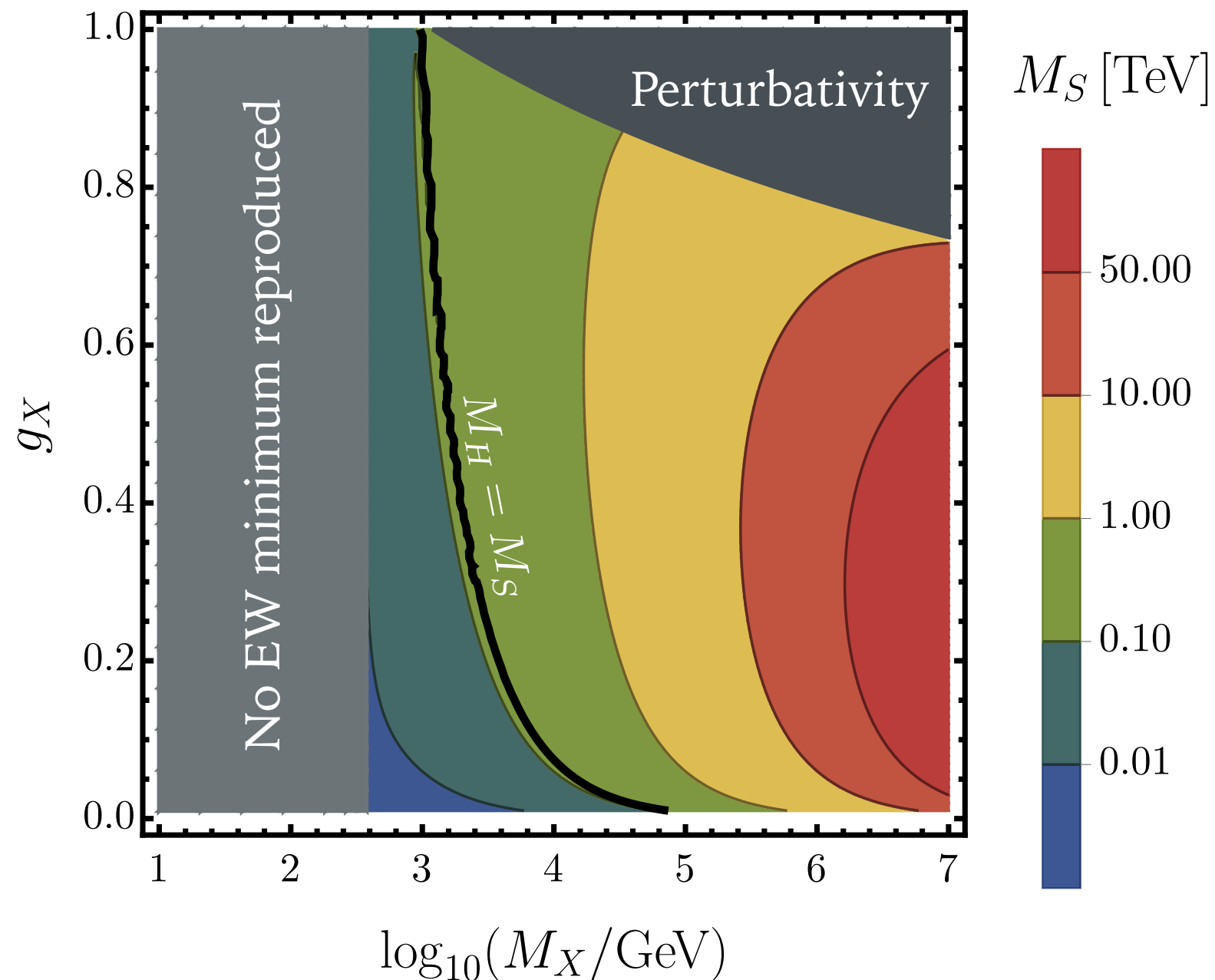
---



[See also: L. Chataignier, T. Prokopec, M.G. Schmidt, BS, JHEP 08 (2018) 083]

# RADIATIVE SYMMETRY BREAKING IN SU(2)CSM

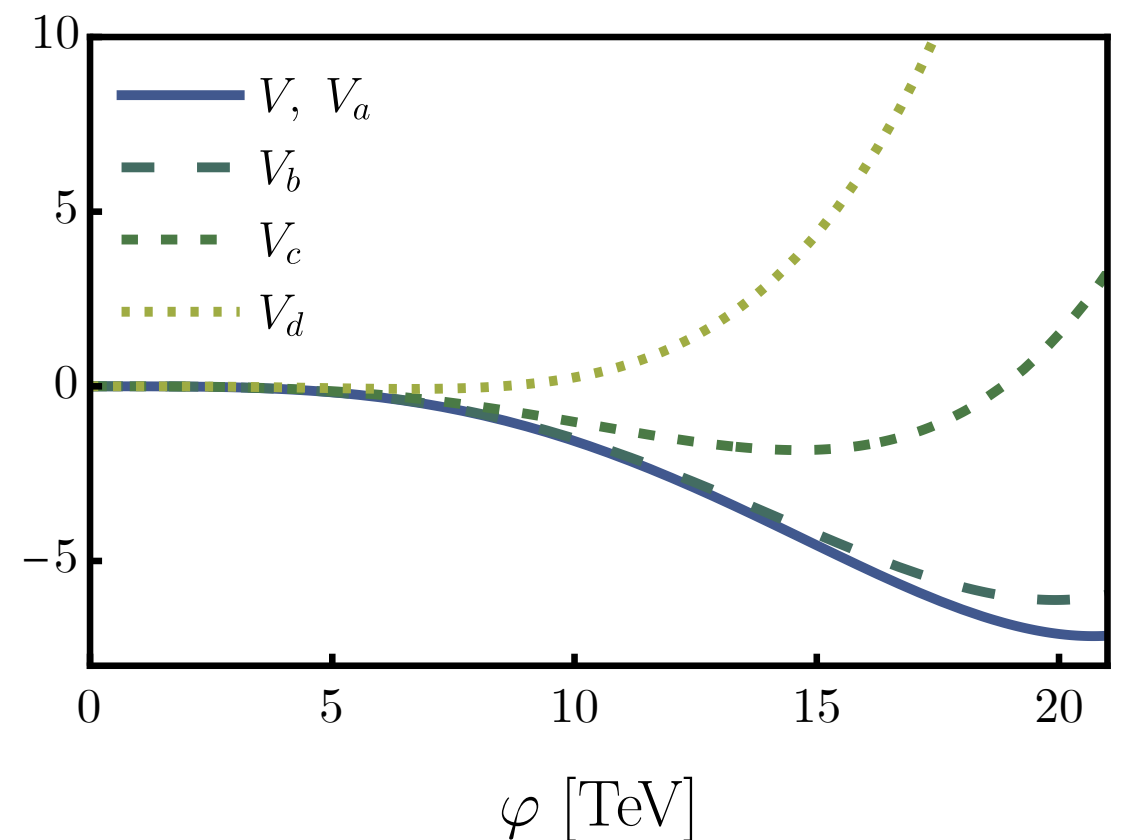
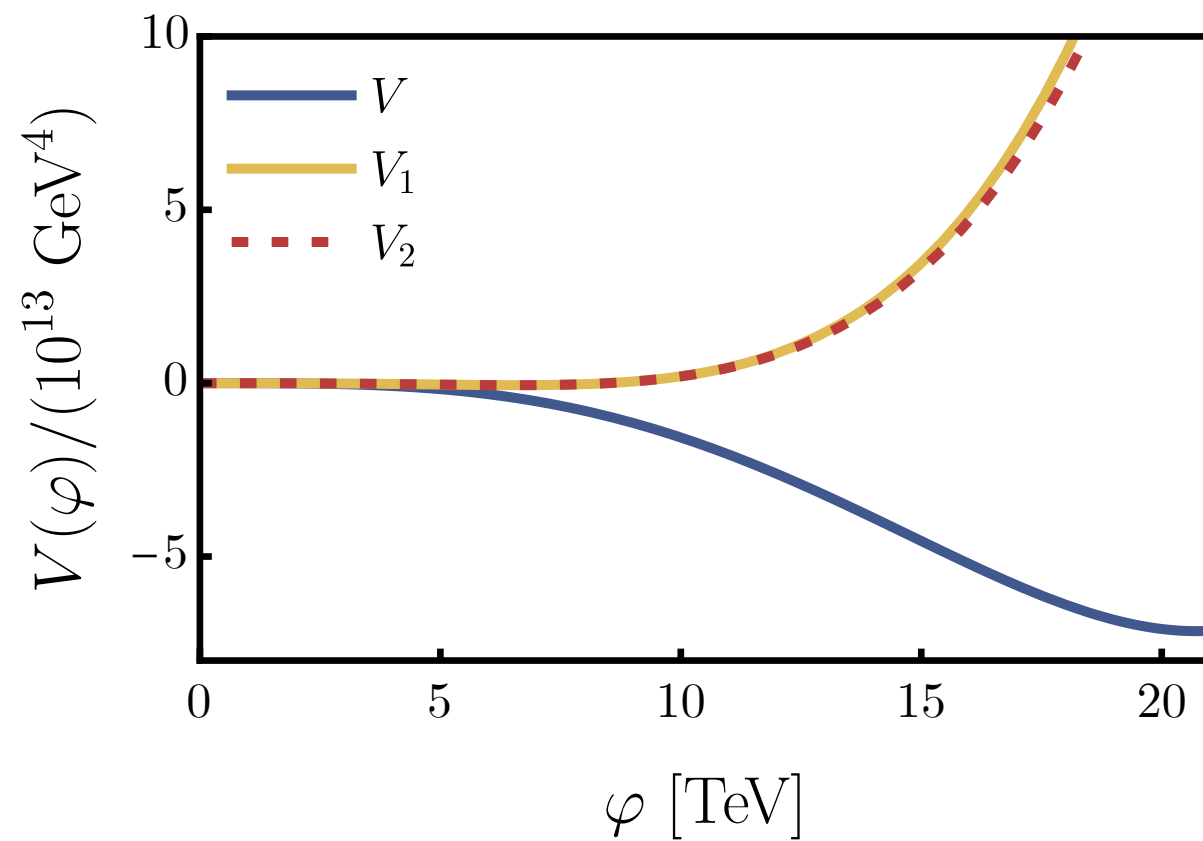
---



[See also: L. Chataignier, T. Prokopec, M.G. Schmidt, BS, JHEP 08 (2018) 083]

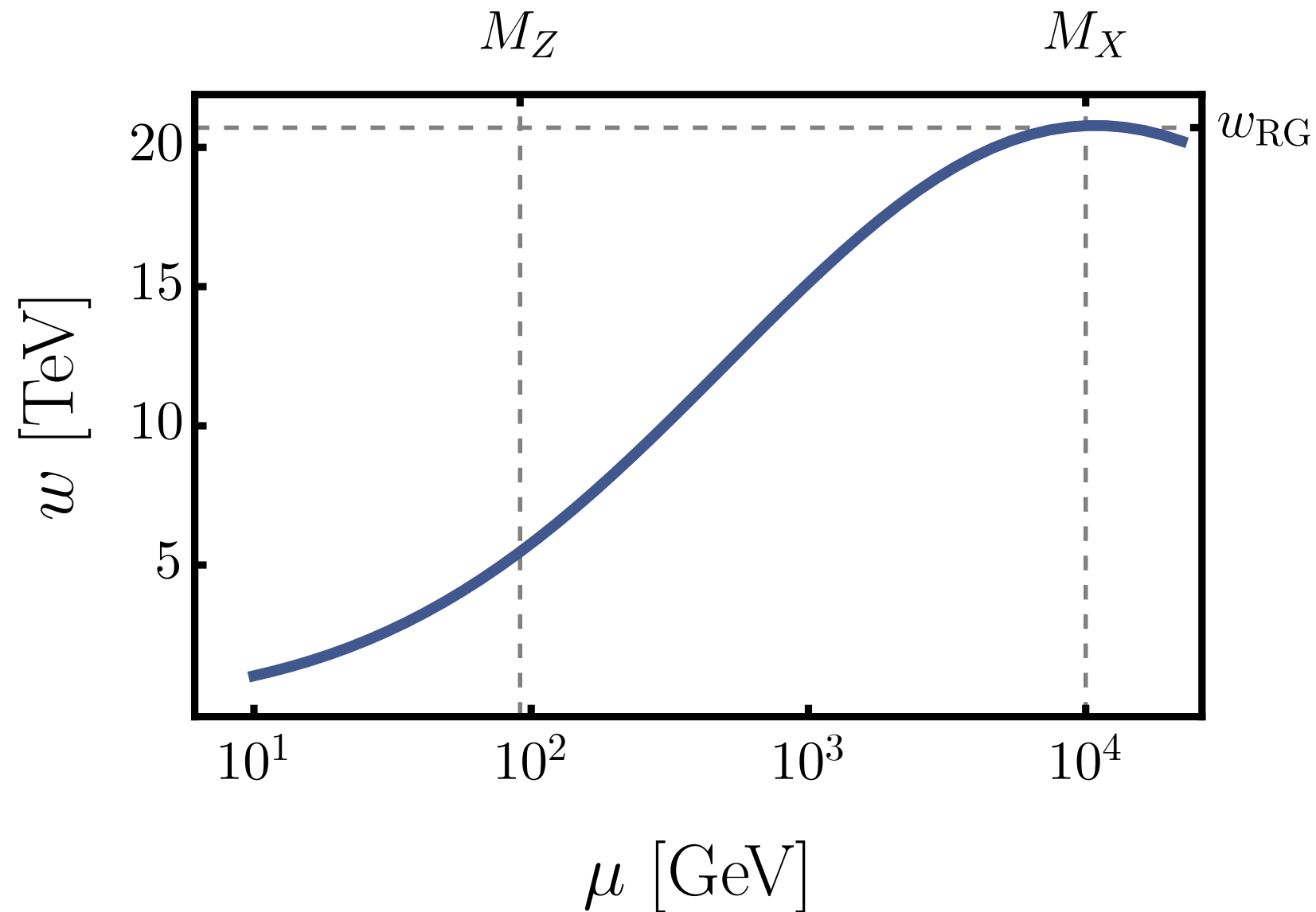
# RG IMPROVEMENT

---



# SCALE DEPENDENCE OF THE VEV

---

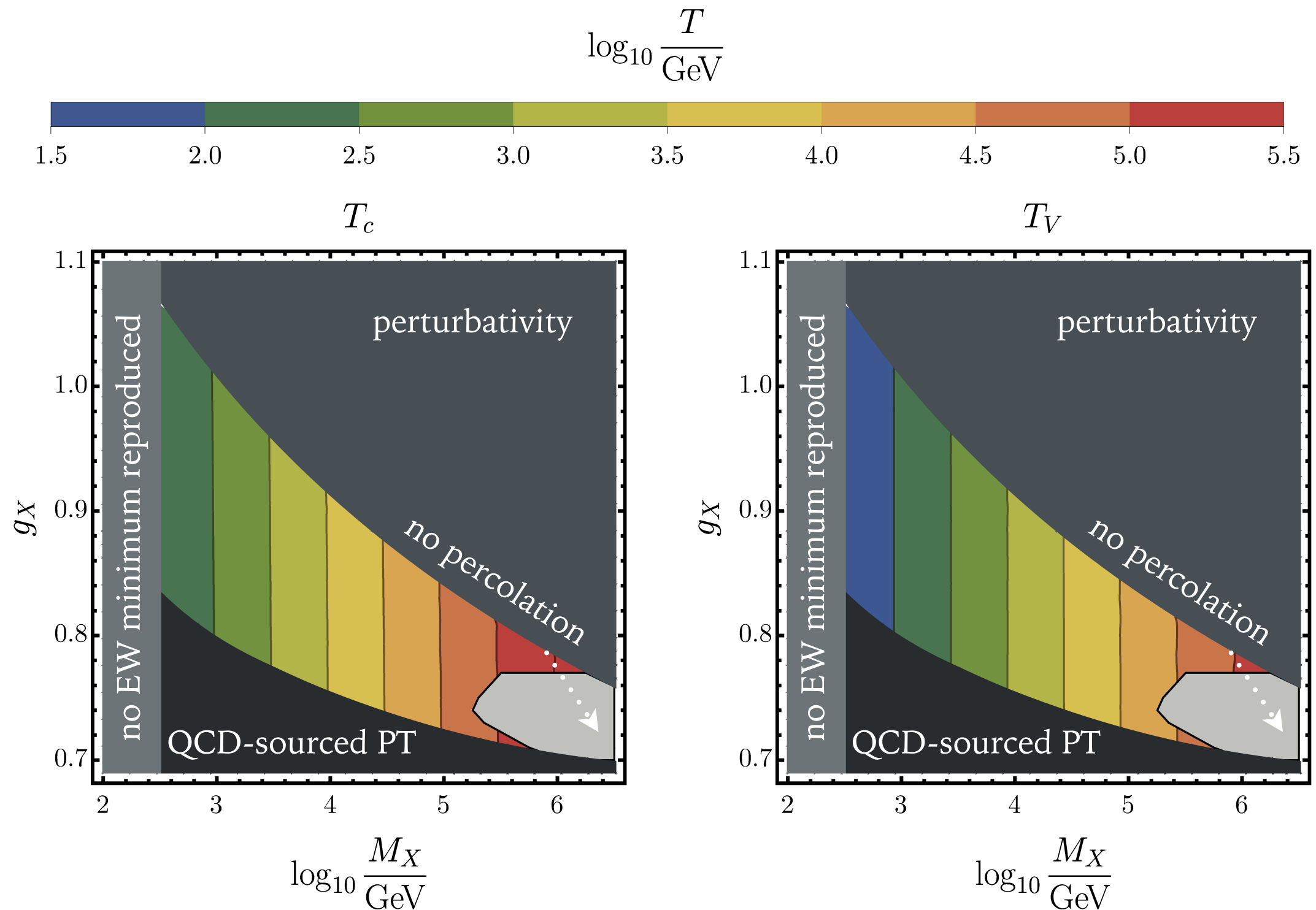


# PHASE TRANSITION IN $SU(2)$ CSM

---



# CRITICAL TEMPERATURE AND VACUUM DOMINATION



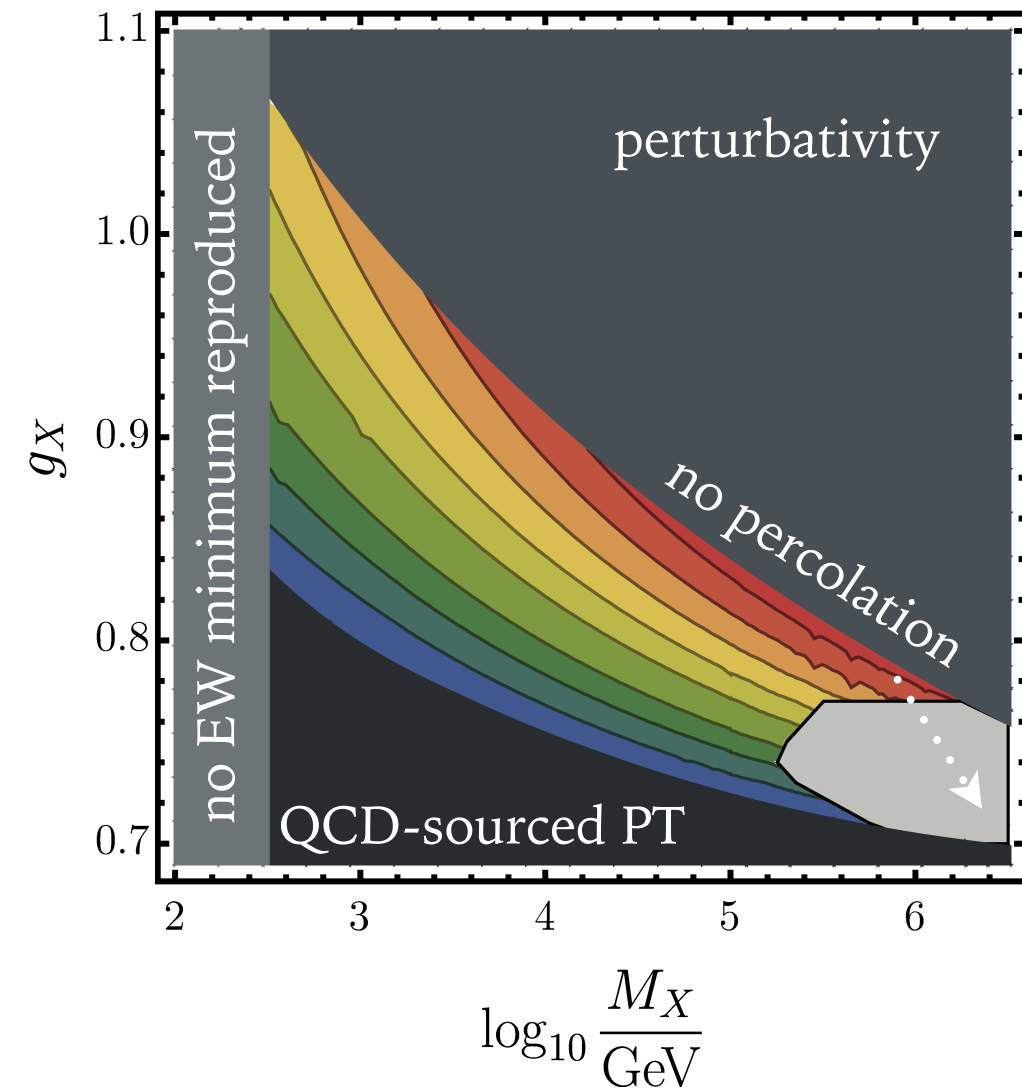
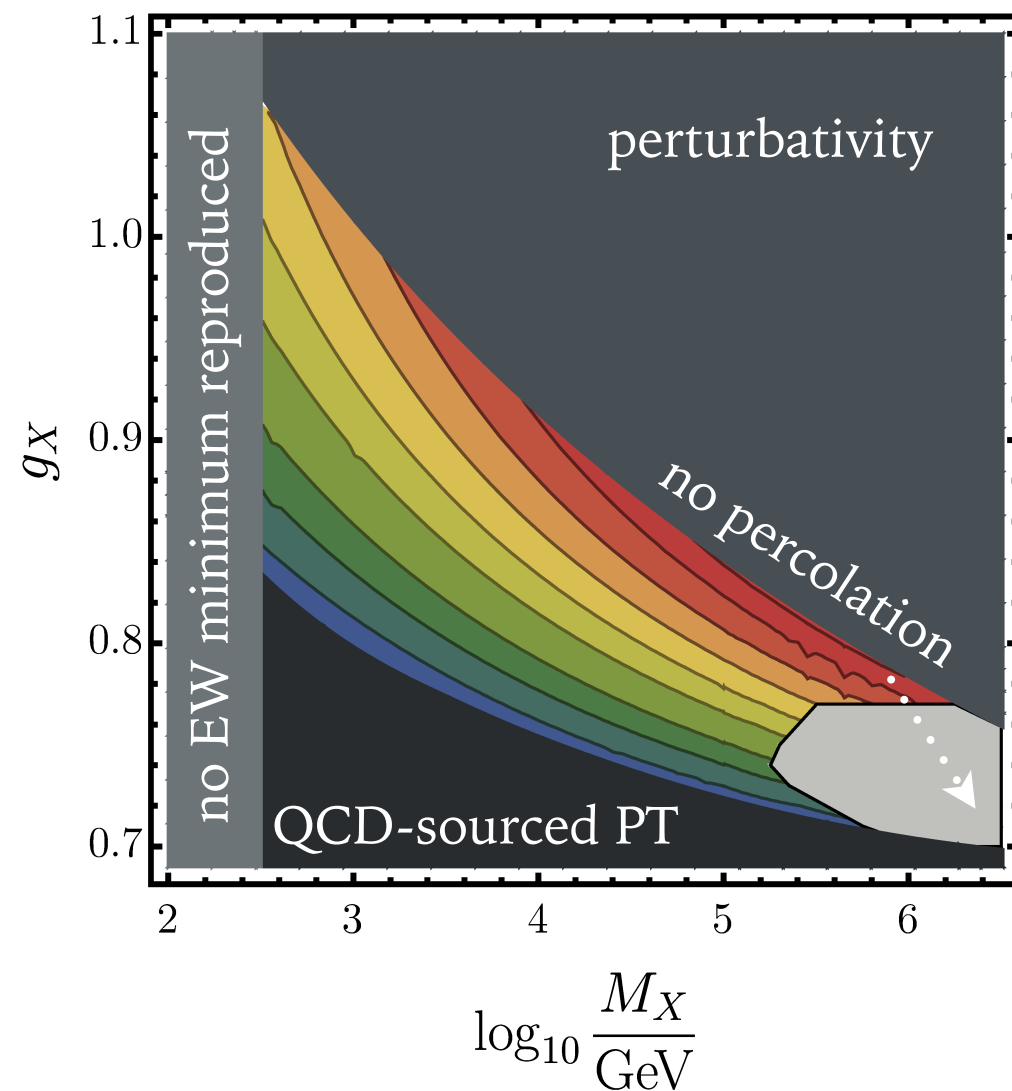
# NUCLEATION AND PERCOLATION TEMPERATURE

$T$  [GeV]



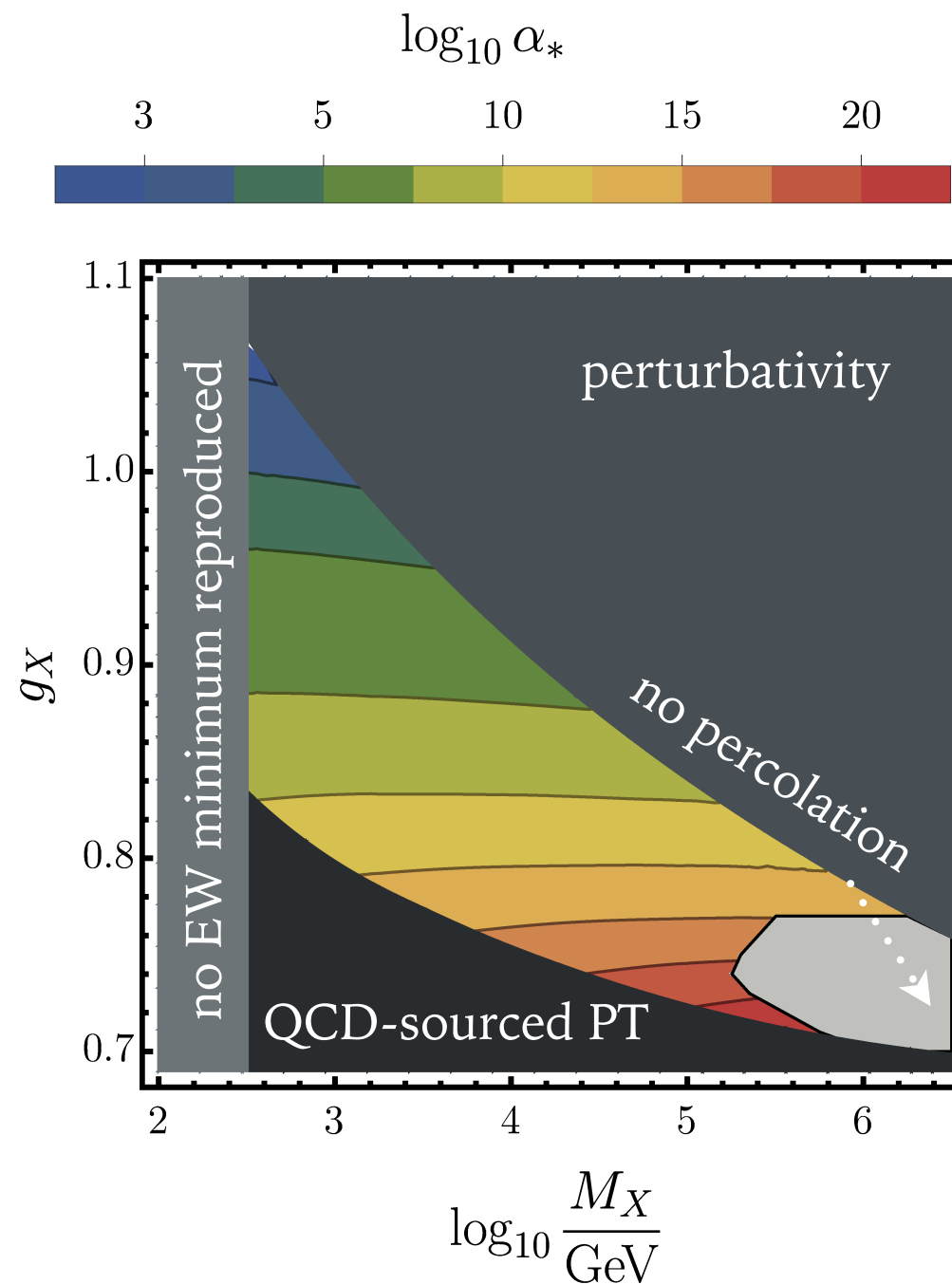
$T_n$

$T_p$

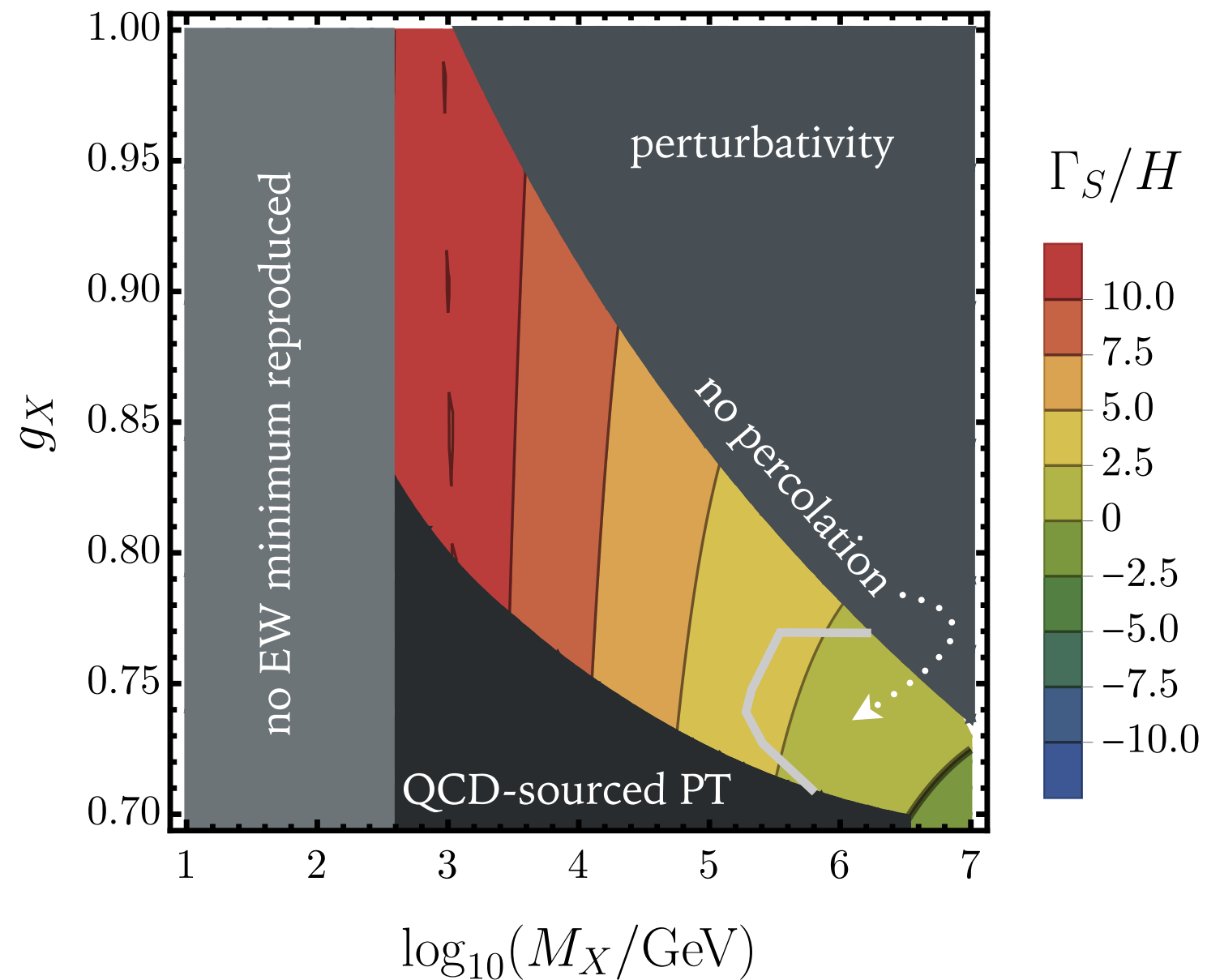


# STRENGTH OF THE TRANSITION

---

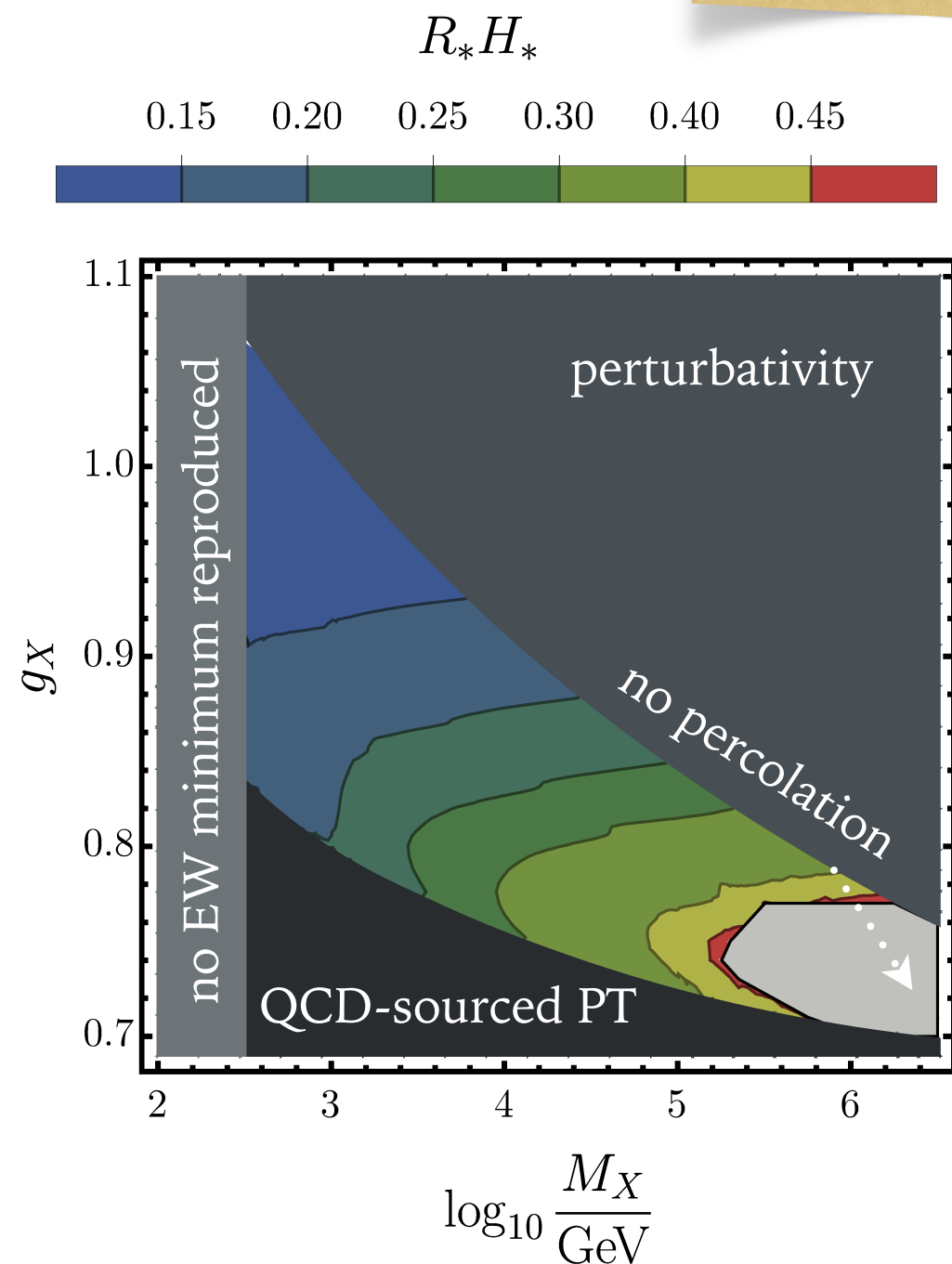
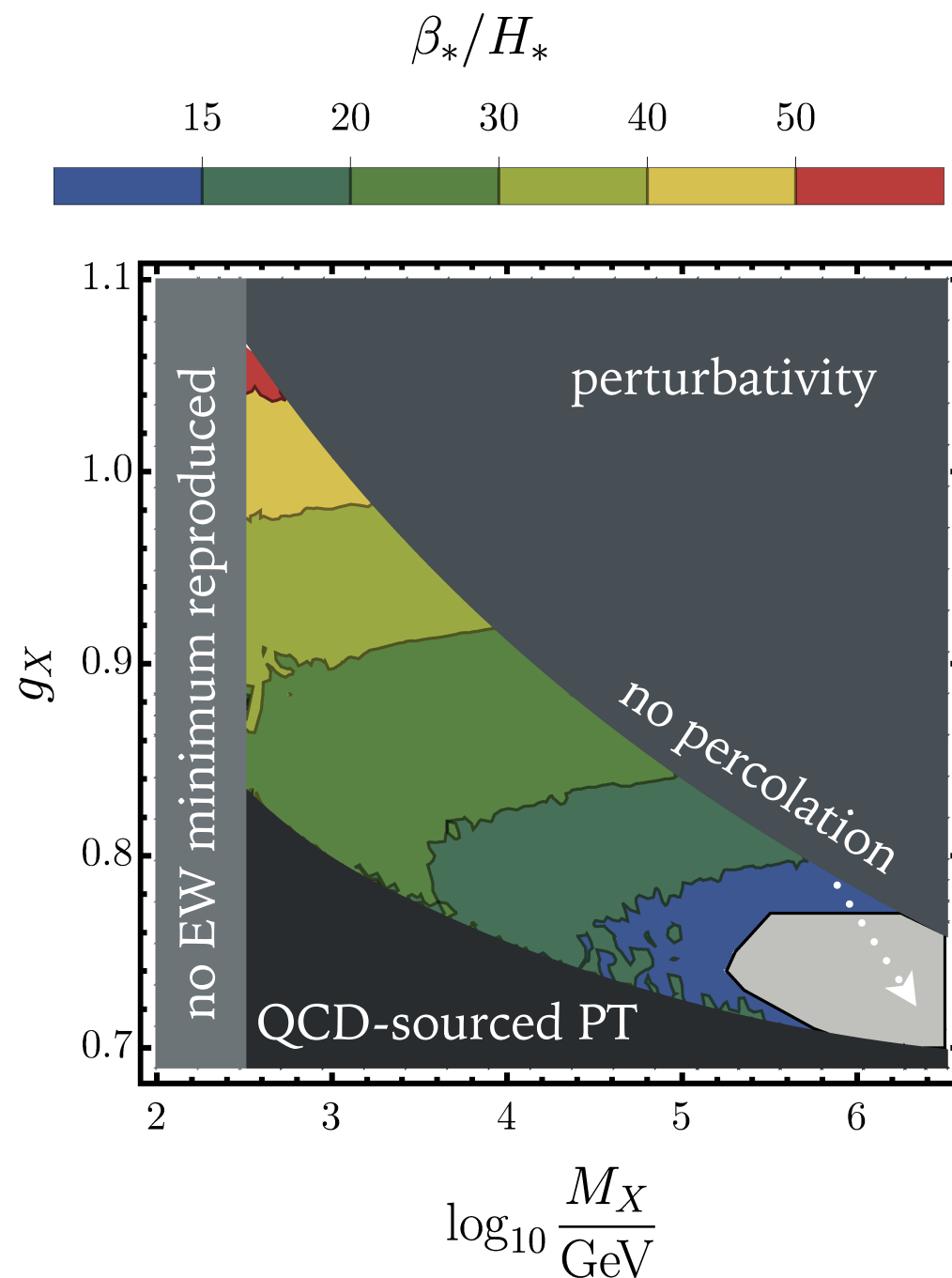


# REHEATING



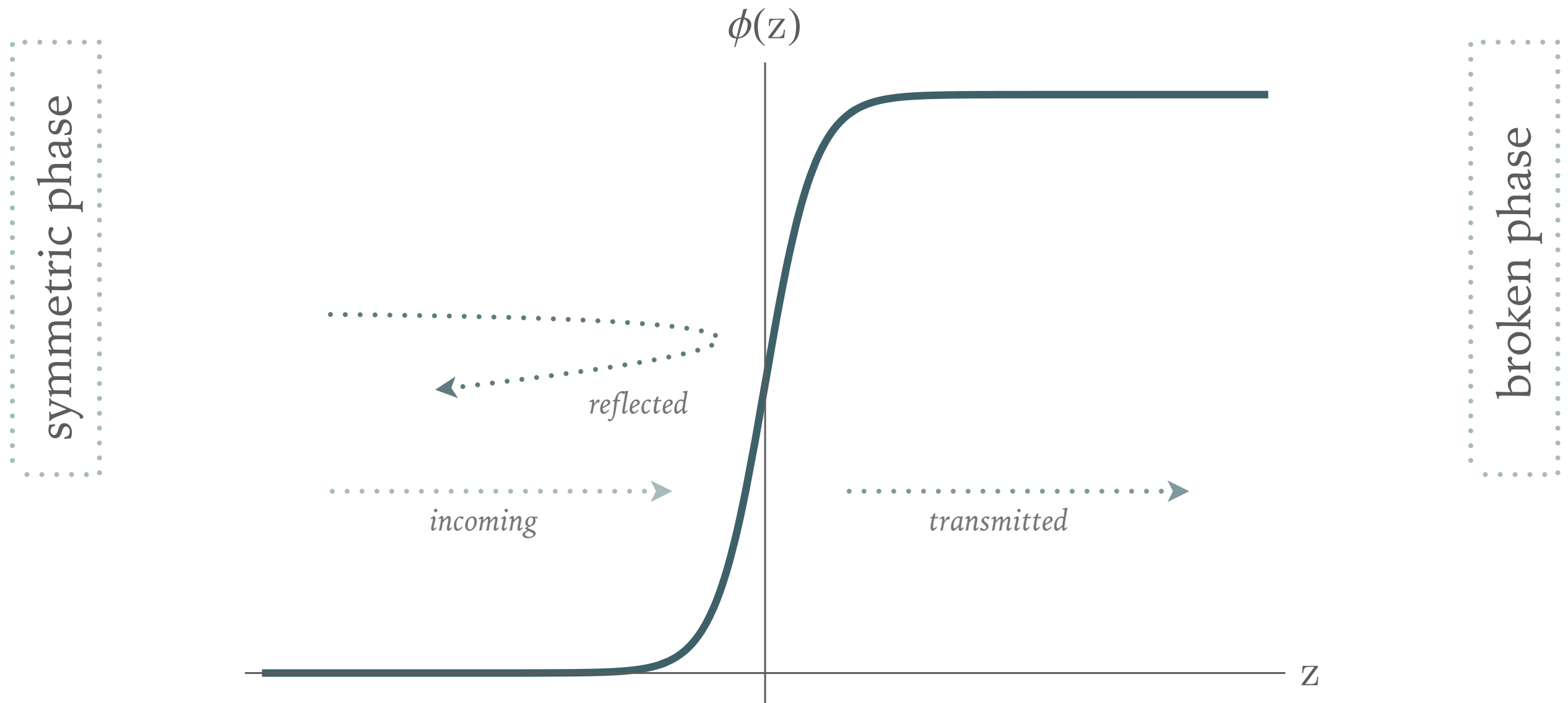
# TIME/LENGTH SCALE OF THE TRANSITION

$$R_* \approx \frac{(8\pi)^{\frac{1}{3}}}{\beta_*}$$



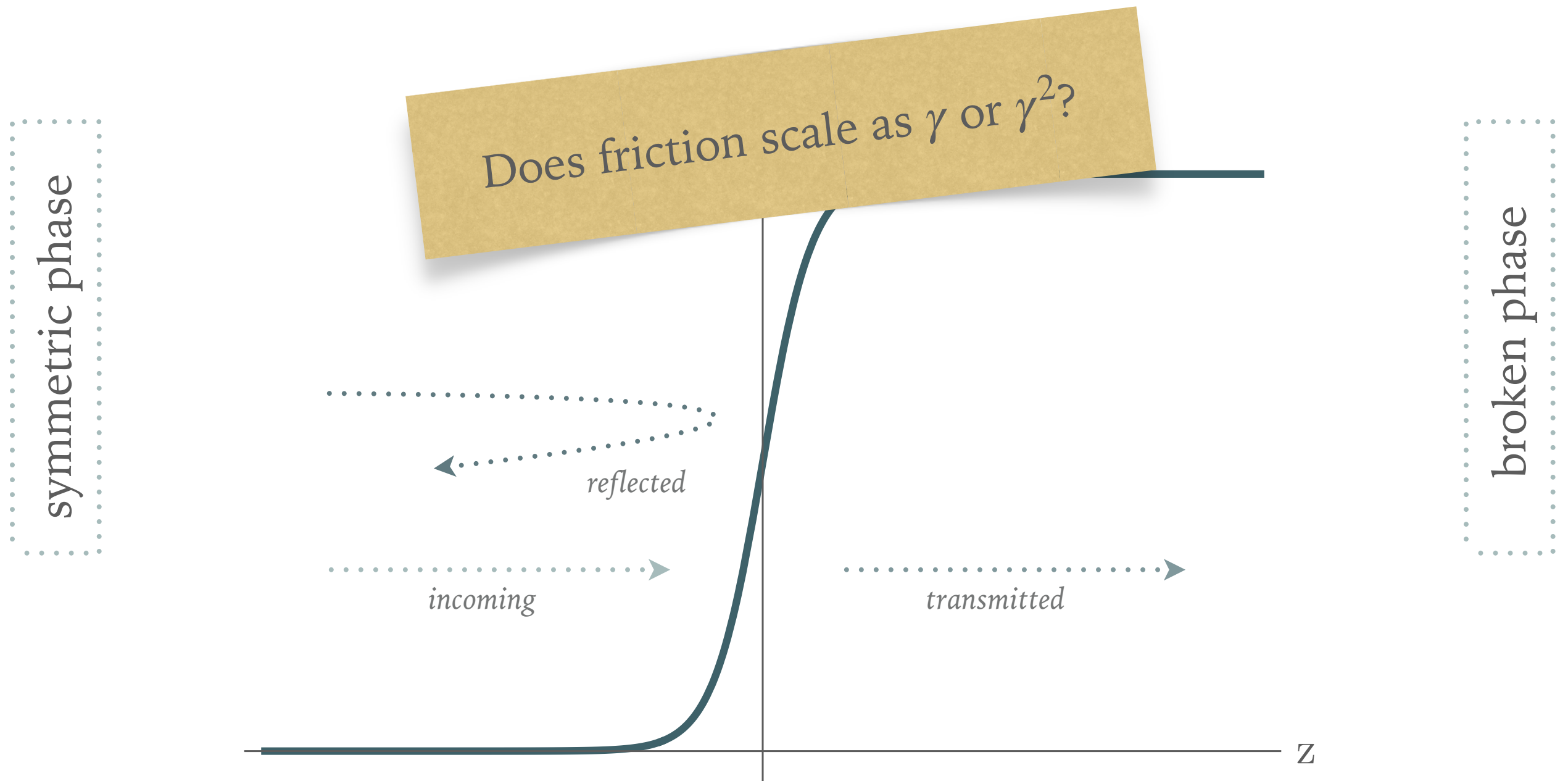
# SOUND WAVES OR BUBBLE COLLISIONS?

---



[G.D. Moore, T. Prokopec, PRL 75 (1995), PRD 52 (1995), P.B. Arnold, PRD 48 (1993) 1539, D. Bodeker, G.D. Moore, JCAP 0905 (2009) 009; JCAP 1705 (2017) 025, G.C. Dorsch, S. J. Huber and T. Konstandin, JCAP 12 (2018); 2106.06547, T. Konstandin, G. Nardini and I. Rues, JCAP 09 (2014), J.Kozaczuk, JHEP 10 (2015), S. Höche et al, 2007.10343, Y. Gouttenoire, R. Jinno, F. Sala, 2112.07686]

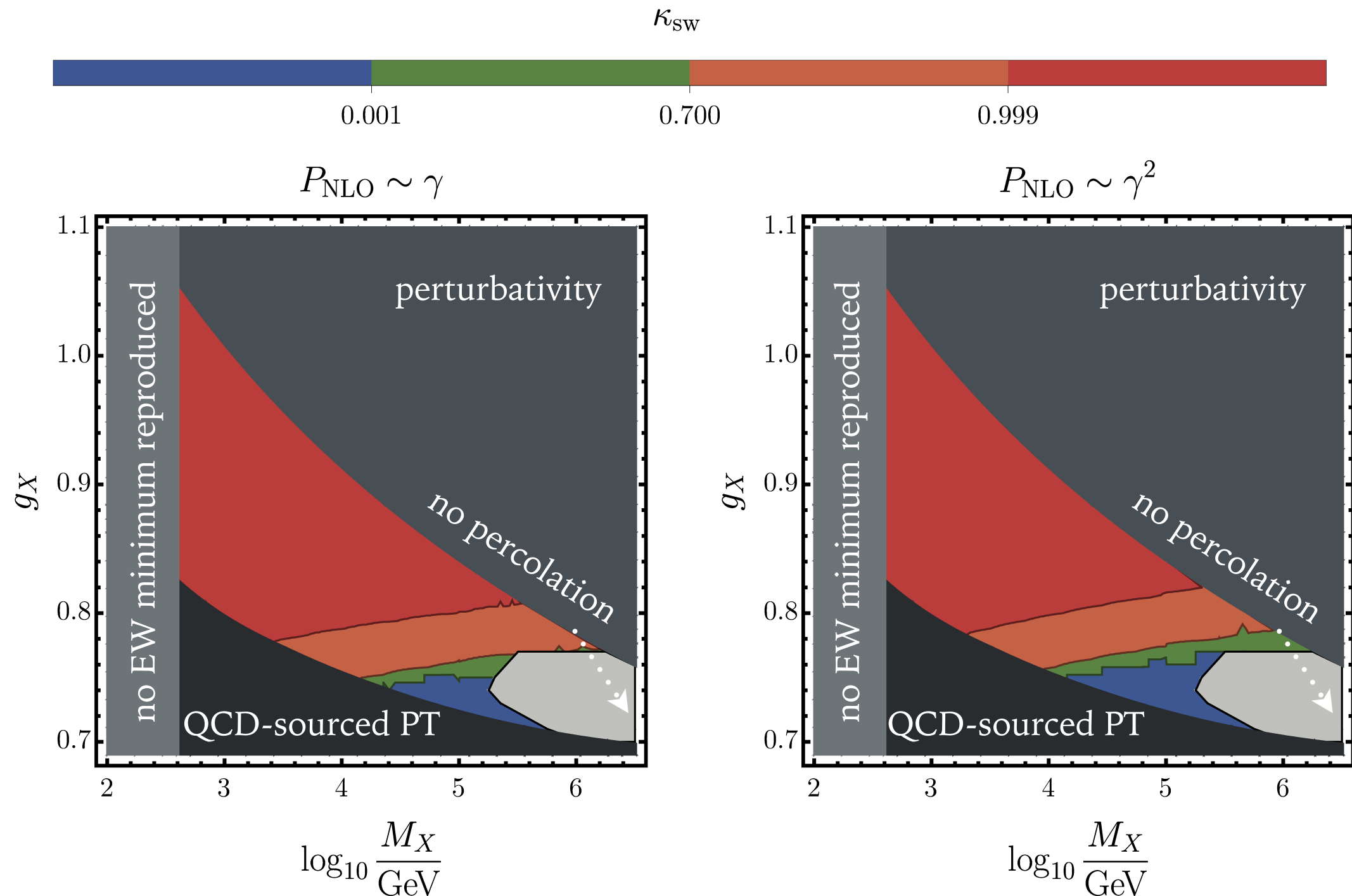
# SOUND WAVES OR BUBBLE COLLISIONS?



[G.D. Moore, T. Prokopec, PRL 75 (1995), PRD 52 (1995), P.B. Arnold, PRD 48 (1993) 1539, D. Bodeker, G.D. Moore, JCAP 0905 (2009) 009; JCAP 1705 (2017) 025, G.C. Dorsch, S. J. Huber and T. Konstandin, JCAP 12 (2018); 2106.06547, T. Konstandin, G. Nardini and I. Rues, JCAP 09 (2014), J.Kozaczuk, JHEP 10 (2015), S. Höche et al, 2007.10343, Y. Gouttenoire, R. Jinno, F. Sala, 2112.07686]

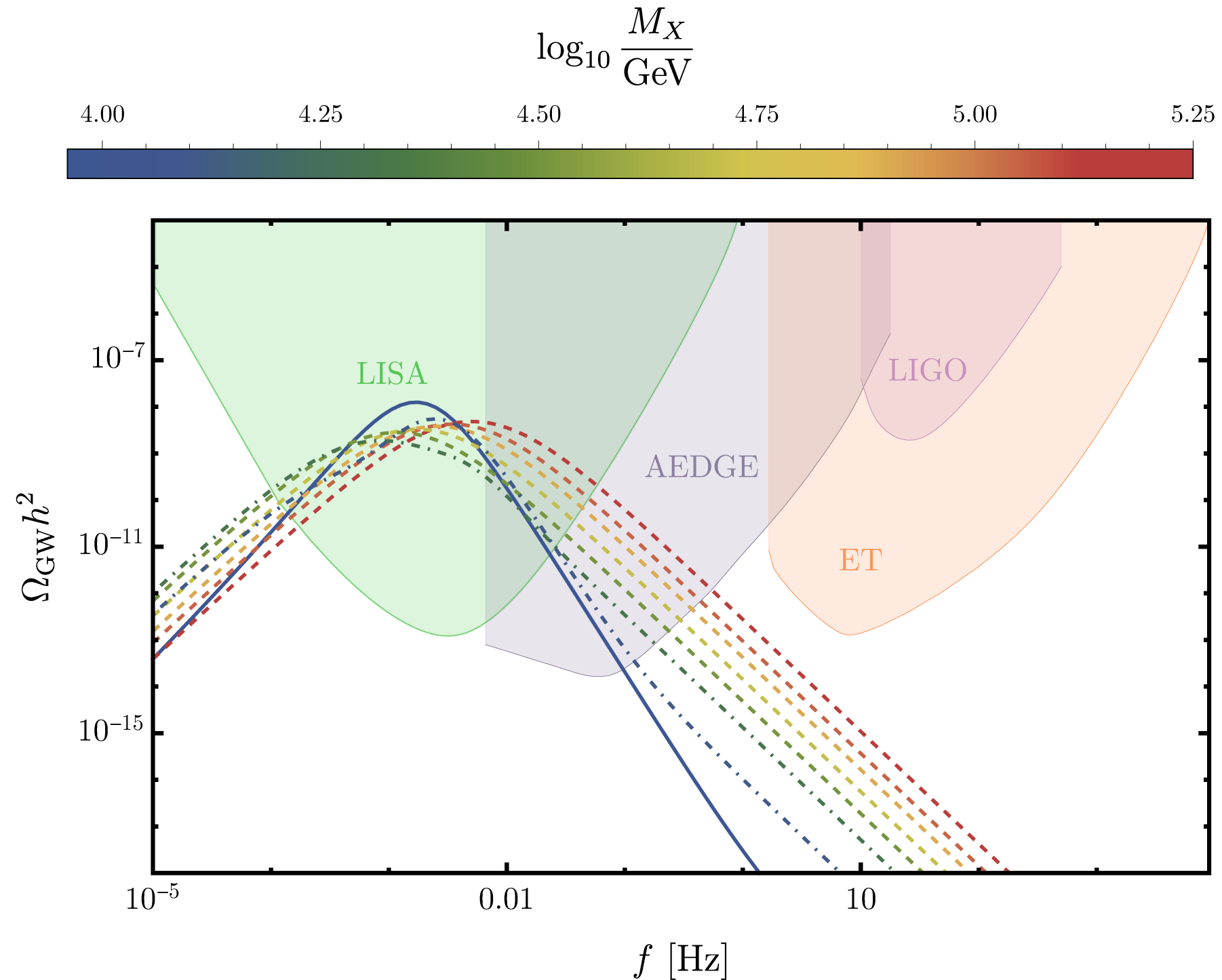


# DETERMINING THE SOURCE



# GRAVITATIONAL WAVE SPECTRA

---



[sensitivity curves courtesy M. Lewicki]

# DARK MATTER PRODUCTION

---

# THE MODEL: SU(2)CSM

.....



$$V = \frac{1}{4} (\lambda_1 h^4 + \lambda_2 h^2 \varphi^2 + \lambda_3 \varphi^4)$$

A light blue rectangular box with a dotted border containing the symmetry breaking pattern  $SU(2) \rightarrow \mathbb{Z}_2 \times \mathbb{Z}_2$ .

DM stability protected by a symmetry

[See also: T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, T.Prokopec, J.Rezacek, BS, JCAP02(2019)009, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

.....

# NON-STANDARD THERMAL EVOLUTION

---

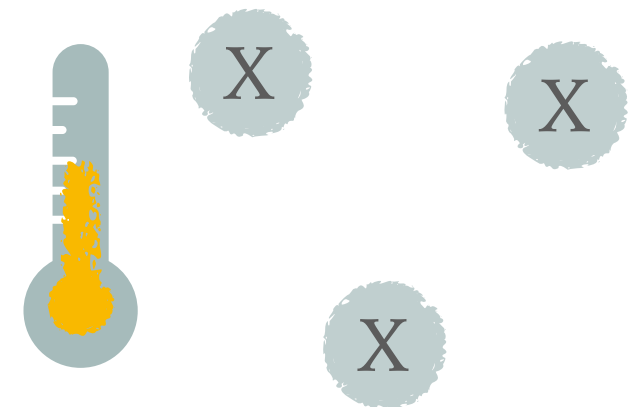
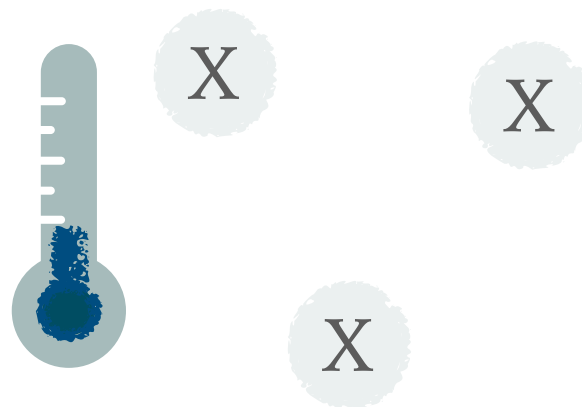
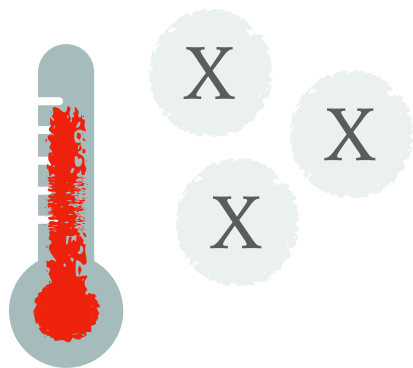
supercooling

PT and reheating

hot Universe,  
massless particles

cool Universe,  
diluted massless  
particles

reheated Universe,  
diluted massive  
particles



[Image credit: M. Kierkla]

# NEW PRODUCTION MECHANISM

---

Standard freezeout  
With nonstandard  
initial condition  
 $T_{\text{dec}} < T_{\text{reh}}$

Supercool DM  
DM diluted by  
thermal inflation  
 $T_{\text{dec}} > T_{\text{reh}}$

[T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]



# NEW PRODUCTION MECHANISM

---

Standard freezeout  
With nonstandard  
initial condition  
 $T_{\text{dec}} < T_{\text{reh}}$

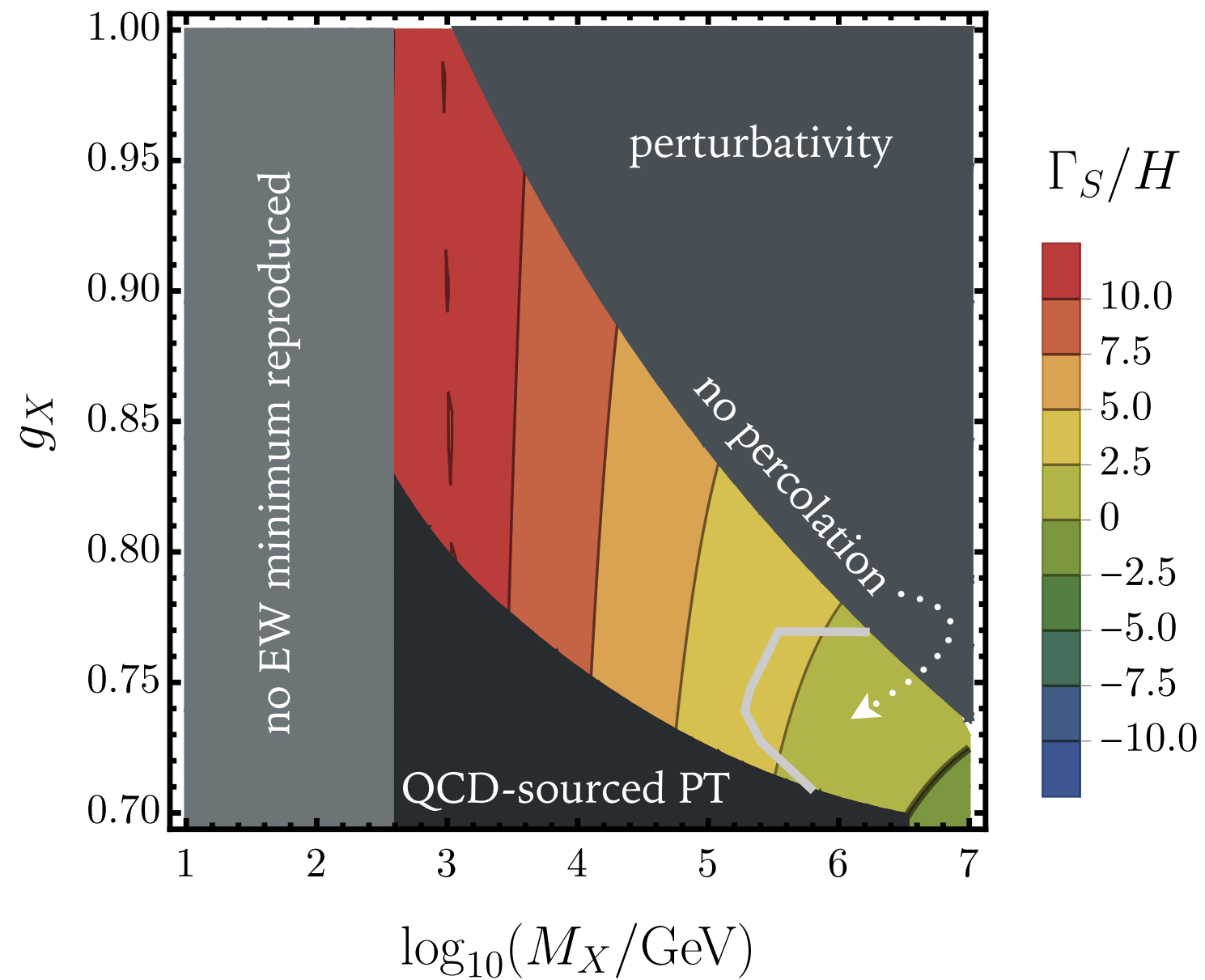
Supercool DM  
DM diluted by  
thermal inflation  
 $T_{\text{dec}} > T_{\text{reh}}$

$$T_{\text{dec}} \approx \frac{M_X}{25}$$

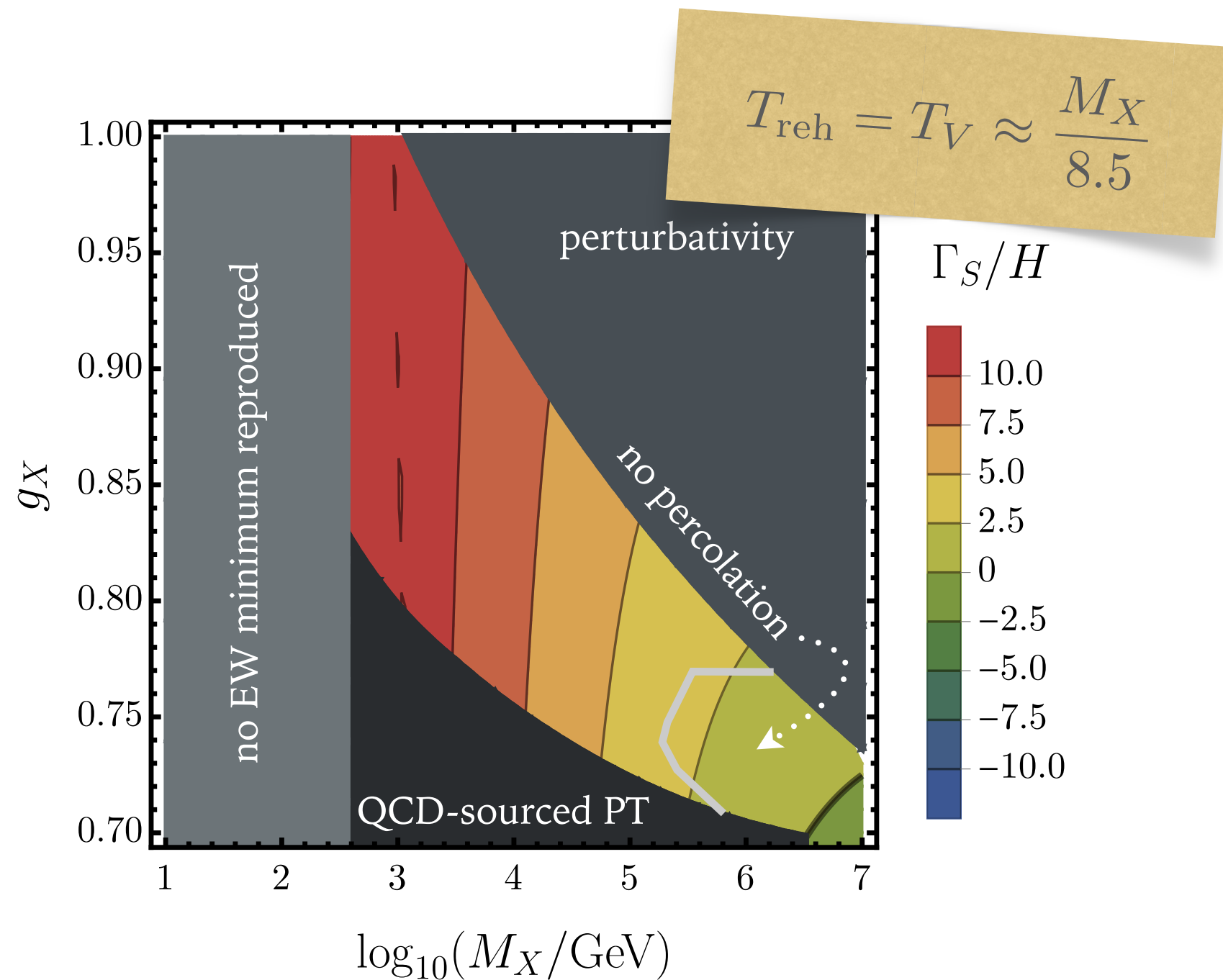
[T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]



# REHEATING



# REHEATING



# NEW PRODUCTION MECHANISM

---

Standard freezeout  
With nonstandard  
initial condition  
 $T_{\text{dec}} < T_{\text{reh}}$

Supercool DM  
DM diluted by  
thermal inflation  
 $T_{\text{dec}} > T_{\text{reh}}$

$$T_{\text{dec}} \approx \frac{M_X}{25}$$

$$T_{\text{reh}} = T_V \approx \frac{M_X}{8.5}$$

[T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

# NEW PRODUCTION MECHANISM

---

Standard freezeout  
With nonstandard  
initial condition  
 $T_{\text{dec}} < T_{\text{reh}}$

Supercool PT  
Disrupted by  
thermal inflation  
 $T_{\text{dec}} > T_{\text{reh}}$

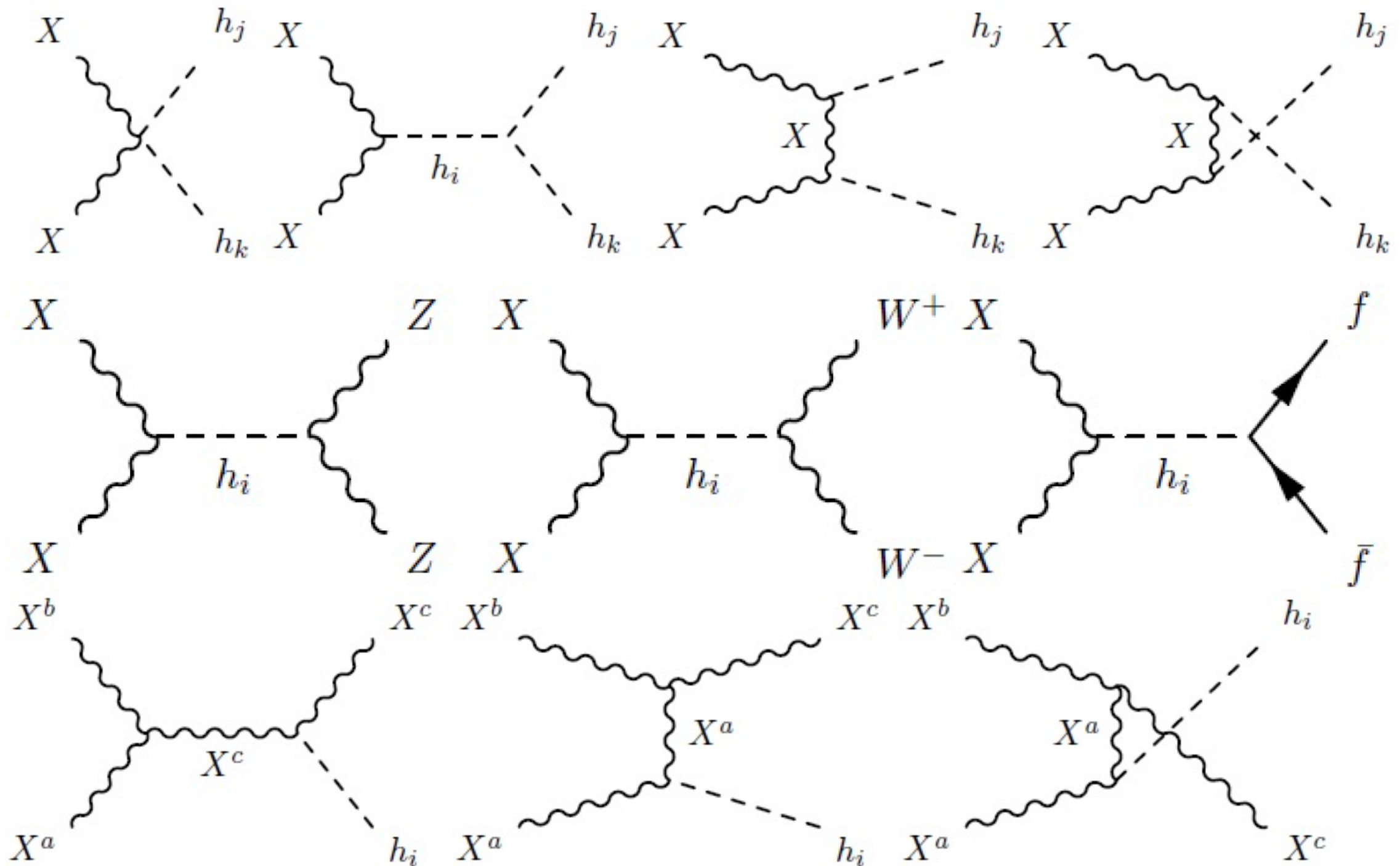
$$T_{\text{dec}} \approx \frac{M_X}{25}$$

$$T_{\text{reh}} = T_V \approx \frac{M_X}{8.5}$$

[T.Hambye, A.Strumia, PRD88 (2013) 055022, C.Carone, R.Ramos, PRD88 (2013) 055020, V.V.Khoze, C.McCabe, G.Ro, JHEP 08 (2014) 026, T. Hambye, A.Strumia, D.Teresi, JHEP 1808 (2018) 188, I.Baldes, C. Garcia-Cely, JHEP 05 (2019) 190, D. Marfaria, P. Tseng, JHEP 02 (2021) 022]

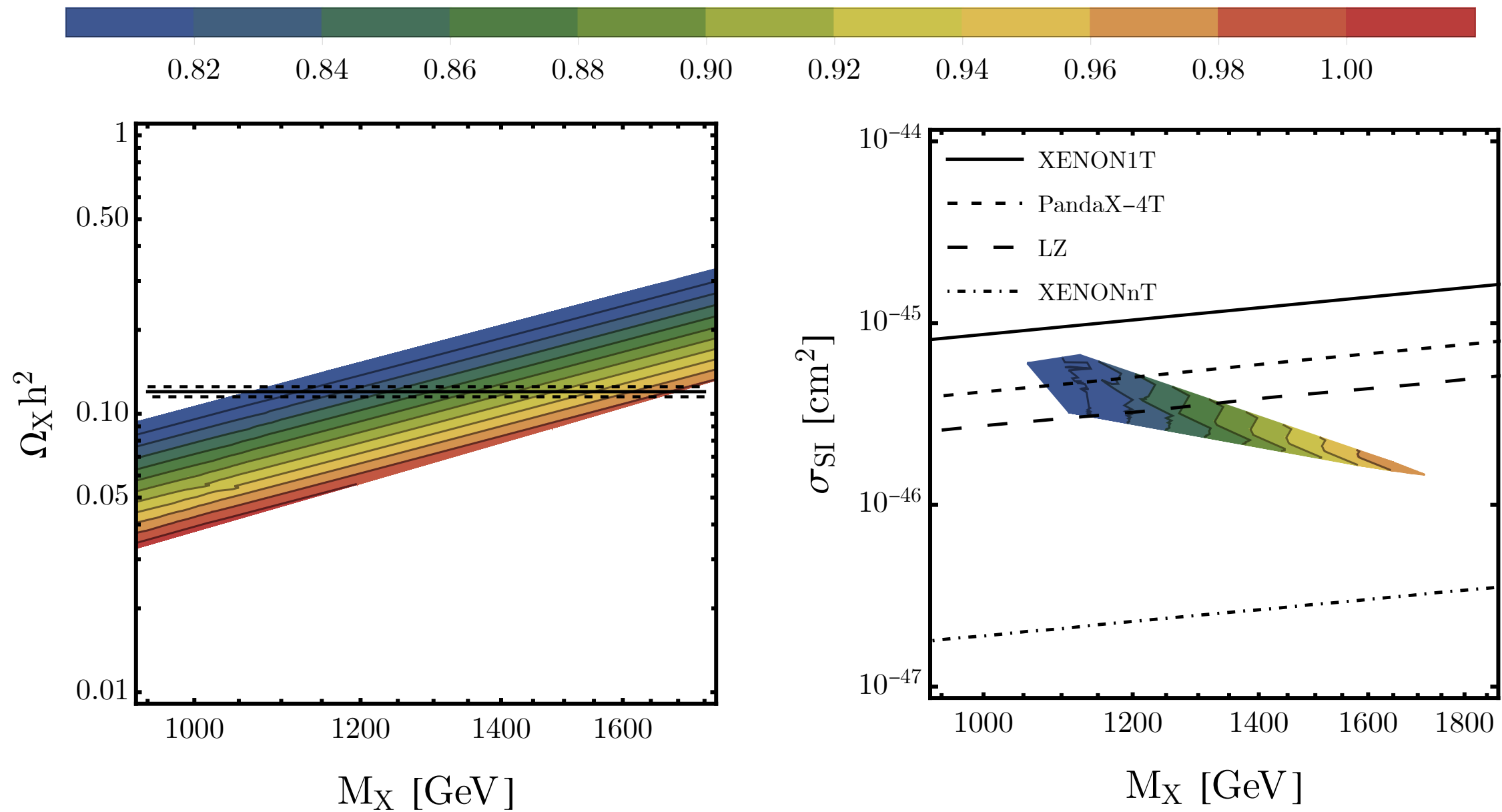


# ANNIHILATION AND SEMIANNIHILATION



# DM ABUNDANCE - FREEZEOUT

$g_X$



# DM PRODUCTION MECHANISMS

---

## Freeze-in

DM not in thermal equilibrium, produced by decays or annihilations in the visible sector

## Dark freeze-out

DM not in equilibrium with the visible sector, freeze-out within the dark sector

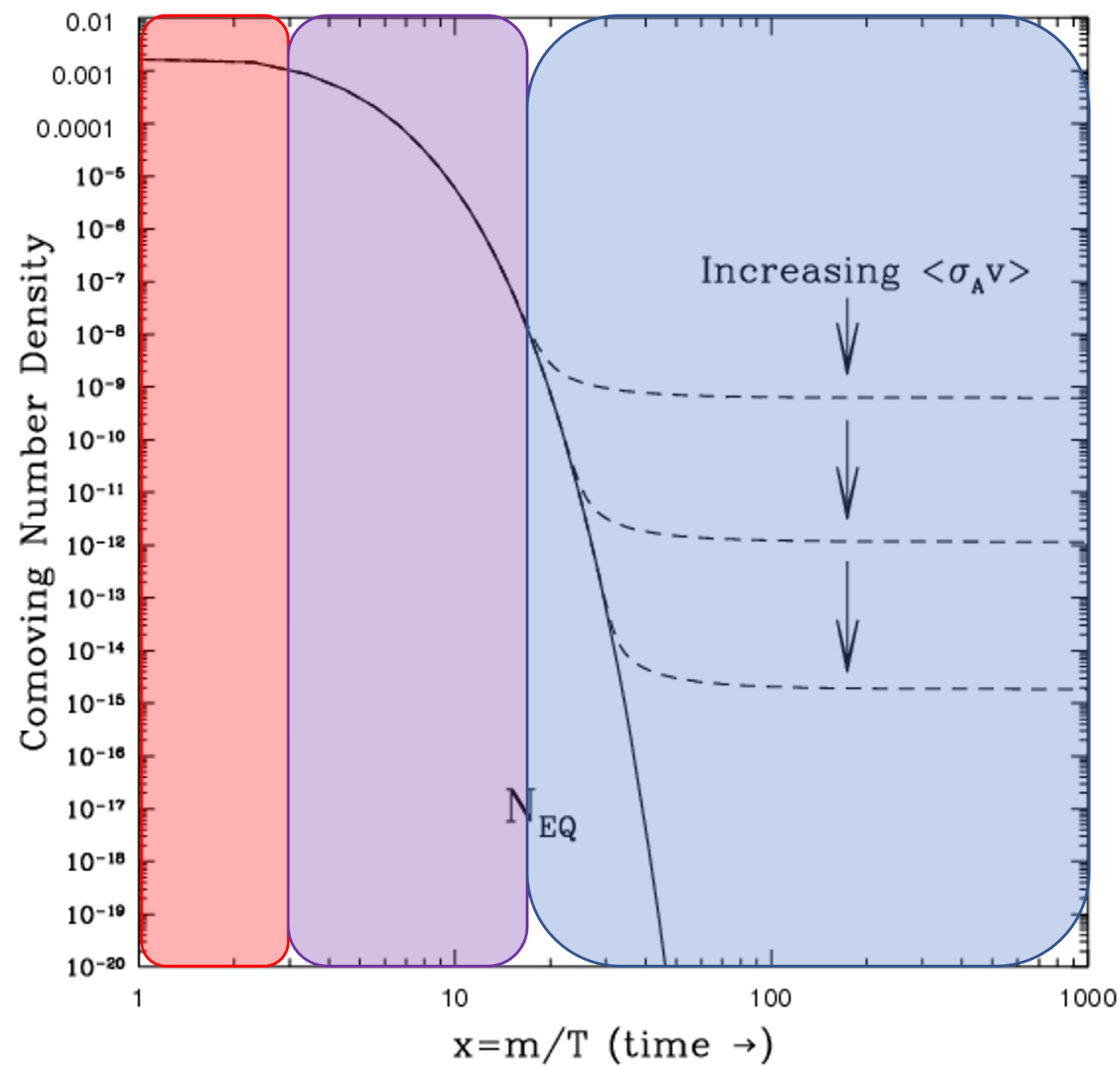
## Reannihilation

DM frozen in the dark sector but produced by the visible sector, final freeze-out when the yield ends

[N. Bernal et al, Int.J.Mod.Phys.A  
32 (2017) 27, 1730023]



# STANDARD FREEZE-OUT



[from Colb and Turner, adapted by particle bites.com]

# OTHER FUTURE IMPROVEMENTS NEEDED

---

# OTHER FUTURE IMPROVEMENTS NEEDED

---

Extend the range  
and precision of  
simulations

# OTHER FUTURE IMPROVEMENTS NEEDED

---

Extend the range  
and precision of  
simulations

Compute the wall  
velocity

# OTHER FUTURE IMPROVEMENTS NEEDED

---

Extend the range  
and precision of  
simulations

Compute the wall  
velocity

Model the noise for  
LISA



# OTHER FUTURE IMPROVEMENTS NEEDED

---

Extend the range  
and precision of  
simulations

Compute the wall  
velocity

Model the noise for  
LISA

What could we  
learn from an  
observation of GW  
from PT?