

Self-Interacting Vector DM Through Freeze-In

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Work still in progress

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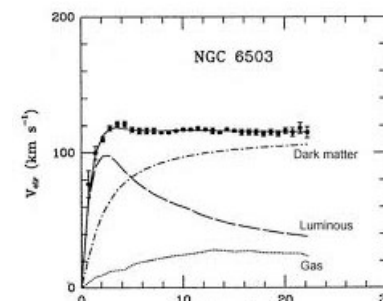
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Motivation

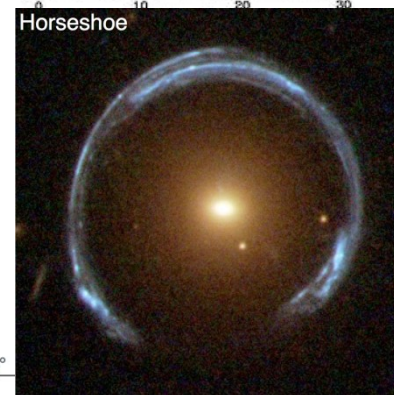
➤ There are already many established evidences for the existence of **dark matter**

- Rotation Curves of Spiral Galaxies

Babcock, 1939, Bosma, 1978; Rubin & Ford, 1980

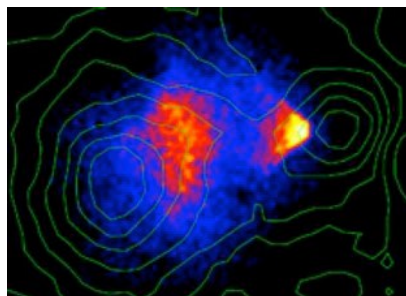


- Gravitational Lensing

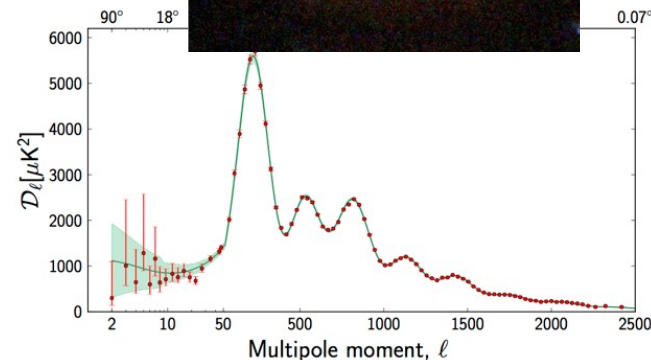


- CMB

- Bullet Clusters



But , they are all **gravitational**



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Motivation

- Currently, the benchmark Dark Matter model is the Collisionless Cold Dark Matter (CCDM)
- CCDM successfully explain all of the above observations, especially for the large scale structure in our Universe
- CCDM meets difficulty in interpreting small scale structures
 - Cusp-Core Problem: Dwarf Galaxies
 - Too Big to Fail Problem:

Motivation

- Possible Solutions: Introduction of DM Self-Interactions

$$0.1 \text{ cm}^2/\text{g} < \sigma_T/m_X < 10 \text{ cm}^2/\text{g}$$

where **transfer cross section** $\sigma_T = \int d\Omega (1 - \cos \theta) \frac{d\sigma}{d\Omega}$

- Constraints:

- **Cluster Ellipticity**

- **Non-Evaporation of Galaxy halo in hot clusters**

- **Bullet Clusters**

- Typical Constraints: $\sigma_T/m_X \leq 1 \text{ cm}^2/\text{g}$

Motivation

- One intriguing mechanism is to consider the DM of broadly **weak scale $1\text{ GeV} \sim 10\text{ TeV}$** , with a light mediator of mass to be **$1\sim 10\text{ MeV}$** .

Long Range Force

- Advantage: Velocity-Dependent Xection, so it is easy for dwarf signal ($v \sim 30\text{ km/s}$) to avoid the cluster constraints ($v \sim 1000\text{ km/s}$)
- We would like to study this scenario in a concrete DM model.

Motivation

➤ Usually, the standard WIMP mechanism to generate DM is through the freeze-out, in which DM is in **thermal equilibrium with the SM particles** at Big Bang, and freeze out at low temperatures $T \sim m_\chi/26$

➤ New Scenario: **Freeze-In**

- Negligible Initial Distribution

- Feeble couplings to SM

- IR dominated: predictability as FO

Vector DM Model

➤ SM + Complex Scalar S + $U(1)_X$ Gauge Boson X + Z_2 Symm.

● S : Unit Charge under $U(1)_X$, but Neutral under SM

● Z_2 Symmetry: Charge Conjugate Symmetry in Dark Sector

$$X_\mu \rightarrow -X_\mu, S \rightarrow S^*,$$

forbids terms $X_\mu B^\mu$ or $X_{\mu\nu} B^{\mu\nu}$.

● After SSB, X is massive and stable due to $Z_2 \rightarrow$ DM Candidate

Vector DM Model

➤ Dark Sector Lagrangian:

$$\mathcal{L}_d = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + \frac{1}{2}(D_\mu S)^\dagger D^\mu S + \mu_S^2|S|^2 - \frac{\lambda_S}{2}|S|^4 - \kappa|S|^2|H|^2,$$

$$D_\mu S \equiv (\partial_\mu + ig_X X_\mu)S$$

κ : Higgs Portal

➤ After SSB:

$$\langle H \rangle \equiv (0, v_H/\sqrt{2})^T \quad \langle S \rangle \equiv v_S/\sqrt{2}$$

$$v_H^2 = \frac{2(\mu_H^2 \lambda_S - \mu_S^2 \kappa)}{\lambda_S \lambda_H - \kappa^2}, \quad v_S^2 = \frac{2(\mu_S^2 \lambda_H - \mu_H^2 \kappa)}{\lambda_S \lambda_H - \kappa^2}.$$

Vector DM Model

➤ After SSB:

● Gauge Boson Mass: $m_X = g_X v_S$

● $H = \begin{pmatrix} H^+ \\ (v_H + \phi_H + i\sigma_H)/\sqrt{2} \end{pmatrix}, \quad S = \frac{1}{\sqrt{2}}(v_S + \phi_S + i\sigma_S).$

● $(\phi_H, \phi_S)^T$ Mass Matrix $\mathcal{M}^2 = \begin{pmatrix} \lambda_H v_H^2 & \kappa v_H v_S \\ \kappa v_H v_S & \lambda_S v_S^2 \end{pmatrix}$

● Physical Mass Eigenstates: $\begin{pmatrix} \phi_H \\ \phi_S \end{pmatrix} = \begin{pmatrix} c_\alpha & -s_\alpha \\ s_\alpha & c_\alpha \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$

$$\kappa = \frac{(m_{h_1}^2 - m_{h_2}^2)s_{2\alpha}}{2v_H v_S}, \quad \lambda_H = \frac{m_{h_1}^2 c_\alpha^2 + m_{h_2}^2 s_\alpha^2}{v_H^2}, \quad \lambda_S = \frac{m_{h_2}^2 c_\alpha^2 + m_{h_1}^2 s_\alpha^2}{v_S^2}.$$

● Parameters: $(m_X, m_{h_2}, \kappa, g_X)$

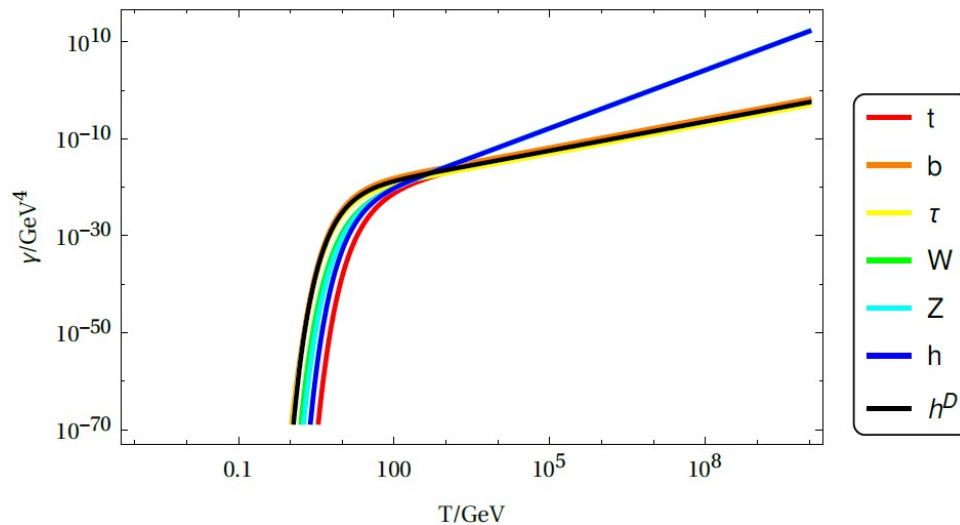
Freeze-In Mechanism

➤ Boltzmann Equation for Freeze-In (SM symm. Broken phase) :

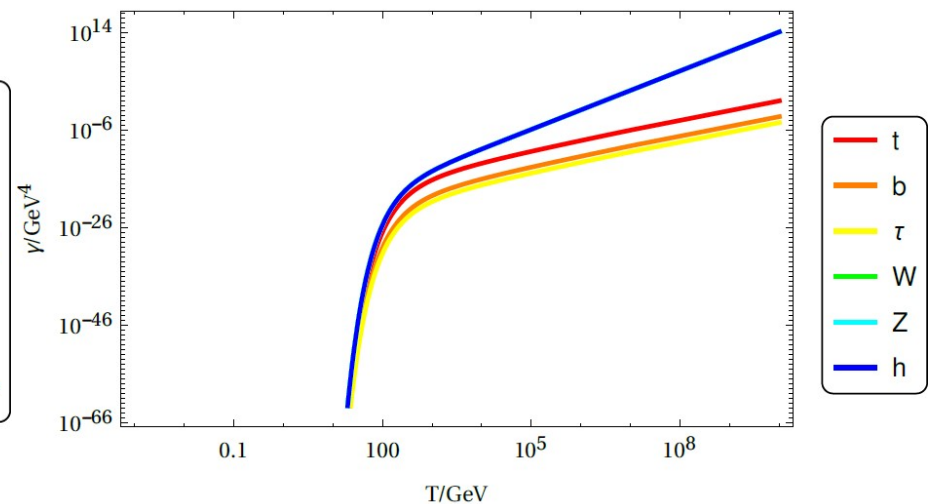
$$xHs \frac{dY_X}{dx} = \sum_f \gamma_f + \gamma_W + \gamma_h + \gamma_Z + \gamma_h^D.$$

Note that all γ 's proportional to κ

$$m_X = 50 \text{ GeV}, \kappa = 1.15 \times 10^{-12}$$

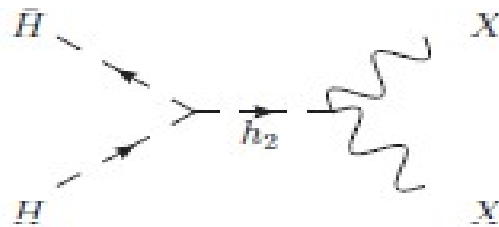


$$m_X = 100 \text{ GeV}, \kappa = 1.04 \times 10^{-11}$$



Freeze-In Mechanism

- At high temperature $T > T_{EW} = 160 \text{ GeV}$, the SM gauge symmetry is recovered, so only the SM Higgs doublet annihilations ($H\bar{H} \rightarrow XX$) contribute



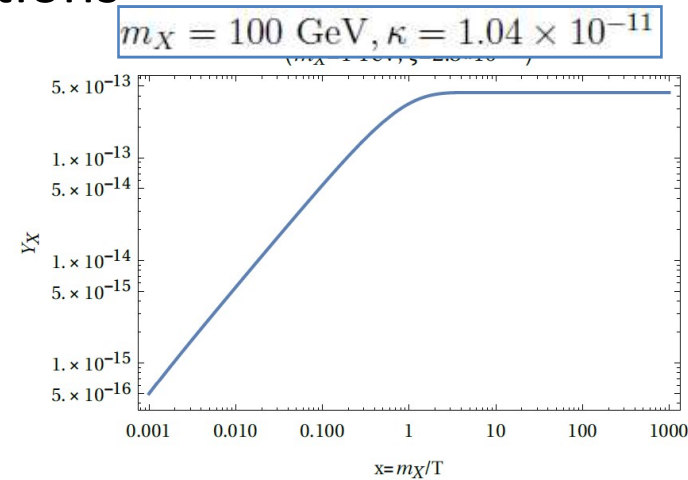
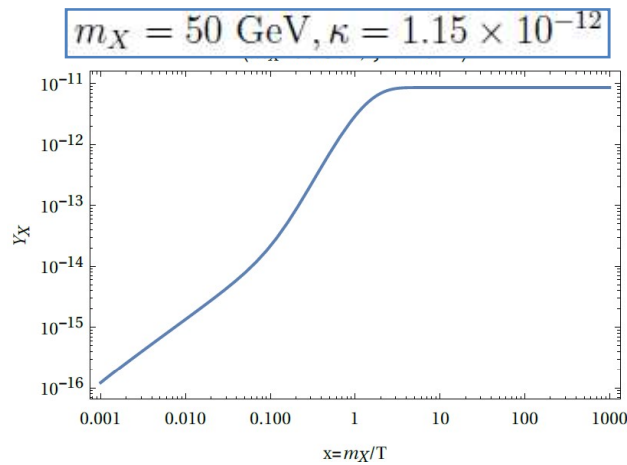
- Boltzmann Equation for Freeze-In is changed to

$$xHs \frac{dY_X}{dx} = \gamma_{H\bar{H}}.$$

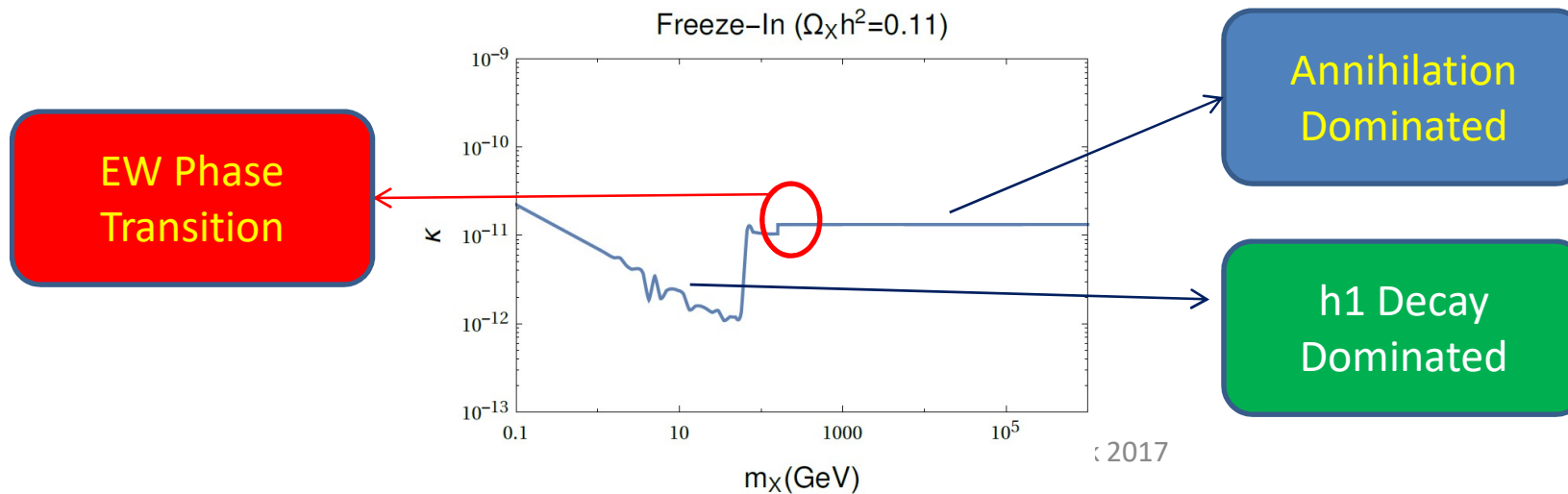
- The EW phase transition effect is important for DM with its mass greater than T_{EW} .

Freeze-In Mechanism

➤ Solution to Boltzmann Equations



➤ Parameter Space



DM Self-Interactions

➤ In order to generate large enough DM Self Interactions, we focus on the parameter space $m_\chi \sim 1 \text{ GeV} - 1 \text{ TeV}$ and $m_{h_2} \leq 100 \text{ MeV}$, so h_2 acts as the light mediator

➤ Effective Yukawa Potential

$$V(r) = -\frac{\alpha_X}{r} e^{-m_{h_2} r}$$

➤ Schrodinger Equation for Partial Waves

$$\frac{1}{r^2} \frac{d}{dr} \left(r^2 \frac{dR_\ell}{dr} \right) + \left(k^2 - \frac{\ell(\ell+1)}{r^2} - 2\mu V(r) \right) R_\ell = 0$$

with boundary condition $\lim_{r \rightarrow \infty} R_\ell(r) \propto \cos \delta_\ell j_\ell(kr) - \sin \delta_\ell n_\ell(kr)$

➤ Transfer Xection: $\frac{\sigma_T k^2}{4\pi} = \sum_{\ell=0}^{\infty} (\ell+1) \sin^2(\delta_{\ell+1} - \delta_\ell)$ with $k = \mu v$

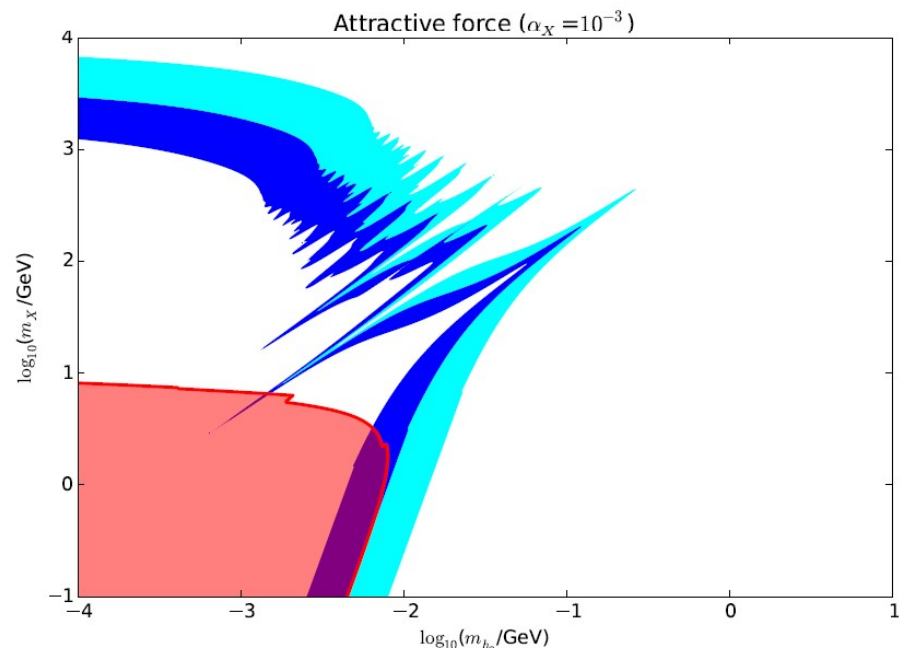
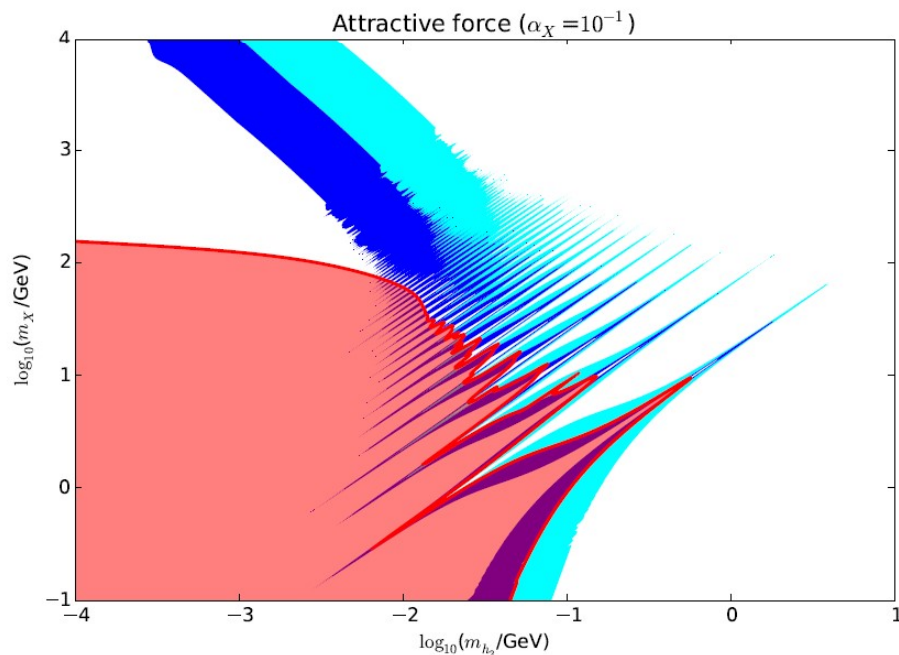
DM Self-Interactions

➤ Numerical Results

Cyan : $0.1 \text{ cm}^3/\text{g} < \sigma_T/mX < 1 \text{ cm}^3/\text{g}$

Blue : $1 \text{ cm}^3/\text{g} < \sigma_T/mX < 10 \text{ cm}^3/\text{g}$

Red: Excluded by Cluster constraints



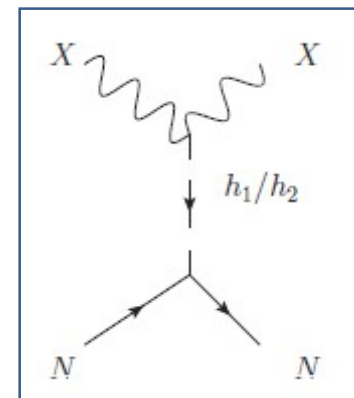
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DM Direct Detection

➤ Process: $XN \rightarrow XN$

➤ Total Cross Section

$$\sigma_{XN} = \frac{\kappa^2 f_N^2 m_X^2 m_N^2 \mu_{XN}^2}{\pi m_{h_1}^4 m_{h_2}^4}$$



➤ Differential Cross Section

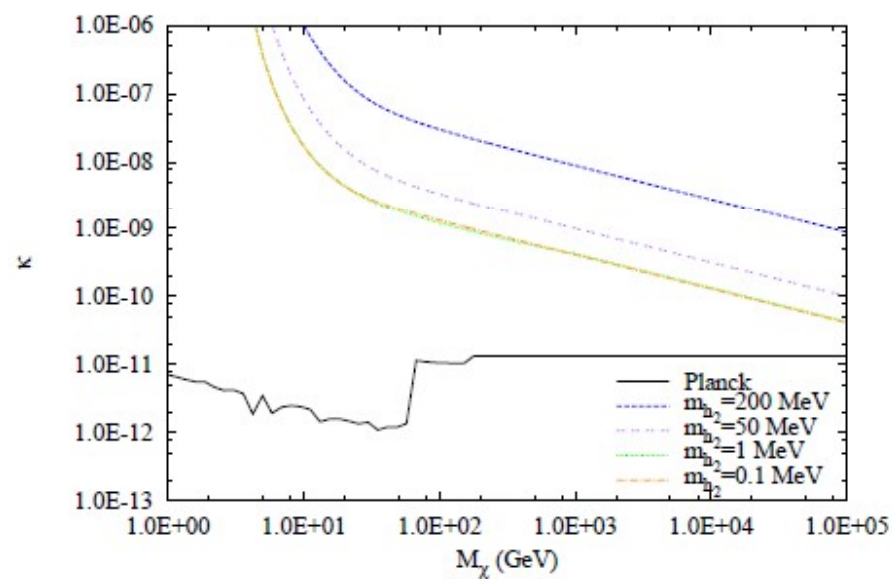
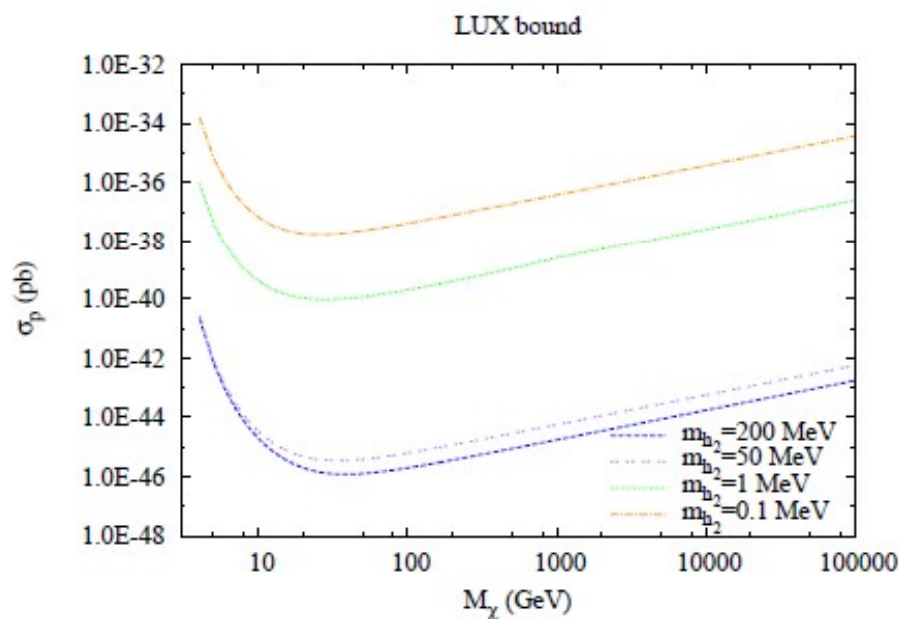
$$\frac{d\sigma_{XN}}{dq^2} = \frac{\sigma_{XN}}{4\mu_{XN}^2 v^2} G(q^2)$$

where

$$G(q^2) = \frac{m_{h_2}^2 (m_{h_2}^2 + 4\mu_{XN}^2 v^2)}{(q^2 + m_{h_2}^2)^2}$$

DM Direct Detection

- Numerical Results for the LUX upper bounds: **Poisson Statistics** by assuming no candidate nucleus recoil events



DM Indirect Detection

➤ **BBN Constraints:** successful prediction of element abundance requires either very short h_2 lifetime or very small density of h_2 when BBN due to h_2 decay

➤ Previous Fitting shows that

$$\tau_{h_2} < 10^{-4} \text{ s} \quad \text{or} \quad \Omega_{h_2} h^2 < 10^{-5}$$

➤ Our model predicts lifetime of h_2 is always larger than 10^{-4} s when $m_{h_2} < 100 \text{ MeV}$, so only **the density option** can be realized

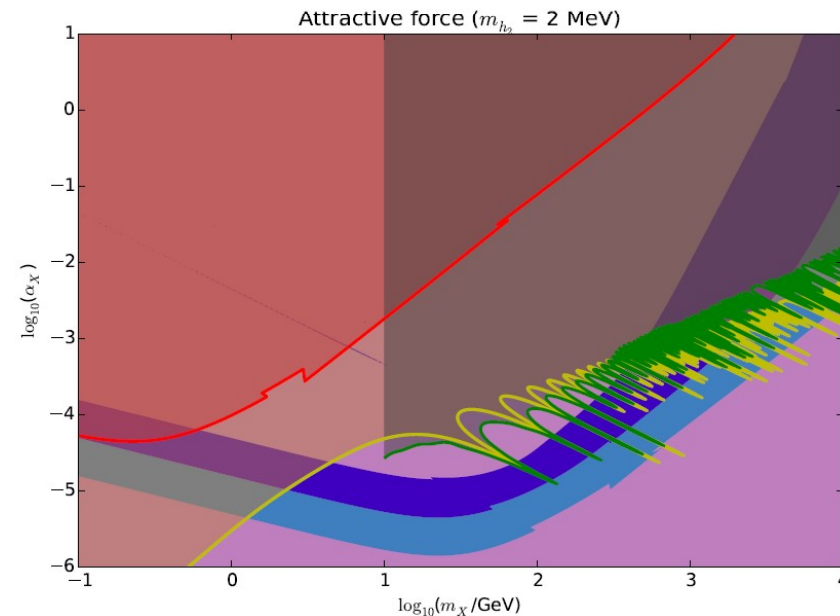
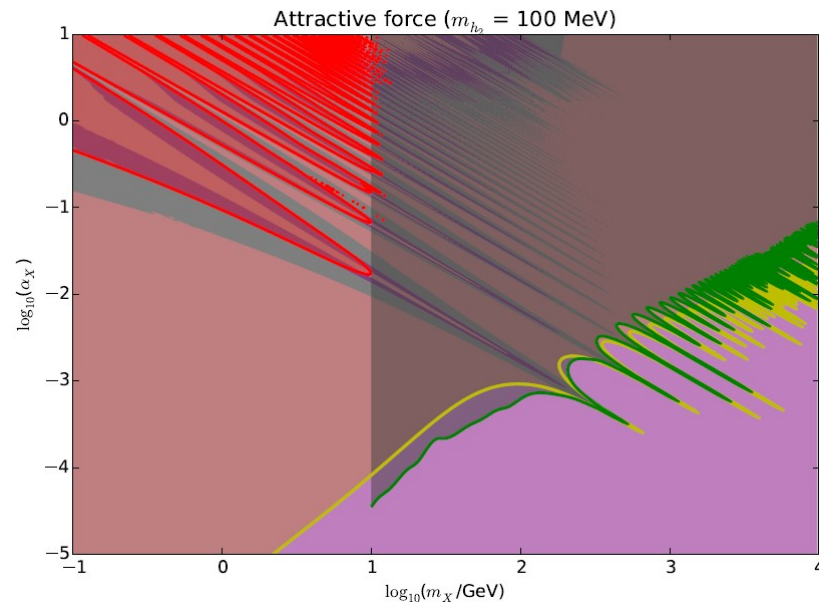
DM Indirect Detection

- For DM Indirect Detection, we use the data from Fermi-LAT dwarf galaxy gamma-ray observation, AMS-02 e^+e^- , and recent Planck data on the CMB power spectrum
- When h_2 's lifetime is longer than the age of the Universe, we also consider the diffuse gamma-ray constraints

Numerical Result

➤ $m_{h_2} > 1 \text{ MeV}$

- ◆ Dominant Decay Channel: e^+e^- pair
- ◆ Typical Lifetime: $10^4 \text{ s} < t_{h_2} < 10^{12} \text{ s}$
- ◆ Constraints: Cluster, BBN, AMS-02, CMB



➤ All the parameter space is excluded by BBN

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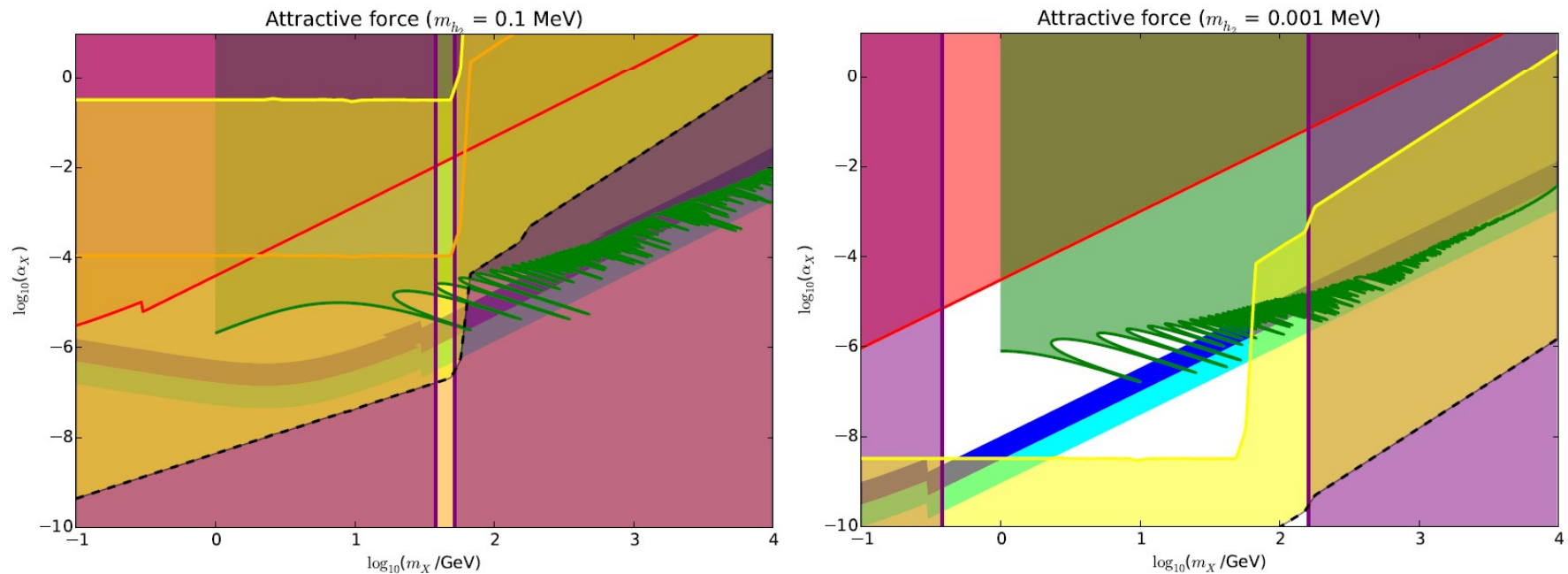
Numerical Result

➤ $m_{h2} < 1 \text{ MeV}$

◆ Dominant Decay Channel: **diphotons**

◆ Typical Lifetime: $t_{h2} > 10^{12} \text{ s}$

◆ Constraints: **Cluster**, **BBN**, **Fermi-LAT**, **CMB**, **Diffuse Gamma**



➤ Only when $m_{h2} \sim \text{keV}$, we find regions satisfying all constraints

Summary

- The VDM model via the Higgs portal is investigated
- We focus on the freeze-in region, in which $m_\chi \sim 1 \text{ GeV} - 1 \text{ TeV}$ and $m_{h_2} \leq 100 \text{ MeV}$, so dark Higgs can act as the **light mediator** to enhance the **DM self interactions** and solve the cosmological small scale problem
- We find that **direct detections** do not constrain the model much, but the **indirect detections** restrict m_{h_2} should be of or smaller than $O(\text{keV})$