

Stability of the inert vacuum state beyond tree level

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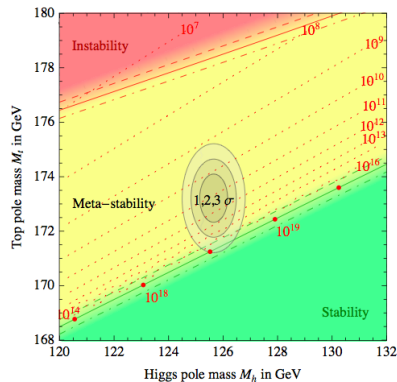
SCALARS 2015, Warsaw, Poland

based on: BŚ, JHEP 1507 (2015) 118,
P. M. Ferreira (ISEL and CFTC, Lisbon), BŚ, arXiv:1511.02879

Aim of the talk

There is a Higgs boson with mass $M_h \approx 125$ GeV!

- measurement of the Higgs mass allows to localize the SM in the phase diagram
- new interactions modify the picture
- **what is the influence of additional scalars on the vacuum structure?**



from: Butazzo et al., JHEP 1312 (2013) 089

[see also: V. Branchina et al., PRL 111 (2013) 241801, Z. Lalak, M. Lewicki, P. Olszewski, JHEP 1405 (2014) 119]

Inert Doublet Model and vacuum stability

IDM = a two-Higgs-doublet model with an **exact \mathbb{Z}_2 symmetry**

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→ one-loop SM potential,
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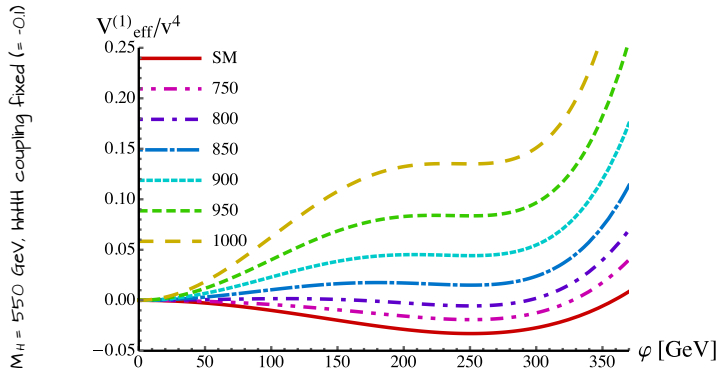


How does loop-level vacuum structure look like?

→ compare values of the full one-loop potential at different minima

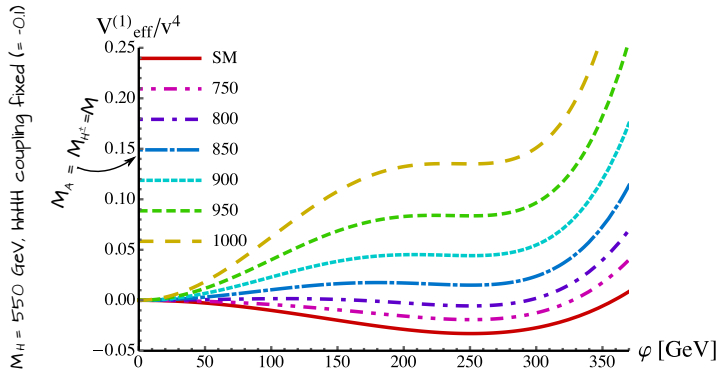
Vacuum stability with heavy scalars

[BŚ, JHEP 1507 (2015) 118]



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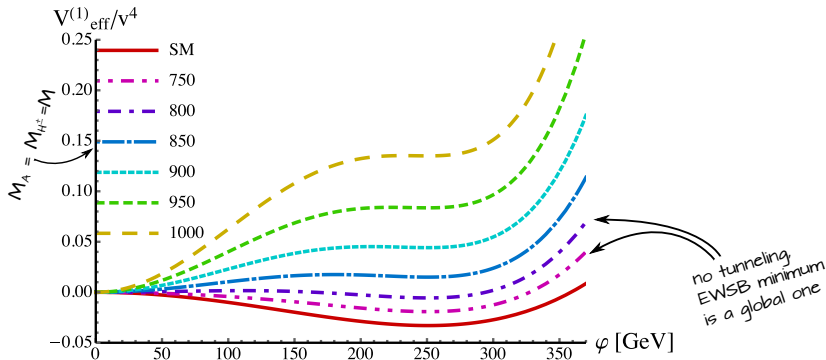
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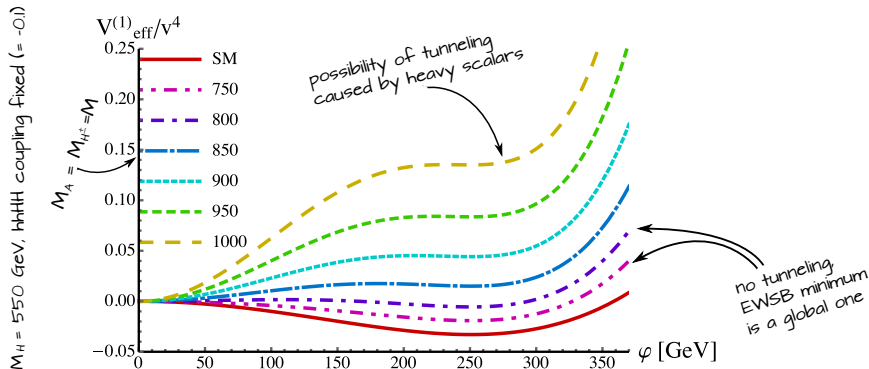
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$M_H = 550$ GeV, $hhHH$ coupling fixed ($= -0.1$)



Vacuum stability with heavy scalars

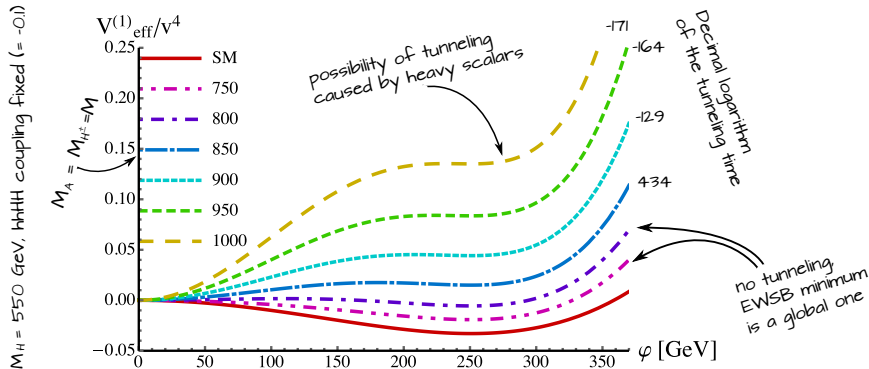
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- maximum at $\varphi = 0$ becomes a minimum

Vacuum stability with heavy scalars

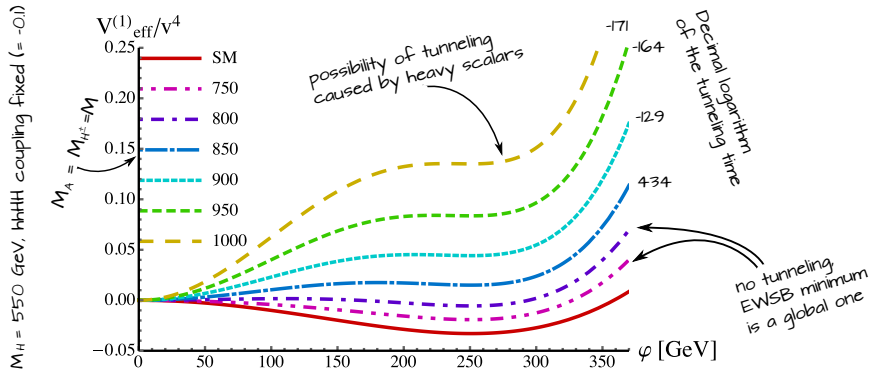
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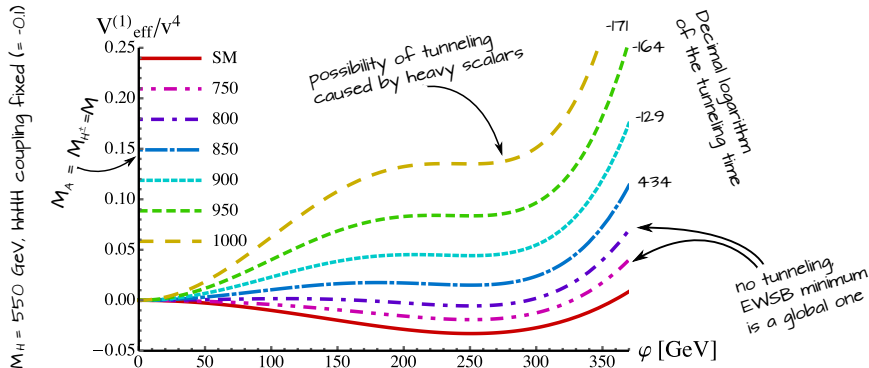
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- for heavy inert scalars – EWSB minimum is highly unstable

Vacuum stability with heavy scalars

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- maximum at $\phi = 0$ becomes a minimum
- **for heavy inert scalars – EWSB minimum is highly unstable**
- instability only when big splittings among inert scalars – in IDM excluded by EWPT and DM relic density

Vacuum structure: inert vs inert-like

Inert extremum

$$\langle \phi_S \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}, \quad \langle \phi_D \rangle = 0$$

Inert-like extremum

$$\langle \phi_S \rangle = 0, \quad \langle \phi_D \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v \end{pmatrix}$$

Can tree-level vacuum structure be inverted by loop corrections?

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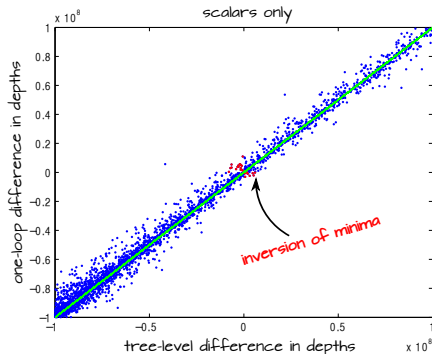
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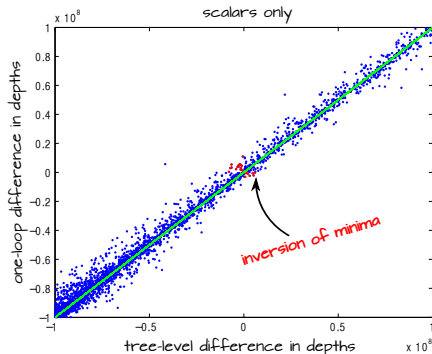
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Inert-like extremum

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Can tree-level vacuum structure be inverted by loop corrections?

- the minima can be inverted by loop corrections
- it only happens when they are close in energies



- Additional scalars do influence the vacuum structure of a model
- Loop contributions may destabilize the SM-like vacuum – not the case in the IDM but has to be checked
- In multi-scalar models the vacuum structure can be rearranged at loop level – sometimes it is crucial to use the one-loop effective potential

Inert Doublet Model (IDM)

[N. G. Deshpande, E. Ma, PRD 18 (1978) 2574, J. F. Gunion, H. E. Haber, G. Kane, S. Dawson, *The Higgs Hunter's Guide*, 1990 Addison-Wesley, R. Barbieri, L. J. Hall, V. S. Rychkov, PRD 74 (2006) 015007, I. F. Ginzburg, K. A. Kanishev, M. Krawczyk, D. Sokołowska, PRD 82 (2010) 123533]

IDM – a 2HDM with the scalar potential (real parameters) for ϕ_S and ϕ_D doublets:

$$V = -\frac{1}{2} \left[m_{11}^2 (\phi_S^\dagger \phi_S) + m_{22}^2 (\phi_D^\dagger \phi_D) \right] + \frac{1}{2} \left[\lambda_1 (\phi_S^\dagger \phi_S)^2 + \lambda_2 (\phi_D^\dagger \phi_D)^2 \right] \\ + \lambda_3 (\phi_S^\dagger \phi_S) (\phi_D^\dagger \phi_D) + \lambda_4 (\phi_S^\dagger \phi_D) (\phi_D^\dagger \phi_S) + \frac{1}{2} \lambda_5 \left[(\phi_S^\dagger \phi_D)^2 + (\phi_D^\dagger \phi_S)^2 \right]$$

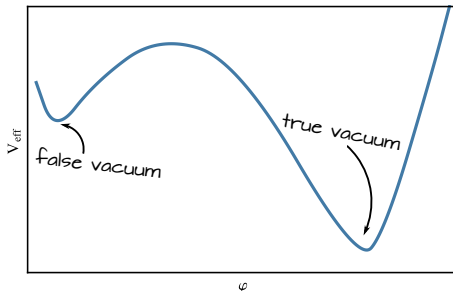
- \mathbb{Z}_2 -type symmetry **D**: $\phi_D \rightarrow -\phi_D$, $\phi_S \rightarrow \phi_S$
- Yukawa interactions: type I (only ϕ_S couples to fermions)
- \mathcal{L} – **D-symmetric**
- **D-symmetric vacuum state** $\langle \phi_S \rangle = \frac{v}{\sqrt{2}}$, $\langle \phi_D \rangle = 0$

\Rightarrow **EXACT D-symmetry**

- **Vacuum stability:** positivity, stability of Inert vacuum
- **Perturbative unitarity:** eigenvalues Λ_i of the high-energy scattering matrix fulfill the condition $|\Lambda_i| < 8\pi$
- **Electroweak Precision Tests** (EWPT): S and T within 2σ ($S = 0.03 \pm 0.09$, $T = 0.07 \pm 0.08$, with correlation of 87%)
- **LEP bounds** on the scalars' masses
- **LHC:** $M_H = 125 \text{ GeV}$, $\text{Br}(h \rightarrow \text{inv})$, $\Gamma(h)$, $R_{\gamma\gamma}$
- **DM constraints:** Planck results on DM relic density

Motivation

$$\delta V_{\text{eff}} = \text{[diagram 1]} + \text{[diagram 2]} + \text{[diagram 3]} + \dots$$

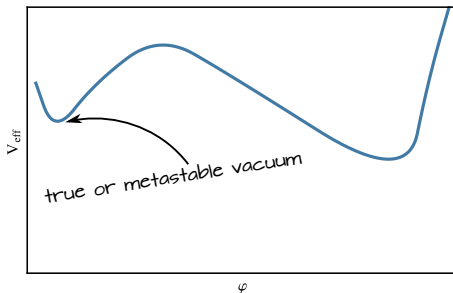


[in the IDM: A. Goudelis, B. Herrmann, and O. Stål, JHEP 1309 (2013) 106, M. Kadastik, K. Kannike, A. Racioppi, and M. Raidal, JHEP 1205 (2012) 061, N. Khan and S. Rakshit, arXiv:1503.03085.]

Motivation

$$\delta V_{\text{eff}} = \text{[Feynman diagrams]} + \dots$$

Idea:
introduce new scalars
to balance the top
contribution at large
energies



[in the IDM: A. Goudelis, B. Herrmann, and O. Stål, JHEP 1309 (2013) 106, M. Kadastik, K. Kannike, A. Racioppi, and M. Raidal, JHEP 1205 (2012) 061, N. Khan and S. Rakshit, arXiv:1503.03085.]

Vacuum stability

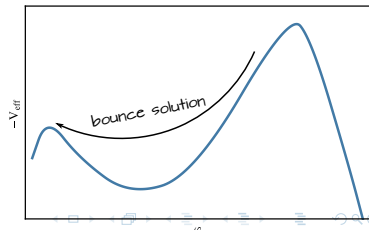
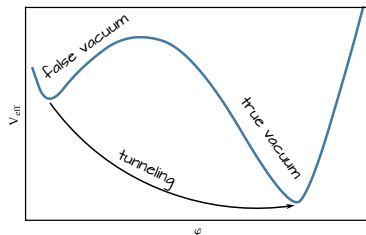
vacuum = ground state of a theory

- **true** vacuum = global minimum of the potential
- **metastable** vacuum = local minimum with long* lifetime
- **unstable** vacuum = local minimum with short* lifetime

*short/long = shorter/longer than the age of the Universe, $T_U \approx 14 \cdot 10^9$ years

If more than one minimum – tunneling possible

- described semi-classically
- τ lifetime of vacuum, in units of T_U



Tunneling time

- Bounce equation:

$$\ddot{\varphi} + \frac{3}{s}\dot{\varphi} = \frac{\partial V_{\text{eff}}^{(1)}(\varphi)}{\partial \varphi},$$

boundary conditions: $\dot{\varphi}_B(0) = 0$, and $\varphi_B(\infty) = v$.

- solved numerically by the **undershoot–overshoot method**
- lifetime of a vacuum

$$\tau = \frac{e^{S_E}}{\varphi_0^4 T_U^4},$$

where $\varphi_0 = \varphi(0)$, and

$$S_E = 2\pi^2 \int ds s^3 \left[\frac{1}{2} \dot{\varphi}_B^2(s) + V(\varphi_B(s)) \right].$$

Effective potential

[S. R. Coleman, E. J. Weinberg, PRD 7 (1973) 1888, G. Gil, P. Chankowski, and M. Krawczyk, PLB 717 (2012) 396]

To take into account quantum corrections we analyse one-loop effective potential

$$V_{\text{eff}} = V^{(0)} + \delta V = V^{(0)} + \text{[one-loop diagrams]} + \dots$$

- in 2HDM – in principle all scalar fields allowed on external legs
 $\Rightarrow V_{\text{eff}}$ – multivariable function
- **assumption: inert scalars are heavy, can be integrated out**
 \Rightarrow inert scalars allowed only in the loops, Higgs field on external legs
- on-shell (OS) renormalized potential

Effective potential in OS scheme

The effective potential:

$$V_{\text{eff}}^{(1)} = V_{\text{eff}}^{(0)} + \delta V_{\text{CW}} + \delta V + \text{const.}$$

- $V_{\text{eff}}^{(0)}$ – tree-level effective potential

$$V_{\text{eff}}^{(0)} = -\frac{1}{4}m_{11}^2\varphi^2 + \frac{1}{8}\lambda_1\varphi^4,$$

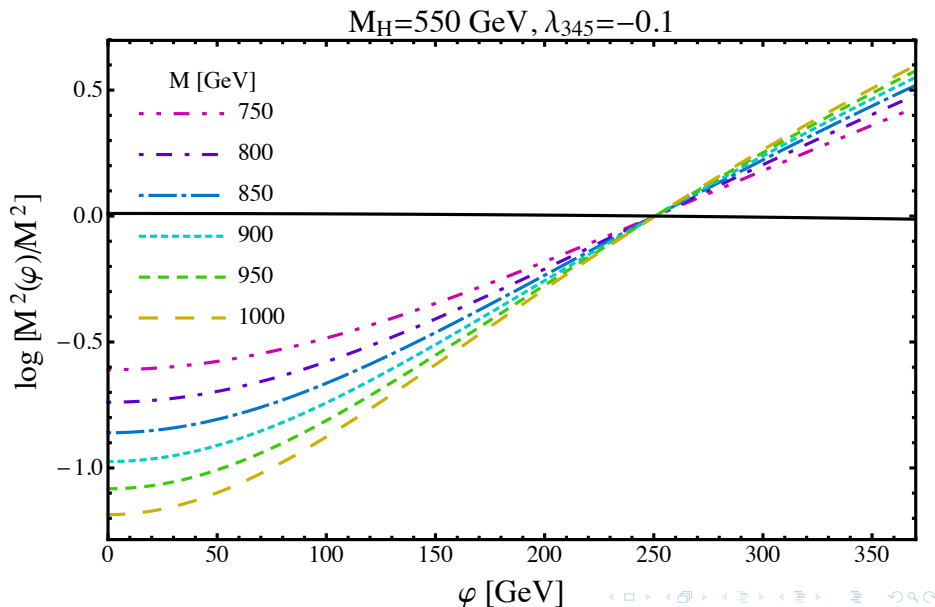
- δV_{CW} – CW potential

$$\delta V_{\text{CW}} = \sum_i \frac{f_i}{64\pi^2} M_i(\varphi)^4 \left[-\frac{2}{\epsilon} + \gamma_E - C_i + \log \left(\frac{M_i(\varphi)^2}{4\pi\mu^2} \right) \right],$$

- δV – counterterm potential in OS scheme

OS scheme: one-loop tadpole of h is cancelled, the Higgs propagator has a pole at M_h with a residue equal to i

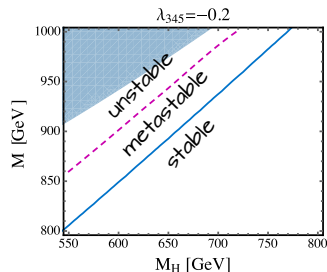
Perturbativity of the expansion



EW metastability in the IDM parameter space

Where in the parameter space is metastability realised?

For $M_A = M_{H^\pm} = M$



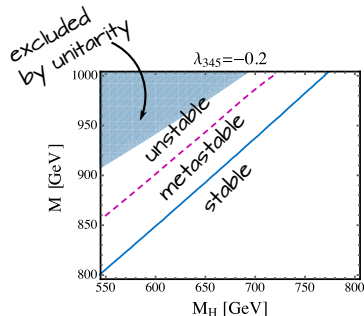
[T. Hambye, F.-S. Ling, L. Lopez Honorez, and J. Rocher, JHEP 0907 (2009) 090, arXiv:0903.4010]

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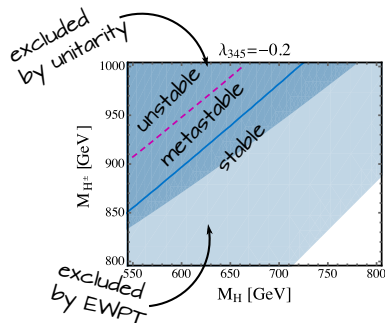
- meta/instability when relatively large splitting between M_H and M ,
 $M^2 - M_H^2 \sim \lambda_{\text{scalar}} v^2$
 \Rightarrow some scalar couplings large
- consistent with perturbative unitarity
- EWPT not constraining ($T = 0$)
- however, DM relic abundance requires small splittings, $\mathcal{O}(10 \text{ GeV})$
 \rightarrow **inconsistent with Planck measurements for heavy DM**



EW metastability in the IDM parameter space

For $M_A = M_H + 1$, M_{H^\pm} – free

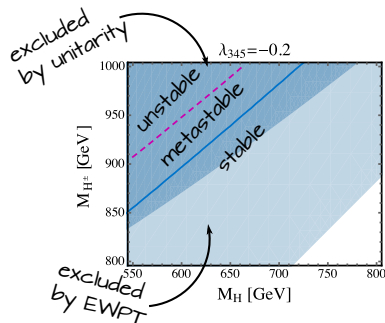
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- excluded by unitarity, EWPT, and relic density



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If IDM is in agreement with theoretical and experimental constraints

⇒ it is free from meta- or unstable vacuum around the EW scale.

- 1 V has to be bounded from below

$$\lambda_1 > 0, \quad \lambda_2 > 0, \quad \lambda_3 + \sqrt{\lambda_1 \lambda_2} > 0, \quad \lambda_{345} + \sqrt{\lambda_1 \lambda_2} > 0,$$

[M. Krawczyk et al., PRD 82 (2010) 123533, see also: A. Barroso et al., JHEP 1306 (2013) 045, J.Phys.Conf.Ser. 447 (2013) 012051, [1305.1235]]

Vacuum stability – the IDM picture

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- 2 The Inert state has to be a minimum of the potential

$$M_{\text{scalar}}^2 \geq 0$$

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- ① V has to be bounded from below

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$$M_{\text{scalar}}^2 \geq 0$$

- ③ The Inert state has to be the **global minimum** of the potential

[M. Krawczyk et al., PRD 82 (2010) 123533, see also: A. Barroso et al., JHEP 1306 (2013) 045, J.Phys.Conf.Ser. 447 (2013) 012051, [1305.1235]]

Possible extrema of the potential

[N. G. Deshpande, E. Ma, PRD 18 (1978) 2574, I. F. Ginzburg, K. A. Kanishev, M. Krawczyk, D. Sokołowska, PRD 82 (2010) 123533, see also: P. M. Ferreira, R. Santos, A. Barroso, Phys.Lett.B 603 (2004), Phys.Lett. B632 (2006) 684-687]

Not realized at present

EW symmetric, Charge breaking

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“standard” choice for 2HDM (MSSM), no DM candidate

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Inert extremum (I_1)

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our choice, DM candidate

Inert-like extremum (I_2)

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massless fermions

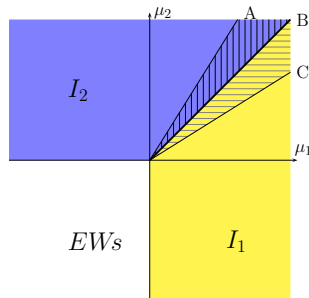
Phase diagram and coexistence of minima

[BŚ, PRD 88 (2013) 055027]

- Inert and Inert-like minima can coexist (at the tree level)
- demand that Inert is global minimum \Rightarrow compare energies

$$\frac{m_{11}^2}{\sqrt{\lambda_1}} > \frac{m_{22}^2}{\sqrt{\lambda_2}} \xrightarrow{+\text{constr.}} m_{22}^2 \leq 9 \cdot 10^4 \text{ GeV}^2$$
$$(M_h^2 = m_{11}^2 = \lambda_1 v^2)$$

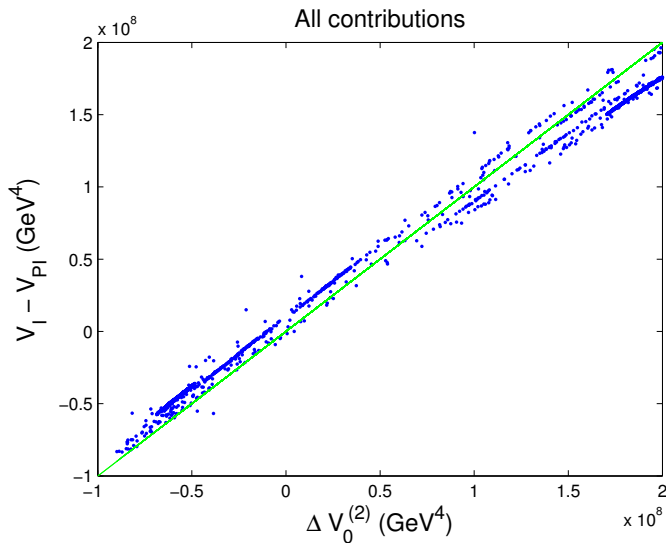
- or possibility of metastability at the tree-level



$$R > 1$$

from D. Sokołowska,
PoS ICHEP2010:457

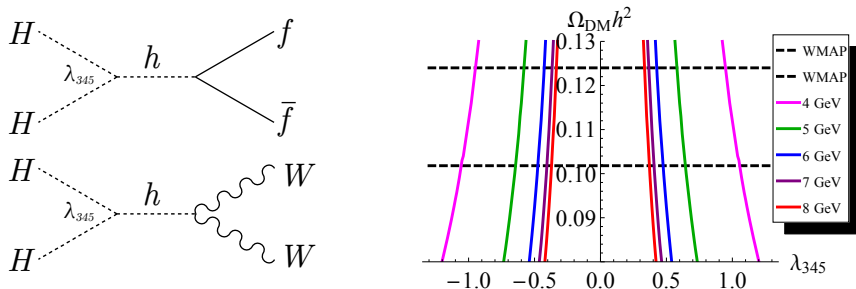
All contributions included



Relic density constraints

[E. M. Dolle, S. Su, Phys. Rev. D 80 (2009) 055012, L. Lopez Honorez, E. Nezri, F. J. Oliver, M. Tytgat, JCAP 0702 (2007) 028, D. Sokolowska, arXiv:1107.1991 [hep-ph]]

$$0.1118 < \Omega_{DM} h^2 < 0.1280 \quad (3\sigma, \text{PLANCK})$$

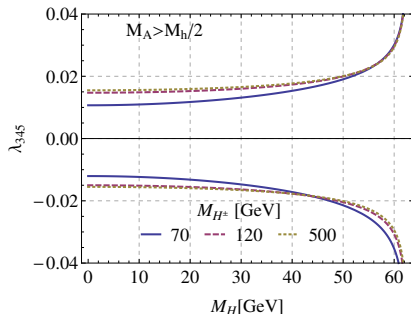
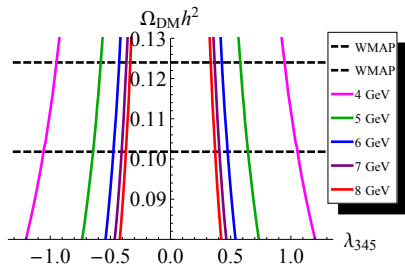


From D. Sokolowska, arXiv:1107.1991

Possible masses:

- **light DM:** $M_H \lesssim 10$ GeV
- **intermediate DM:** $40 \text{ GeV} \lesssim M_H \lesssim 160$ GeV
- **heavy DM:** $M_H \gtrsim 500$ GeV

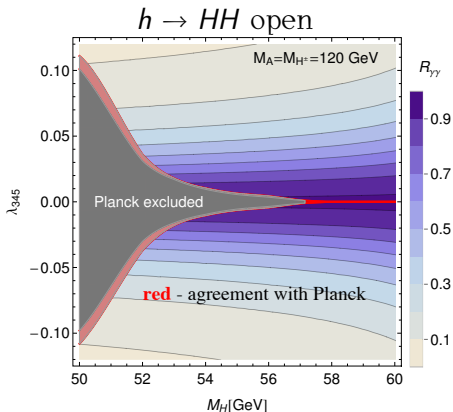
Light DM, $M_H \lesssim 10$ GeV



- correct relic density $\Rightarrow |\lambda_{345}| \sim \mathcal{O}(0.5)$
- too small $\lambda_{345} \Rightarrow$ overclosing the Universe
- $R_{\gamma\gamma} > 0.7 \Rightarrow |\lambda_{345}| < 0.04$

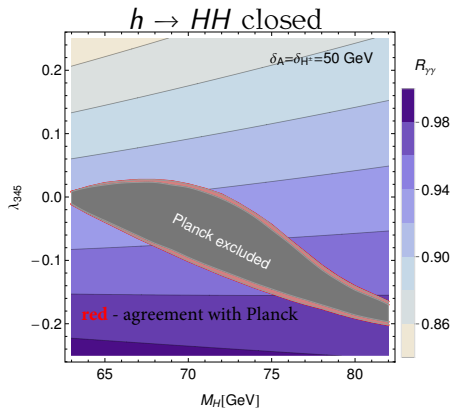
Light DM excluded

[Planck update: D. Sokołowska, P. Swaczyna, 2014]



$50 \text{ GeV} < M_H < M_{h/2}, M_A = M_{H^\pm} = 120 \text{ GeV}$

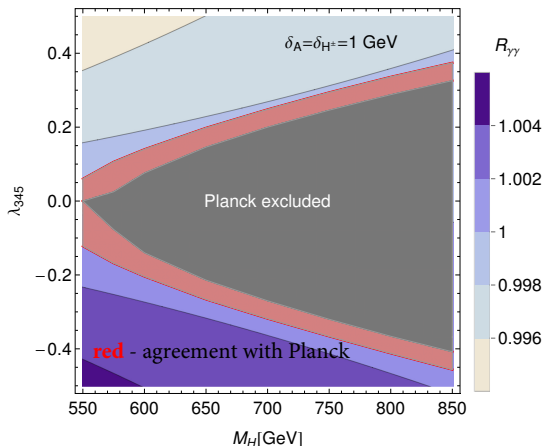
$R_{\gamma\gamma} > 0.7$ & PLANCK
 $\Rightarrow M_H > 53 \text{ GeV}$



$M_{h/2} < M_H < 83 \text{ GeV}, M_A = M_{H^\pm} = M_H + 50 \text{ GeV}$

agreement with PLANCK and
 $R_{\gamma\gamma} > 0.7$, but then $R_{\gamma\gamma} < 1$

$M_H > 500 \text{ GeV}$, $M_A = M_{H^\pm} = M_H + 1 \text{ GeV}$ (because of S, T)



Agreement with PLANCK and $R_{\gamma\gamma} \approx 1$.