The minimal curvaton-higgs (MCH) model

Rose Lerner

Based on: Kari Enqvist, RL, Tomo Takahashi [arXiv:1310.1374] Kari Enqvist, RL, Stanislav Rusak [arXiv:1308.3321] Kari Enqvist, Daniel Figueroa, RL [arXiv:1211.5028] Kari Enqvist, RL, Olli Taanila, Anders Tranberg [1205.5446] RL, Scott Melville, [1402.3176] RL, Anders Tranberg [to appear]

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Overview

Motivation Perturbations in the CMB Minimal models Curvaton models

The MCH model Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NL}

Initial conditions

Summary

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Perturbations in the CMB Minimal models Curvaton models

CMB perturbations



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CMB perturbations



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Perturbations in the CMB Minimal models Curvaton models

What does a complete cosmological model require?

Observational:

- inflation
- perturbations: ζ , n, r, f_{NL} ...
- reheating
- dark matter
- baryogenesis
- ▶ ...

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Perturbations in the CMB Minimal models Curvaton models

What does a complete cosmological model require?

Observational:

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Theoretical:

...

- specify all fields in the theory
- consider all interactions
- quantum corrections
- explain initial conditions

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- inflation
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- reheating

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Theoretical:

. . .

- specify all fields in the theory
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- quantum corrections
- explain initial conditions

Minimal extensions to the standard model allow precise calculations of cosmological processes

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Where is SUSY?



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What is a curvaton model?

Single field inflaton: A single field ϕ both drives inflation and is the source of the perturbations.

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What is a curvaton model?

Single field inflaton: A single field ϕ both drives inflation and is the source of the perturbations.

Curvaton paradigm:

One field ϕ drives inflation but has negligible perturbations; a second field σ is the source of perturbations but is negligible during inflation.

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Energy densities in the curvaton paradigm



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Why study curvaton models?

because they exist!

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Why study curvaton models?

- because they exist!
- because they can give measurable non-Gaussianity and isocurvature

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Why study curvaton models?

- because they exist!
- because they can give measurable non-Gaussianity and isocurvature
- ▶ because light scalar fields (m < H) might exist and it is important to calculate their consequences

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- because the curvaton mechanism gives more freedom for the inflation model

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Perturbations in the CMB Minimal models Curvaton models

Why study curvaton models?

- because they exist!
- because they can give measurable non-Gaussianity and isocurvature
- ▶ because light scalar fields (m < H) might exist and it is important to calculate their consequences
- because the curvaton mechanism gives more freedom for the inflation model
- because they have interesting, constrainable dynamics after inflation

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

The minimal curvaton-higgs (MCH) model

MCH Lagrangian

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{2}\partial_{\mu}\sigma\partial^{\mu}\sigma + \frac{1}{2}m_{\sigma}^{2}\sigma^{2} + \frac{\lambda}{4!}\sigma^{4} + \frac{1}{2}g^{2}\sigma^{2}\Phi^{\dagger}\Phi$$

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- ▶ assume $\sigma \rightarrow -\sigma$ symmetry
- assume $\lambda = 0$
- assume instant inflaton decay
- free parameters: $g, m_{\sigma}, H_*, \sigma_*$

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Consequences of coupling g

• correction to $V(\sigma)$

$$\Delta V(\sigma) = \frac{\left(g^2 \sigma^2 + m_h^2\right)^2}{64\pi^2} \log\left(\frac{g^2 \sigma^2 + m_h^2}{\mu^2}\right)$$

[choose
$$\mu = m_h = 126 \text{ GeV}$$
]

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 $\blacktriangleright~\sigma$ can feel any thermal background of Higges

$$m_\sigma^2
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[choose $\mu = m_h = 126 \text{ GeV}]$

• σ can feel any thermal background of Higges

$$m_\sigma^2
ightarrow m_\sigma^2 + rac{1}{12} g^2 T^2$$

▶ homogeneous σ can decay: $\Gamma_{eff} = \Gamma_{NP} + \Gamma_{pert} + \Gamma_5$

- 1. non-perturbative decay
- 2. perturbative scattering with thermal bath
- 3. dimension-5 operators

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Decay 1: non-perturbative decay

Summary

- after inflation, higgs is thermalised and gains large thermal mass $\propto g_{\tau} T$, where $g_{\tau}^2 = 0.1$
- curvaton couples to higgs and could also get a thermal mass
- ▶ these thermal masses block resonant preheating until *T* falls

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Decay 1: Broad and narrow resonances

- After inflation, usually in broad resonance regime, $q(t) = \left(\frac{g\Sigma(t)}{2m_{\sigma}}\right)^2 \gg 1$
- We found that the broad resonance is almost always blocked
- Curvaton amplitude $\Sigma(t)$ decreases and we eventually reach narrow resonance region with $q \ll 1$
- narrow resonance is a continuous process; excites modes within a thin momentum band
- this is where we start our (outline) calculation
- ► assume we have already calculated the decaying Σ(t) and form of oscillations in the relevant background.

Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Decay 1: The narrow resonance

• Higgs equation of motion: $\ddot{\phi}_{\alpha} + 3H\dot{\phi}_{\alpha} + \left(\frac{k^2}{a^2} + g^2\Sigma^2(t)\sin^2\left(m_{\sigma}t + \frac{\pi}{8}\right) + g_{\tau}^2T^2\right)\phi_{\alpha} = 0$

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

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- conservation of energy: $2m_{\sigma} = 2E(k)$

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

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- conservation of energy: $2m_{\sigma} = 2E(k)$
- energy of produced higgs: $E(k) = \frac{k^2}{a^2} + 4q(t)m_{\sigma}^2 \sin^2\left(m_{\sigma}t + \frac{\pi}{8}\right) + g_{\tau}^2 T^2$

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 Require: g_{\tau}^2 T^2 + 4q(t)m_{\sigma}^2 \sin^2 (m_{\sigma}t + \frac{\pi}{8}) \le m_{\sigma}^2

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- Remember that $q \ll 1$

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- conservation of energy: $2m_{\sigma} = 2E(k)$
- energy of produced higgs: $E(k) = \frac{k^2}{a^2} + 4q(t)m_{\sigma}^2 \sin^2\left(m_{\sigma}t + \frac{\pi}{8}\right) + g_{\tau}^2 T^2$
- Require: $g_{\tau}^2 T^2 + 4q(t)m_{\sigma}^2 \sin^2\left(m_{\sigma}t + \frac{\pi}{8}\right) \le m_{\sigma}^2$
- Remember that $q \ll 1$
- ▶ Thus, narrow resonance can only occur for $T \leq \frac{m_{\sigma}}{g_{\tau}}$

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Decay 1: Thermal blocking

From previous slide

$$g_{\tau}^2 T^2 + 4q(t)m_{\sigma}^2 \sin^2\left(m_{\sigma}t + \frac{\pi}{8}\right) \leq m_{\sigma}^2$$

Notes

- If the higgs had no coupling to the thermal background $(g_{\tau} = 0)$, then there would be no blocking of the resonance!
- Rate of energy transfer typically very slow
- Thermal blocking typically lasts for a huge number of oscillations
- The curvaton's thermal mass modifies $\Sigma(t)$ (see paper)
- Without thermal blocking, the curvaton would quickly disappear and may not be a good curvaton candidate

Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Decay 2: perturbative scattering with thermal bath

Simple calculation:

$$\Gamma_{pert} = \frac{1}{576\pi} \frac{g^4 T^2}{m_{\sigma}(T)}$$

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Decay 2: perturbative scattering with thermal bath

Simple calculation:

$$\Gamma_{pert} = \frac{1}{576\pi} \frac{g^4 T^2}{m_{\sigma}(T)}$$

- process efficient at $\Gamma(t) \ge H(t)$
- $H \propto T^2$
- ▶ so if $m_{\sigma}(T) = m_{\sigma}$, occurs immediately or never!
- if $m_{\sigma}(T) = \frac{1}{\sqrt{12}}gT$, efficient process if

$$g \geq 4.9 g_*^{1/8} \left(rac{m_\sigma}{M_{_{Pl}}}
ight)^{1/4}$$

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Decay 2: perturbative scattering with thermal bath

Simple calculation:

$$\Gamma_{pert} = \frac{1}{576\pi} \frac{g^4 T^2}{m_{\sigma}(T)}$$

- this is a very simple calculation
- ignores e.g. fact that momenta are soft
- many recent papers give improvement e.g. Mukaida, Nakayama, Takimoto [1308.4394]

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Decay 3: dimension-5 operators

Example dimension-5 coupling:

$$\mathcal{L}_5 \propto rac{1}{M_P} \sigma ar{f} \Phi f$$

Gives:

$$\Gamma_5 pprox rac{m_\sigma^3}{M_P^2}$$

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Other constraints

- big bang nucleosynthesis (BBN)
 - neutrinos decouple at 4 MeV
 - avoid spoiling BBN if curvaton decay occurs before this
 - requires $m_{\sigma} > 8 \times 10^4$ GeV
- dark matter
 - isocurvature if dark matter freezes out before curvaton decay
 - large isocurvature is ruled out by WMAP and Planck
 - \blacktriangleright standard WIMP scenario with decoupling at ${\cal T}=10~GeV$ gives $\Gamma>10^{-16}~GeV$
 - from Γ_5 , we get $m_\sigma = 10^7$ GeV

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Methodology

- split into two solutions
- include full $V = V_0 + \Delta V + V(T)$
- numerically follow oscillations
- use scaling law evolution between transitions
- use δN formalism to obtain ζ, f_{NL} and g_{NL}



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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Parameter space for large σ_*



Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NL}

$f_{_{NI}}$ for large σ_*



▶ $H_* = 10^{12} \text{ GeV}$

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Constraints including $f_{_{NL}}$ for small σ_*



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Constraints including $f_{_{NL}}$ for small σ_*



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▶ $H_* = 10^{11} \text{ GeV}$

Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Remaining unknowns are (in principle!) calculable

Including:

- numerical (lattice) consideration of thermal blocking
- baryogenesis
- dark matter
- running of coupling constant and other quantum corrections
- spectral index n and tensor-to-scalar ratio r, once inflaton specified
- ► ...
- value of initial condition (?)

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Thermal blocking on the lattice (PRELIMINARY!)

Is the analytical analysis of thermal blocking sufficient?



Figure 1: The (log of) the particle number after preheating for $m_{\sigma}t = 1000$, corresponding to approximately 160 inflaton oscillations. Inset is the energy in the preheated field(s). The Higgs field is self-interacting and coupled to the "by-hand" inflaton, but has no coupling to any other fields. Without an additional mass (left), and with a mass of $M^2 = 0.5m_{\sigma}^2$ (right)

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Lagrangian and assumptions Three decay modes Parameter space: ζ and f_{NI}

Thermal blocking on the lattice (PRELIMINARY!)

- Is the analytical analysis of thermal blocking sufficient?
- Preliminary results say "yes"



Figure 3: The position of the resonance peaks as a function of the corresponding effective (LO) mass, when varying T. Filled symbols: With the leading order effective mass and Higgs self-interaction. Open symbols: Interacting with full dynamical light fields. Shaded symbols: Interacting with $N_f = 6$ full dynamical light fields.

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The questions

- if (non-inflaton) scalar fields exist in a theory, do they either rule out the theory or otherwise affect observational predictions?
- 2. if we design a curvaton model, does this have natural or fine-tuned initial conditions?

Initial Condition

The curvaton field value σ_* when observable scales exit the horizon determines the observational predictions (given model parameters).

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We did this:



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Specify model: minimal curvaton-higgs (MCH)

Reminder: MCH Lagrangian

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{2}\partial_{\mu}\sigma\partial^{\mu}\sigma + \frac{1}{2}m_{\sigma}^{2}\sigma^{2} + \frac{\lambda}{4!}\sigma^{4} + \frac{1}{2}g^{2}\sigma^{2}\Phi^{\dagger}\Phi$$

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Specify model: effective mass from the Higgs

 during inflation, curvaton gets a contribution to effective mass from interaction with higgs

•
$$m_{eff}^2 = m_{\sigma}^2 + \frac{1}{2}g^2h_*^2$$

after inflation the higgs contribution quickly disappears

Two regimes:

- 1. $gh_* \gg m_\sigma$: g determines m_{eff} , m_σ determines Γ_{eff}
- 2. $gh_* \ll m_\sigma$: m_σ determines both

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Interpretation of $P(\sigma)$

- 1. set up background inflation
- 2. add a curvaton
- 3. curvaton experiences slow roll and random quantum kicks
- 4. find value of σ_* in our patch
- 5. run the simulation many times
- 6. plot final σ_* from all runs this is $P(\sigma)$

The distribution of σ_*

Fokker-Planck equation

 $\dot{P}(\sigma, N) = \frac{1}{3H_*^2} V''(\sigma) P(\sigma, N) + \frac{1}{3H_*^2} V'(\sigma) P'(\sigma, N) + \frac{H_*^2}{8\pi^2} P''(\sigma, N)$ Derivation:

- Integrate out short wavelength modes with $k \gg H_*$
- Langevin equation $\dot{\sigma} = \frac{V'(\sigma)}{3H_*} + \xi(t)$
- ► random Gaussian noise: $\langle \xi(t)\xi(t')\rangle = \delta(t-t')\frac{H_*^3}{8\pi^2}$

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Evolution of $P(\sigma, N)$ for $V(\sigma) = \frac{1}{2}m_{eff}^2\sigma^2$



 $(N = 1, 10, 100; m_{eff} = 0.2H_*; \sigma_0 = 0.)$ Rose Lerner The minimal curvaton-higgs (MCH) model

Solution for quadratic potential $V(\sigma) = \frac{1}{2}m_{eff}^2\sigma^2$

$$P(\sigma, N) = \frac{1}{\sqrt{2\pi w^2(N)}} \exp\left(-\frac{(\sigma - \sigma_c(N))^2}{2H_*^2 w^2(N)}\right)$$

where

$$\sigma_c(N) = \sigma_c(0) \exp\left(-\frac{m_{eff}^2}{3H_*^2}N\right)$$

and

$$w^{2}(N) = \frac{3H_{*}^{2}}{8\pi^{2}m_{eff}^{2}} - \left(\frac{3H_{*}^{2}}{8\pi^{2}m_{eff}^{2}} - \frac{w^{2}(0)}{H_{*}^{2}}\right)\exp\left(-\frac{2m_{eff}^{2}}{3H_{*}^{2}}N\right)$$

- initial central value of the distribution: $\sigma_c(0) \equiv \sigma_0$
- ▶ initial width: w(0)

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Translate to ζ : valid for $V(\sigma) = \frac{1}{2}m_{eff}^2\sigma^2$

• Probability distribution of ζ given by

$$P(\zeta, N) = P[\sigma_*^-, N] \left| \frac{d\sigma_*}{d\zeta} \right|_{\sigma_*^-} + P[\sigma_*^+, N] \left| \frac{d\sigma_*}{d\zeta} \right|_{\sigma_*^+}$$

... resulting in

$$P(\zeta, N) = \frac{1}{\sqrt{2\pi w^2(N)}} \exp\left(-\frac{\left(\left[\frac{H_*}{6\pi\zeta}(1-Y(\zeta))\right] - \sigma_c(N)\right)^2}{2H_*^2 w^2(N)}\right) \frac{H_*(1-Y(\zeta))}{6\pi\zeta^2 Y(\zeta)} + \frac{1}{\sqrt{2\pi w^2(N)}} \exp\left(-\frac{\left(\left[\frac{H_*}{6\pi\zeta}(1+Y(\zeta))\right] - \sigma_c(N)\right)^2}{2H_*^2 w^2(N)}\right) \frac{H_*(1+Y(\zeta))}{6\pi\zeta^2 Y(\zeta)} + Y(\zeta) \equiv \sqrt{1 - \frac{288\pi^2 M_{Pl} m_\sigma \zeta^2}{H_*^2}}$$

... and something similar for f_{NL} .

Add opinion: defining "observable", "negligible" and "excluded"

As working definitions, we take:

observable $0.1\zeta_{WMAP} \leq \zeta \leq \zeta_{WMAP}$ or $5 < f_{_{NL}} < 14.3$

negligible

 $\zeta < 0.1 \zeta_{WMAP} ~{\rm and}~ f_{_{NL}} < 5$

excluded

- $\zeta > \zeta_{WMAP} \text{ or } f_{_{NL}} > 14.3$
 - ► Note that we must integrate over ζ to obtain P(0.1ζ_{WMAP} < ζ_{curvaton} < ζ_{WMAP})

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Wait ages and ages: P(observable)



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Wait ages and ages: P(negligible)



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Wait ages and ages: P(excluded)



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Wait just a little

- ζ is calculated when the perturbations leave the horizon, about 60 *e*-foldings before the end of inflation
- ► the N shown here is the number of e-foldings before horizon exit
- timescale to reach equilibrium given by $N_{dec} = \frac{3H_*^2}{2m^2}$
- ► N_{dec} can be large



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P(observable) for $\sigma_0 = 0$; N = 10



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P(observable) for $\sigma_0 = 0$; $N = 10^2$



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P(observable) for $\sigma_0 = 0$; $N = 10^4$



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P(observable) for $\sigma_0=0;~N=10^6$



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P(observable) for $\sigma_0 = 0$; $N = 10^{12}$



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P(negligible) for $\sigma_0 = 0$; N = 10



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P(negligible) for $\sigma_0 = 0$; $N = 10^2$



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P(negligible) for $\sigma_0 = 0$; $N = 10^4$



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P(negligible) for $\sigma_0 = 0$; $N = 10^6$



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P(negligible) for $\sigma_0 = 0$; $N = 10^{12}$



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P(excluded) for $\sigma_0 = 0$; N = 10



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P(excluded) for $\sigma_0 = 0$; $N = 10^2$



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P(excluded) for $\sigma_0 = 0$; $N = 10^4$



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P(excluded) for $\sigma_0 = 0$; $N = 10^6$



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P(excluded) for $\sigma_0 = 0$; $N = 10^{12}$



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P(observable) for $\sigma_0 = M_P$; $N = 10^4$



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P(observable) for $\sigma_0 = M_P$; $N = 10^6$



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P(observable) for $\sigma_0 = M_P$; $N = 10^8$



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P(observable) for $\sigma_0 = M_P$; $N = 10^{10}$



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P(observable) for $\sigma_0 = M_P$; $N = 10^{12}$



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Notes



 "probable" regions of parameter space exist for some range of model parameters

- ► large masses m_σ > 2 × 10⁷ GeV are (dis)favoured
- ► m_σ < 8 × 10⁴ GeV are excluded due to a late curvaton decay
- results valid for $g < (m_\sigma/M_P)^{1/4}$
- ► very little dependence on the initial conditions for large effective mass $m_{\text{off}}^2 = m_{\pi}^2 + g^2 h_*^2$
- scalars with certain properties should not be a society

Speculate: new observations



New information?

- tensor-to-scalar ratio $r \rightarrow H_*$
- Planck $\rightarrow f_{_{NL}}$
- Planck \rightarrow spectral index n_s \rightarrow constrains g and m_σ

(once V_{inf} specified)

• WIMP dark matter detection \rightarrow increased lower bound on m_{σ}

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Speculate: linking N, g and m_{σ}



- if large m_σ favoured, would need very large N.
- if small m_σ and large g was instead favoured,

N = O(10 - 100) would be sufficient, if $\sigma_0 = 0$ justified.

 Conversely, knowledge from fundamental theories about N could give information about m_σ and g.

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The questions

- if (non-inflaton) scalar fields exist in a theory, do they either rule out the theory or otherwise affect observational predictions?
- 2. if we design a curvaton model, does this have natural or fine-tuned initial conditions?

See also arxiv/1402.3176



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The minimal curvaton-higgs (MCH) model

The MCH model: summary

- MCH model is standard model + one real scalar curvaton
- non-perturbative decay into higgses is thermally blocked
- decay via dimension-5 operators determines predictions
- BBN, DM and interactions with the thermal background impose constraints
- \blacktriangleright distribution of initial field value σ_* could be determined under assumptions
- scalars with certain properties should not be ignored as possible curvatons!