

Radiative Neutrino Masses

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But

- Why m_ν are so small?
- Why omit terms of the form $\overline{\nu_R^c} M \nu_R$ in the Lagrangian?

Effective Lagrangian Approach

If the all new particles are much heavier than m_Z their effect can be parametrized at low energies by an effective Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{n=5}^{\infty} \sum_i \left(\frac{C_i^{(n)}}{\Lambda^{n-4}} \mathcal{O}_i^{(n)} + \text{h.c.} \right)$$

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If $E \ll \Lambda$, effects of $\mathcal{O}_i^{(n)}$ **suppressed by powers of E/Λ**

Dominated by the **lowest dimension operators**.

Only a dimension 5 operator (Weinberg operator)

$$\mathcal{O}^{(5)} = (\bar{L}_L \Phi)(\tilde{\Phi}^\dagger L_L) \rightarrow -\frac{1}{2} v^2 \overline{v}_L^c \rightarrow (M_\nu)_{\alpha\beta} = C_{\alpha\beta}^{(5)} \frac{v^2}{\Lambda}$$

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If $C^{(5)} \sim 1$, to obtain $m_\nu < 1 \text{ eV}$ one needs $\Lambda > 10^{14} \text{ GeV}$

The See-Saw Models

Type I (fermion singlet ν_R as discussed)

$$C^{(5)} \approx Y_\nu Y_\nu^T, \quad \Lambda = M$$

Type II (scalar triplet χ with $Y = 1$)

$$\mathcal{L}_\chi = - \left(\bar{L}_L Y_\chi \chi L_L - \mu \tilde{\Phi}^\dagger \chi^\dagger \Phi + \text{h.c.} \right)$$

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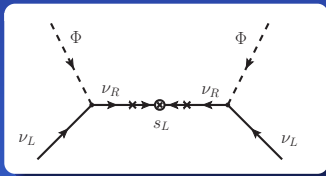
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Variation (Inverse see-saw): $3\nu_R$ and $3s_L$ fermion singlets



$$\begin{pmatrix} 0 & M_D & 0 \\ M_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}, \quad \begin{matrix} C^{(5)} \approx Y_\nu Y_\nu^T \frac{\mu}{M} \\ \Lambda = M \end{matrix}$$

One-loop Majorana Masses

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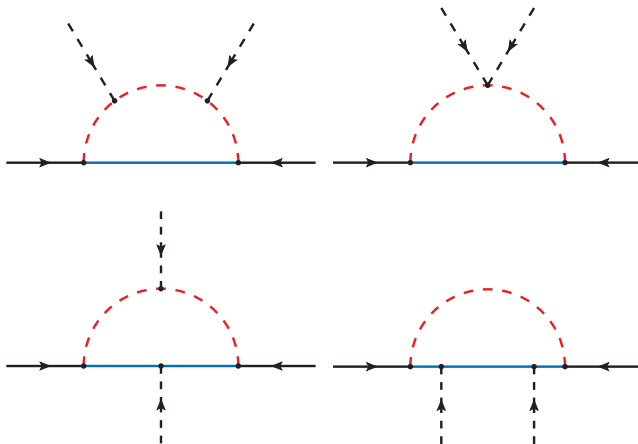
If there are no fields with the quantum numbers of the see-saw ν_R, χ, Σ masses cannot be generated at tree level

If LN is not conserved the Weinberg operator will be generated **at one loop (or more)**.

Natural justification for $C^{(5)} \ll 1$

Opening the Weinberg at One Loop

(Bonnet, Hirsch, Ota, Winter, '12)



Many possibilities

The Zee Model

Adds to the SM a scalar singlet h^+ and a new doublet Φ'
 $h^+ \sim (1, 1), \quad \Phi' \sim (2, \frac{1}{2})$

$$\mathcal{L}_{\text{Zee}} = \overline{\tilde{L}_L} f L_L h^+ + \mu h^+ \Phi'^{\dagger} \tilde{\Phi}' + \dots$$

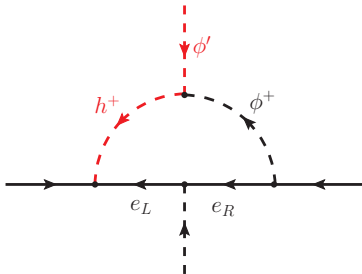
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Simplest versions give

$$C^{(5)} \approx \frac{1}{(4\pi)^2} f Y_e Y_e^T \frac{\mu}{M_h}, \quad \Lambda = M_h$$

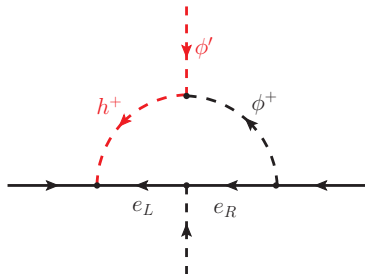


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- “Too predictive”: excluded
- Type III 2HDM versions OK (Balaji, Grimus, Schwetz '01)
- $H \rightarrow \tau\mu$ linked to ν masses? (Herrero-Garcia, Rius, AS, '15, Herrero-Garcia, Wiren in preparation)
- Rich LFV phenomenology ($\mu \rightarrow e\gamma, \tau \rightarrow e\gamma, \dots$)

The Inert/Scotogenic Doublet

Add a fermion singlet s_R and scalar doublet η (Ma '06)

$$\mathcal{L}_Y = -\bar{L}_L Y_s \tilde{\eta} s_R - \frac{1}{2} \overline{s_R^c} M s_R - \lambda_5 (\Phi^\dagger \eta)^2 + \dots + \text{h.c.}$$

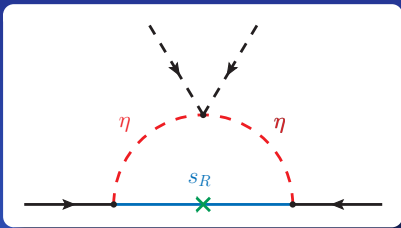
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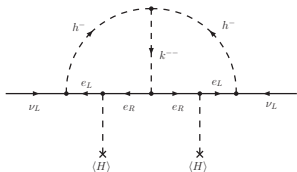
- Charged particles could be seen in the LHC
- s_R or η 's stable: good dark matter candidate

(Ma '06, Barbieri '06,
Lopez-Honorez, Nezri, Oliver, Tytgat '07)

The Zee-Babu Model

Add two scalar singlets h^+, k^{++} (Zee '86, Babu '88, Babu, Macesanu '03)
(Aristizabal, Hirsch '06, Nebot, Oliver, Palao, AS '08, Ohlsson, Schwetz, Zhang '09, Schmidt, Schwetz, Zhang '14)

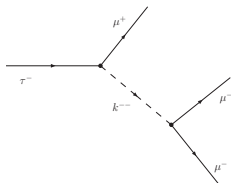
$$\mathcal{L}_{\text{ZB}} = \bar{L}_L f L_L h^+ + \bar{e}_R^c g e_R k^{++} + \mu (h^-)^2 k^{++} + \dots$$



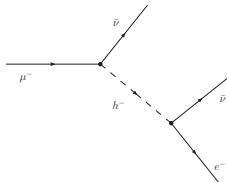
$$C^{(5)} \sim \frac{f Y g^\dagger Y^T f^T \mu}{(4\pi)^4 M}, \quad \Lambda = M_k$$

- Lightest ν is massless
- $f_{e\tau}/f_{\mu\tau}, f_{e\mu}/f_{\mu\tau}$ fixed from mixings

$\ell_a^- \rightarrow \ell_b^+ \ell_c^- \ell_d^-$: limits on g_{ab}



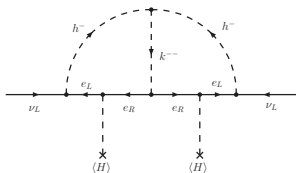
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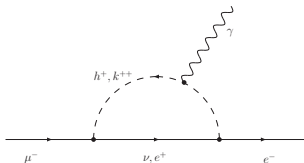
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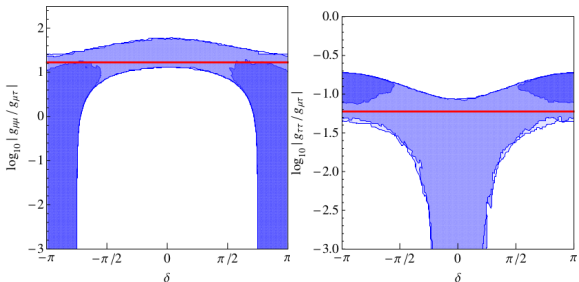
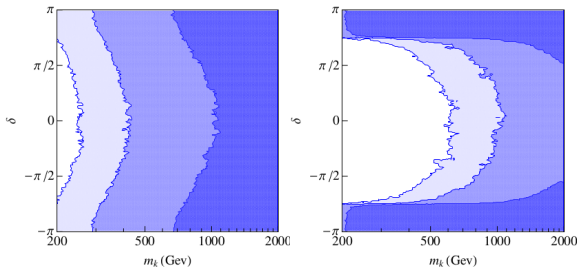
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$\ell_a^- \rightarrow \ell_b^- \gamma$: bounds g_{ab} and f_{ab}



Constrained Parameter Space

(Nebot, Oliver, Palao, AS '08, Herrero-Garcia, Nebot, Rius, AS '14)



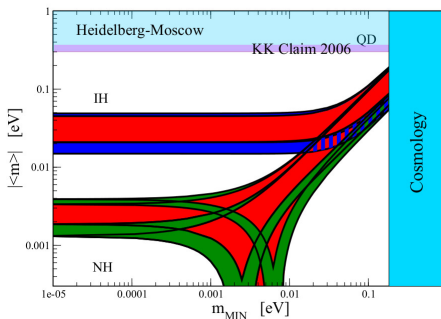
m_ν Contribution to $0\nu\beta\beta$

Present:

$m_{\beta\beta} \lesssim 0.12\text{--}0.25\text{ eV}$ (KamLAND-Zen, EXO-200, GERDA)

Future:

$m_{\beta\beta} \sim 0.01\text{ eV}$ (KamLAND2-Zen, nEXO, GERDA2, CUORE, ...)



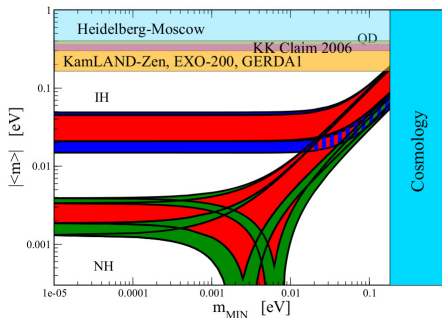
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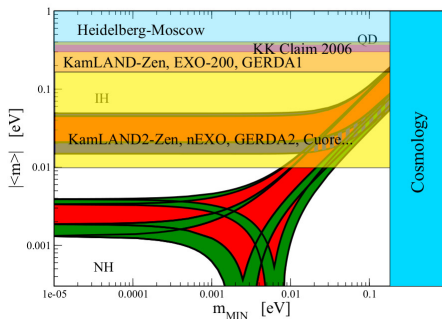
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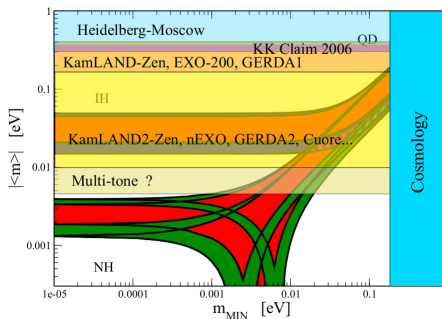
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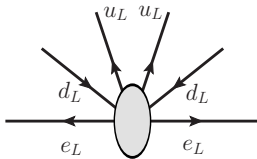
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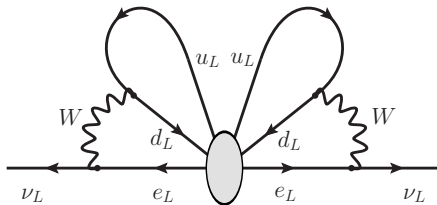
$0\nu\beta\beta$ Contribution to m_ν

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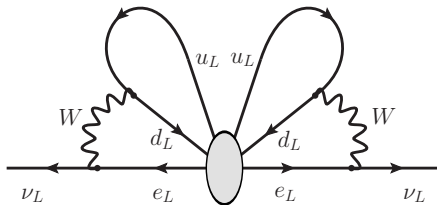
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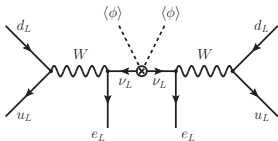
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Fermion chirality

$$\text{Majorana } \nu : \quad \nu_L \nu_L, \quad 0\nu\beta\beta : \quad \begin{cases} e_L e_L \\ e_L e_R \\ e_R e_R \end{cases}$$

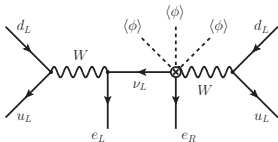
Operators Contributing to $0\nu 2\beta$

(del Aguila, Aparici, Bhattacharya, AS, Wudka '12)



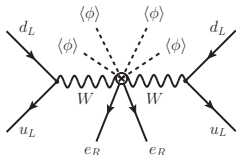
$$\mathcal{O}^{(5)} = (\bar{L}_L \phi) (\tilde{\phi}^\dagger L_L)$$

$$\mathcal{A}_{0\nu 2\beta}^{(5)} \sim \frac{C_{ee}^{(5)}}{\Lambda p_{\text{eff}}^2 v^2}$$



$$\mathcal{O}^{(7)} = (\phi^\dagger D_\mu \tilde{\phi}) (\phi^\dagger \bar{e}_R \gamma^\mu \tilde{L}_L)$$

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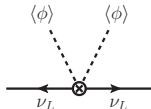
$$\mathcal{O}^{(9)} = \bar{e}_R e_R^c (\phi^\dagger D_\mu \tilde{\phi}) (\phi^\dagger D^\mu \tilde{\phi})$$

$$\mathcal{A}_{0\nu 2\beta}^{(9)} \sim \frac{C_{ee}^{(9)}}{\Lambda^5}$$

Contribution to ν Masses

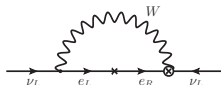
Neutrino masses

$\mathcal{O}^{(5)}$



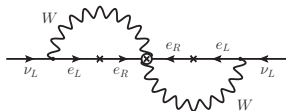
$$(m_\nu)_{ab} \sim \frac{v^2}{\Lambda} C_{ab}^{(5)}$$

$\mathcal{O}^{(7)}$



$$\frac{v}{16\pi^2\Lambda} \left(m_a C_{ab}^{(7)} + m_b C_{ba}^{(7)} \right)$$

$\mathcal{O}^{(9)}$



$$\frac{1}{(16\pi^2)^2\Lambda} m_a C_{ab}^{(9)} m_b$$

An Example of RR-type Model

3 new scalars $\chi \sim (3, 1)$, $\kappa \sim (1, 2)$, $\sigma \sim (1, 0)$ and Z_2 symmetry

$$\mathcal{L} = g_{\alpha\beta} \overline{e_{\alpha R}^c} e_{\beta R} \kappa - \mu_\kappa \kappa \text{Tr} \{ \chi^\dagger \chi \} - \lambda_6 \sigma \phi^\dagger \chi \tilde{\phi} + \dots$$

- No new fermions \Rightarrow No see-saw I-III
- No $\chi L_L L_L$ coupling (Z_2 symmetry) \Rightarrow No see-saw II

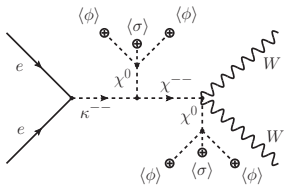
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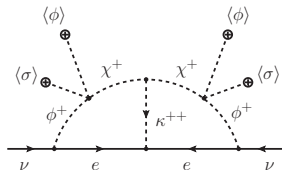
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The $0\nu 2\beta$ Operator



The neutrino mass



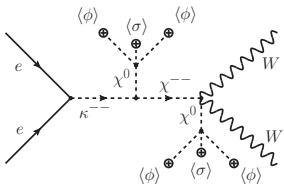
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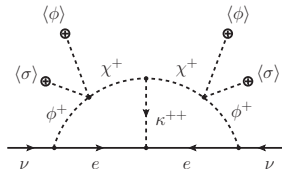
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Variations (Gustafsson, No, Rivera, '13 and '14): If Z_2 exact

- $0\nu\beta\beta$ at one loop and m_ν at three loops
- Dark matter candidate

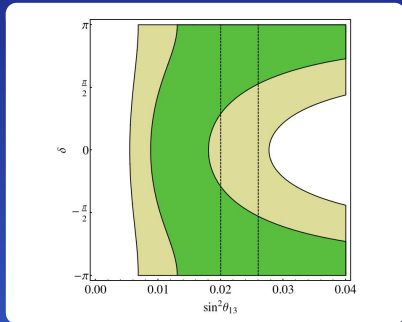
Constraints on the ν Mass Matrix

- Large $0\nu\beta\beta$: relatively large g_{ee} and small scalar masses
- $(M_\nu)_{ee}$ highly suppressed by the factor m_e^2
- $(M_\nu)_{e\mu}$ also suppressed because the $\mu \rightarrow 3e$ bound on $g_{e\mu}$

ν mass matrix highly constrained

$$|m_\nu| = \begin{pmatrix} < 10^{-4} & < 10^{-4} & \sim 0.01 \\ < 10^{-4} & \sim 0.01 & \sim 0.01 \\ \sim 0.01 & \sim 0.01 & \sim 0.01 \end{pmatrix} \text{ eV}$$

- Only NH allowed
- Prediction for $m_{\text{light}} \sim 0.004 \text{ eV}$
- Prediction for $\sin^2 \theta_{13}$



2012: $\sin^2 \theta_{13} \sim 0.02 - 0.026$

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- New contributions to $0\nu 2\beta$

Thanks for your attention

BACKUP SLIDES