

Dark Matter: from 10^{-22} eV to 10^{67} eV



PLANCK 2017, Warsaw

John March-Russell
Oxford University

The Dark Matter Landscape



The Dark Matter Landscape

(in mass)



The Dark Matter Landscape



One Possibility: DM at same scale as SM - (WIMPs)

WIMPs heavy so low phase space density and looking for *particles*

The Dark Matter Landscape

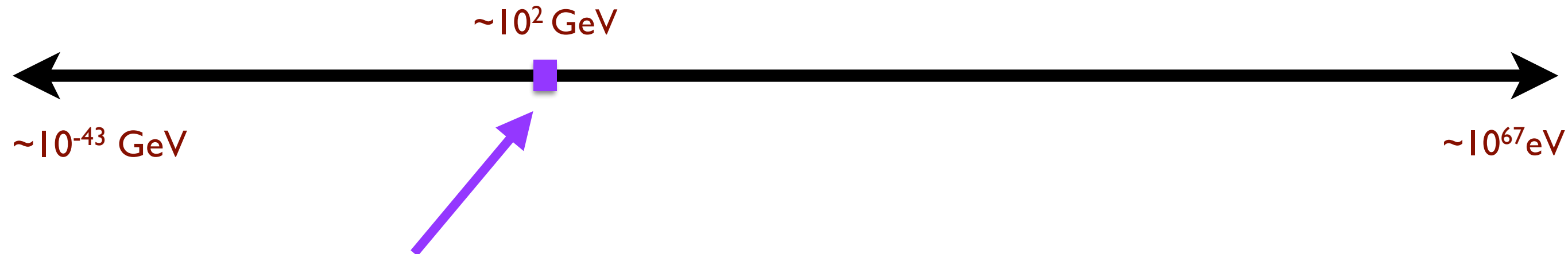


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WIMPs heavy so low phase space density and looking for *particles*

“a simple, elegant, compelling explanation for a complex physical phenomenon”

The Dark Matter Landscape



One Possibility: DM at same scale as SM - (WIMPs)

WIMPs heavy so low phase space density and looking for *particles*

“For every complex natural phenomenon there is a simple, elegant, compelling, wrong explanation.”

- Tommy Gold

The Dark Matter Landscape

(fermions)



The Dark Matter Landscape

(bosons)



The Dark Matter Landscape

(bosons)



DM well-described as a *field* (BEC) as phase space density high (in galaxies now) as

$$\rho_{\text{DM}} \approx 0.3 \frac{\text{GeV}}{\text{cm}^3} \approx (0.04 \text{ eV})^4$$

The Dark Matter Landscape

(bosons)



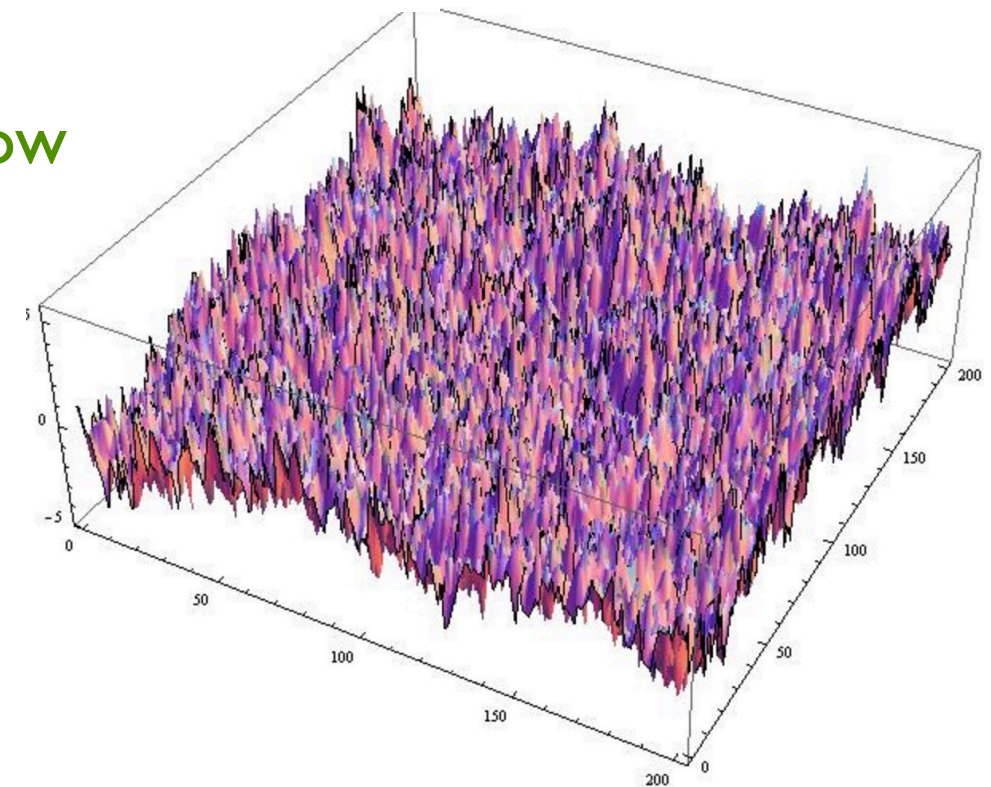
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(phase) correlation length & time now

$$\ell_c \sim 1/(m_a v)$$

$$t_c \sim 1/(m_a v^2)$$



The Dark Matter Landscape

(bosons)



DM well-described as a *field* (BEC) as phase space density high (in galaxies now)

Much old & especially recent interest: super-light pNGBs (QCD Axion, ALPs),
Hidden "Photon" DM,...



Peccei-Quinn-Weinberg-Wilczek
Kim-Shifman-Vainshtein-Zakharov
Dine-Fischler-Srednicki-Zhitnitsky

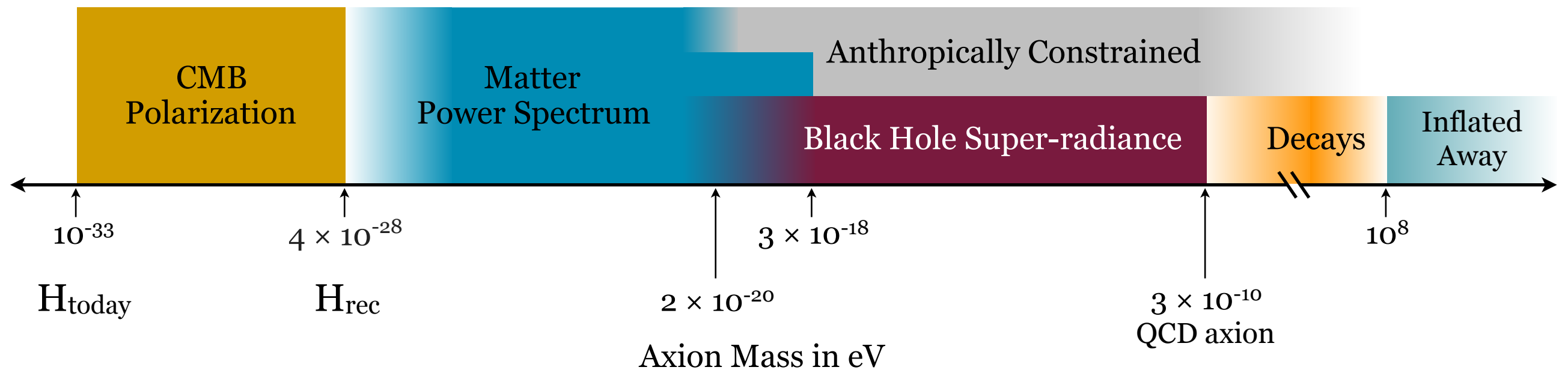
The Dark Matter Landscape

(bosons)



DM well-described as a *field* (BEC) as phase space density high (in galaxies now)

String Axiverse: A Plenitude of Axions:



Arvanitaki, Dimopoulos, Dubovsky, Kaloper, JMR; arXiv:0905.4720

Here they are...!



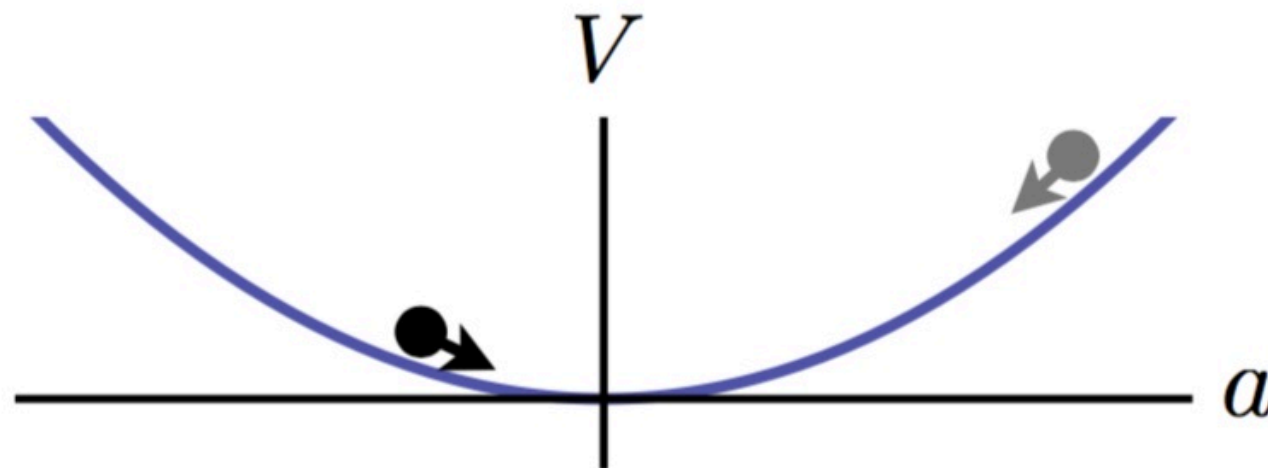
The Dark Matter Landscape

(bosons)



DM well-described as a *field* (BEC)

Attractive production mechanism: misalignment (others possible)



Focus today...

The Dark Matter Landscape



Focus today...

The Dark Matter Landscape



Question: Is this region also populated by interesting DM candidates with motivated production mechanisms??

Recall....

Freeze-In Production

Hall, Jedamzik, JMR, West; arXiv:0911.1120
McDonald; arXiv:hep-ph/0106249

- X only *feebly* coupled to visible-sector thermal bath particles V_i
- X never in thermal equilibrium with SM

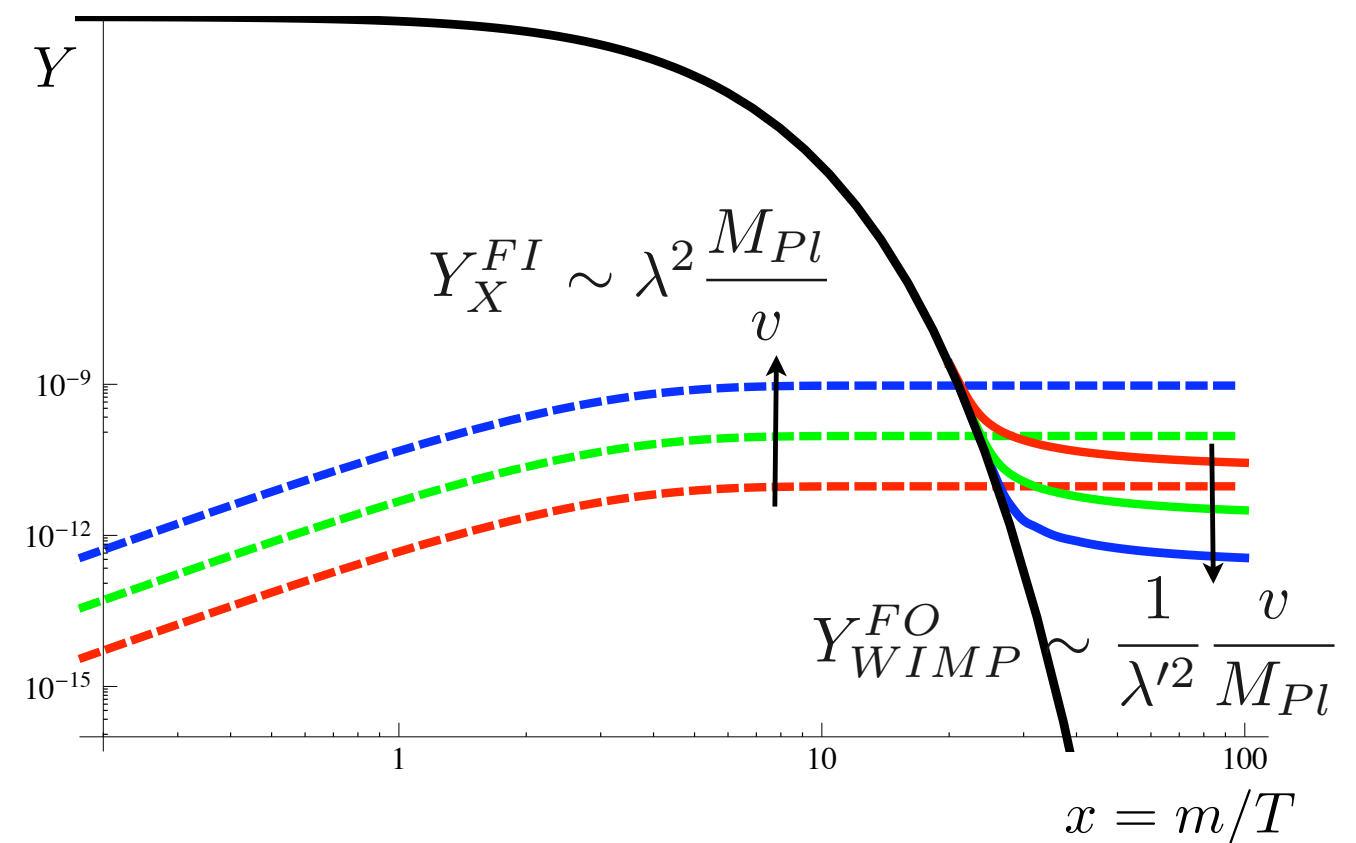
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as universe evolves, a tiny
X abundance is produced



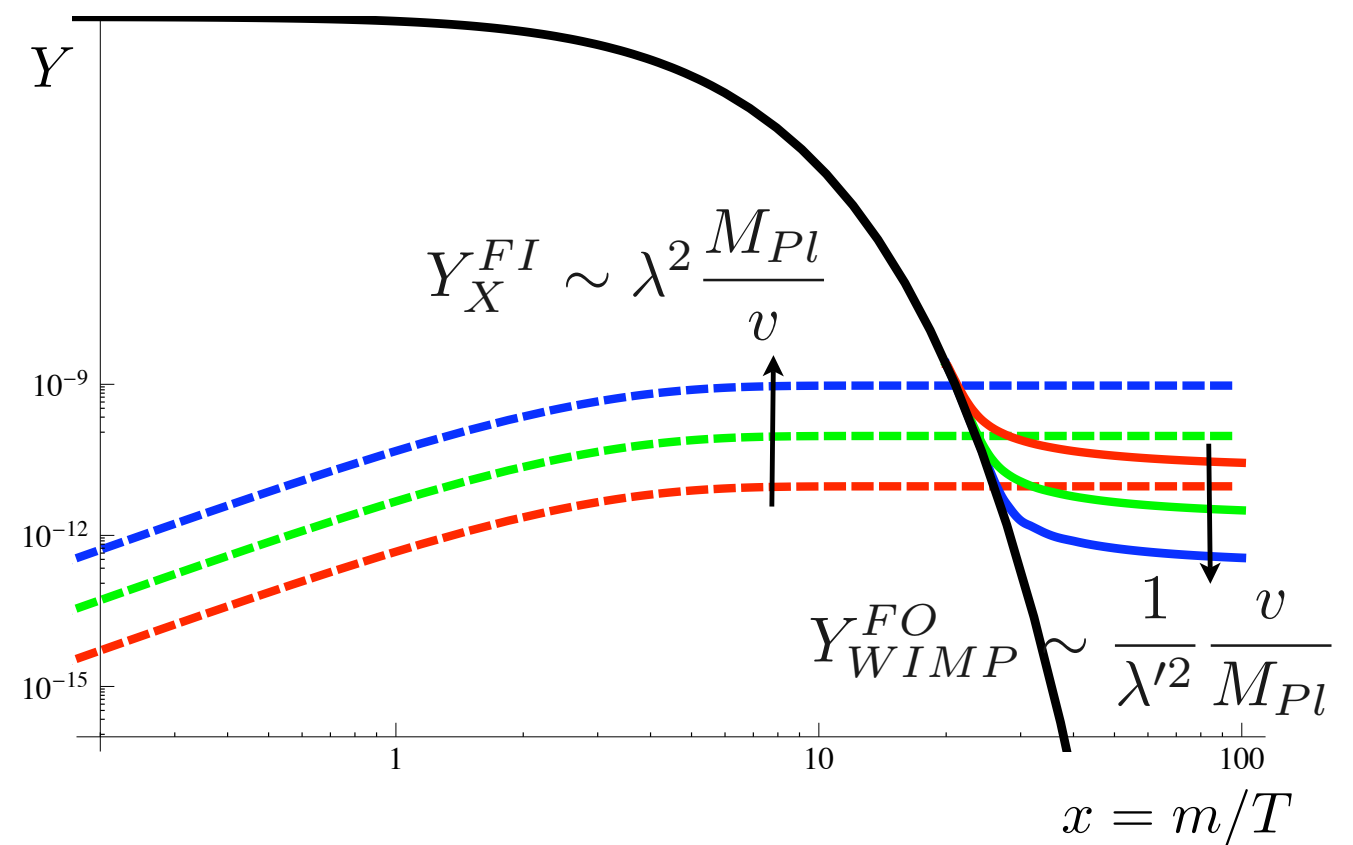
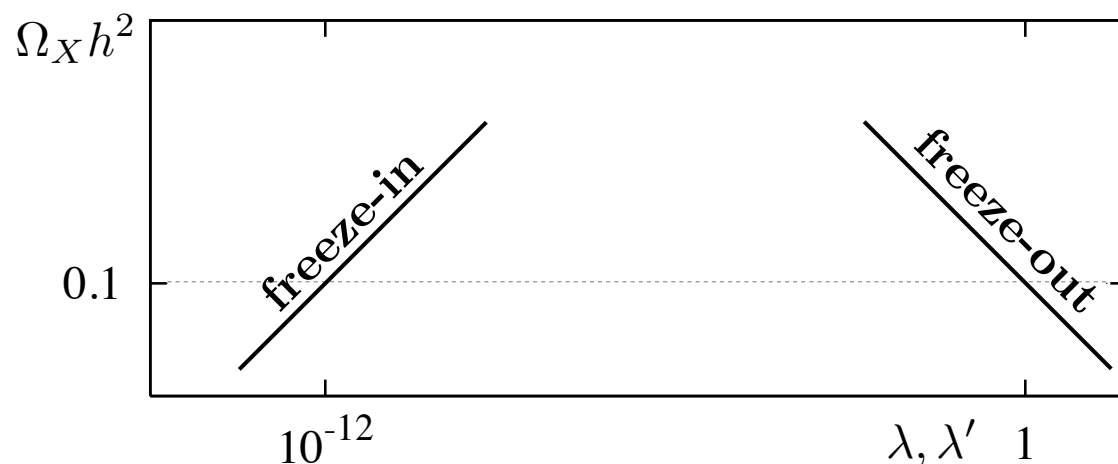
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two calculable thermal mechanisms
(heading either in or out of equilibrium)

Freeze-In Production

Comments

📌 'Explains' why direct detection hasn't seen anything yet...

📌 FI yield is **IR-dominated** for renormalizable interactions

$$Y_X^{FI}(T) \sim \lambda^2 \frac{m^2 M_{Pl}}{T^3}$$

$\Delta L = \lambda X V_1 V_2$

*dominant production occurs at $T \sim m$
(heaviest particle in vertex)*

📌 Lightest ordinary-sector particle (**LOSP**) transforming under X-stabilising symmetry is **automatically long-lived and interesting for future LHC searches** if $m \sim \text{TeV}$

Freeze-In Production

Origin of Feeble Coupling?

The 'WIMP miracle' is that for $m' \sim v$ and $\lambda' \sim 1$

$$m' Y_{FO} \sim \frac{1}{M_{pl} \langle \sigma v \rangle} \sim \frac{m'^2}{M_{pl} \lambda'^2} \sim \frac{v^2}{M_{pl}}$$

gives the observed value of $\Omega_{DM} h^2$

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Freeze-In Production

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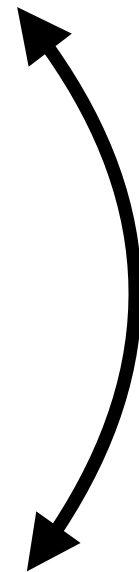
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Suggests that **FIMPs occur where tiny couplings arise at linear order in weak scale**

eg...

Freeze-In Production

moduli of the SUSY-breaking sector giving SUSY-SM soft terms

$$\begin{array}{lll}
 m^2 \left(1 + \frac{T}{M}\right) (\phi^\dagger \phi + h^\dagger h) & \mu B \left(1 + \frac{T}{M}\right) h^2 & Ay \left(1 + \frac{T}{M}\right) \phi^2 h \\
 m_{\tilde{g}} \left(1 + \frac{T}{M}\right) \tilde{g}\tilde{g} & \mu y \left(1 + \frac{T}{M}\right) \phi^2 h^* & \mu \left(1 + \frac{T}{M}\right) \tilde{h}\tilde{h},
 \end{array}$$

or for modulini

$$\mu \frac{\tilde{T}}{M} \tilde{h}h \qquad \frac{m_{susy}}{M} \tilde{T}(q\tilde{q}^\dagger, l\tilde{l}^\dagger, \tilde{h}h^\dagger)$$

give tiny renormalizable couplings...

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give tiny renormalizable couplings...

$\lambda \sim 10^{-13}$ for either $m_{susy} \sim \text{TeV}$ and $M \sim M_{GUT}$ (natural value of compactification scale & f_a in realistic string theories) or $m_{susy} \sim 10^{2-3} \text{TeV}$ and $M \sim M_{pl}$

Freeze-In Production

So far assumed FIMP mass close to weak-scale. For WIMPs this must be so as unitarity limits size of annihilation cross-section

FIMPs completely different:

$$m Y_{FI} \sim m \lambda^2 \left(\frac{M_{pl}}{m} \right) \sim \lambda^2 M_{pl}$$

Remarkably this is **independent of mass!** (as long as $m < T_{\text{reheat,SM}}$)

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Calculable thermal production of
superheavy FIMP DM possible

w/ apologies to Rocky: **FIMPzilla's!**

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however hard to see apart from indirect detection (annihilation or decay via $d=6$ ops)

The Dark Matter Landscape



Are there calculable very heavy DM objects with more signatures (not just indirect detection)?

Yes!

Asymmetric DM

Asymmetric DM allows for existence and formation of

very heavy composite objects (DM-"Nuclei", Q-balls,...)

with a wide variety of striking signatures in LHC, direct detection and indirect detection

Many novel possibilities...!

Recall...

Asymmetric DM

Similar physics underlies both Ω_B and Ω_{DM}

(Nussinov '85; Gelmini, Hall, Lin '87; Barr '91; Kaplan '92; Thomas '95; Hooper, JMR, West '04; explosion in last few yrs esp work of Zurek etal; JMR etal; Sarkar etal; Sannino etal; now many others...)

Baryons: $U(1)_B$ $u, d, s...$ p stable $\Omega_B \propto m_B \eta_B$

DM: $U(1)_X$ $X_0, X_1, X_2...$ X_0 stable $\Omega_X \propto m_X \eta_X$

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At some era

Interactions violate B and X to yield related values for η_B and η_X

$$\frac{\Omega_X}{\Omega_B} = \frac{\eta_X}{\eta_B} \frac{m_X}{m_B}$$

Asymmetric DM

$$\frac{\Omega_X}{\Omega_B} = \frac{\eta_X}{\eta_B} \frac{m_X}{m_B}$$

only true if X density is determined
by the asymmetric part otherwise

$$\frac{\Omega_X}{\Omega_B} = \frac{Y_X + Y_{\bar{X}}}{Y_B + Y_{\bar{B}}} \frac{m_X}{m_B}$$

need $Y_X + Y_{\bar{X}} = Y_X - Y_{\bar{X}} + \text{small corrections}$

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non-trivial constraint as initially

$$Y_X + Y_{\bar{X}} = \frac{Y_X - Y_{\bar{X}}}{\epsilon}$$

where expect $\epsilon \ll 1$ measures CP-violation

Asymmetric DM

⇒ Must efficiently annihilate away symmetric part to light states

there has to be an efficient X-preserving freeze-out process

Options:



direct FO to light SM dof

⇒ operators connecting X & SM sectors with strength bounded below



direct FO to light dark sector dof

⇒ (potentially) new "long-range" DM interactions



FO to (light) dark sector dof which then late decay to SM

⇒ late-time energy injection in early universe, as well as (potentially) new "long-range" DM interactions

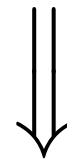
Asymmetric DM

 direct FO to light SM dof

limits from direct detection experiments and monojet etc
searches at LHC are very constraining

with slight exceptions if we want asymmetric DM in natural
region $m_X < 10$ GeV then direct FO to SM is disfavoured

eg, JMR, Unwin, West; arXiv:1203.4854
and many others....



eliminating symm component likely implies new dark-sector dynamics

Asymmetric DM

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DM: $U(1)_X$ $X_0, X_1, X_2 \dots$ X_0 stable $\Omega_X \propto m_X \eta_X$

$m_X \sim \text{few GeV}$ is favoured as $O(1)$ ratio of asymmetries most "natural"

(but see, eg, JMR+McCullough, arXiv:1106.4319, and Sarkar et al for other possibilities)

major issue: *why* is DM mass near that of baryon?

(but see, eg, Garcia Garcia, Lasenby, JMR; arXiv:1505.07410
for automatic explanation *directly connected with naturalness*-
the "Twin Higgs" mechanism: also see work on "mirror world"
models, by Foot, Volkas, et al)

Nuclear DM

Hardy, Lasenby, JMR, & West; arXiv:1411.3739 & arXiv:1504.05419
Detmold, McCullough, Pochinsky; arXiv:1406.2276

Large composite DM states

- ▶ Standard model: example of conserved baryon number, attractive interactions leading to multitude of large, stable bound states (nuclei)
- ▶ What if a similar thing happens for dark matter?

Large composite DM states

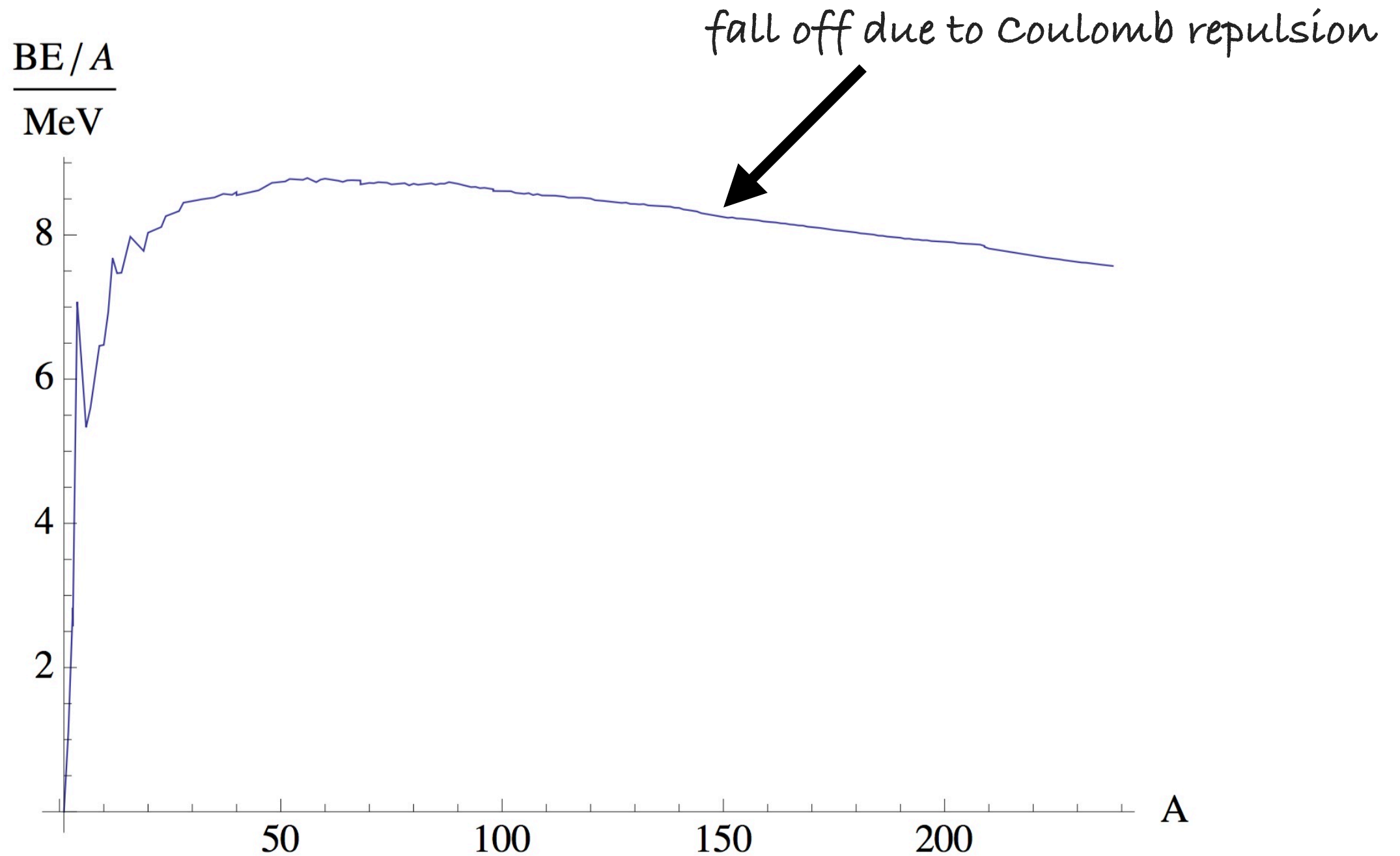
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- ▶ Possibilities:
 - ▶ Number distribution over DM states
 - ▶ States with large spin
 - ▶ Structure on scales $\gg 1/m$ — form factors in scattering, possibility of larger cross sections
 - ▶ Coherent enhancement of interactions
 - ▶ Inelastic processes — fusions, fissions, excited states
 - ▶ ‘Late-time’ ($T \ll m$) synthesis — can achieve very heavy ($\gtrsim 100$ TeV) DM from thermal freeze-out

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 - ▶ ‘Late-time’ ($T \ll m$) synthesis — can achieve very heavy ($\gtrsim 100$ TeV) DM from thermal freeze-out
- ▶ Example of Q-balls — non-topological solitons of scalar fields
(will return to this at end if time...)

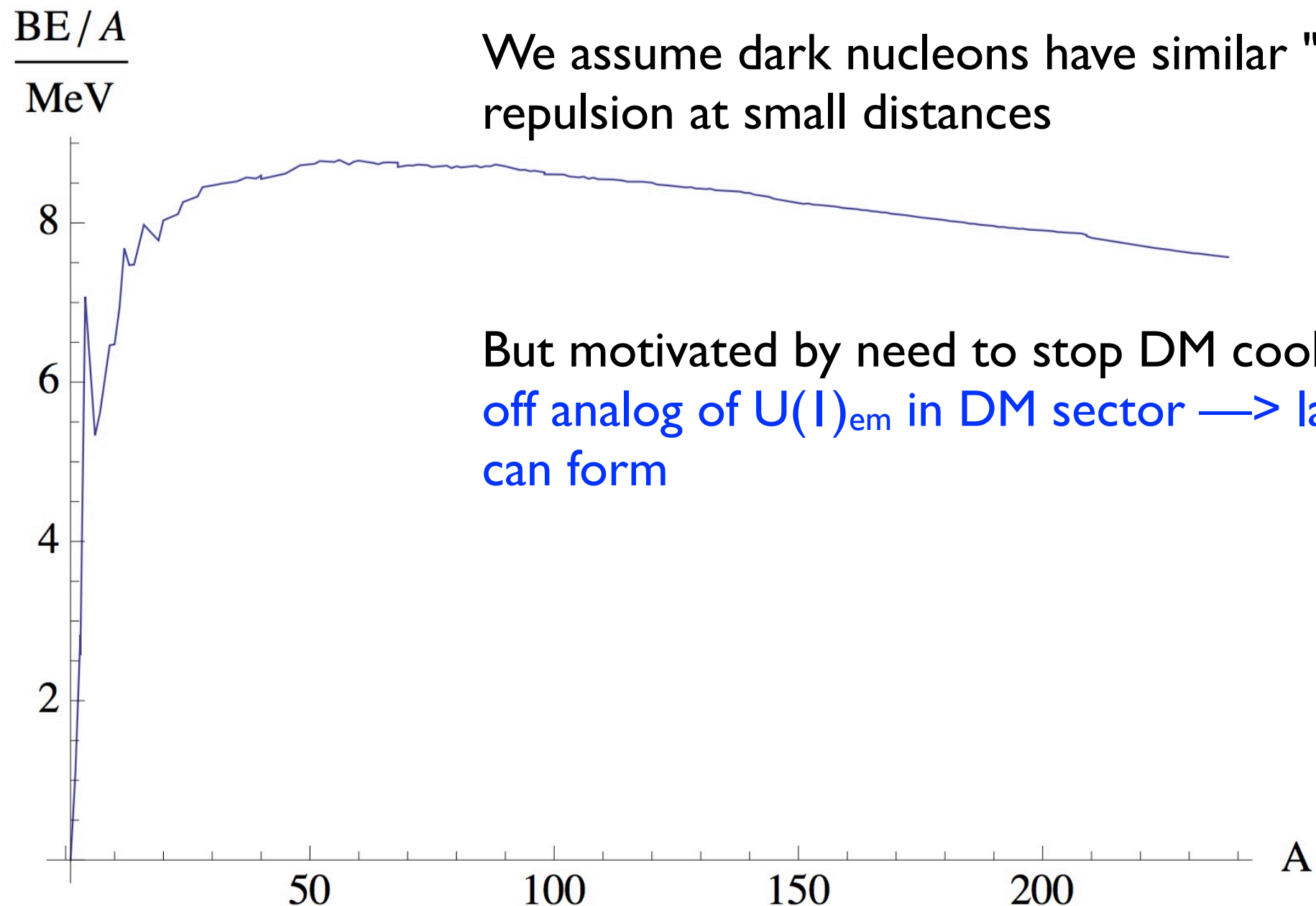
Nuclear DM

SM nuclei



Nuclear DM

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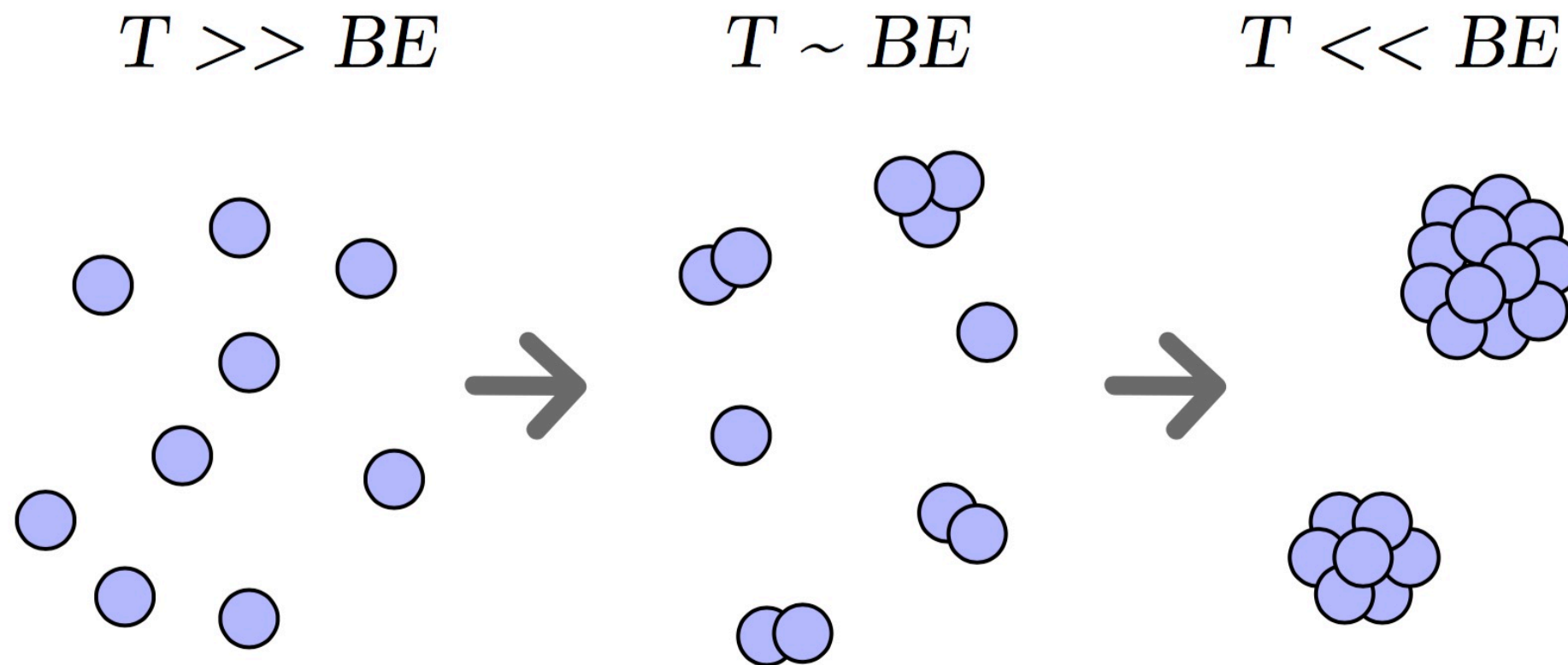
Nuclear DM

Dark nucleosynthesis

Free energy $F = E - T S$:

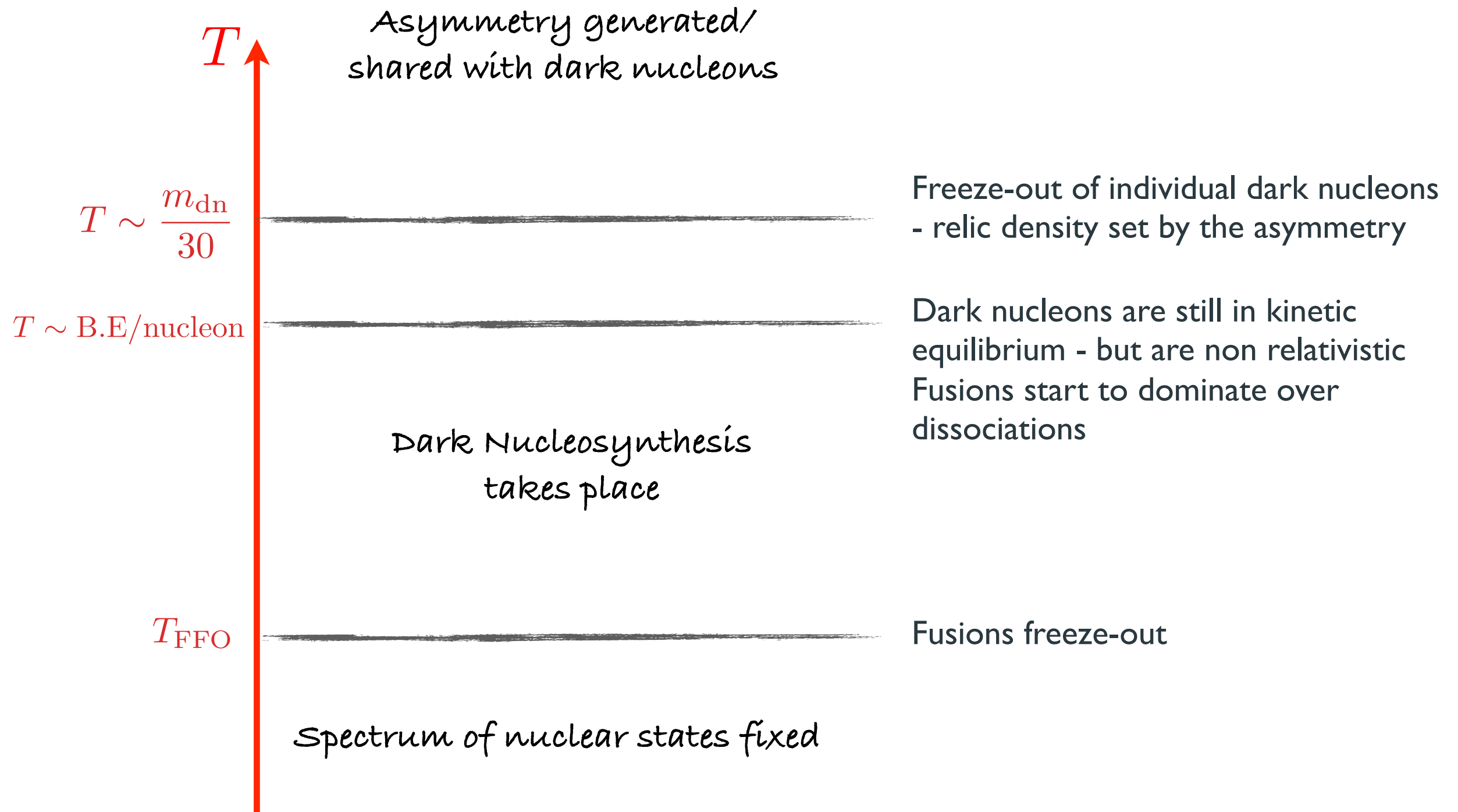
large $T \Rightarrow$ everything dissociated

small $T \Rightarrow$ large states favoured



Nuclear DM

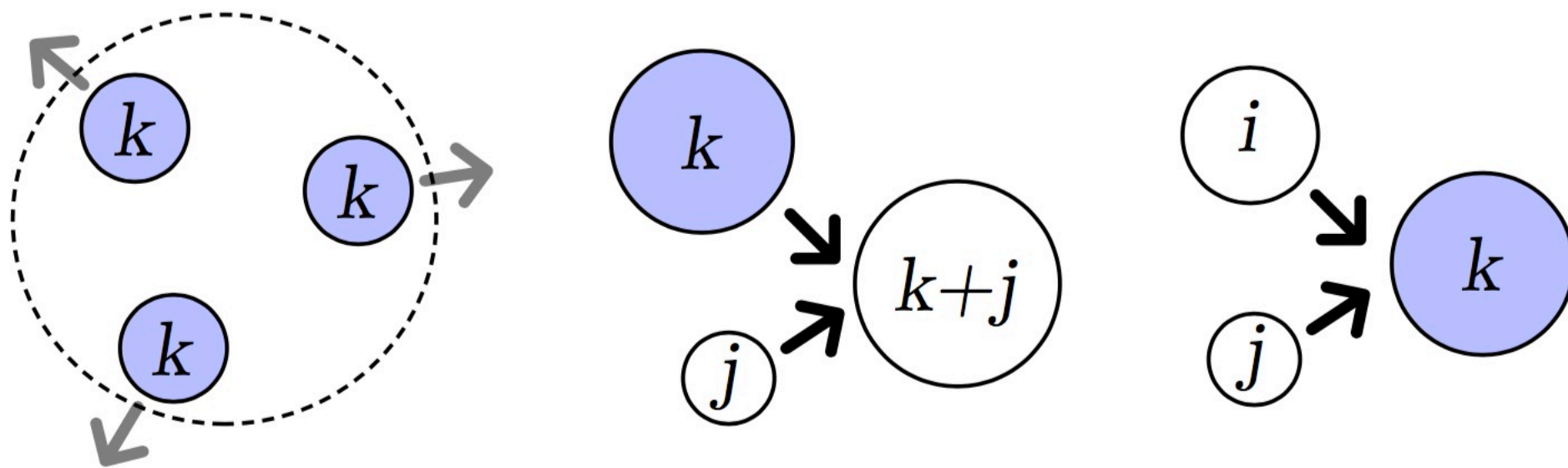
Schematic thermal evolution



Nuclear DM

Aggregation process after dissociations freeze-out

$$\frac{dn_k(t)}{dt} + 3H(t)n_k(t) = - \sum_{j=1}^{\infty} \langle \sigma v \rangle_{j,k} n_j(t) n_k(t) + \frac{1}{2} \sum_{i+j=k} \langle \sigma v \rangle_{i,j} n_i(t) n_j(t) ,$$



Defining relative "yields" $y_k = Y_k/Y_0 = (n_k/s)/Y_0$

and scaled cross section $K_{i,j} = \frac{\langle \sigma v \rangle_{i,j}}{\sigma_1 v_1}$

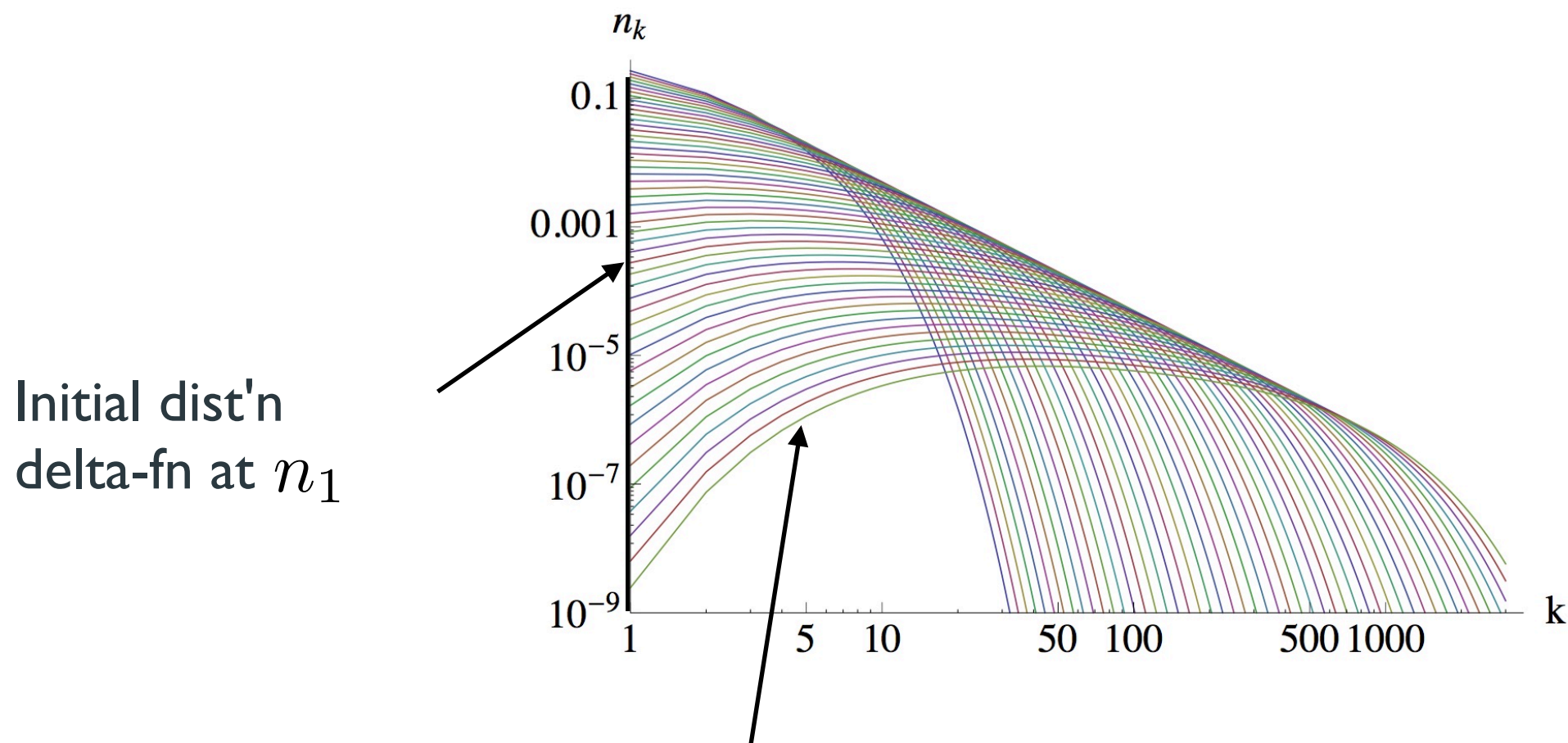
total dark nucleon yield

Nuclear DM

Scaling solution

$$\langle \sigma v \rangle_{i,j} \sim (\text{area}_i + \text{area}_j) v_{\text{rel}}$$

$$\implies K_{i,j} = (i^{2/3} + j^{2/3})(i^{-1/2} + j^{-1/2}) \quad , \quad K_{\lambda i, \lambda j} = \lambda^{1/6} K_{i,j}$$



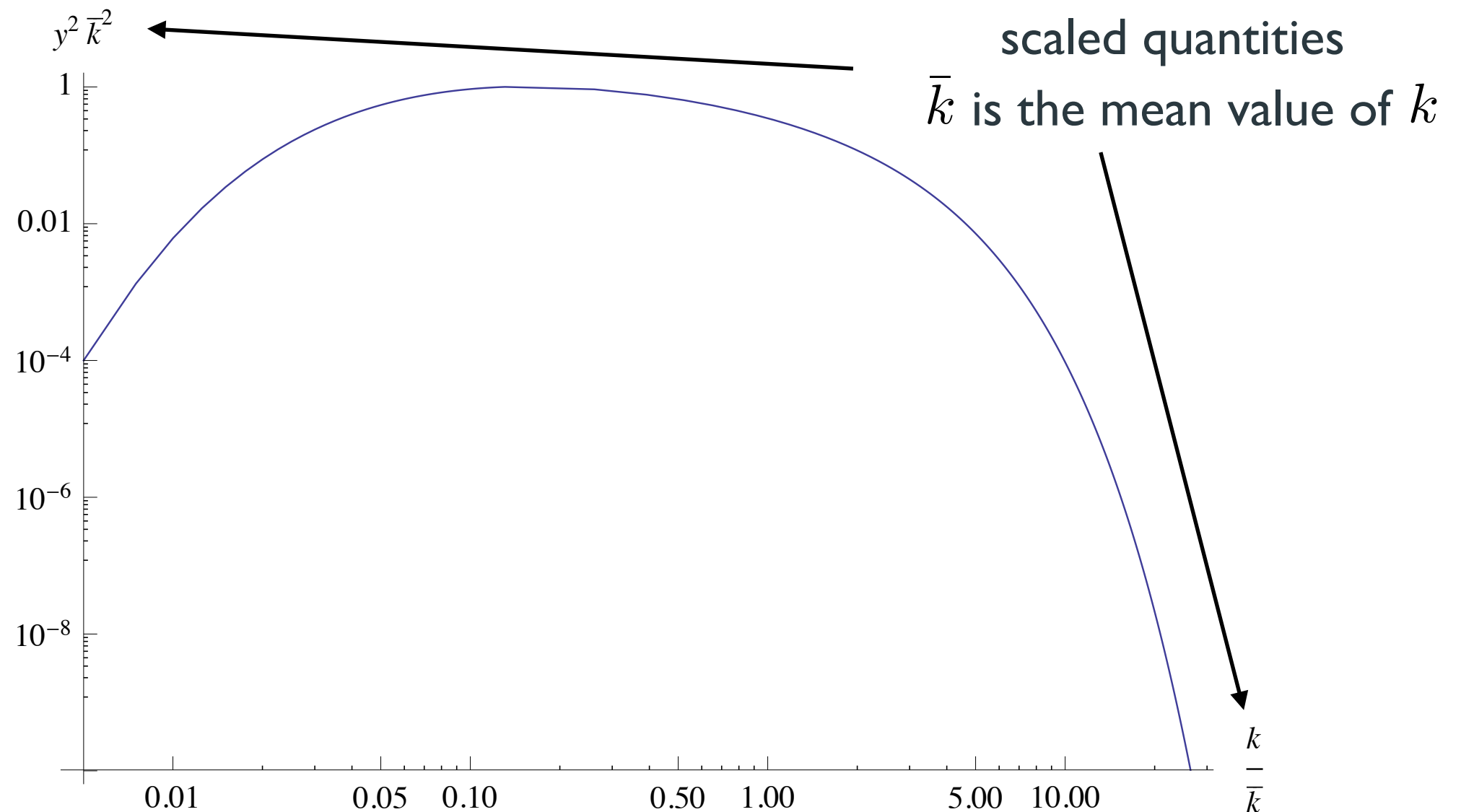
For this case there is an **attractor scaling solution** independent of details of initial conditions or small- k kernel (within limits)

See e.g. Krapivsky, Redner, Ben-Naim, A Kinetic View of Statistical Physics, CUP, '10

Nuclear DM

For most reasonable kernels and initial conditions scaling solution is reached within one Hubble time

From then on **distribution shape stays same but average size of dark nuclei continues to increase until fusions finally freeze-out**



Nuclear DM

Can estimate how big nuclei can be by looking at scaling of freeze-out of equal size fusions

Using
$$\frac{\sigma_1 v_1 n_0}{H} \sim 2 \times 10^7 \left(\frac{1 \text{ GeV fm}^{-3}}{\rho_{dark B}} \right)^{2/3} \left(\frac{T}{1 \text{ MeV}} \right)^{3/2} \left(\frac{m_1}{1 \text{ GeV}} \right)^{-5/6}$$

(where motivated by ADM, dark parameters are scaled to SM values)

freeze-out criterion
$$\frac{\Gamma}{H} \sim \frac{\langle \sigma v \rangle_{k,k} n_k}{H} \sim \frac{\sigma_1 v_1 n_0}{H} k^{-5/6}$$

$$\sigma_{k,k} \sim \sigma_1 k^{2/3}$$

$$v_k \sim v_1 k^{-1/2}$$

$$n_k = n_0/k$$

$$\Rightarrow k_{max} \sim 10^9 \quad !$$

(If we have severe bottle-neck at small k small-large fusions can, counter-intuitively, imply even larger final nuclei produced with different scaling solution...)

see Hardy, Lasenby, JMR, & West; arXiv:1411.3739 & arXiv:1504.05419

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Thus Dark Nucleosynthesis can generate extremely large and massive composite dark nuclei, even if constituent dark nucleons are in usual ADM range

*Rich
Phenomenology!*

Nuclear DM

Changes for direct detection signals

- ◆ Coherent enhancement of scattering from dark nuclei
- ◆ Dark matter momentum dependent form factor
- ◆ Inelastic processes
- ◆ Collective low energy excitations

Indirect detection signals

- ◆ Inelastic self-interactions (may modify distribution in Halo)

Capture in stars

- ◆ Asymmetric in nature so can build up in stars
- ◆ Model dependent consequences

Nuclear DM

- ◆ Coherent enhancement of scattering from dark nuclei

Nuclear DM

- ◆ Coherent enhancement of scattering from dark nuclei

For a k -dark-nucleus interactions with SM enhanced by $k^2 \times$ (form factor)

Number density $\sim 1/k$ compared to single nucleons

$\Rightarrow$ effective direct detection rate enhanced by k (could be $\sim 10^9$!)

$\Rightarrow$ in other words, for given direct detection rate, collider production of kinematically accessible individual dark nucleons suppressed by k

Nuclear DM

- ◆ Dark matter momentum dependent form factor

If momentum-transfer q in direction detection $> 1/R_k$ (radius of k -dark-nucleus)
probe DM form factor

Nuclear DM

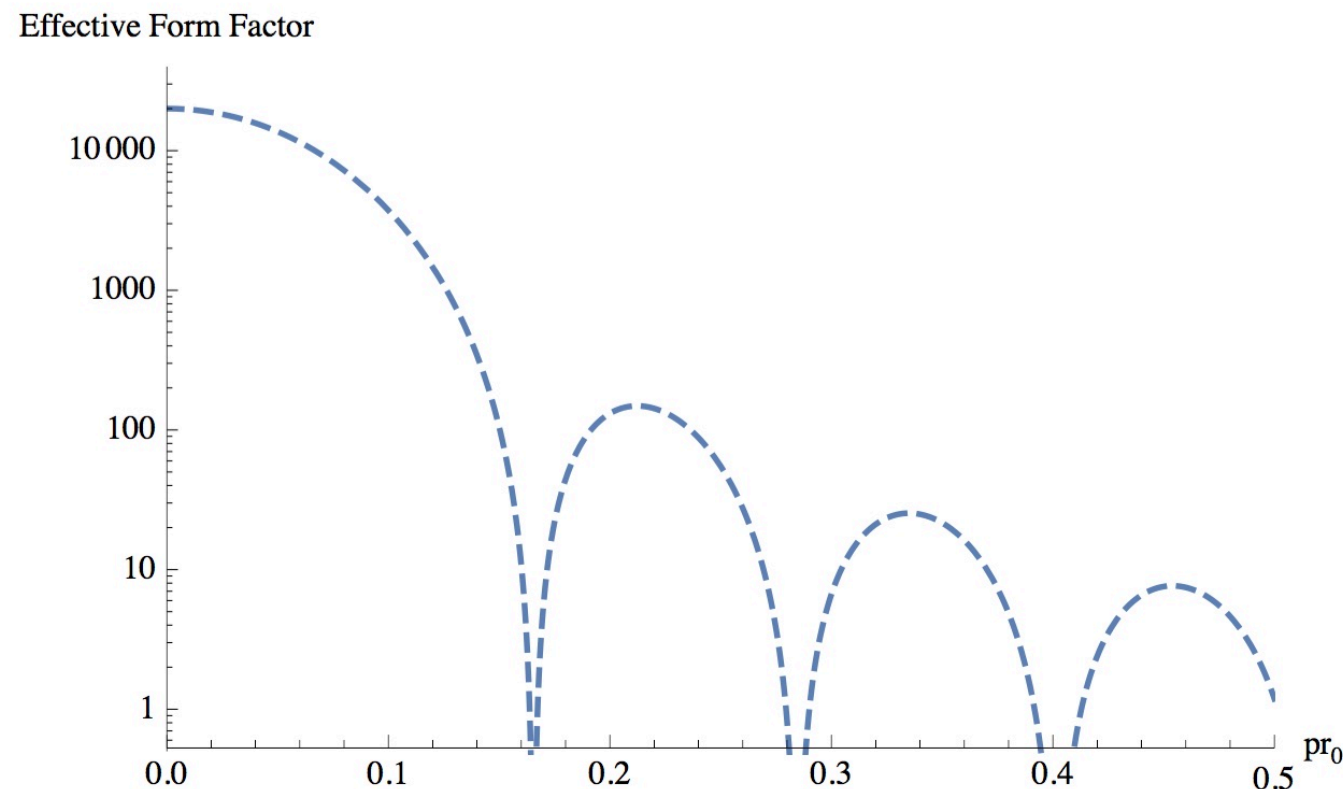
◆ Dark matter momentum dependent form factor

If momentum-transfer q in direction detection $> 1/R_k$ (radius of k -dark-nucleus)
probe DM form factor

If skin-depth of DM-nucleus smaller than SM nuclear size then get "spherical top hat" form factor

$$F_k(q) = \frac{qR_k \cos(qR_k) - \sin(qR_k)}{(qR_k)^3}$$

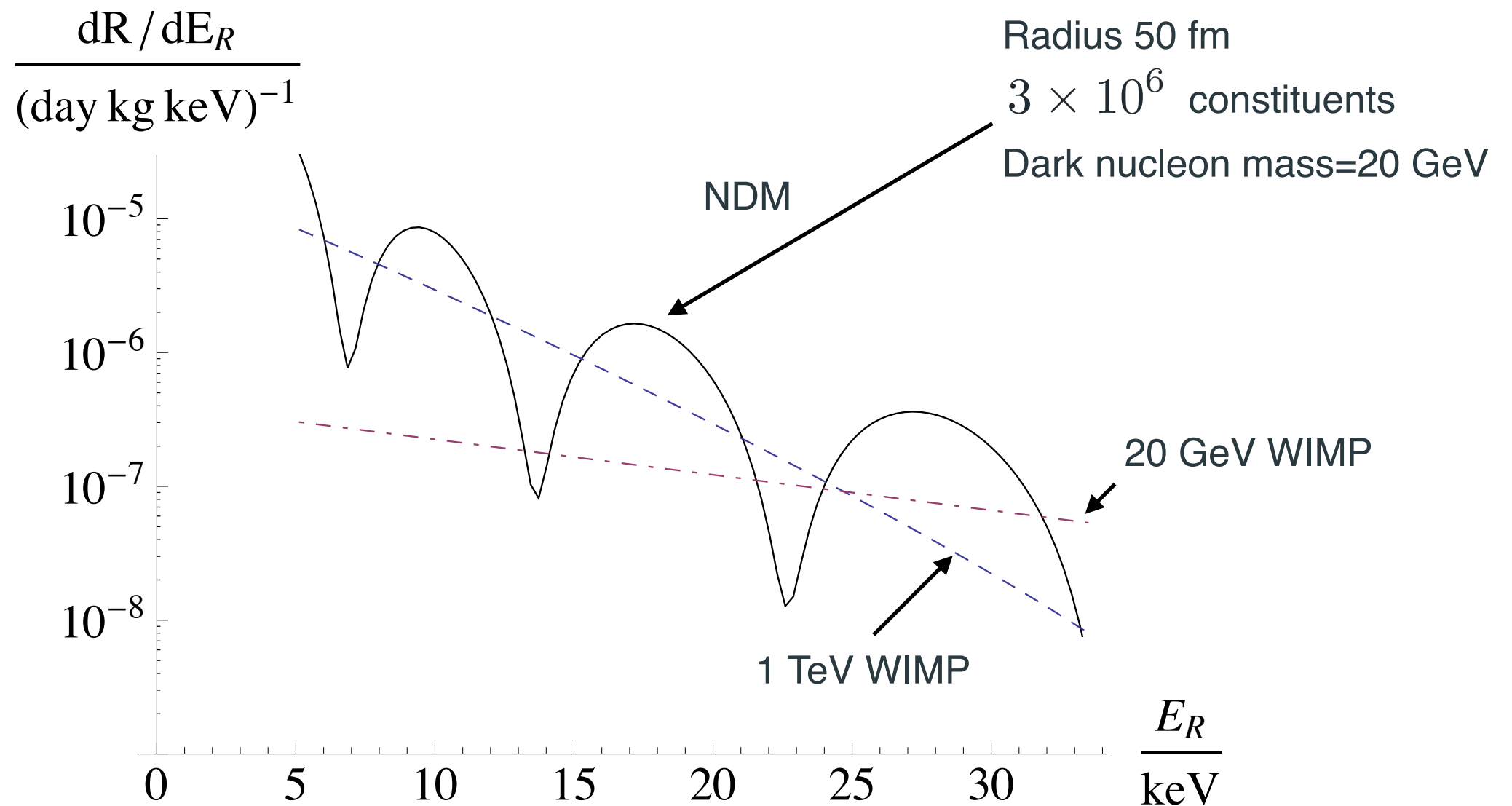
$$R_k \sim R_0 k^{1/3}$$



Nuclear DM

More generally with skin-depth of DM-nucleus and response function of detector included get modifications like, eg,

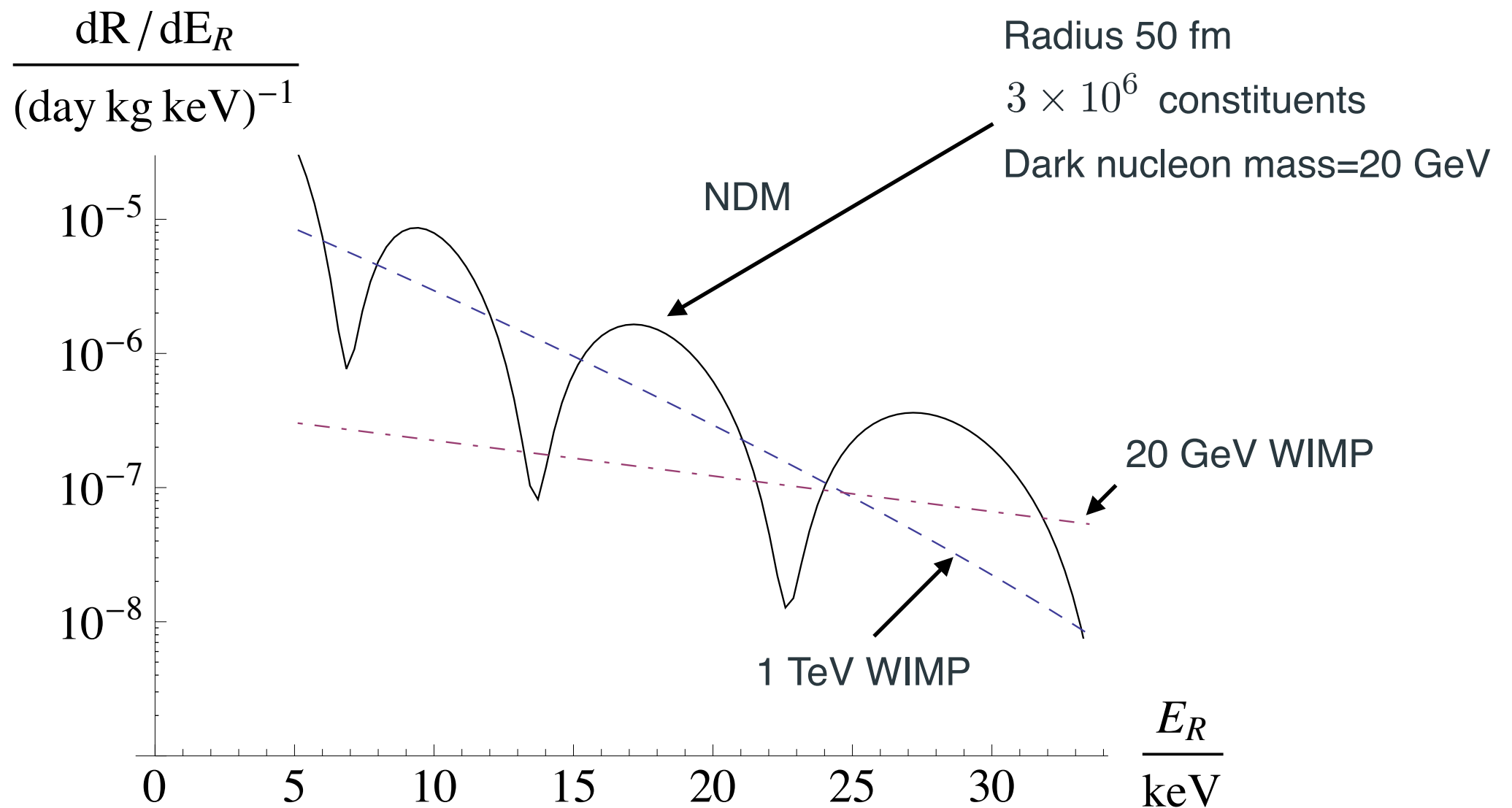
(Germanium detector
response function)



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(Germanium detector
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In principle can distinguish this scenario, and investigate some details of composite state

see Butcher, Kirk, Monroe, West; arXiv:1610.01840, for details of what is possible

Nuclear DM

There are *many* other striking, but largely unexplored consequences of Nuclear DM....

Finally...

Macroscopic DM

There are rich possibilities for getting "macroscopic" DM beyond just NuclearDM linked to Asymm DM

eg,



Scalar solitons like Q-balls...

Kusenko, Shaposhnikov, etal



Primordial BHs...

Carr; Bird etal; Garcia Bellido, etal

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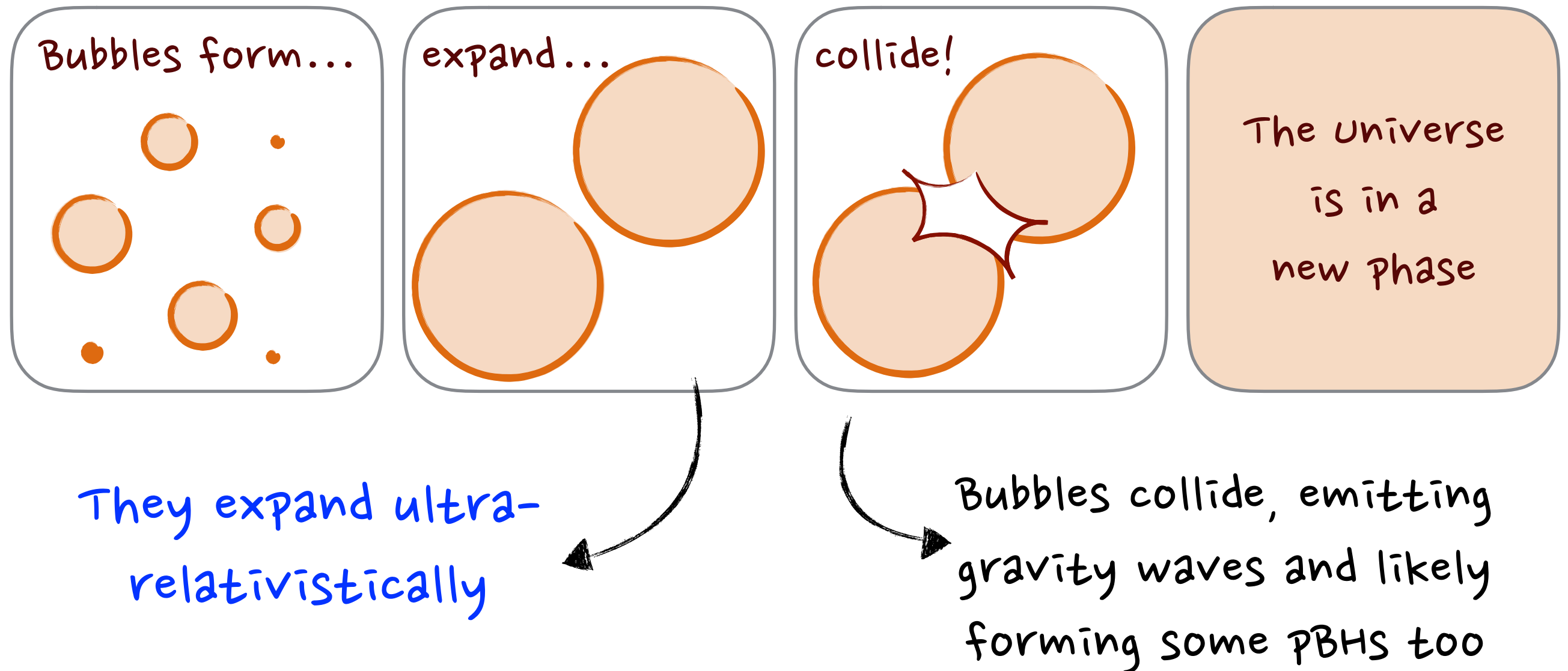
📍 Scalar solitons like Q-balls...
Kusenko, Shaposhnikov, etal

📍 Primordial BHs...
Carr; Bird etal; Garcia Bellido, etal

Crucial that we investigate both resulting (novel) phenomenology, and assess if there are calculable production mechanisms (ideally, not exponentially sensitive to parameters)

PBHs from $T=0$ (quantum) vacuum decay?

Garcia Garcia, Kripendorff, JMR; arXiv:1607.06813



Nobody has reliably computed resulting PBH mass spectrum...!

Garcia Garcia, JMR, work in progress...

Conclusions

come on...

Huge amount of exciting thy/expt awaits!

embrace the dark side