

Comprehensive studies of loop-corrected decays of various Higgs bosons

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Collaborators;

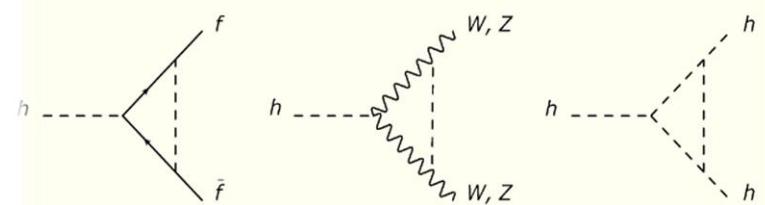
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Kei Yagyu (Osaka U.)

H-COUP



1. NPB 983(2022)115906, Kanemura, MK, Yagyu
2. In preparation, Aiko, Kanemura, MK, Sakurai, Yagyu

Why is Higgs sector important?

- What is Structure of Higgs sector ?

Various extended Higgs sectors

Multi Doublets

Doublet + Singlet

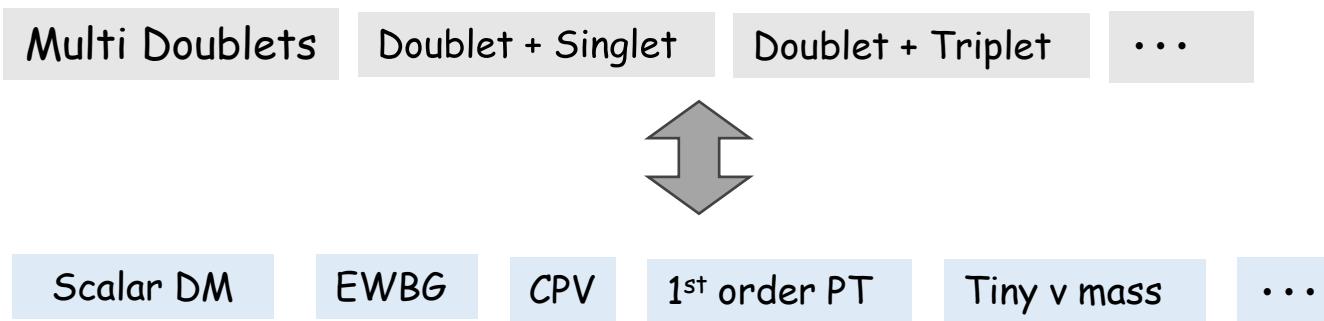
Doublet + Triplet

...

Why is Higgs sector important?

- What is Structure of Higgs sector ?

Various extended Higgs sectors



- Higgs sector is related to new physics scenarios.

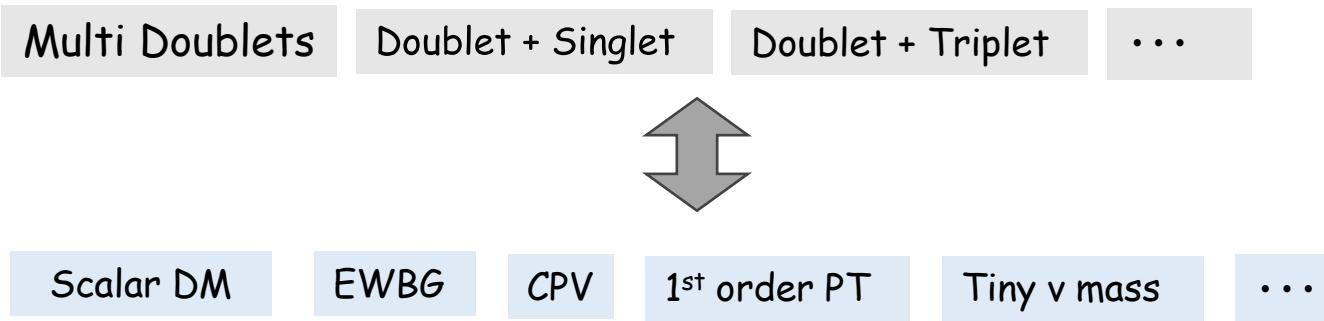
Each new physics model requires a characteristic Higgs sector.

It is important to explore Higgs sector
by bottom-up approach.

Why is Higgs sector important?

- What is Structure of Higgs sector ?

Various extended Higgs sectors



- Higgs sector is related to new physics scenarios.

Each new physics model requires a characteristic Higgs sector.

**It is important to explore Higgs sector
by bottom-up approach.**

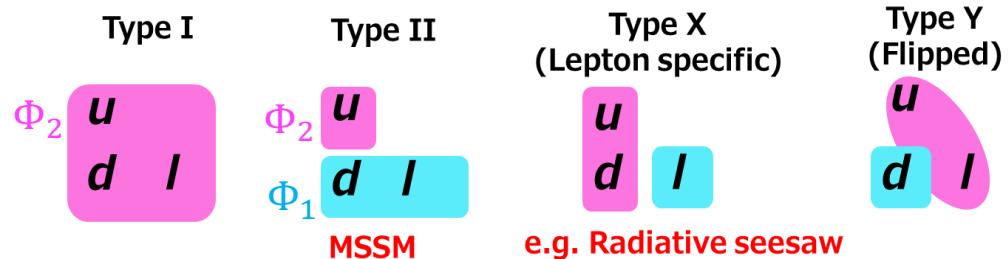
- We here focus on “Doublet + an additional scalar”.

Higgs singlet model (HSM), Two Higgs doublet model (THDM), Inert doublet (IDM), ...

Two Higgs doublets (THDMs)

- Some new physics models contain two Higgs doublets.
(MSSM, Inert DM, loop induced m_ν , CPV, ...)
- We focus on THDM with softly broken Z2.
Can avoid FCNC.

4 types of Yukawa interactions



- We focus on CP-conserving case
- Mass eigenstates

Higgs basis

h (125GeV Higgs), H , A , H^\pm

$$\Phi = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(h'_1 + v + iG^0) \end{pmatrix} \quad \Phi' = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h'_2 + iA) \end{pmatrix} \quad \begin{pmatrix} h'_1 \\ h'_2 \end{pmatrix} = \begin{pmatrix} \cos(\beta - \alpha) & \sin(\beta - \alpha) \\ -\sin(\beta - \alpha) & \cos(\beta - \alpha) \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

- Parameters in potential
- m_h v m_H m_A m_{H^\pm} $\sin(\beta - \alpha)$ $\tan\beta$ M^2

$$\therefore M^2 = \frac{m_3^2}{\sin\beta\cos\beta} \quad \tan\beta = \frac{v_2}{v_1}$$

Deviations from SM predictions

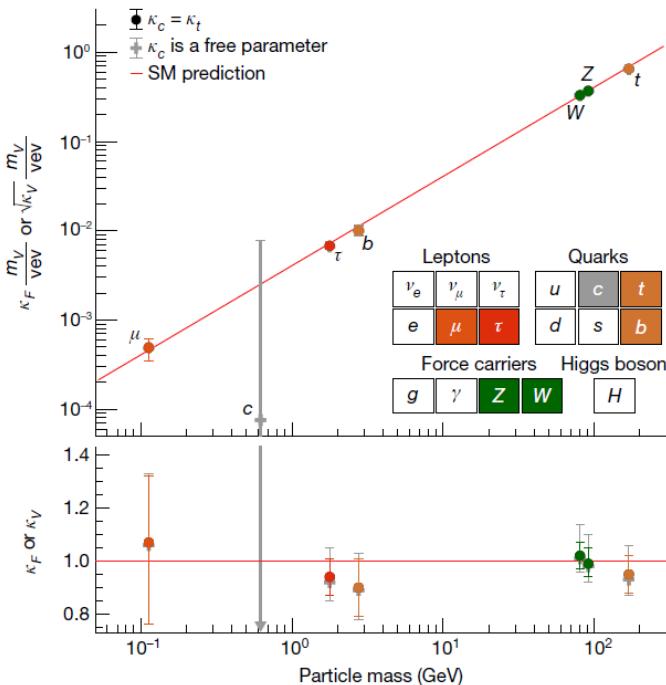
- h -couplings can change via field mixing (α, β)

$$\kappa_X = \frac{g_{hXX}^{NP}}{g_{hXX}^{SM}}$$

$\sin(\beta - \alpha) = \kappa_V \rightarrow 1 \cdots$ (Higgs) alignment limit

[Couplings of h are aligned to those of SM.]

- LHC Run2 results of h_{125} measurement



Current data is consistent with SM prediction within experimental uncertainties.

→ We focus on "nearly-alignment" case.

Additional Higgs bosons' decay in nearly-alignment

In nearly alignment case, additional Higgs bosons' decays are very interesting !!

- Additional Higgs couplings with SM particles

$$HWW, HZZ \quad \kappa_V^H = \frac{g_{HVV}^{NP}}{g_{hVV}^{SM}} = \cos(\beta - \alpha)$$

Alignment limit

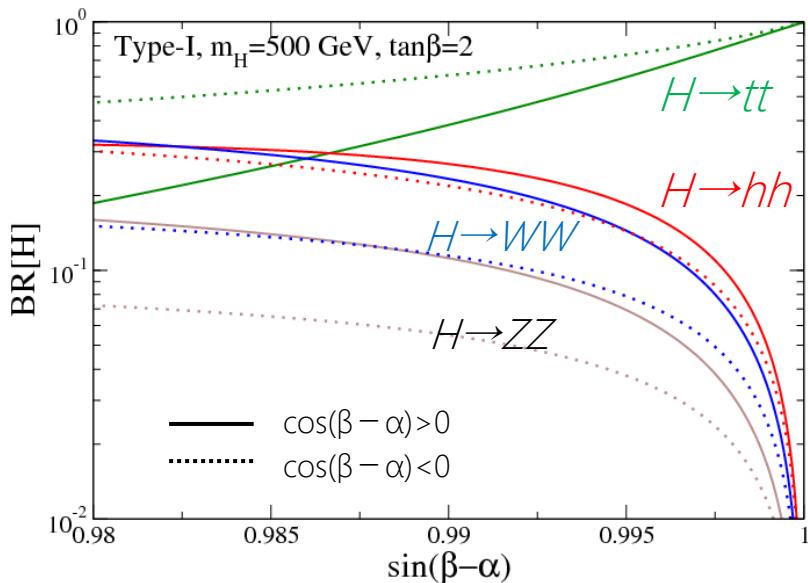
→ C

But, in nearly alignment
they play important roles

$$\lambda_{Hhh} = -\frac{\cos(\beta - \alpha)}{2v \sin 2\beta} \left\{ (2m_h^2 + m_H^2 - 3M^2) \sin 2\alpha + M^2 \sin 2\beta \right\} \rightarrow 0$$

$$Hff \quad \text{Type-I THDM} \quad \kappa_f^H = \cos(\beta - \alpha) - \cot\beta \sin(\beta - \alpha) \quad \rightarrow -\cot\beta$$

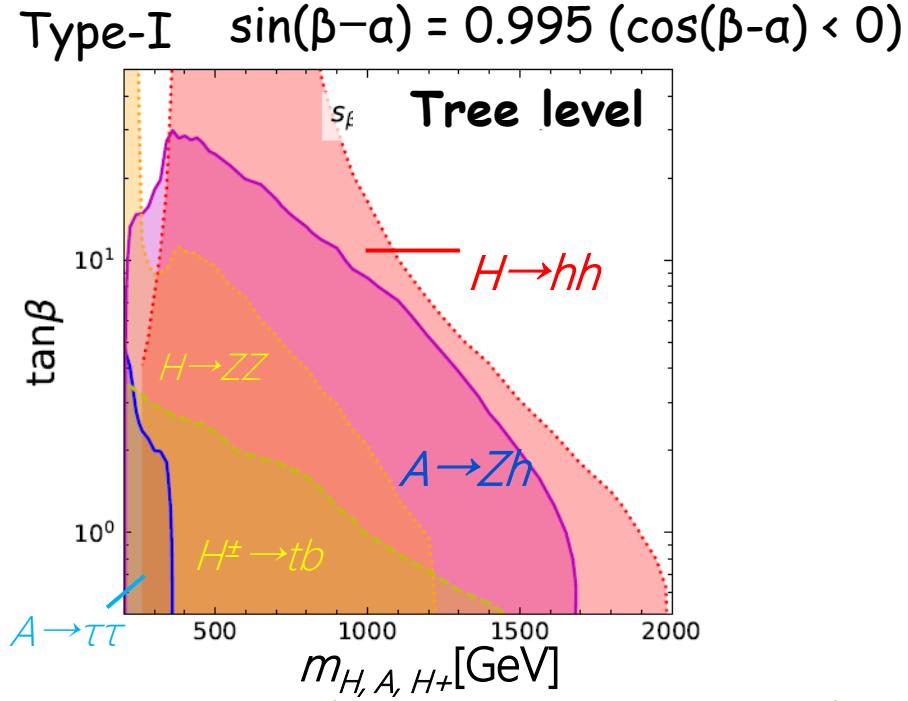
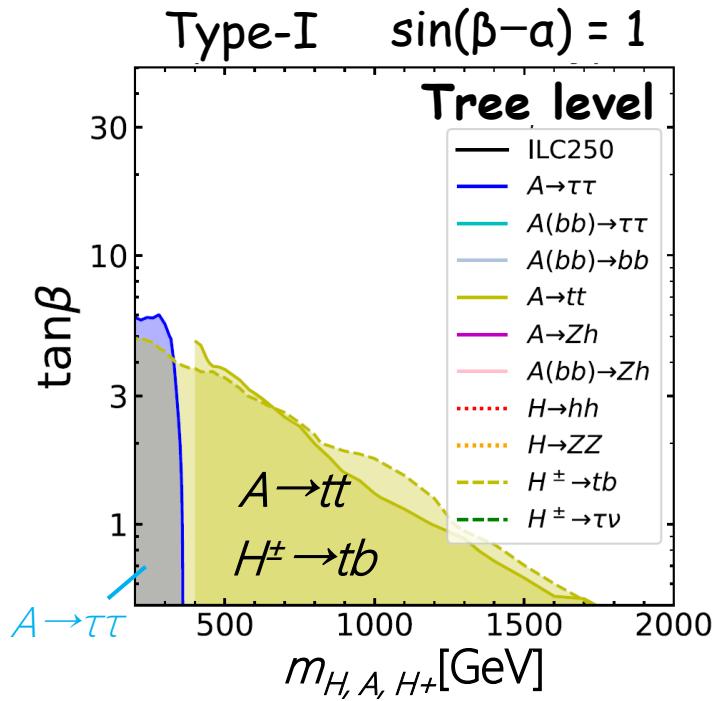
- Branching ratio of H



H-decays are very sensitive to $\sin(\beta - \alpha)$.

Searchable regions in nearly-alignment

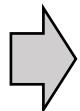
Expected excluded region by direct searches @HL-LHC(3000fb⁻¹) (95%CL)



Aiko, Kanemura, MK, Mawatari, Sakurai,
Yagyu [NPB966(2021)115375]

- Wide parameter region is expected to be surveyed by "Higgs to Higgs decays".
- Additional Higgs decays are very sensitive to $\sin(\beta-\alpha)$.

They are results at tree level.



Precise calculation is necessary for not only h -decays but also additional Higgs decays.

H-COUP project

Numerical program for Full set of BRs of Higgs bosons with radiative corrections.

H-COUP

[éɪtʃ-kú:]

Aiko, Kanemura, MK, Sakurai, Yagyu

Various observables
Couplings,
BR, Γ , ...
 $h \rightarrow VV, h \rightarrow ff, h \rightarrow \gamma\gamma, \dots$

Including radiative corr.

SM
HSM ($\Phi+S$)
THDMs ($\Phi_1+\Phi_2$)
(Type-I, II, X, Y)
IDM ($\Phi+\eta$)

Model Variations



Future precision data

HL-LHC,
ILC, CEPC, FCC, ...

➤ EW and scalar-NLO by on-shell scheme

Kanemura, MK, Yagyu, NPB 896 (2015) 80, Kanemura, MK, Yagyu NPB 917 (2017) 154,
Kanemura, MK, Mawatari, Sakurai, Yagyu, NPB 949 (2019) 114791,
Kanemura, MK, Sakurai, PRD 94 (2016) , Kanemura, MK, Sakurai, Yagyu, PRD 96 (2017)

➤ NNLO QCD corrections by MS-bar scheme

A. Djouadi, Phys. Rept., 457, 1 (2008), M. Spira, Prog. Part. Nucl. Phys., 95, 98 (2017),
K. G. Chetyrkin, A. Kwiatkowski, Nucl. Phys., B461, 3 (1996)...

Explore Higgs sector

Ver. 1 (2017)

: Renormalized vertices of $h(125)$. Kanemura, MK, Sakurai, Yagyu, CPC.233(2018)134

Ver. 2 (2019)

: Decay BRs of $h(125)$. Kanemura, MK, Mawatari, Sakurai, Yagyu, CPC 257(2020) 107512

Ver. 3(Coming soon) : Decay BRs of additional Higgs bosons

【Other public tools】

★2HDECAY : [M. Krause, M. Mühlleitner, M. Spira], ★Prophecy4f : [A. Denner, S. Dittmaier, A. Mück]

H-COUP ver.3

Processes in THDMs

NPB 973 (2021) 115581, Aiko, Kanemura, Sakurai

NPB 983(2022)115906 Kanemura, MK, Yagyu

NPB 986 (2023) 116047 Aiko, Kanemura, Sakurai,

CP-even	CP-odd	Charged
$H \rightarrow VV$	$A \rightarrow ff$	$H^\pm \rightarrow ff'$
$H \rightarrow ff$	$A \rightarrow Zh, ZH$	$H^\pm \rightarrow AW$
$H \rightarrow hh$	$A \rightarrow H^\pm W$	$H^\pm \rightarrow HW, hW$
$H \rightarrow AA, H^+H^-$	$A \rightarrow ZZ, WW, \gamma\gamma, \gamma Z$	$H^\pm \rightarrow W\gamma, WZ$
$H \rightarrow AZ, H^\pm W$		
$H \rightarrow \gamma\gamma, \gamma Z, gg$		

HSM

CP-even
$H \rightarrow VV$
$H \rightarrow ff$
$H \rightarrow hh$
$H \rightarrow \gamma\gamma, \gamma Z, gg$

IDM

CP-even	CP-odd	Charged
$H \rightarrow AZ$	$A \rightarrow Zh$	$H^\pm \rightarrow AW$
$H \rightarrow H^\pm W$	$A \rightarrow H^\pm W$	$H^\pm \rightarrow HW$

We show results for decays of $H \rightarrow hh$, $A \rightarrow Zh$, $h \rightarrow VV^*$, $h \rightarrow ff$ in THDMs.

Loop corrections to $\Gamma[H \rightarrow hh]$

- NLO contributions works constructively or destructively
 $\cos(\beta - \alpha) > 0 \cdots$ constructively, $\cos(\beta - \alpha) < 0 \cdots$ destructively

$$\Gamma_{\text{NLO}}[H \rightarrow hh] = \left| \begin{array}{c} \text{cos}(\beta - \alpha) \\ \text{---} \quad \text{---} \end{array} \right|^2 + 2\text{Re} \left[\begin{array}{c} \text{---} \quad \text{---} \\ \text{---} \quad \text{---} \end{array} \times \begin{array}{c} \text{cos}(\beta - \alpha) \\ \text{---} \quad \text{---} \end{array} \right]$$

- Decoupling? Or Non-decoupling?

$M^2 \gg \lambda_\Phi v^2$ ($m_\Phi^2 \simeq M^2$) \cdots Decoupling

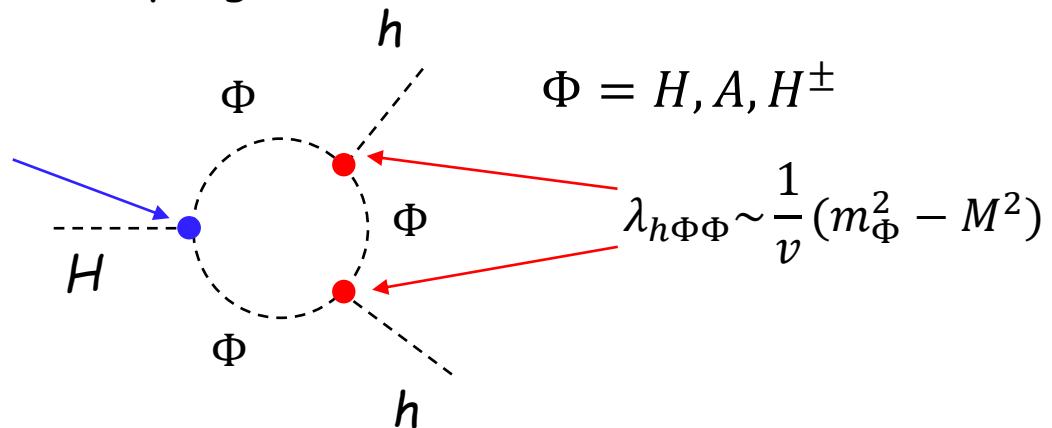
Scalar self couplings

$$m_\Phi^2 \cong \lambda_\Phi v^2 + M^2$$

$M^2 \simeq \lambda' v^2$ \cdots Non-decoupling

$\cos(\beta - \alpha) \ll 1$ case

$$\lambda_{H\Phi\Phi} \sim \frac{1}{v} (m_H^2 - M^2)$$

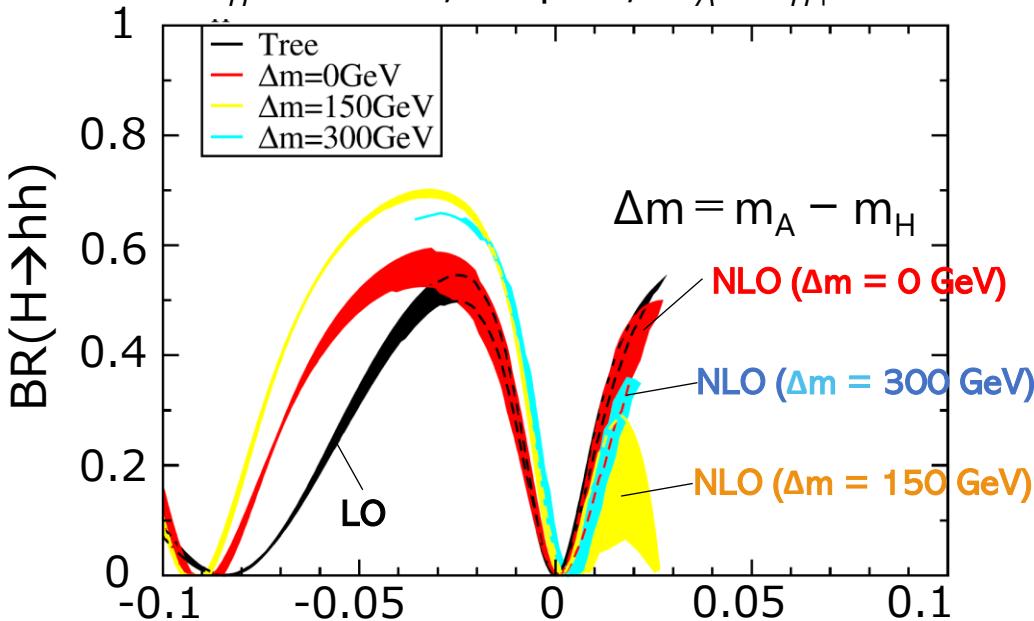


$(m_{A,H^\pm} - m_H \neq 0)$ case

Even if $m_H^2 \simeq M^2$, corrections of H^\pm, A loop diagrams are not suppressed.

Correlation between $H \rightarrow hh$ and $h \rightarrow WW^*$ ¹⁰

Type-I $m_H = 500\text{GeV}$, $\tan\beta = 5$, $m_A = m_{H+}$



NPB 983(2022)115906
Kanemura, MK, Yagyu

$$\Gamma_{\text{LO}}^{\text{THDM}}[h \rightarrow WW^*] \propto \sin^2(\beta - \alpha)$$

$$\text{If } \cos(\beta - \alpha) > 0 \cdots \Gamma_h^{\text{THDM}} > \Gamma_h^{\text{SM}}$$

$$\text{If } \cos(\beta - \alpha) < 0 \cdots \Gamma_h^{\text{THDM}} < \Gamma_h^{\text{SM}}$$

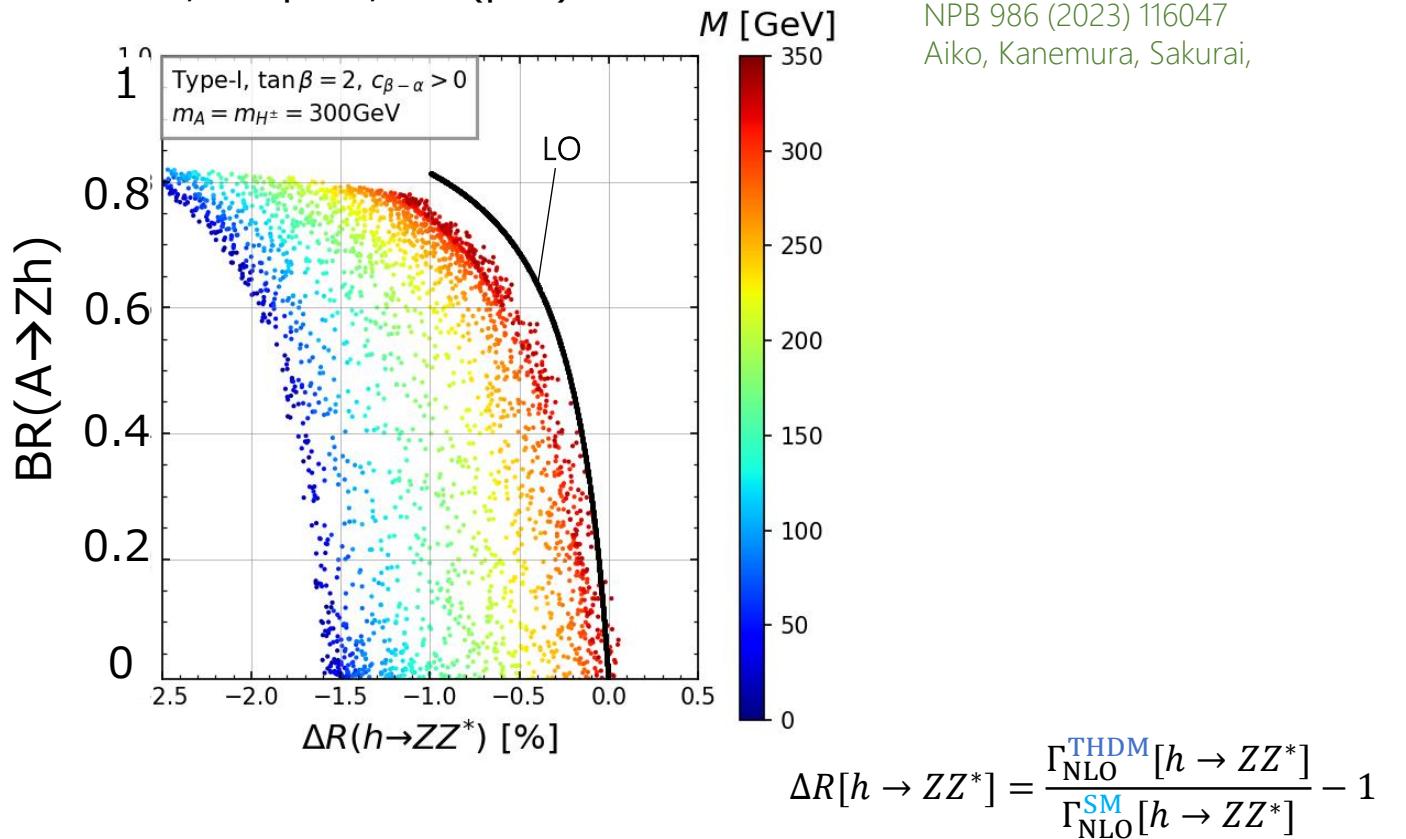
$$\Delta\mu[h \rightarrow WW^*] = \frac{\text{BR}_{\text{NLO}}^{\text{THDM}}[h \rightarrow WW^*]}{\text{BR}_{\text{NLO}}^{\text{SM}}[h \rightarrow WW^*]} - 1$$

Correlation between $\text{BR}(H \rightarrow hh)$ and $\text{BR}(h \rightarrow WW^*)$ is changed from LO by $O(10)\%$.

It is important to evaluate both h -decays and H -decays with loop corrections simultaneously.

Correlation between $A \rightarrow Zh$ and $h \rightarrow ZZ^*$

Type-I $m_A = m_{H^\pm} = 300\text{GeV}$, $\tan\beta = 2$, $\cos(\beta - \alpha) > 0$

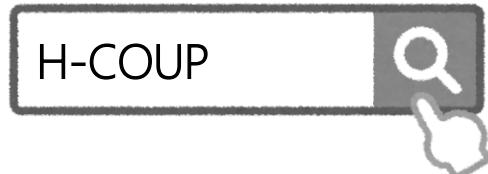


$\text{BR}[A \rightarrow Zh]$ also receives $O(10)\%$ correction if $\tan\beta \approx 2$.

Correlation between $\text{BR}(A \rightarrow Zh)$ and $\Delta R(h \rightarrow ZZ^*)$ is significantly changed from LO.

Summary

- LHC results of h_{125} measurements indicate "nearly alignment", where additional Higgs bosons' decays are very interesting !!
- Study of radiative corrections to decays of both additional Higgs bosons and h_{125} are essentially important.
- We show results of $\text{BR}[\text{Higgs to Higgs decays}]$ and $\text{BR}[h_{125}]$ including radiative corrections.
- $\text{BR}[H \rightarrow hh]$ with NLO correction can change LO prediction by $O(10)\%$.
 $\text{BR}[A \rightarrow Zh]$ also receives $O(10)\%$ correction if $\tan\beta \approx 2$.
- Correlations between $A \rightarrow Zh$ / $H \rightarrow hh$ and $h \rightarrow VV^*$ are significantly changed from LO.
- We will release H-COUP ver.3.



Counter terms

Parameter shift :

$$m_\varphi^2 \rightarrow m_\varphi^2 + \delta m_\varphi^2, \quad \alpha \rightarrow \alpha + \delta\alpha, \quad \beta \rightarrow \beta + \delta\beta, \quad M^2 \rightarrow M^2 + \delta M^2, \quad 8$$

Field shift :

$$\begin{pmatrix} H \\ h \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_H & \delta C_{Hh} + \delta\alpha \\ \delta C_{hH} - \delta\alpha & 1 + \delta Z_h \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

$$\begin{pmatrix} G^0 \\ A \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_G & \delta C_{GA} + \delta\beta \\ \delta C_{AG} - \delta\beta & 1 + \delta Z_A \end{pmatrix} \begin{pmatrix} G^0 \\ A \end{pmatrix}$$

$$\begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix} \rightarrow \begin{pmatrix} 1 + \delta Z_{G+} & \delta C_{GH^\pm} + \delta\beta \\ \delta C_{H^\pm G} - \delta\beta & 1 + \delta Z_{H^\pm} \end{pmatrix} \begin{pmatrix} G^\pm \\ H^\pm \end{pmatrix}$$

6 + 6

8(parameters) + 6(fields) + 6(field mixing) = 20

On-shell renormalization conditions

$$\delta m_i^2 \quad \delta Z_i \quad i = h, H, A, H^\pm$$

$$\hat{\Pi}_{ii}[m_i^2] = 0, \quad \frac{d}{dp^2} \hat{\Pi}_{ii}[p^2] \Big|_{p^2=m_i^2} = 1, \quad \rightarrow \quad \delta m_i^2 = \tilde{\Pi}_{ii}^{1\text{PI}}[m_i^2], \quad \delta Z_i = -\frac{d}{dp^2} \Pi_{ii}^{1\text{PI}}[p^2] \Big|_{p^2=m_i^2}.$$

$$\delta C_h \quad \delta C_A \quad \delta \alpha \quad \delta \beta$$

$$\hat{\Pi}_{hH}[m_h^2] = \hat{\Pi}_{hH}[m_H^2] = 0, \quad \hat{\Pi}_{AG^0}[m_A^2] = \hat{\Pi}_{AG^0}[0] = 0,$$



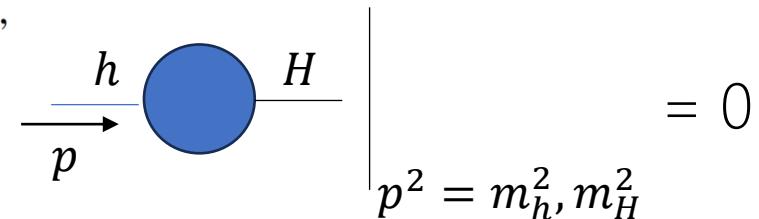
$$\delta C_h = \frac{1}{2(m_H^2 - m_h^2)} \left(\Pi_{Hh}^{1\text{PI}}[m_h^2] - \Pi_{Hh}^{1\text{PI}}[m_H^2] \right),$$

$$\delta C_A = -\frac{1}{2m_A^2} \left(\Pi_{Hh}^{1\text{PI}}[m_A^2] - \Pi_{Hh}^{1\text{PI}}[0] \right),$$

$$\delta \alpha_f = \frac{1}{2(m_H^2 - m_h^2)} \left(\tilde{\Pi}_{Hh}^{1\text{PI}}[m_h^2] + \tilde{\Pi}_{Hh}^{1\text{PI}}[m_H^2] \right),$$

$$\delta \beta_f = -\frac{1}{2m_A^2} \left(\tilde{\Pi}_{AG}^{1\text{PI}}[m_A^2] + \tilde{\Pi}_{AG}^{1\text{PI}}[0] \right),$$

we take $\delta C_{hH} = \delta C_{Hh} \equiv \delta C_h$ and $\delta C_{AG^0} = \delta C_{G^0A} \equiv \delta C_A$.

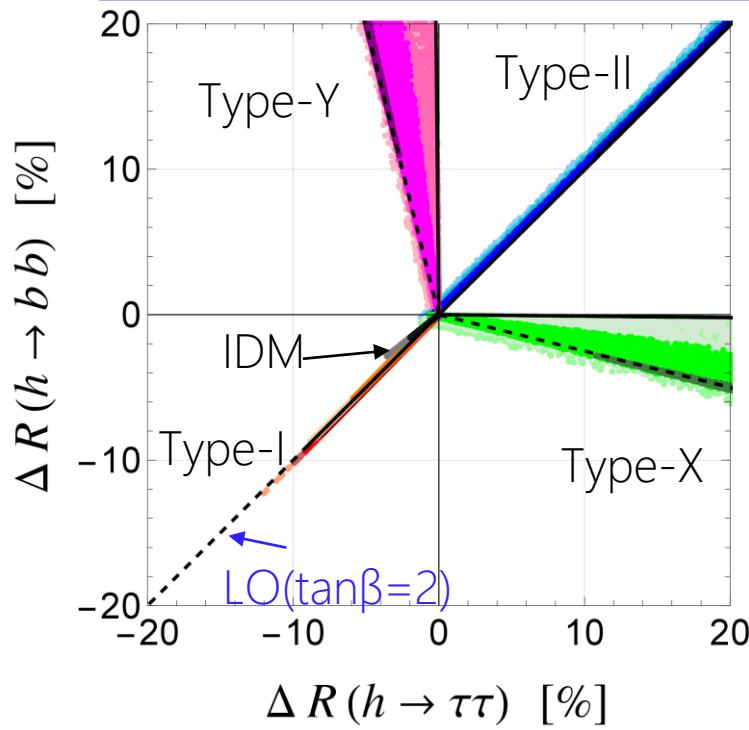


$$= 0$$

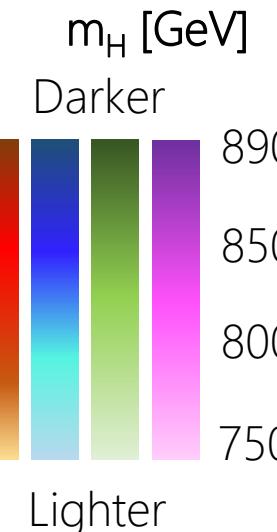
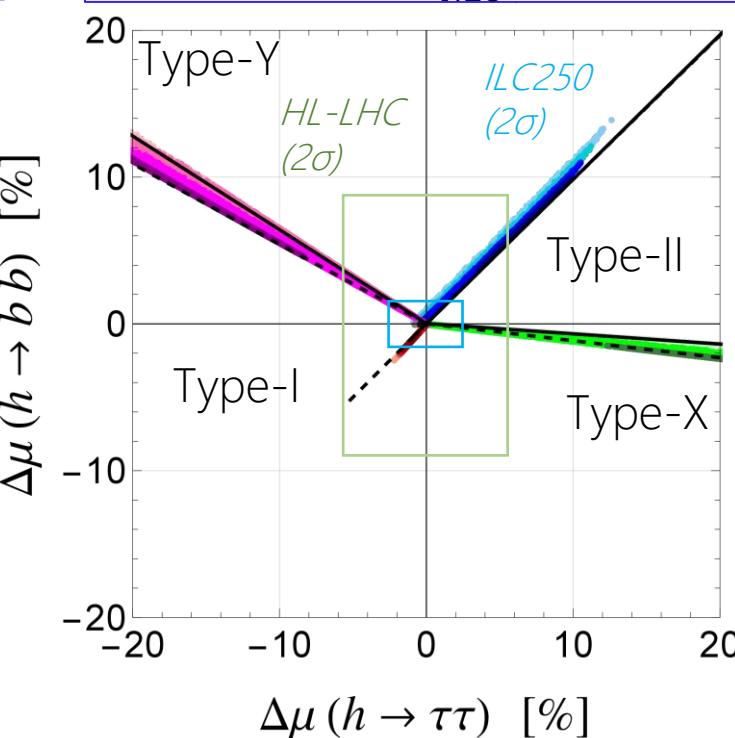
$h \rightarrow bb, h \rightarrow \tau\tau$

$m_A = m_{H^\pm} = 800 \text{ GeV}, \cos(\beta - \alpha) < 0$

$$\Delta R[h \rightarrow XX] = \frac{\Gamma_{\text{NLO}}^{\text{THDM}}[h \rightarrow XX]}{\Gamma_{\text{NLO}}^{\text{SM}}[h \rightarrow XX]} - 1$$



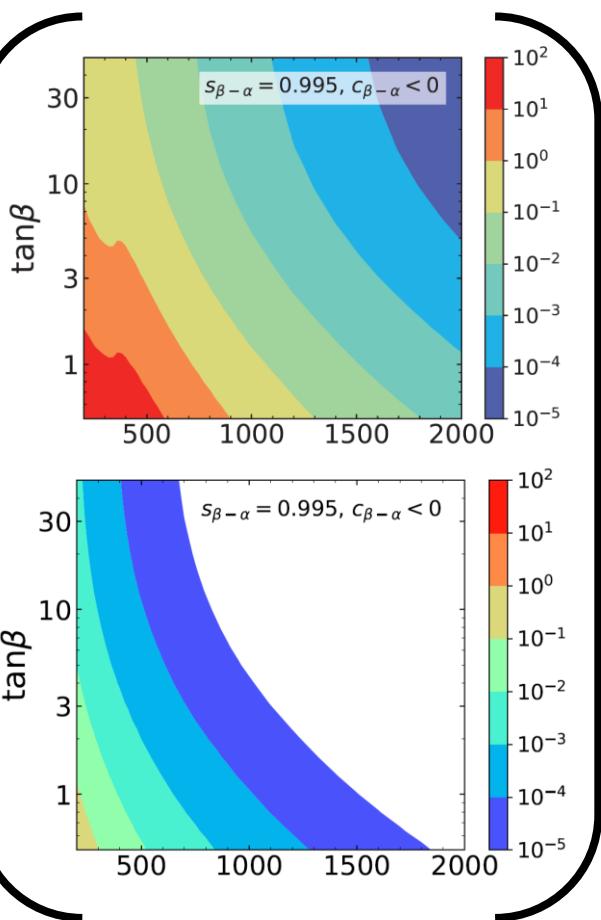
$$\Delta\mu[h \rightarrow XX] = \frac{\text{BR}_{\text{NLO}}^{\text{THDM}}[h \rightarrow XY]}{\text{BR}_{\text{NLO}}^{\text{SM}}[h \rightarrow XY]} - 1$$



If $|\Delta R[h \rightarrow bb/\tau\tau]| >$ several %, prediction of each Type does not overlap

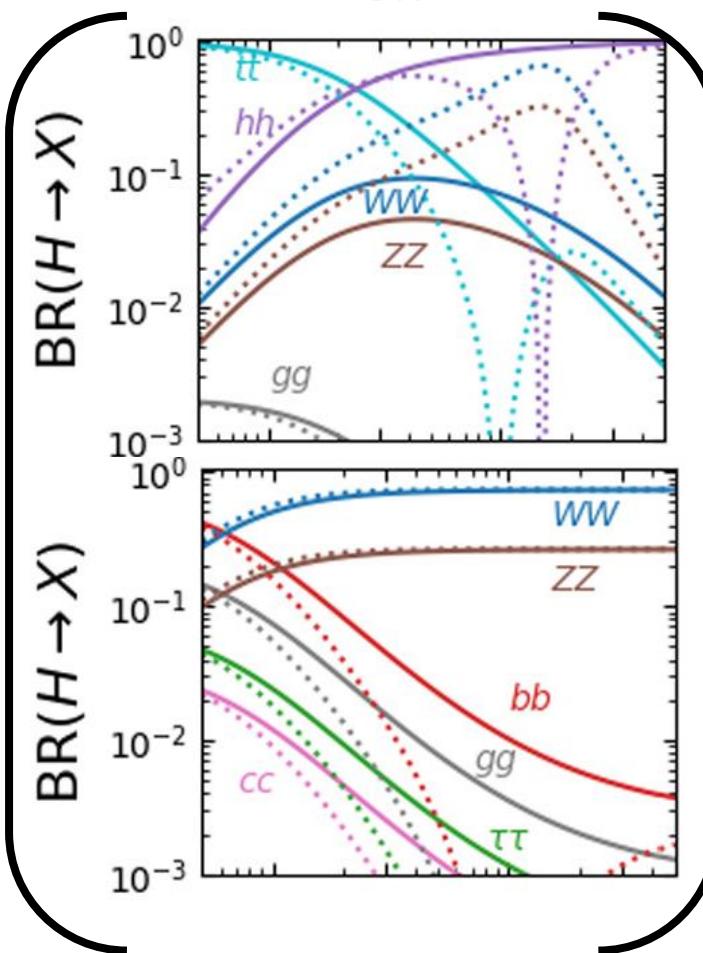
Constraint from direct searches (Run2)

Production cross section



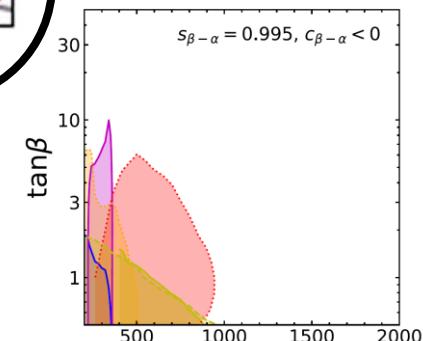
✗

BR



Compare

obtain
Constraints

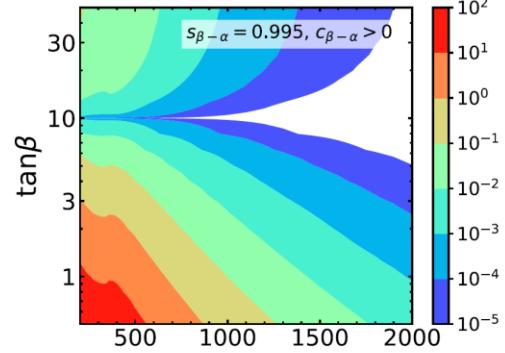


Upper limits
at 95% CL
with 36fb^-1
data

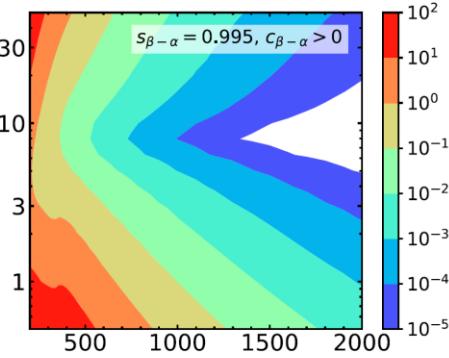
H production

$\text{Cos}(\beta - \alpha) > 0$

gluon-fusion process ($\text{pp} \rightarrow \text{H}$),

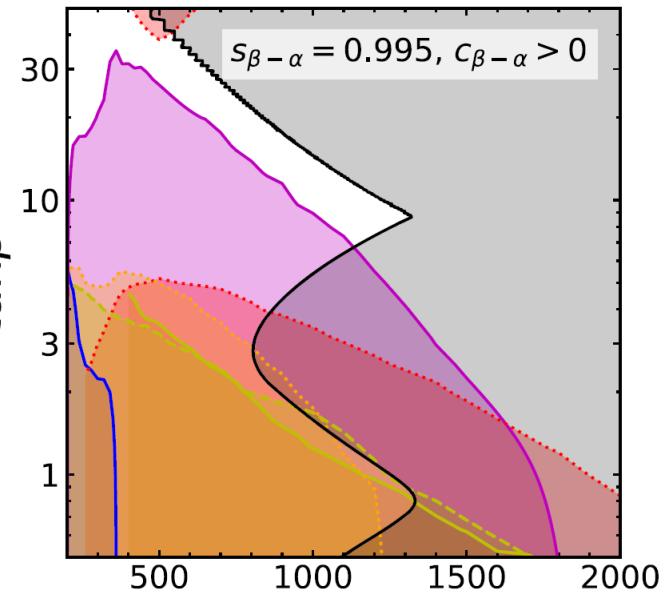
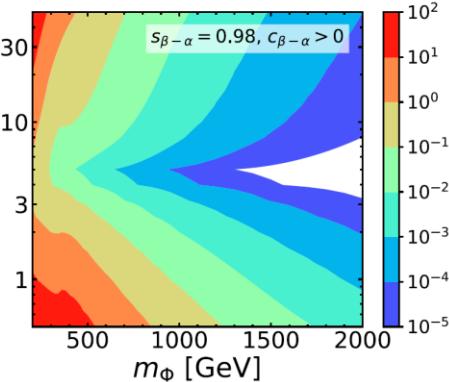
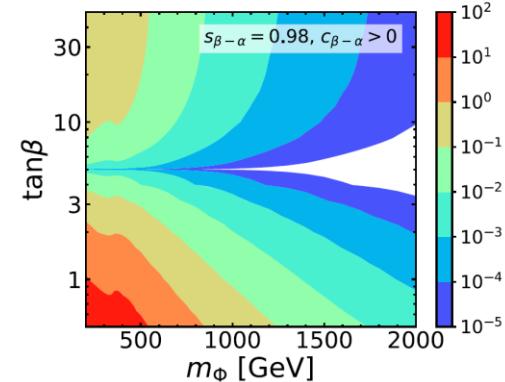
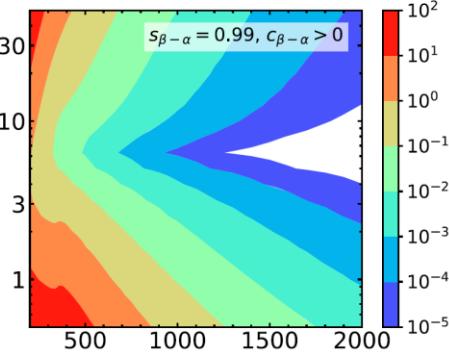
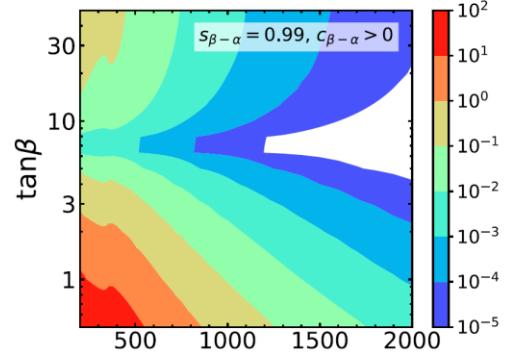


bottom associated process($\text{pp} \rightarrow \text{H(bb)}$)



13TeV LHC

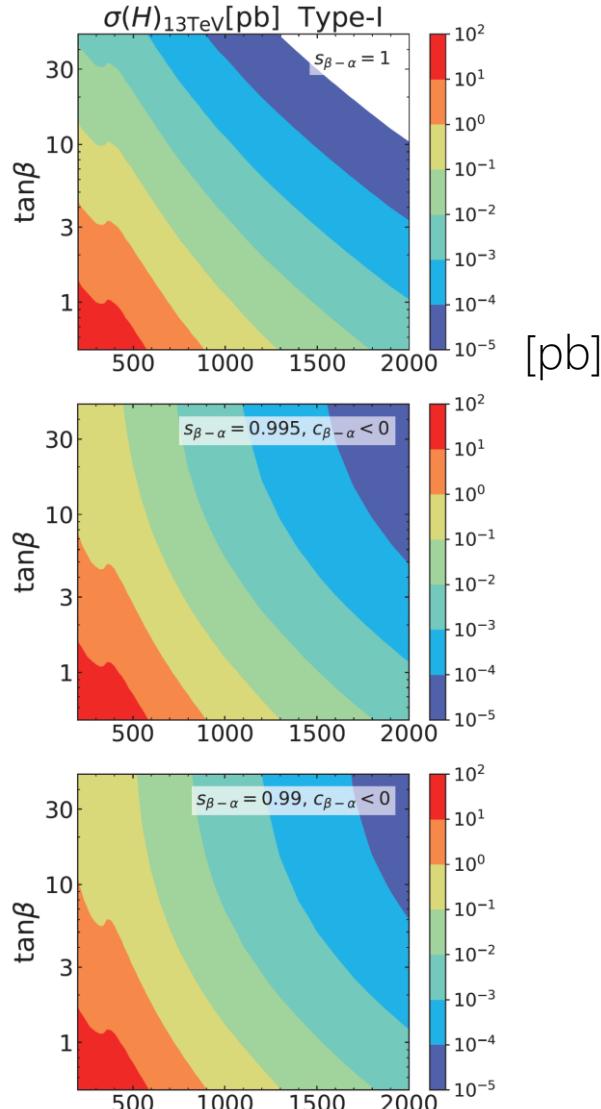
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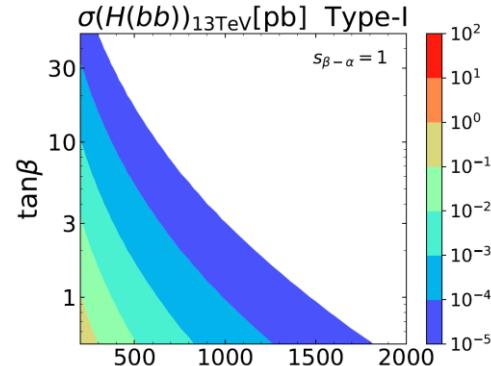
H production

$\text{Cos}(\beta - \alpha) < 0$

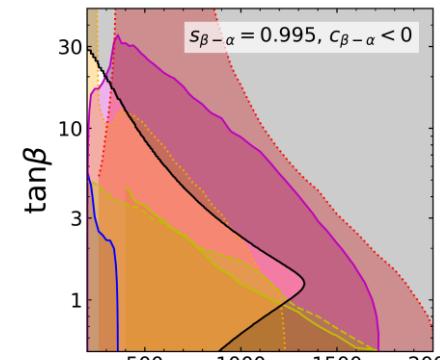
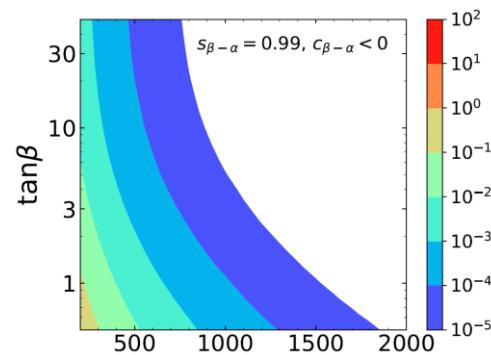
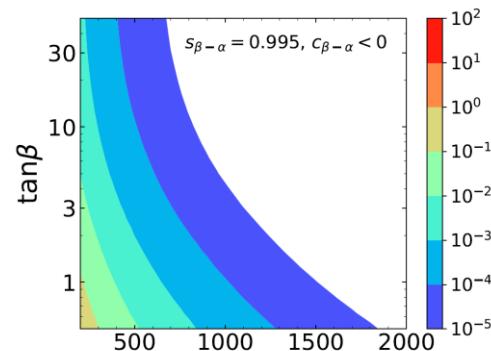
gluon-fusion process ($\text{pp} \rightarrow \text{H}$),



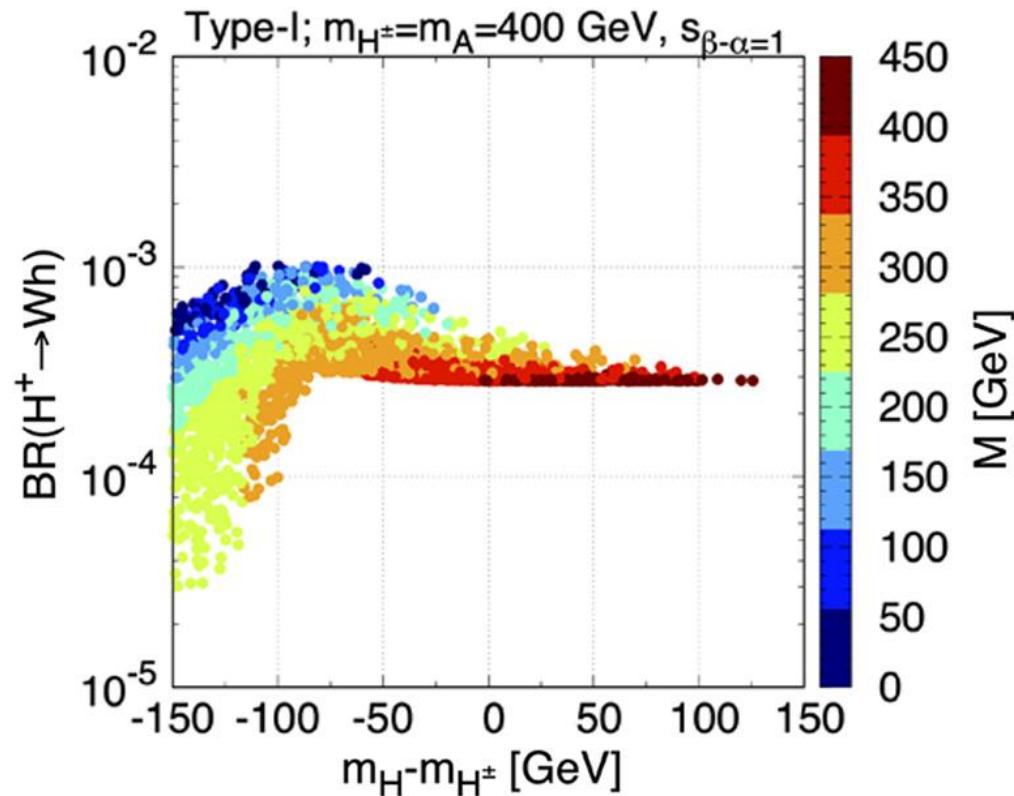
bottom associated process($\text{pp} \rightarrow \text{H(bb)}$)



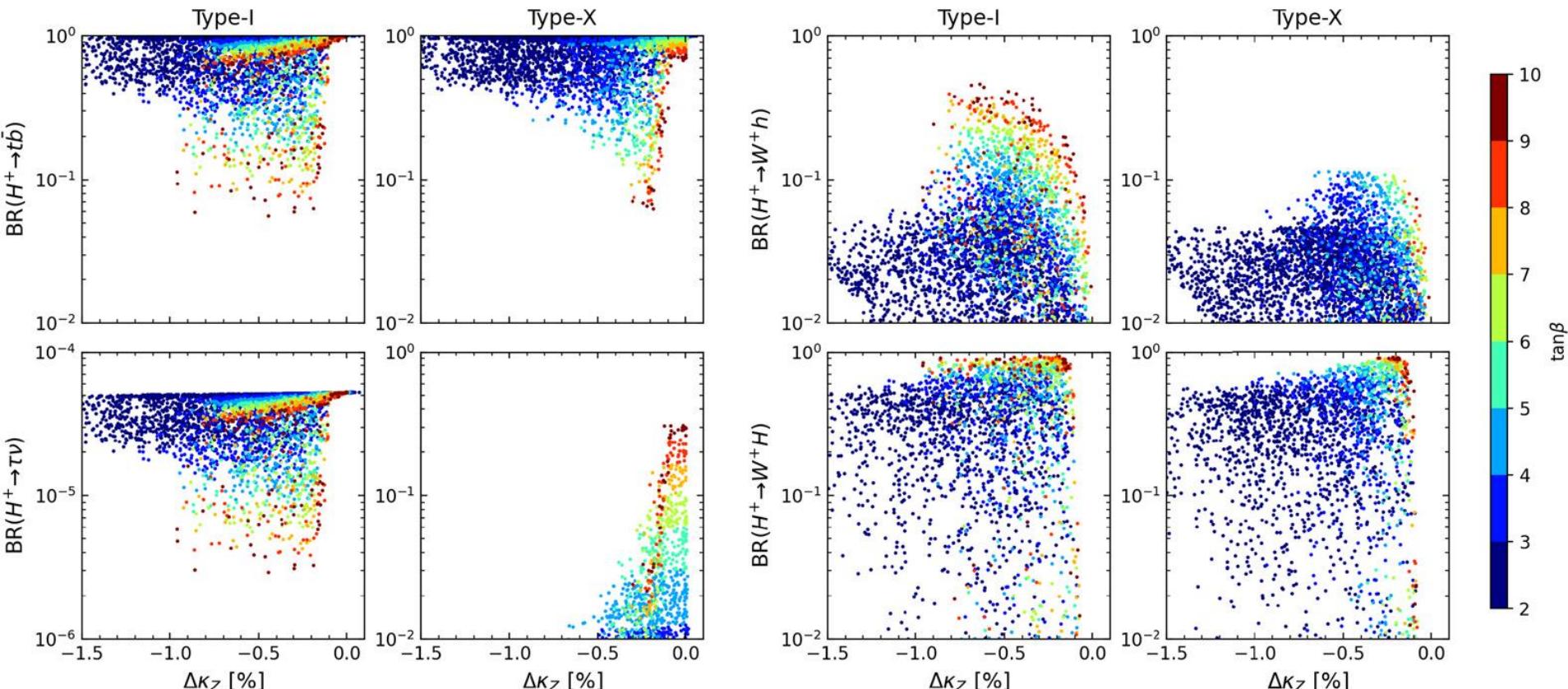
13TeV LHC



H^+ decays

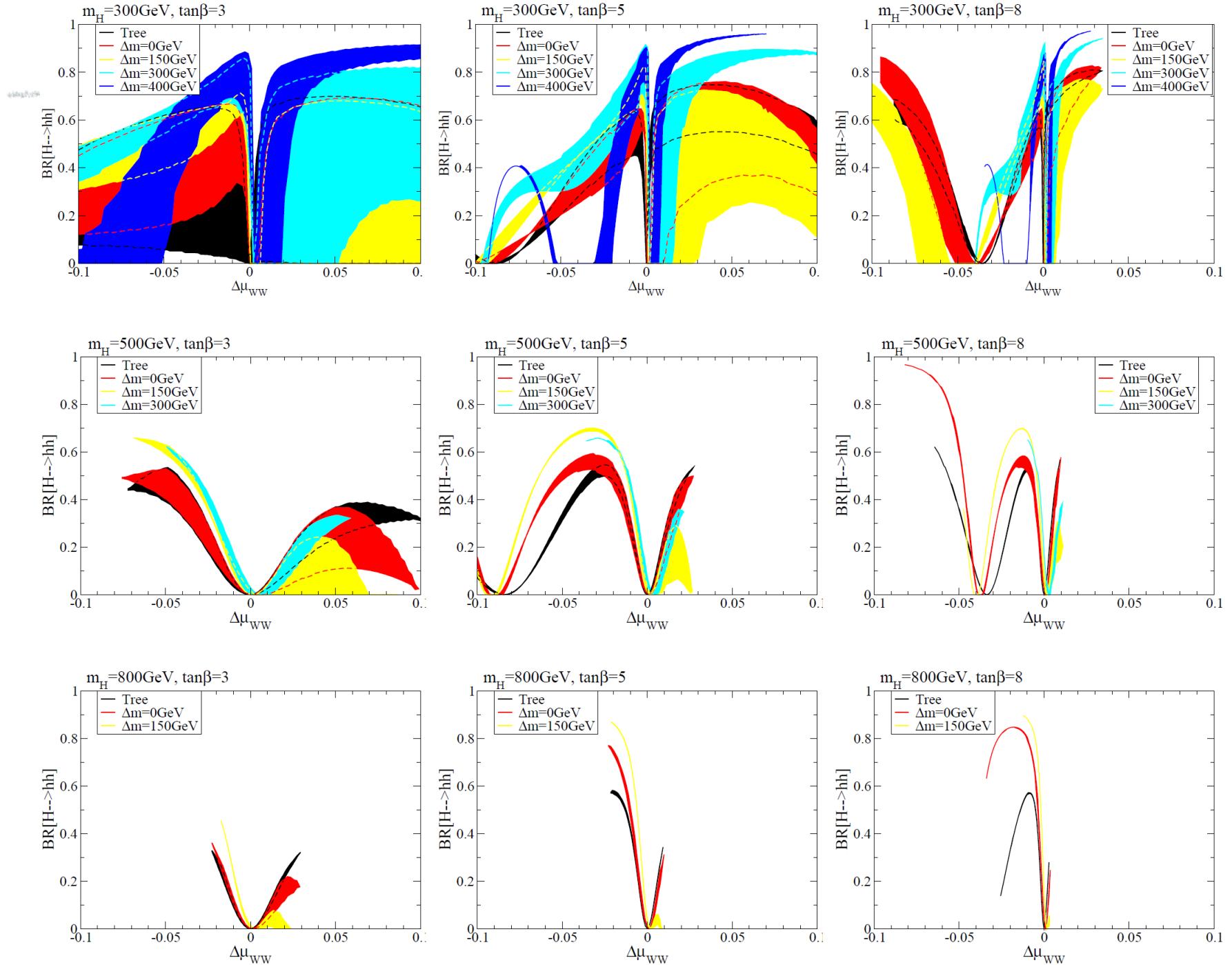


H^+ decays



$$m_{H^+} = m_A = 400 \text{ GeV}$$

$$\Delta\kappa_Z = \sqrt{\frac{a}{b}}$$



Correlation between $A \rightarrow Zh$ and $h \rightarrow ZZ^*$

