

Inflatable Dark Matter

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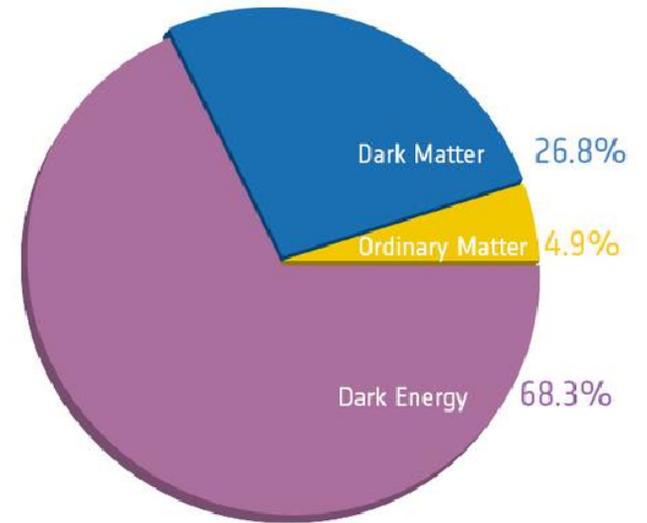
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Based on: H. D., D. Hooper and S. D. McDermott, Phys. Rev. Lett. **116**, no. 3, 031303 (2016)
arXiv:1507.08660 [hep-ph]

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- Dark matter (DM): a new substance
- Something beyond the Standard Model (SM)
- Stable on cosmological time scales
- So far manifested only through gravity
- Generally expected to have other interactions
- Couplings: DM-SM weak; DM-DM not too strong



Planck

★ *Guiding principles needed to narrow multitude of possibilities*

- Is there a bigger picture where DM naturally arises?
- Hierarchy and extended EW sectors → WIMP miracle
- Can the same physics address another mystery?
- Strong CP → QCD axion DM
- Do observations offer a clue?
- $\Omega_{\text{DM}} \sim 5 \Omega_{\text{baryon}} \rightarrow$ Asymmetric DM

DM and SM Extensions

- $\Omega^{\text{th}} < \Omega^{\text{meas}} \Rightarrow$ Other contributions to $\Omega^{\text{meas}} \simeq 0.26$
- Less economical, but does not rule out a model per se
- Generally, models get ruled out when $\Omega^{\text{th}} > \Omega^{\text{meas}}$
- “Overclosing” the Universe (premised on *standard cosmology*)

Examples:

- Thermal Relic WIMP: $\Omega_{\text{WIMP}}^{\text{th}} \propto 1/\langle\sigma v\rangle_{\text{ann}} \sim M^2/g^4$, with $M \sim \text{TeV}$
- Experimental searches: g gets smaller and/or M gets larger $\Rightarrow \Omega_{\text{WIMP}}^{\text{th}} > \Omega^{\text{meas}}$
- QCD axion good DM if Peccei-Quinn scale $f_{\text{PQ}} \lesssim 10^{12}$ GeV
- Assuming “natural” misalignment
- String theory offers multitude of axion candidates ($f_{\text{PQ}} \gg 10^{12}$ GeV)
- $\Omega_a \propto f_{\text{PQ}}^n$ with $n \approx 1 \Rightarrow$ disfavors natural UV scales $M_{\text{Planck}}, M_{\text{GUT}}$
- Anthropic arguments? [Linde, 1988](#); [Wilczek, 2004](#)

This talk: consider diluting DM density through **inflation**

- Inflation after DM “production”
- Thermal relic freeze-out at $T \lesssim m_{\text{DM}}/20$
- Axion oscillation at $T \lesssim \Lambda_{\text{QCD}}$ (200 MeV)
- ...
- For illustrative purposes, we focus on *thermal inflation*
- Dilutions of $\mathcal{O}(10 - 1000)$ can be realized in simple models
- Inflation can originate in a “hidden sector” largely decoupled from the SM
- Elusive laboratory signals, yet significant effect on the visible sector cosmology
- Space of viable DM models opens up for **“Inflatable DM”**

Inflation: Guth 1981; Linde 1982; Albrecht, Steinhardt, 1982

Thermal Inflation: Lyth, Stewart, 1995

Some Background

- Similar effects may obtain from late decay of moduli, massive states

Recent work: Patwardhan, Fuller, Kishimoto, Kusenko, 2015

- Earlier discussions of inflation for axion DM with $f_{\text{PQ}} \gg 10^{12}$ GeV

Dimopoulos, Hall, 1988; Fox, Pierce, Thomas, 2004

- Thermal inflation has been invoked to address cosmological problems (gravitinos, baryogenesis, moduli)

Lazarides, Panagiotakopoulos, Shafi, 1986; Yamamoto, 1986; Lyth, Stewart, 1995

- Inflation from first order QCD phase transition with $\mathcal{O}(1)$ baryon asymmetry

Kämpfer, 1986; Borghini, Cottingham, Vinh Mau, 2000; Boeckel, Schaffner-Bielich, 2009

Inflation: A period of exponential expansion

- Driven by energy density with negative pressure
- Happens whenever $\rho_\Lambda g_{\mu\nu}$ dominates cosmic $\langle \Theta_{\mu\nu} \rangle$
- ρ_Λ : scalar potentials, confining dynamics, cosmological constant
- “Inflation” can then be quite generic during cosmological evolution
- Apparently happened at the beginning ($\gtrsim 60$ e -folds) and happening right now!
- Moderate amounts of inflation easy to achieve

We entertain the possibility that the radiation dominated era may have been punctuated by brief inflationary interludes.

- We consider $T \gtrsim 1$ MeV to avoid conflict with BBN data

A Toy Model

- Simple inflationary sector: scalar ϕ and fermions f

$$\mathcal{L} \supset -\frac{1}{2}\mu_\phi^2\phi^2 + \sum_f y_f \bar{f}f\phi + \frac{1}{4!}\lambda_\phi\phi^4$$

- These fields do not need to carry any SM charges (hidden sector)
- Similar to SM; not very exotic!
- $v_\phi = \langle\phi\rangle = \mu_\phi\sqrt{6/\lambda_\phi}$; $m_\phi^2 = 2\mu_\phi^2$
- For simplicity, assume $(\phi, \forall f)$ in thermal equilibrium with SM
- For example, from a small degree of mixing via $\phi^2 H^\dagger H$
- Similar physics may arise from non-trivial (QCD-like) dynamics
- Estimates requires non-perturbative analysis (lattice)

- Thermal Potential

$$V(\phi) = V_0 + \frac{1}{4!}\lambda_\phi\phi^4 + \frac{1}{2} \left[\frac{1}{12} \left(\sum_f \mathbf{g}_f y_f^2 + \frac{1}{2}\lambda_\phi \right) T^2 - \mu_\phi^2 \right] \phi^2$$

- $V_0 = 3\mu_\phi^4/2\lambda_\phi$; $V(v_\phi) = 0$
- $\mathbf{g}_f = 1(2)$ for a Majorana (Dirac) f with $m_f \lesssim T$
- Cubic term forbidden by \mathbb{Z}_2 at $T = 0$, and higher order for $T \neq 0$ (λ_ϕ small)
- Inflation starts when $V_0 > \rho_R(T)$ $\rho_R(T) = \pi^2 g_{\text{eff}}(T) T^4/30$

$$T_s \simeq \mu_\phi \left(\frac{45}{\pi^2 g_s \lambda_\phi} \right)^{1/4}$$

- Inflation ends upon phase transition (thermal mass < 0)

$$T_{pt} = \sqrt{\frac{12}{\sum_f \mathbf{g}_f y_f^2 + \lambda_\phi/2}} \mu_\phi$$

See also: Cohen, Morrissey, Pierce, 2008

- Inflation possible if $T_s \gtrsim T_{pt}$, implies bound on $\lambda_\phi \lesssim \lambda_c$
- For perturbative branch (N_D Dirac fermions, $y_f = y$):

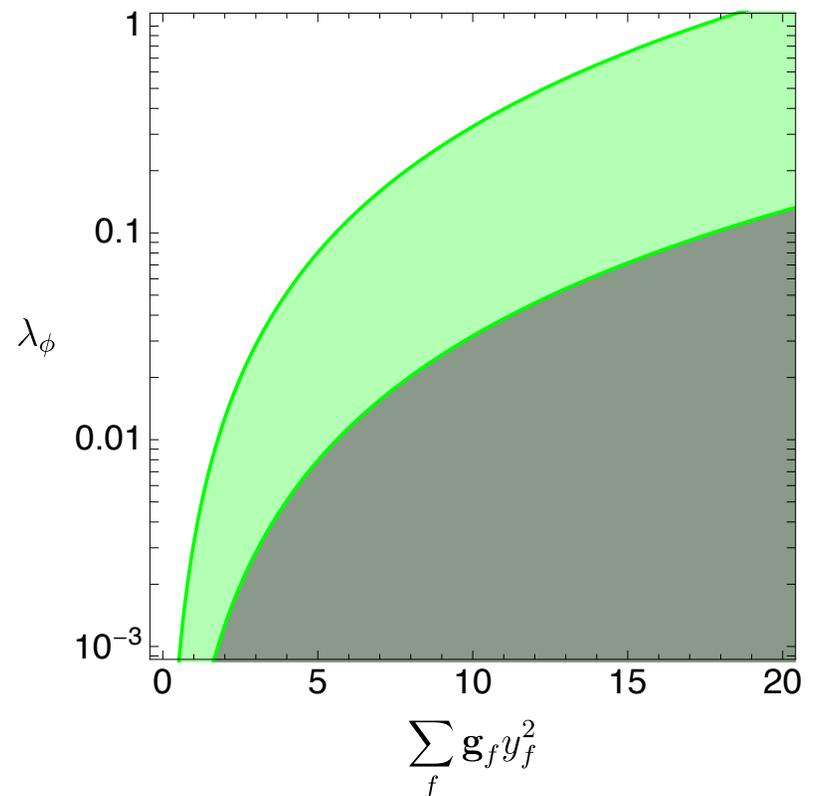
$$\lambda_c \equiv \frac{5}{16\pi^2 g_s} \left(\sum_f g_f y_f^2 \right)^2 \simeq \frac{N_D^2 y^4}{790} \times \left(\frac{100}{g_s} \right)$$

$$(\lambda_\phi \ll 2 \sum_f g_f y_f^2)$$

- Quantum loops:

$$\delta(\lambda_\phi)_f \sim -\left(3 \sum_f y_f^4 / 2\pi^2\right) \log(\phi^2 / v_\phi^2)$$

- $\lambda_c < |\delta(\lambda_\phi)_f|$: Model is fine-tuned
- Instability for $\lambda_\phi < 0$
- ★ Live in a long-lived meta-stable universe
- ★ Or:
 - Use only scalars
 - Add scalars in the UV model
 - Can be above $\sim T_s$, thermally decoupled



Green (gray) $g_s = 10$ (100)

- Thermal potential turns off as Universe inflates, ϕ rolls to $\langle\phi\rangle$
- ϕ oscillates and decays (instantaneous), reheating to $T = T_{\text{RH}}$
- Large entropy release, dilution of DM density by $\Delta = s_{\text{RH}}/s_{\text{pt}}$

- Toy model:

$$\Delta_{\phi} = \frac{g_{\text{RH}}}{g_{\text{pt}}} \left(\frac{T_{\text{RH}}}{T_{\text{pt}}} \right)^3 = \left[\left(\frac{g_{\text{RH}}}{g_{\text{pt}}} \right)^{1/3} + \frac{g_{\text{RH}}^{1/3} g_s \lambda_c}{g_{\text{pt}}^{4/3} \lambda_{\phi}} \right]^{3/4}$$

Δ_{ϕ} commensurate with fine-tuning

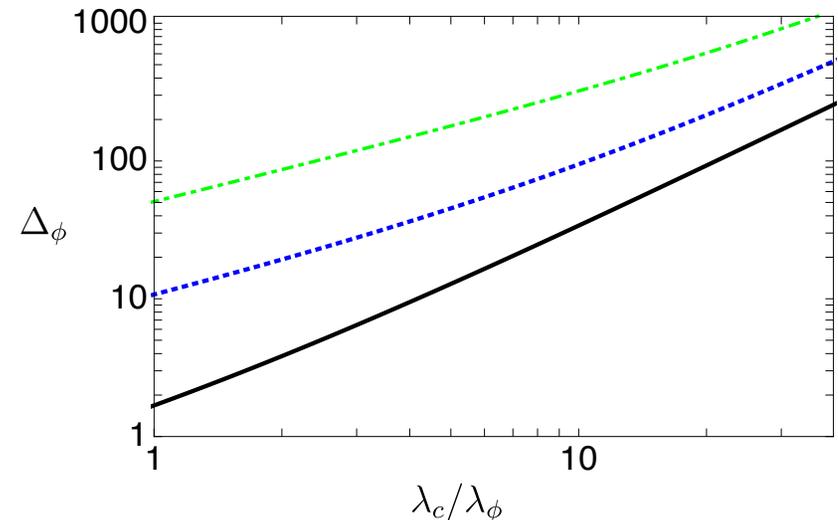
Cohen, Morrissey, Pierce, 2008

Using conservation of energy

$$\rho_R(T_{\text{RH}}) = \rho_R(T_{\text{pt}}) + \rho_{\phi}$$

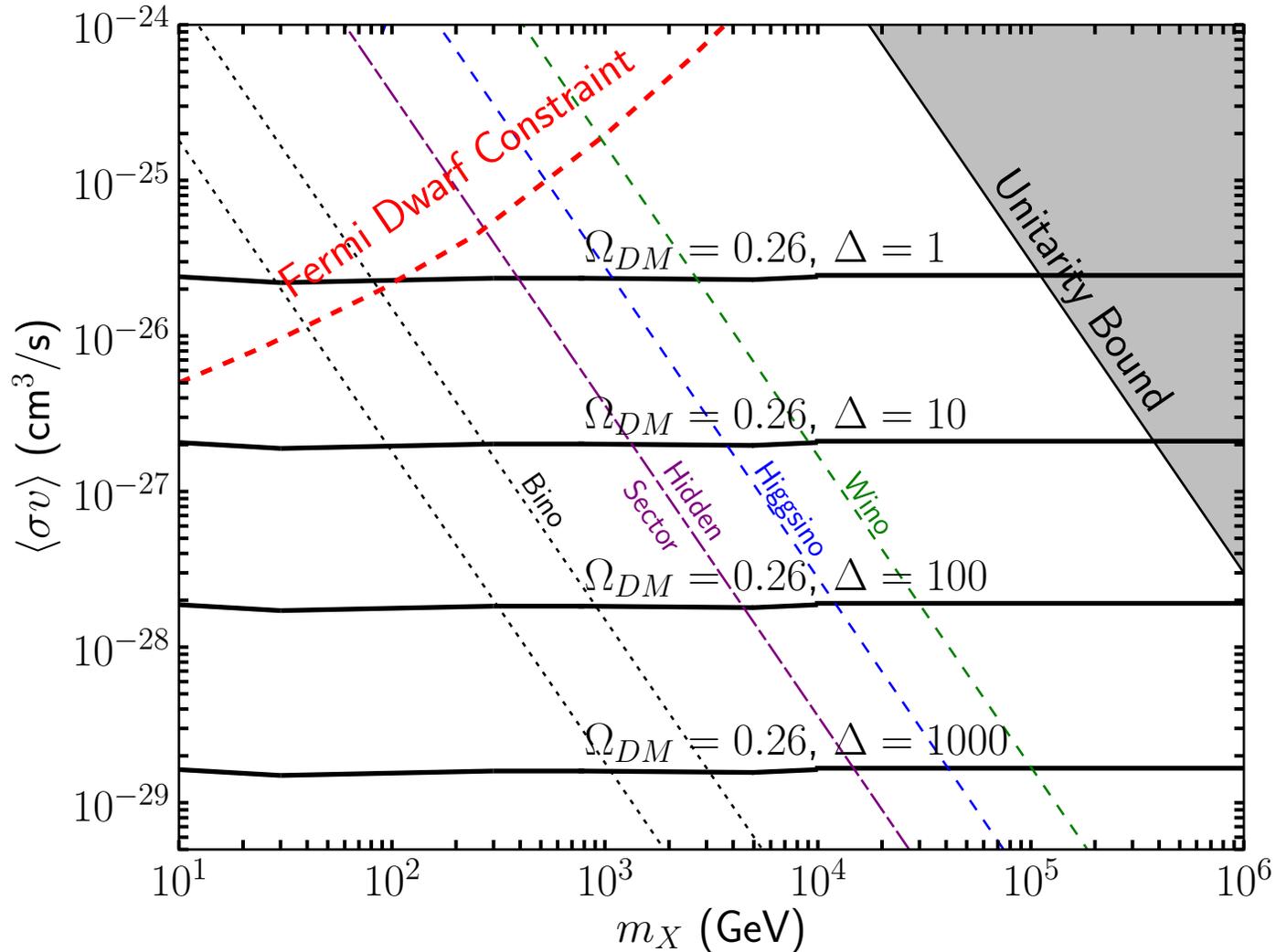
$$\rho_{\phi} = \rho_R(T_s)$$

$$g_{\text{RH}}/g_{\text{pt}} = 1, 10, 50; \quad g_s = g_{\text{RH}}$$



Thermal DM benchmark models:

- **Pure bino:** Annihilate largely via t -channel sfermion exchange. If significantly lighter than squarks, right-handed charged sleptons will be the most efficient mediator. LHC and LEP constrain slepton masses, reducing bino annihilation cross section and thus increasing its minimal relic abundance (we will consider $m_{\tilde{t}_R}/m_\chi = 1.2, 3$).
- **Pure higgsino:** The μ parameter sets the masses of four quasi-degenerate higgsinos which annihilate and coannihilate in t -channel, largely to gauge boson pairs, with modest Sommerfeld enhanced annihilation at freeze-out.
- **Pure wino:** The wino mass parameter M_2 sets the masses of neutral and charged winos, which annihilate and coannihilate (largely to gauge boson pairs) via t -channel, with significant Sommerfeld enhancements at freeze-out.
- **A simple hidden sector model:** Dirac fermion DM that annihilates into a pair of light SM singlet gauge bosons; $\langle\sigma v\rangle \sim 2 \times 10^{-26} \text{cm}^3/\text{s} \left(\frac{g_X}{0.35}\right)^4 \left(\frac{400 \text{ GeV}}{m_X}\right)^2$.
- Supersymmetric cross sections: Arkani-Hamed, Delgado, Giudice 2006
- Sommerfeld enhancement: Hisano, Matsumoto, Nagai, Saito, Senami, 2007
- Hidden sector model: *E.g.*, Pospelov, Ritz, Voloshin, 2008



- Unitarity: $\sigma v \lesssim 3 \times 10^{-22} \text{ cm}^3/\text{s} \times (2J + 1) (\text{TeV}/m_X)^2 \rightarrow m_X \lesssim 120 \text{ TeV} \times \sqrt{2J + 1}$

Griest, Kamionkowski, 1990

Recent work: e.g., Betre, El Hedri, Walker, 2014; Cahill-Rowley, El Hedri, Shepherd, Walker, 2015

★ Inflationary DM can cover a wide range of masses

- Very Heavy DM (disfavored by “naturalness” or unitarity)
- Distinct possibility if LHC does not uncover new physics
- Can become viable with moderate inflation

- Light DM at $\mathcal{O}(\text{GeV})$ scales
 - Conflict with CMB observations, unless p -wave suppressed
[Madhavacheril, Sehgal, Slatyer, 2014](#)
 - $\Delta > 1$ allows smaller $\langle \sigma v \rangle$ at freeze-out \Rightarrow suppressed CMB era signals
 - Difficult to detect via nuclear recoil, but may be probed at fixed target experiments
[Batell, Pospelov, Ritz, 2009; Izaguirre, Krnjaic, Schuster, Toro, 2013](#)

- Ultra light DM: QCD Axion with $f_{\text{PQ}} \gg 10^{12} \text{ GeV}$ ($M_{\text{GUT}}, M_{\text{Planck}}$)
 - Typically, a tuned misalignment angle assumed
 - For $T_s \lesssim \Lambda_{\text{QCD}}$: correct density (without tuning, depending on the model)
 - Potentially detectable via time varying CP odd nuclear moments
[Budker, Graham, Ledbetter, Rajendran, Sushkov, 2013 \(CASPER\)](#)

★ Mild inflation could arise within some typical models

- Hidden sector DM with a $U(1)$ dark force
- Low mass “dark photons” (also possible resolution of $g_\mu - 2$ anomaly)
- $U(1)$ breaking via a dark Higgs with $\langle \phi \rangle \lesssim \mathcal{O}(\text{GeV})$
- $V(\phi, T)$ may support a brief period of inflation

- Inflation could result from hidden non-trivial dynamics
- No need for light scalars
- “Dark QCD” of twin Higgs models [Chacko, Goh, Harnik, 2005](#)
- Hidden valleys models [Strassler, Zurek, 2006](#)

- Gravity waves generated by inflation from first order phase transition
[Grojean, Servant, 2006](#); [Schwaller, 2015](#)

Asymmetric DM: [See, for example, Kaplan, Luty, Zurek, 2009](#)

- Usually requires stronger than “weak” symmetric annihilation
- Depending on the setup, asymmetric DM can be inflatable
- Initial asymmetries, annihilation cross section, reheat

Example:

- Initial baryon and DM asymmetries larger than typical values
- T_{RH} below that of symmetric annihilation freeze-out (and asymmetry generation)
- “Weak” annihilation of symmetric population may then be sufficient
- Mild inflation could open up new avenues for asymmetric DM
- A number of variations possible, *e.g.*, “asymmetric reheating”
- Implications for baryogenesis in general

Conclusions

- Theoretical expectations of DM abundance premised on cosmological history
 - *Otherwise interesting models may be deemed disfavored with a standard history*
- Brief inflation from a “Hidden Sector” can dramatically change conclusions
- The “Inflatable DM” scenario may be realized through very simple models
 - *Can be largely decoupled from the visible sector*
- Some well-studied extensions of SM may in principle give rise to inflation
 - *Dark sector scalar condensation (massive dark photon models)*
 - *Non-trivial dynamics: Twin QCD, Hidden Valleys*
- Many typical inflatable DM scenarios require inflationary sectors below $\mathcal{O}(\text{GeV})$
 - *Additional targets for low energy intensity frontier searches*

