

[*JHEP* 07 (2022) 124]

Anomaly-free axion and heavy Higgs bosons in 3HDM

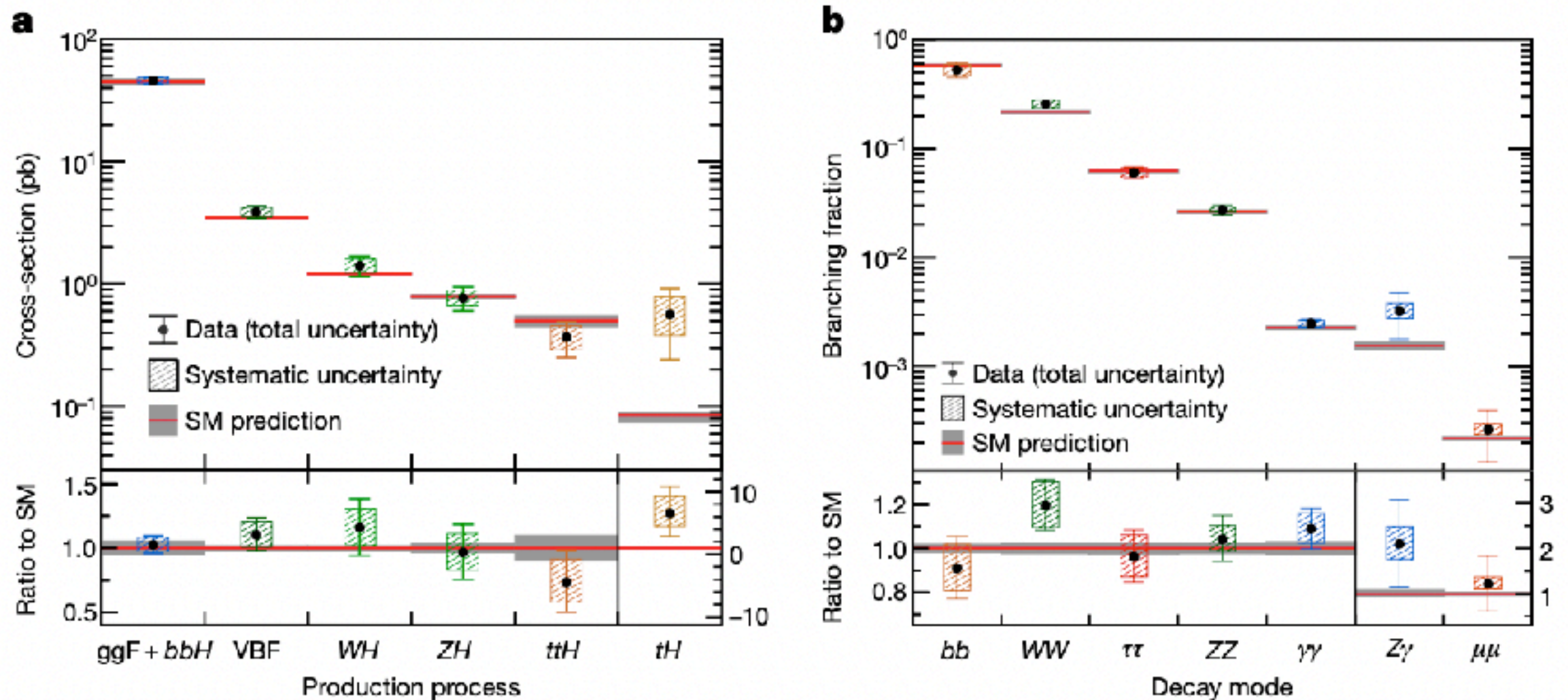
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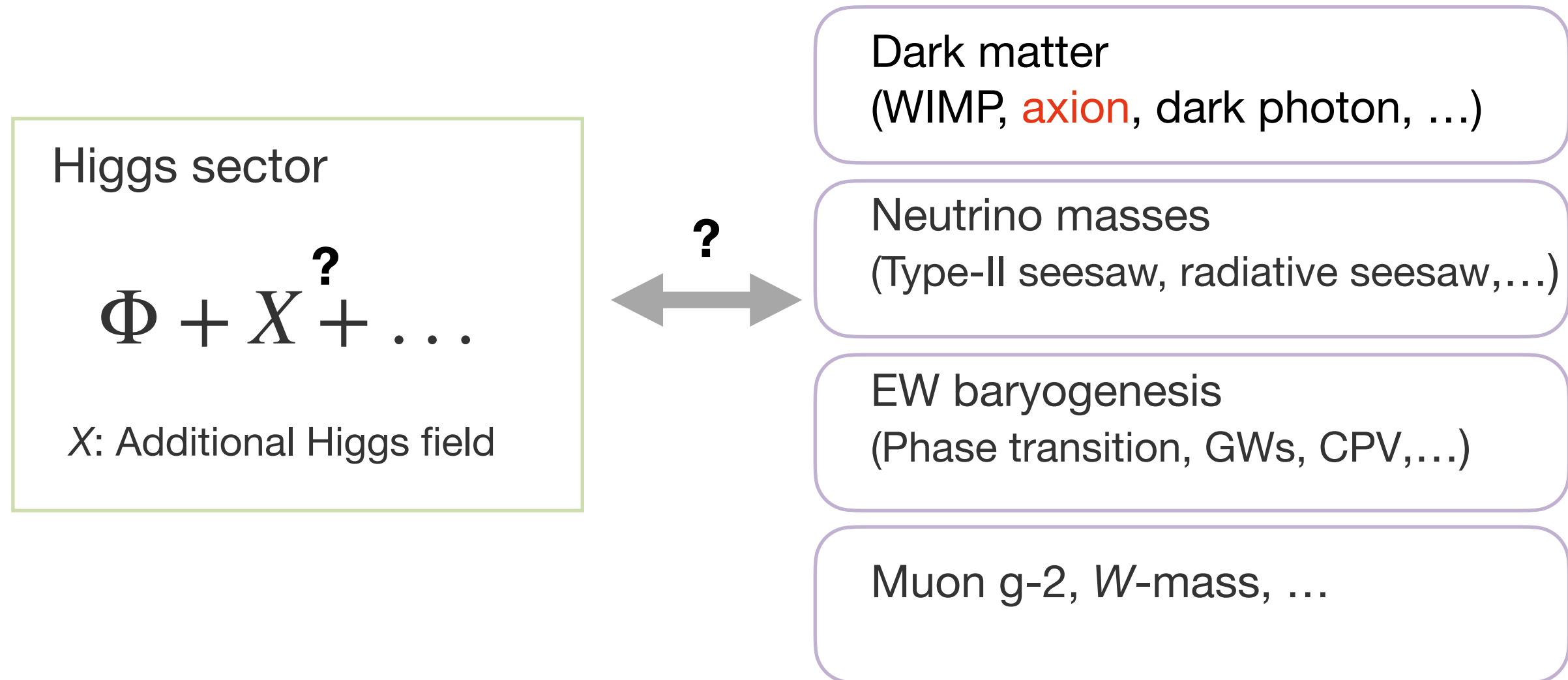
Current status of Higgs measurements

[ATLAS, Nature607, 52 (2022)]



- The data show success of the SM.
- However possibility of extended Higgs sector is not excluded at all.
 - E.g., Alignment limit, decoupling limit.

Probe of NP from Higgs sector

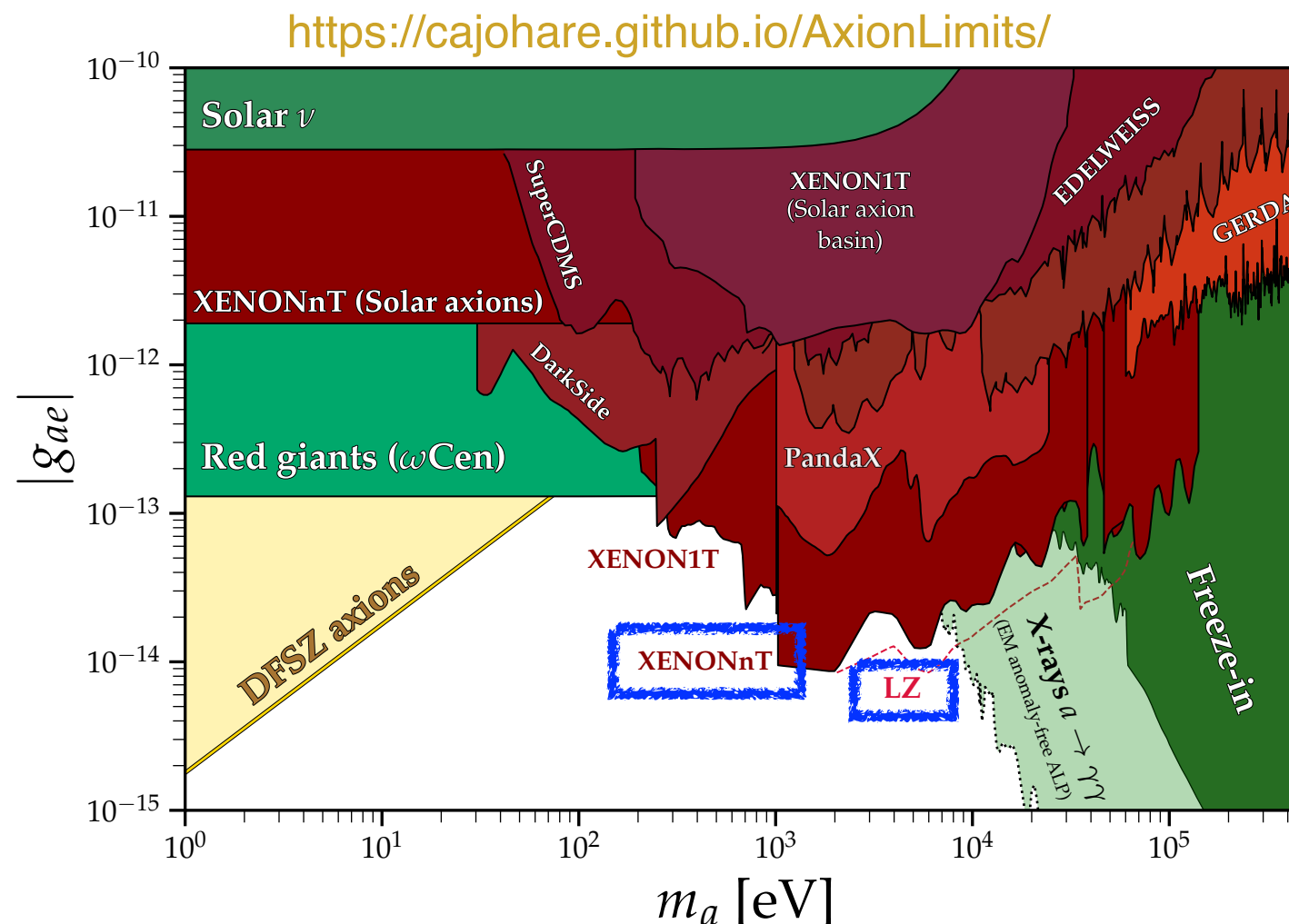


In this talk, we will discuss how axion DM can be embedded in the context of the extended Higgs model.

- Correlation between axion mass and heavy Higgs boson masses.
- Axion couplings have the corrections from the mixing btw axion and heavy Higgs.

Axion in keV scale

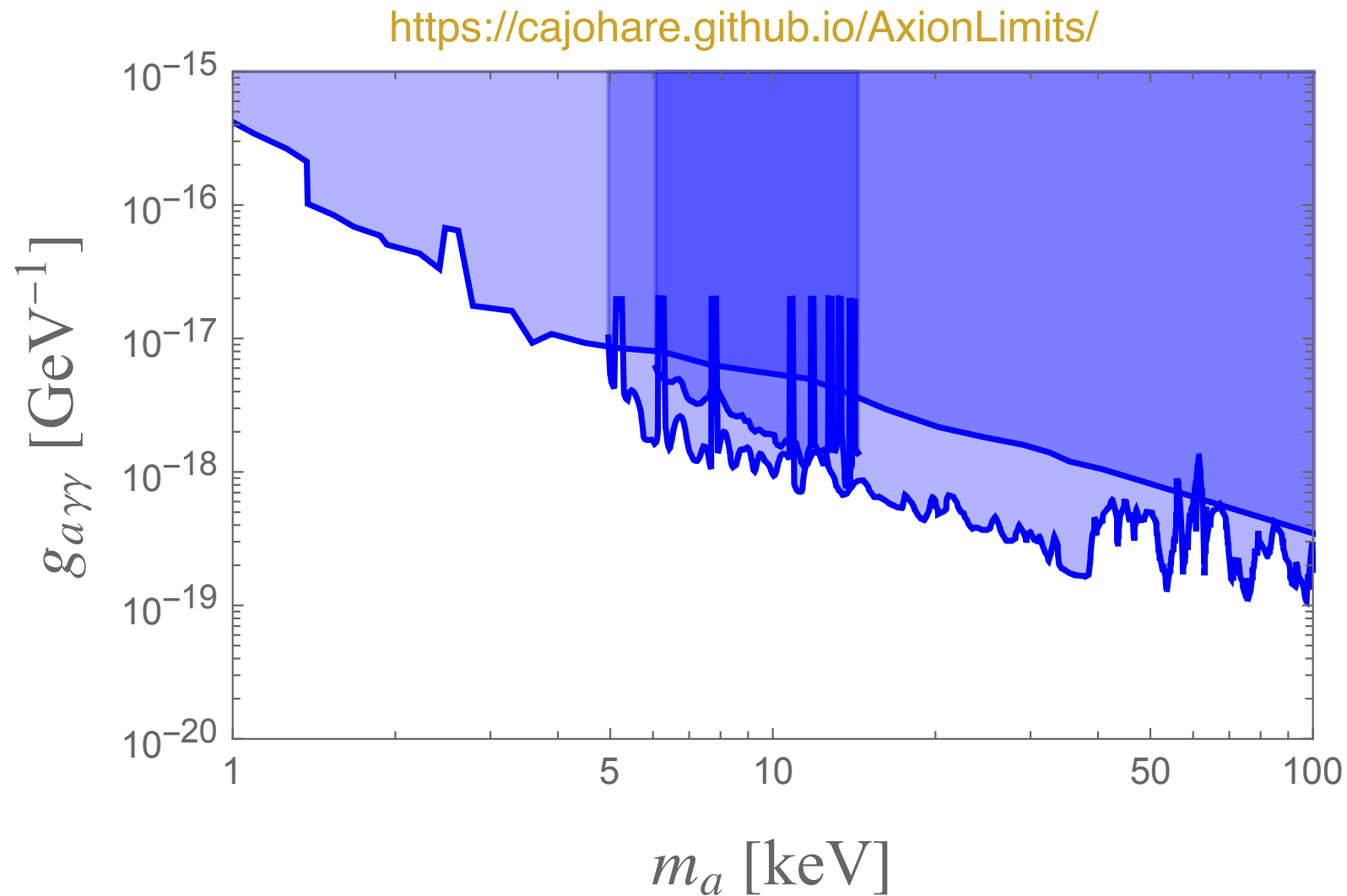
- Axion has a good nature as DM.
 - Thermal production and/or non thermal production
 - The stability is explained by the lightness: $\Gamma(a \rightarrow \gamma\gamma) \simeq \frac{m_a^3}{64\pi} g_{a\gamma\gamma}$
- KeV scale is accessible by direct searches of DM experiments.



XENONnT (current) :
 $g_{ae} \sim 10^{-14}$ at $m_a \sim 1\text{keV}$

LZ (future) :
 $g_{ae} \sim 10^{-14}$ at $m_a \sim \mathcal{O}(10)\text{keV}$

X-ray constraint



DFSZ type-axion

$$g_{a\gamma\gamma} = \frac{\alpha_{em}}{2\pi f_a} \frac{E}{N}$$

$$g_{aee} = q_e \frac{m_e}{f_a}$$

E : EM anomaly coefficient

N : QCD anomaly coefficient

q_e : PQ charge for electron

X-ray bounds
($m_a \sim 5\text{keV}$)



$$g_{a\gamma\gamma} \sim 10^{-18} \text{GeV}^{-1} \left(\frac{10^{15} \text{GeV}}{f_a} \right) \quad g_{aee} = 5 \times 10^{-19} \left(\frac{10^{15} \text{GeV}}{f_a} \right)$$

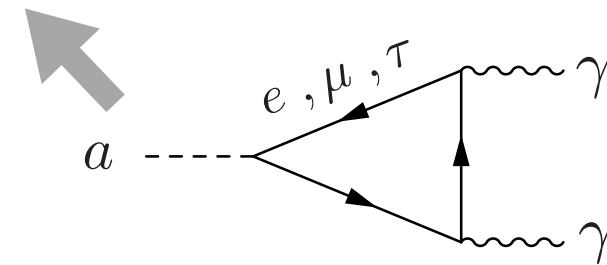
X-ray gives better
sensitivity than DD exp.

Anomaly-free axion

[K. Nakayama, F. Takahashi, T. Yanagida, Phys.Lett.B 734 (2014) 178]

[F. Takahashi, M. Yamada, W. Yin, Phys.Rev.Lett. 125 (2020) 161801]

$$\mathcal{L}_{\text{eff}} \simeq -(\underbrace{q_e + q_\mu + q_\tau}_{=0}) \frac{\alpha_{\text{ew}}}{4\pi f_a} a F_{\mu\nu} \tilde{F}^{\mu\nu} + \frac{\alpha_{\text{em}} m_a^2}{48\pi f_a} \left(\frac{q_e}{m_e^2} + \frac{q_\mu}{m_\mu^2} + \frac{q_\tau}{m_\tau^2} \right) a F_{\mu\nu} \tilde{F}^{\mu\nu}$$



Due to the suppression m_a^2/m_e^2 , the X-ray constraint is relaxed.

$$g_{a\gamma\gamma} \simeq \frac{\alpha}{48\pi} \frac{q_e}{f_a} \frac{m_a^2}{m_e^2} \simeq 1 \times 10^{-18} \left(\frac{q_e}{1} \right) \left(\frac{4.8 \times 10^9 \text{ GeV}}{f_a} \right) \left(\frac{m_a}{5 \text{ keV}} \right)^2$$

$$g_{ae}^{\text{X-ray}} \sim 1 \times 10^{-13} \left(\frac{q_e}{1} \right) \left(\frac{4.8 \times 10^9 \text{ GeV}}{f_a} \right) > g_{ae}^{\text{LZ}} \sim 10^{-15} \quad \text{at } m_a = 5 \text{ keV}$$

→ Both X-ray and DD experiments can explore anomaly-free axion.

Three Higgs doublet models with B-L Higgs bosons

	Higgs doublet			B-L Higgs			SM leptons						SM quarks	
	ϕ_1	ϕ_2	ϕ_3	S_0	S_1	S_2	L_e	L_μ	L_τ	e_R	μ_R	τ_R	Q_L	q_R
U(1) _F charge q	-3	3	0	0	1	-2	1	-1	0	-2	2	0	0	0

- Axion is indeed anomaly-free.

$$\underline{q_{L_e} + q_{L_\mu} + q_{L_\tau} = 0}, \quad \underline{q_{e_R} + q_{\mu_R} + q_{\tau_R} = 0} \quad \text{i.e., Anomalous photon coupling vanishes.}$$

- Three Φ s are needed to write down the Yukawa interactions for each lepton generation:

$$\mathcal{L}_Y = -y_e \bar{L}_e \phi_2 e_R - y_\ell \bar{L}_\ell \phi_3 \ell_R - y_{\ell'} \bar{L}_{\ell'} \phi_1 \ell'_R + \text{h.c.}$$

- Physical states: $H_{1,2,3}, H_{1,2}^\pm, A_{1,2}, a$

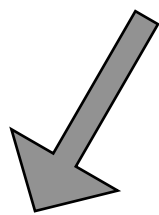
Masses for axion and heavy Higgs bosons

We assume $U(1)_F$ preserving Z_6 . $\rightarrow$ One soft breaking parameter appears only in Higgs sector.

$$V(\phi_i, S_j) \ni \left[\kappa_1 S_1^\dagger S_2 (\phi_1^\dagger \phi_2) + \kappa_2 S_2^\dagger S_1 (\phi_2^\dagger \phi_3) + \text{h.c.} \right] \\ - \left[m_{12}^2 \phi_1^\dagger \phi_2 + \text{h.c.} \right]$$

Portal interaction

Soft $U(1)_F$ breaking terms



Mass of heavy Higgs: ($\Phi = H_{2,3} = H_{1,2}^\pm = A_{1,2}$)

$$m_\Phi^2 \sim \frac{m_{12}^2 v^2}{v_1 v_2} + \lambda_i v^2$$

Mass of axion:

$$m_a^2 \sim \frac{m_{12}^2 (\kappa_1 + \kappa_2) v_{S_1} v_{S_2}}{2m_{12}^2 + (\kappa_1 + \kappa_2) v_{S_1} v_{S_2}} \frac{v^2}{f_a^2}$$

$\rightarrow$ The mass of heavy Higgs bosons and axion are related.

Axion-photon coupling

$$g_{a\gamma} \simeq g_{a\gamma}^{ch} + g_{a\gamma}^{th} + g_{a\gamma}^{mix}$$

[U(1) charge contributions] : $g_{a\gamma}^{ch} \simeq \frac{\alpha_{em}}{\pi f_a} \sum_{\ell} q_{\ell} = 0$

[Threshold corrections] : $g_{a\gamma}^{th} \simeq \frac{\alpha_{em}}{\pi v} \frac{m_a^2}{12} \frac{q_e}{m_e^2}$

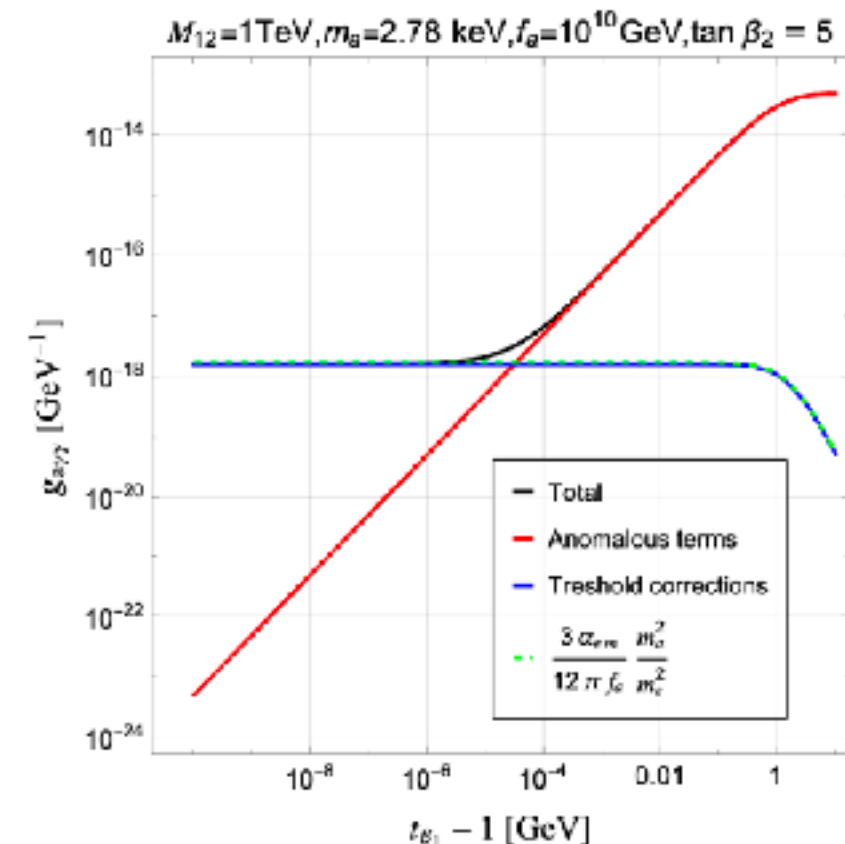
[Mixing contributions] : It arises due to the mixing among a and $G_0, A_{1,2}$.

(a-G mixing) $\sim \frac{\alpha_{em}}{\pi v} \sum_f N_c^f Q_f^2 X_f = 0$ (Due to shift symmetry)

$$X_f = -6I_f(c_{\beta_1}^2 - s_{\beta_1}^2)c_{\beta_2}^2$$

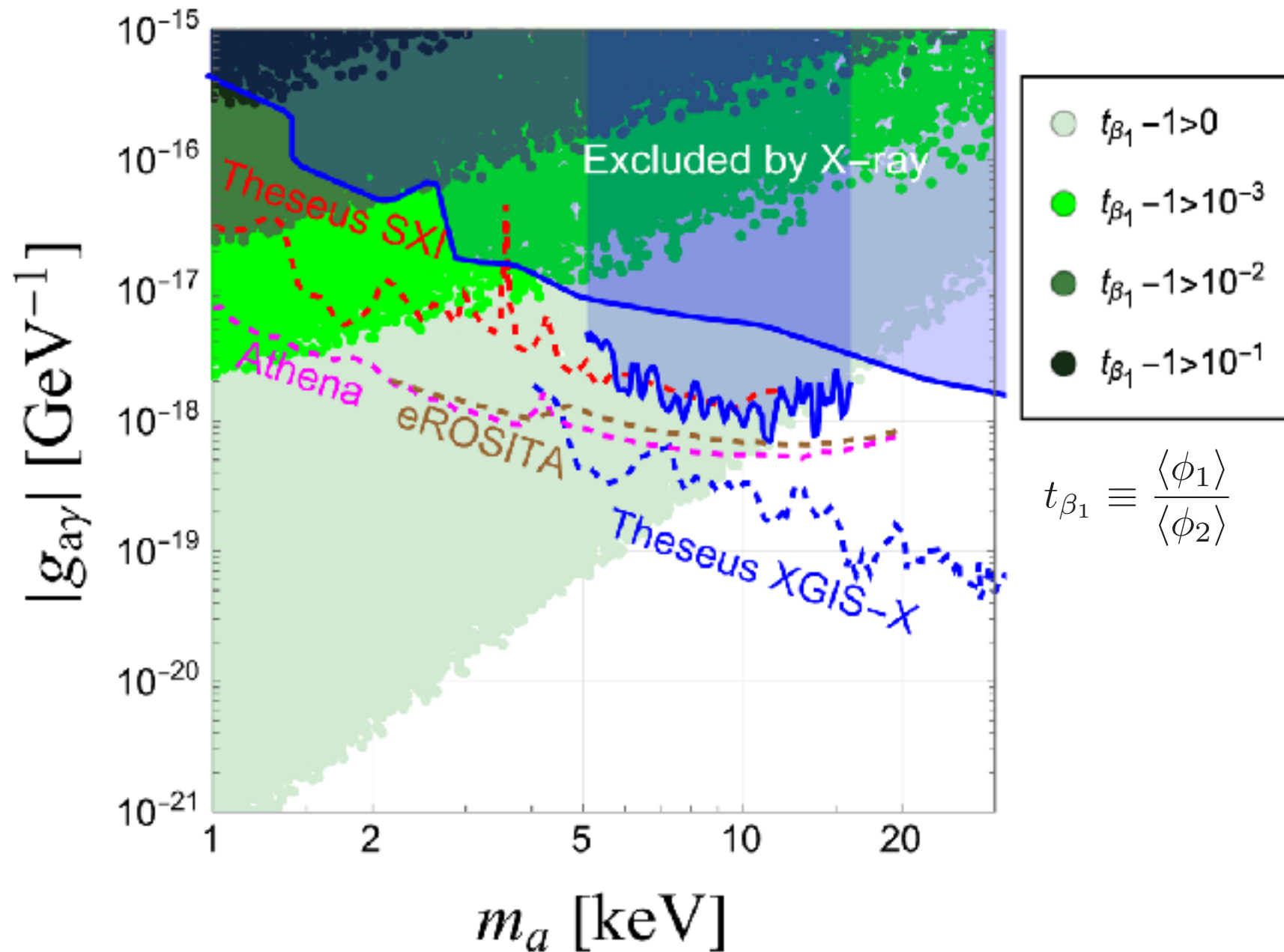
(a-A mixing) $\sim (c_{\beta_1}^2 - s_{\beta_1}^2) \frac{\alpha_{EW}}{\pi v} \frac{m_{12}^2}{v f_a}$

- The difference is 4 digit at $t_{\beta_1} \sim 2$.
- $g_{a\gamma}$ is suppressed by $t_{\beta_1} - 1$.



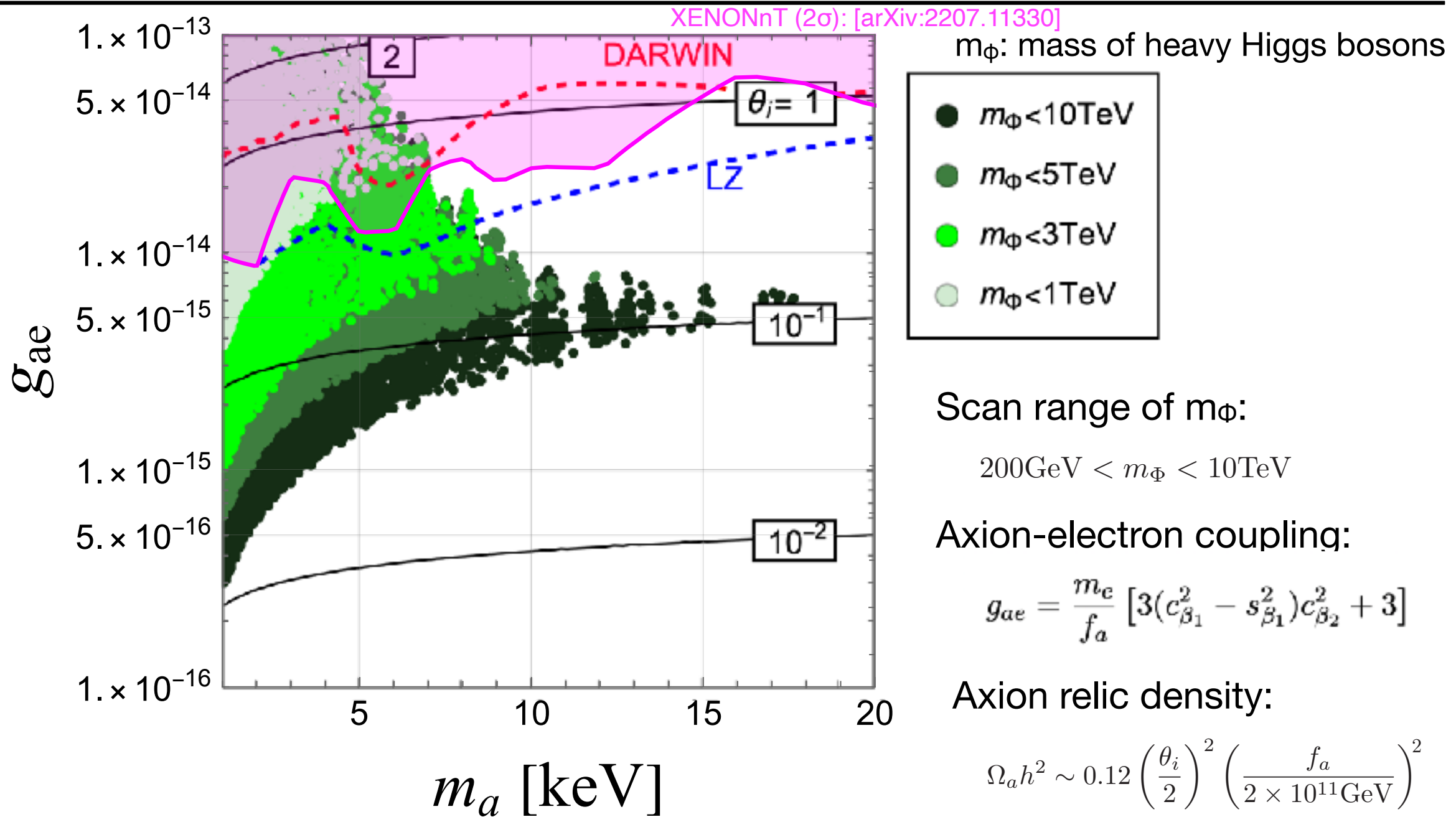
Comparison with X-ray bounds

[KS, F. Takahashi]



- $g_{a\gamma}$ is constrained as usual axion if $t_{\beta_1} - 1 \sim \mathcal{O}(1)$.
- Only in the limit of $t_{\beta_1} \rightarrow 1$, threshold corrections dominates.
- $t_{\beta_1} < 1.1$ is needed to evade current X-ray bounds.

Correlation between Higgs and axion



- We imposed the current X-ray bounds as well as various theoretical and exp. constraints.
 - The heavy Higgs masses are correlated with the m_a and g_{ae} .
- If axion is detected by future experiments, the information of extra Higgs can be extracted.

Summary

- Anomaly-free axion can be probed by the future direct searches and future X-ray searches.
- We consider 3HDM as a possible UV completion to predict the anomaly-free axion.
- We find that $g_{a\gamma}$ receive sizable corrections due to the mixing.
 - $g_{a\gamma} \sim (\text{Threshold corrections})$ [No extra CP-odd Higgs]
 - $g_{a\gamma} \sim (\text{Mixing corrections})$ [Additional CP-odd Higgs exists]
- Properties of the additional Higgs are related to those of axion.

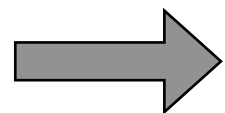
Buck up

Can two Higgs doublet models realize anomaly-free axion?

→ It wouldn't work.

- Two of three generations should have same $U(1)_F$ charge.

$$Q(e_i) = (-a, -b, -b) \quad Q(\ell_i) = (c, d, d)$$



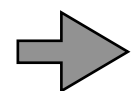
$$a + 2b = 0,$$

(Anomalous photon
coupling is zero)

$$c + 2d = 0$$

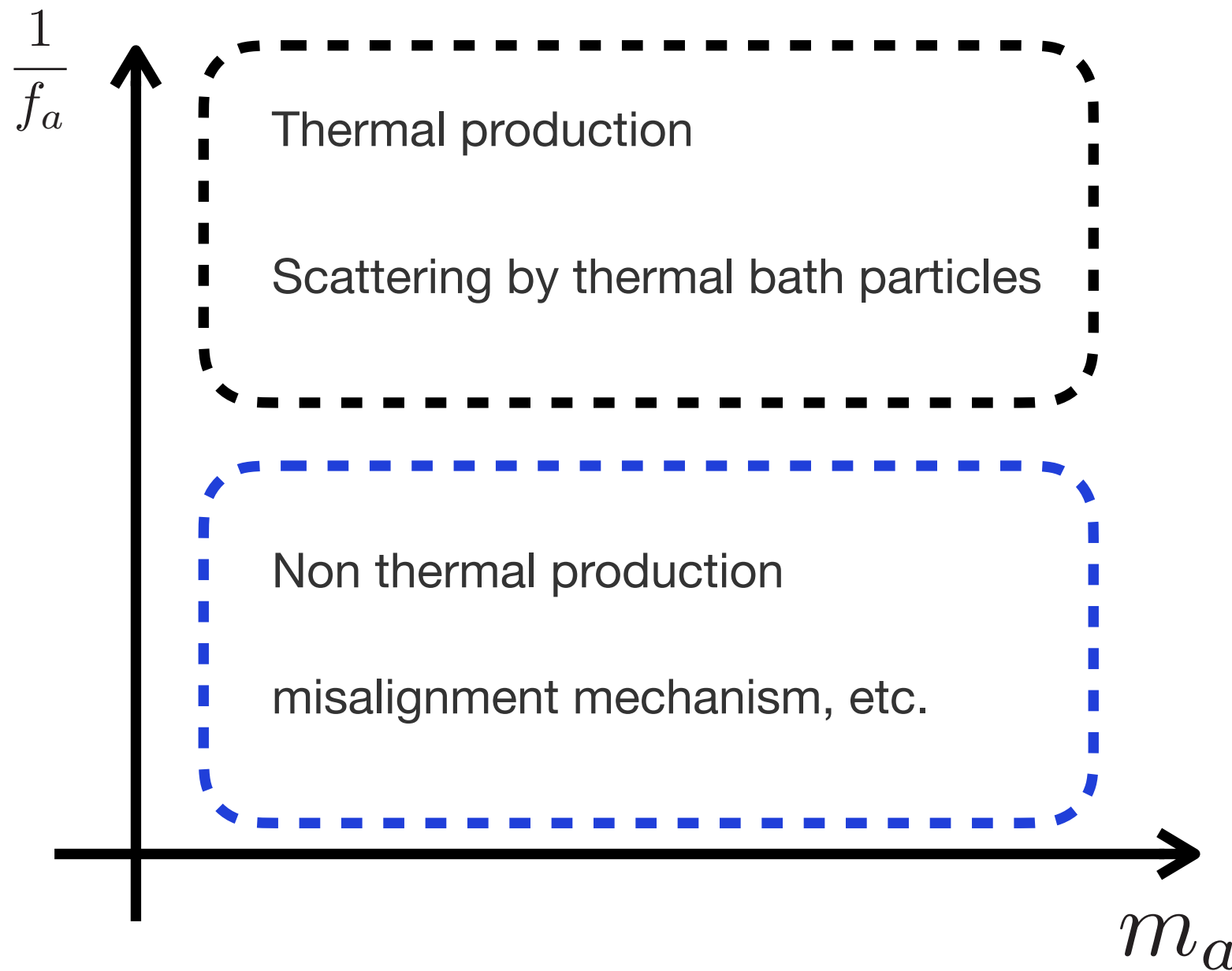
- Axion necessarily couples with quarks. $H(-a - c) \quad H(\frac{a + c}{2})$

$$\begin{aligned} \mathcal{L} \ni & y_e \bar{e}_R \ell_1 H(-a - c) + y_\mu \bar{\mu}_R \ell_2 H(\frac{a + c}{2}) + y_\tau \bar{\tau}_R \ell_3 H(\frac{a + c}{2}) \\ & + y_U u_R Q H(\frac{a + c}{2}) + y_D d_R Q H(\frac{a + c}{2}) \end{aligned}$$

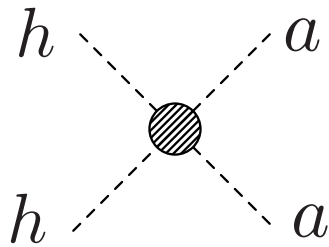


$g_{a\gamma}$ receives QCD corrections and a - π mixing, which gives $O(1)$ contributions.

Axion production



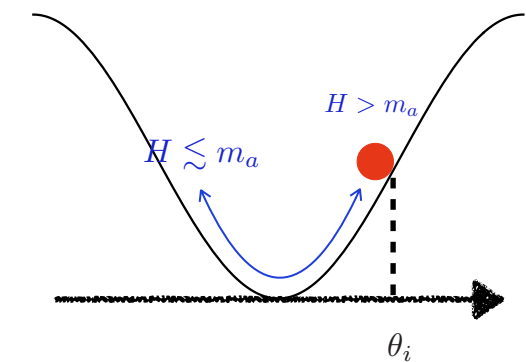
- Thermal production

Ex.)  [e.g., M. Bauer, G. Rostagni, J. Spinner, PRD 107 (2023)]

$$- \mathcal{M}_a \sim \frac{1}{f_a^n} \quad (n=4 \text{ for } hh \rightarrow aa)$$

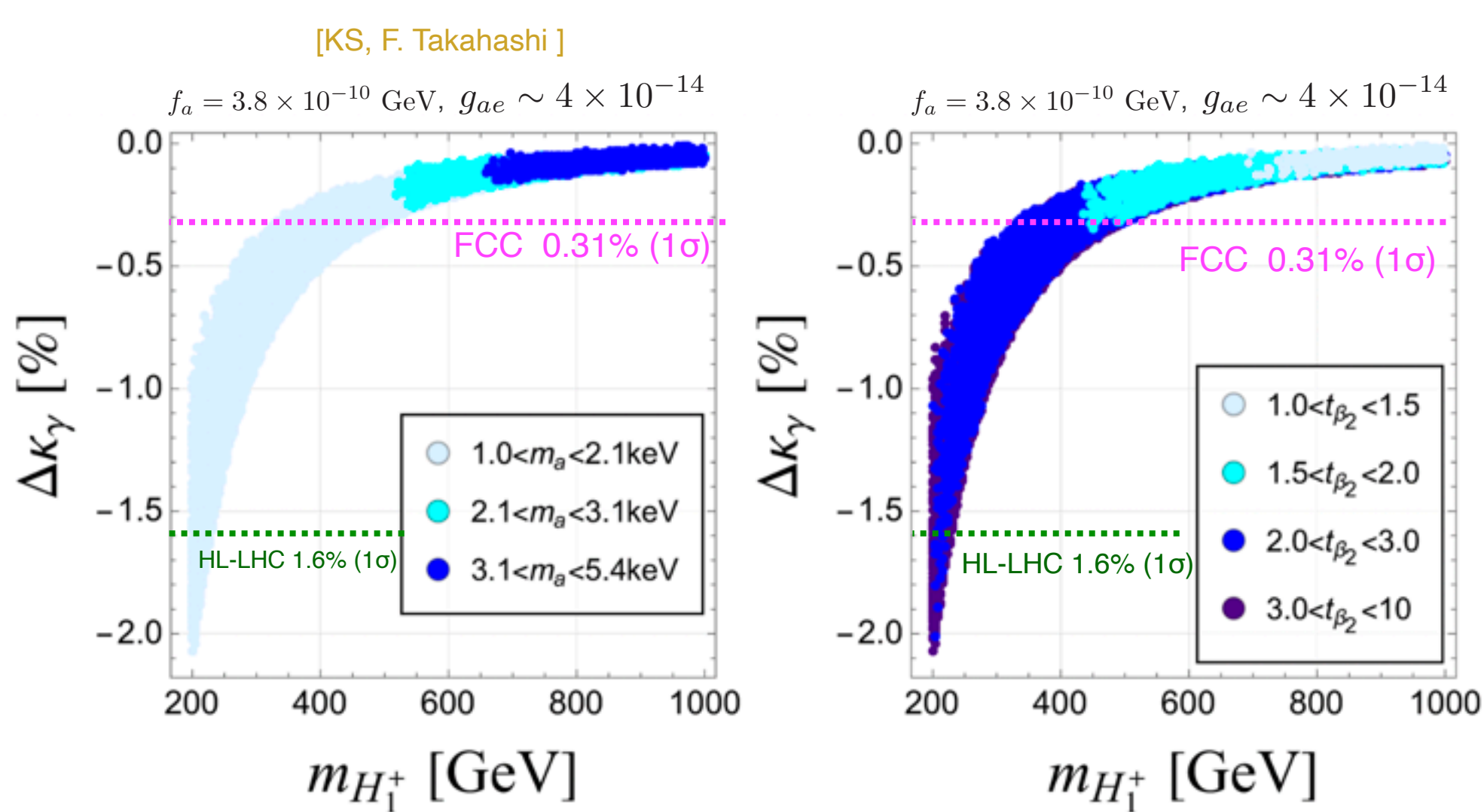
- Many parameter space is excluded by X-ray.

- Misalignment mechanism



$$\Omega_a h^2 \sim 0.12 \left(\frac{\theta_i}{2} \right)^2 \left(\frac{f_a}{2 \times 10^{11} \text{ GeV}} \right)^2$$

Correlation between axion mass and Higgs coupling



$$\Delta\kappa_\gamma \equiv \sqrt{\frac{\Gamma_{h \rightarrow \gamma\gamma}^{\text{3HDM}}}{\Gamma_{h \rightarrow \gamma\gamma}^{\text{SM}}}} - 1$$

$$t_{\beta_2} \equiv \frac{\langle \phi_1 \rangle}{\langle \phi_3 \rangle}$$

- The maximal size of deviation is around 2%.



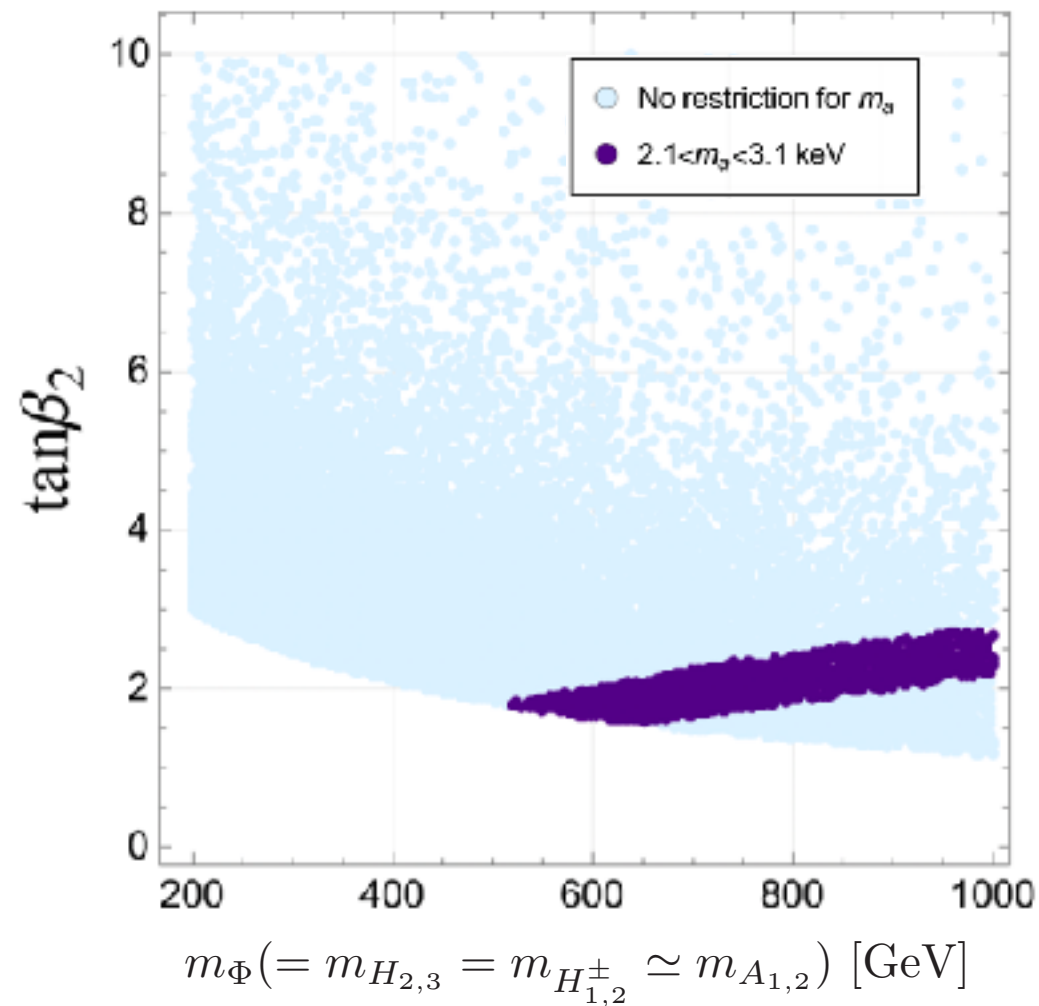
Perturbativity for the running coupling constants

- The keV scale axion can be tested by future colliders.

Correlations for the potential parameters

$$\tan \beta_1 \equiv \frac{v_2}{v_1}, \quad \tan \beta_2 \equiv \frac{v_3}{\sqrt{v_1^2 + v_2^2}}$$

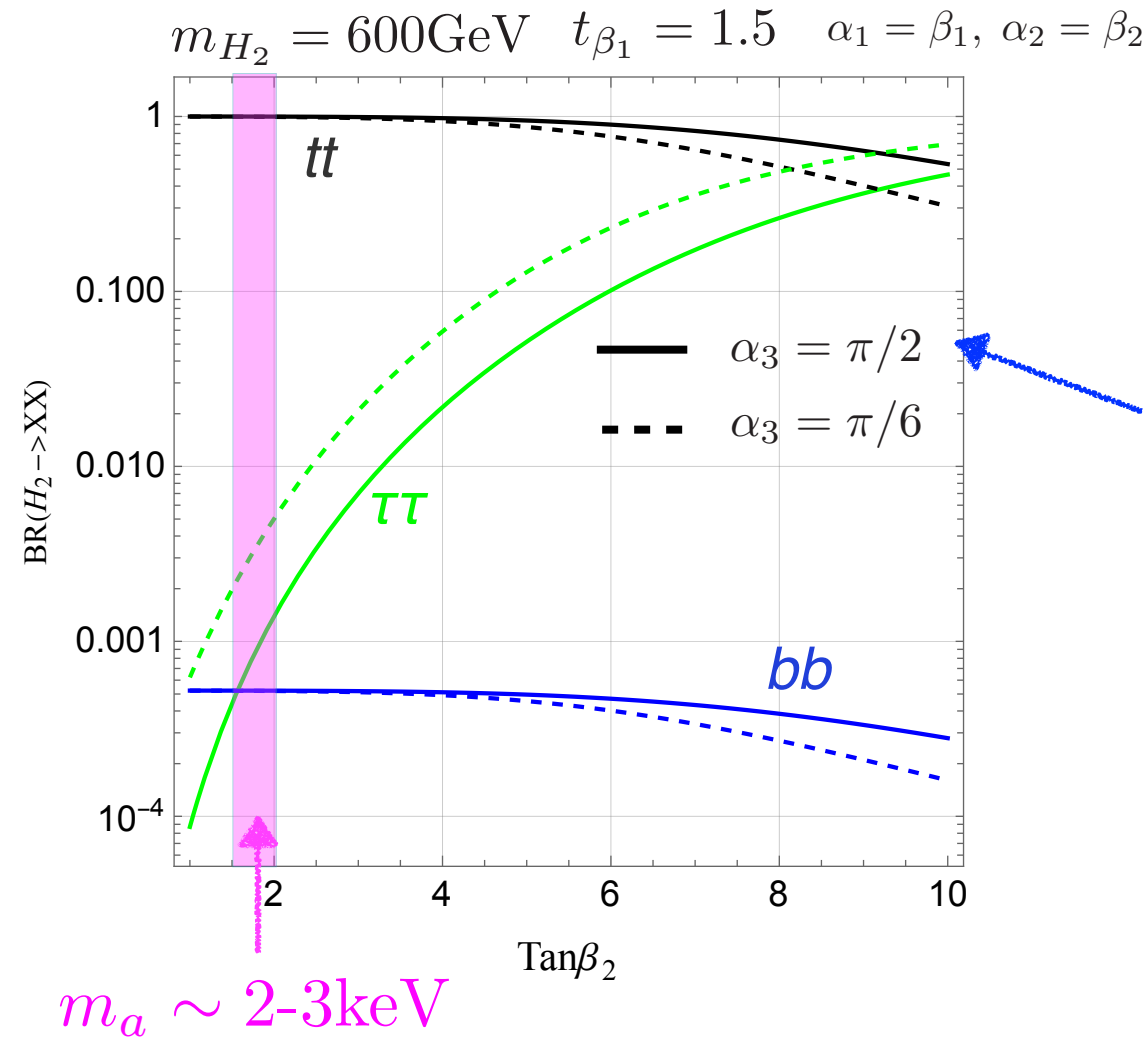
[KS, F. Takahashi]



→ m_Φ should be heavier than around 500 GeV if the mass of axion is fixed.

→ There is a correlation between m_Φ and $\tan \beta_{1,2}$ ➡ Characteristic decay pattern of Φ .

Predictions for decays of the heavy Higgs bosons



$$\xi_{H_2}^{t,b} = -\frac{1}{t_{\beta_2}} s_{\alpha_3}$$

$$\xi_{H_2}^{\tau} = -\frac{t_{\beta_1}}{c_{\beta_2}} c_{\alpha_3} + t_{\beta_2} s_{\alpha_3}$$

2HDM Type X

$$\begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix} = R_S \begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix}$$

$\equiv \mathcal{O}_{\alpha_3} \mathcal{O}_{\alpha_2} \mathcal{O}_{\alpha_1}$

- BR($H_2 \rightarrow \tau\tau$) is relatively larger than the case of Type X 2HDM.
- If the axion is detected at a few keV, one can obtain predictions of a similar decay pattern of H_2 except for $H_2 \rightarrow \tau\tau$.

Higgs potential

$$V = V_{\text{3HDM}} + V_{\text{B-L}} + V_I .$$

$$\begin{aligned} V_{\text{3HDM}} = & m_{11}^2(\phi_1^\dagger\phi_1) + m_{22}^2(\phi_2^\dagger\phi_2) + m_{33}^2(\phi_3^\dagger\phi_3) \\ & + \lambda_1(\phi_1^\dagger\phi_1)^2 + \lambda_2(\phi_2^\dagger\phi_2)^2 + \lambda_3(\phi_3^\dagger\phi_3)^2 \\ & + \lambda_4(\phi_1^\dagger\phi_1)(\phi_2^\dagger\phi_2) + \lambda_5(\phi_1^\dagger\phi_1)(\phi_3^\dagger\phi_3) + \lambda_6(\phi_2^\dagger\phi_2)(\phi_3^\dagger\phi_3) \\ & + \lambda_7(\phi_1^\dagger\phi_2)(\phi_2^\dagger\phi_1) + \lambda_8(\phi_1^\dagger\phi_3)(\phi_3^\dagger\phi_1) + \lambda_9(\phi_2^\dagger\phi_3)(\phi_3^\dagger\phi_2) \\ & + \left[\lambda_{10}(\phi_3^\dagger\phi_1)(\phi_3^\dagger\phi_2) + \text{h.c.} \right] + V_{\text{soft}} , \end{aligned}$$

$$V_{\text{soft}} = - \left[m_{12}^2(\phi_1^\dagger\phi_2) + \text{h.c.} \right]$$

$$\begin{aligned} V_I = & \sum_{m=0,1,\bar{2}} \sum_{n=1,2,3} \kappa_{m\phi n} |S_m|^2 (\phi_n^\dagger\phi_n) \\ & + \left[\kappa_{1\bar{2}\phi_1\phi_3} S_1^\dagger S_{\bar{2}} (\phi_1^\dagger\phi_3) + \kappa_{\bar{2}1\phi_2\phi_3} S_{\bar{2}}^\dagger S_1 (\phi_2^\dagger\phi_3) + \text{h.c.} \right] \end{aligned}$$

$$\begin{aligned} V_{\text{B-L}} = & \sum_{i=0,1,\bar{2}} (\mu_i |S_i|^2 + \kappa_i |S_i|^4) + \kappa_{01} |S_0|^2 |S_1|^2 + \kappa_{0\bar{2}} |S_0|^2 |S_{\bar{2}}|^2 + \kappa_{1\bar{2}} |S_1|^2 |S_{\bar{2}}|^2 \\ & + \kappa_{0110} |S_0^\dagger S_1|^2 + \kappa_{0\bar{2}\bar{2}0} |S_0^\dagger S_{\bar{2}}|^2 + \kappa_{1\bar{2}\bar{2}1} |S_1^\dagger S_{\bar{2}}|^2 , \end{aligned}$$

Yukawa interaction for the heavy Higgs

$$\begin{aligned}
 \mathcal{L}_Y^M \ni & \frac{\sqrt{2}}{v} V_{\text{CKM}} \sum_{i=1}^2 \xi_{H_i^\pm}^q H_i^\pm \left\{ \bar{u}(m_u P_L - m_d P_R) d + \text{h.c.} \right\} \\
 & - \frac{m_q}{v} \sum_{i=1}^3 \xi_{H_i}^q H_i \bar{q} q + i 2 I_q \frac{m_q}{v} \sum_{i=1}^2 \xi_{A_i}^q A_i \bar{q} \gamma_5 q \\
 & - \sqrt{2} \frac{m_l}{v} \sum_{i=1}^2 \xi_{H_i^\pm}^l H_i^\pm \left\{ \bar{\nu}_L P_R l + \text{h.c.} \right\} - \frac{m_l}{v} \sum_{i=1}^3 \xi_{H_i}^l H_i \bar{l} l \\
 & - i \sum_l \frac{m_l}{v} \sum_{i=1}^2 \xi_{A_i}^l A_i \bar{l} \gamma_5 l - i \sum_l g_{a\ell} a \bar{l} \gamma_5 l ,
 \end{aligned}$$

$\xi_{H_i^\pm}^f$	q	e	ℓ	ℓ'
$H_1^\pm$	$-\frac{1}{t_{\beta_2}} s_{\gamma+}$	$\frac{1}{t_{\beta_1}} \frac{c_{\gamma+}}{c_{\beta_2}} + t_{\beta_2} s_{\gamma+}$	$-\frac{1}{t_{\beta_2}} s_{\gamma+}$	$-t_{\beta_1} \frac{c_{\gamma+}}{c_{\beta_2}} + t_{\beta_2} s_{\gamma+}$
$H_2^\pm$	$\frac{1}{t_{\beta_2}} c_{\gamma+}$	$-t_{\beta_1} c_{\gamma+} + \frac{1}{t_{\beta_2}} \frac{s_{\gamma+}}{c_{\beta_2}}$	$\frac{1}{t_{\beta_2}} c_{\gamma+}$	$-t_{\beta_2} c_{\gamma+} - t_{\beta_1} \frac{s_{\gamma+}}{c_{\beta_2}}$

$\xi_{A_i, a}^f$	q	e	ℓ	ℓ'
A_1	$\frac{1}{s_{\beta_2}} (R_P)_{23}$	$\frac{1}{s_{\beta_1} c_{\beta_2}} (R_P)_{22}$	$\frac{1}{s_{\beta_2}} (R_P)_{23}$	$\frac{1}{c_{\beta_1} c_{\beta_2}} (R_P)_{21}$
A_2	$\frac{1}{s_{\beta_2}} (R_P)_{33}$	$\frac{1}{s_{\beta_1} c_{\beta_2}} (R_P)_{32}$	$\frac{1}{s_{\beta_2}} (R_P)_{33}$	$\frac{1}{c_{\beta_1} c_{\beta_2}} (R_P)_{31}$
a	$\frac{1}{s_{\beta_2}} (R_P)_{43}$	$\frac{1}{s_{\beta_1} c_{\beta_2}} (R_P)_{42}$	$\frac{1}{s_{\beta_2}} (R_P)_{43}$	$\frac{1}{c_{\beta_1} c_{\beta_2}} (R_P)_{41}$

$\xi_{H_i}^f$	q	e	ℓ	ℓ'
H_1	$\frac{s_{\alpha_2}}{s_{\beta_2}}$	$\frac{s_{\alpha_1} c_{\alpha_2}}{s_{\beta_1} c_{\beta_2}}$	$\frac{s_{\alpha_2}}{s_{\beta_2}}$	$\frac{c_{\alpha_1} c_{\alpha_2}}{c_{\beta_1} c_{\beta_2}}$
H_2	$\frac{c_{\alpha_2} s_{\alpha_3}}{s_{\beta_2}}$	$\frac{1}{s_{\beta_1} c_{\beta_2}} (c_{\alpha_1} c_{\alpha_3} - s_{\alpha_1} s_{\alpha_2} s_{\alpha_3})$	$\frac{c_{\alpha_2} s_{\alpha_3}}{s_{\beta_2}}$	$\frac{1}{c_{\beta_1} c_{\beta_2}} (-s_{\alpha_1} c_{\alpha_3} - c_{\alpha_1} s_{\alpha_2} s_{\alpha_3})$
H_3	$\frac{c_{\alpha_2} c_{\alpha_3}}{s_{\beta_2}}$	$\frac{1}{s_{\beta_1} c_{\beta_2}} (-s_{\alpha_1} s_{\alpha_2} c_{\alpha_3} - c_{\alpha_1} s_{\alpha_3})$	$\frac{c_{\alpha_2} c_{\alpha_3}}{s_{\beta_2}}$	$\frac{1}{c_{\beta_1} c_{\beta_2}} (-c_{\alpha_1} s_{\alpha_2} c_{\alpha_3} + s_{\alpha_1} s_{\alpha_3})$

$$v_1 = v \cos \beta_1 \cos \beta_2 , \quad v_2 = v \sin \beta_1 \cos \beta_2 ,$$

$$v_3 = v \sin \beta_2$$

Alignment limit

- The alignment limit in 3HDM is defined by [D. Das, I. Saha, PRD100 (2019)]

$$\alpha_1 = \beta_1, \quad \alpha_2 = \beta_2$$

- Higgs coupling: $\kappa_V^{H_1} = c_{\alpha_2} c_{\alpha_1 - \beta_1} c_{\beta_2} + s_{\alpha_2} s_{\beta_2} \rightarrow 1$

- Mixing matrix:

$$\begin{pmatrix} H_1 \\ H_2 \\ H_3 \end{pmatrix} = R_S \begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix}$$

$\underbrace{\quad}_{\mathcal{O}_{\alpha_3} \mathcal{O}_{\alpha_2} \mathcal{O}_{\alpha_1}} \rightarrow \mathcal{O}_{\alpha_3} \mathcal{O}_{\beta}$

c.f.) 2HDM

 $\sin(\beta - \alpha) = 1 \rightarrow \alpha = \beta + \frac{\pi}{2}$
 $\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} -\sin \beta & -\cos \beta \\ \cos \beta & -\sin \beta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$

Neutrino masses

If we introduce right-handed neutrinos N_i , we can explain the neutrino mass by the seesaw mechanism.

- $U(1)_F$ charge: $Q(N_i) = (1, -1, 0)$ $\leftarrow$ Same assignment as e_{Ri}
(Type A)
- Lagrangian for neutrinos:

$$-\mathcal{L} = y_1 \bar{L}_e N_1 \tilde{\phi}_3 + y_2 \bar{L}_\tau N_2 \tilde{\phi}_3 + y_3 \bar{L}_\mu N_3 \tilde{\phi}_3 + \frac{1}{2} (M_N)_{ij} \bar{N}_i^c N_j + \text{h.c.}$$

$$\uparrow (y^N)_{ij} \bar{N}_i^c N_j S_{0,1,\bar{2}}$$

$$(M_N)_{ij} \sim \begin{pmatrix} \langle S_{\bar{2}} \rangle & \langle S_0 \rangle & 0 \\ \langle S_0 \rangle & 0 & \langle S_1 \rangle \\ 0 & \langle S_1 \rangle & \langle S_0 \rangle \end{pmatrix} \quad \text{If } y^N \sim \mathcal{O}(1)$$

- Neutrino mass and mixing ($m_D = \text{diag}(y_1, y_2, y_3) \frac{v_3}{\sqrt{2}}$)

$$m_\nu \simeq m_D^T M_N^{-1} m_D \propto \frac{y_i^2 v^2}{v_S} \sim 0.1 \text{eV} \left(\frac{y_i}{0.01} \right)^2 \left(\frac{10^{10} \text{GeV}}{v_S} \right)$$

$$U_{PMNS}^\dagger m_\nu U_{PMNS} = \text{diag}(m_1, m_2, m_3)$$

Large neutrino mixings are checked by scanning $\{y_i, (M_N)_{ij}\}$.

