Scalars 2023

An opportunity to discuss various aspects of scalar particles.





The Four Pillars of the Standard Model



The Standard Model is Structurally Complete



The Standard Model is Structurally Complete - But







Strong Fírst Order Electroweak Phase Transítion (SFOEWPT) The Code BSMPT



• Electroweak Baryogenesis (EWBG): generation of the observed baryon-antibaryon asymmetry in the electroweak phase transition (EWPT) [Riemer-Sorensen, Jenssen '17]

$$5.8 \cdot 10^{-10} < \frac{n_B - n_{\bar{B}}}{n_{\gamma}} < 6.6 \cdot 10^{-10}$$

• Sakharov Conditions:

- * (i) B number violaton (sphaleron processes)
- * (ii) C and CP violation
- * (*iii*) Departure from thermal equilibrium
- Additional constraint: EW phase transition must be strong first order PT [Quiros '94; Moore '99]

$$\xi_c \equiv \frac{\left< \Phi_c \right>}{T_c} \ge 1$$

 $\langle \Phi_c \rangle$ and T_c field configuration and temperature at phase transition

[Sakharov '67]

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Strong First Order Electroweak Phase Transition (SFOEWPT)

[From Ph. Basler, PhD Thesis]



Strong First Order Electroweak Phase Transition (SFOEWPT)

[From Ph. Basler, PhD Thesis]



Strong First Order Electroweak Phase Transition (SFOEWPT)



The Code BSMPT

[v1:Basler,MM,'18]



- Computation of the loop-corrected effective potential V_{eff} at finite temperature, including thermal masses
- For extended Higgs sectors
- Determination of VEV $\langle \phi \rangle$ (T) $\rightarrow \xi_c = v_c/T_c$
- In on-shell (OS) renormalization scheme: masses and mixing angles from V^{loop}_{eff} are equal to leading-order values → efficient scan of parameter space of the models
- Computation of loop-corrected trilinear Higgs self-couplings in OS scheme
- Easy implementation of new models
- Programming language: C++

The Effective Potential



BSMPT: Global minimization of loop-corrected effective potential at T ϵ {0,300} GeV in all possible field directions ω at T \neq 0 GeV.

SFOEWPT: $\xi = v_c/T_c > 1$

Upgrade to BSMPTv2

- Calculation of the BAU for the CP-violating 2HDM (C2HDM), using
 * the semiclassical force approximation (FH)
 - * the VEV-insertion approximation (VIA)
 - (wall profile is approximated by the Kink profile)
- Implementation of a new model: CxSM further code improvements



[Basler,MM,Müller,'20, +Biermann,'21]

Code available at: https://github.com/phbasler/BSMPT

Ξ README.md Program: BSMPT version 2.6.0 Released by: Philipp Basler and Lisa Biermann and Margarete Mühlleitner and Jonas Müller 💭 Ubuntu unit tests passing 💭 Mac unit tests passing 💭 Windows unit tests passing GitHub Discussions codecov 81% Benchmark master Maintained? yes license GPL-3.0 release v2.6.0 Documentation master Manual: version 2.0 BSMPT - Beyond the Standard Model Phase Transitions: The C++ program package BSMPT calculates the strength of the electroweak phase transition in extended Higgs sectors. For this the loop-corrected effective potential at finite temperature is calculated including the daisy resummation of the bosonic masses. The program computes the vacuum expectation value (VEV) \f\$ v \f\$ of the potential as a function of the temperature, and in particular the critical VEV \f\$v_c\f\$ at the temperature \f\$T_c\f\$ where the phase transition takes place. In addition, the loop-corrected trilinear Higgs self-couplings are provided. We apply an 'on-shell' renormalization scheme in the sense that the loop-corrected masses and mixing angles are required to be equal to their tree-level input values. This allows for efficient scans in the parameter space of the models.

The models implemented so far are

- CP-conserving 2-Higgs-Doublet Models (R2HDM)
- CP-violating 2-Higgs-Doublet Models (C2HDM)
- Next-to-Minimal 2HDM (N2HDM)
- CP in the Dark (arXiv 1807.10322, arXiv 2204.13425)
- Complex Singlet Extension (CxSM)

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SFOEWPT and Gravitational Waves





[Azfal et al.,'23]

NANOGrav: 3 evidence for stochastic GW background which could come from FOEWPT



Experiments Sensitive to GW from FOEWPT

ESA | NAS

LISA: expected sensitivity in frequency range associated w/ FOEWPT [Amaro-Second et al., '17]



Gravitational Waves from an FOEWPT

- FOEWPT → bubble nucleation
- Bubble wall expands into hot plasma
 ⇒ spherical symmetry breaking ~ gravitational waves
- Source of gravitational waves:
 - bubble collisions and mergers [Kosowsky et al., '92, 93, 94]
 - magnetohydronamic turbulence (shocks in fluid) [Caprini,Durer,'06;Kahniashvili eal,'08/10]
 - sound waves (bubble-wall accelerated plasma) [Giblin,Mertens,'13/14;Hindmarsh eal,'14/15]
- Sound waves dominant contribution:
 - if bubble walls interact w/ surrounding plasma, hence for
 - enough friction with the plasma \Rightarrow non-runaway bubbles, reaching a terminal velocity v_b
 - no early onset of turbulent regime, α < 1





Vacuum Decay

 Vacuum decay: transition from false to true vacuum through quantum tunneling or thermal fluctuations

[Plot from Athron eal,'23]



• Tunneling rate per unit volume:

$$\Gamma(T) = A(T) e^{\frac{\hat{S}_3}{T}} \simeq T^4 \left(\frac{\hat{S}_3}{2\pi T}\right)^{\frac{3}{2}} e^{\frac{\hat{S}_3}{T}}$$

 \hat{S}_3 : minimized O₃-symmetric Euclidean action (action of the bounce solution)

Expanding bubbles w/ true vacuum, racing against expanding universe, interactions with plasma in front of bubble wall

• Critical Temperature T_c : true (v≠0) and false (v=0) vacuum are degenerate, PT starts via quantum tunneling

• Nucleation Temperature T_n : one bubble nucleated per cosmological horizon; resp. tunneling rate matches Hubble rate

if not matched \rightarrow vacuum trapped in false vacuum

[see e.g. Baum eal,'21; Biekötter eal,'23]

• Percolation temperature T*: probability of finding point in false vacuum is 70% [Ellis eal,'19]

$$P_f(T_*) = e^{-I(T_*)} \equiv 0.7 \text{ with } I(T) = \frac{4\pi v_b^3}{3} \int_T^{T_c} \frac{\Gamma(T')dT'}{T'^4 H(T')} \left(\int_T^{T'} \frac{d\tilde{T}}{H(\tilde{T})} \right)^3$$





- Relevant quantities for GW spectrum:
 - PT strength, resp. released latent heat during PT

$$\boldsymbol{\alpha} = \frac{1}{\rho_{\gamma}} \Big[V(\vec{\phi_f}) - V(\vec{\phi_t}) - \frac{T}{4} \Big(\frac{\partial V(\vec{\phi_f})}{\partial T} - \frac{\partial V(\vec{\phi_t})}{\partial T} \Big) \Big]_{T=T_*}$$

 $\frac{\boldsymbol{\beta}}{\boldsymbol{H}} = T_* \left. \frac{d}{dT} \left(\frac{\hat{S}_3(T)}{T} \right) \right|_T$

- inverse time scale of the PT

- H Hubble constant
- $\tau_{\rm sh}$ fluid turnover time shock formation time
- g_* eff. number of rel. energy d.o.f.
- c_s sound speed
- κ efficiency factor

- bubble wall velocity v_b
- Peak frequency and amplitude of acoustic GWs [Hindmarsh eal,'17; Caprini eal,'20]

$$f^{\text{peak}} = 26 \times 10^{-6} \frac{\beta}{H} \left(\frac{1}{(8\pi)^{\frac{1}{3}} \max(\mathbf{v}_{b}, c_{s})} \right) \left(\frac{T_{*}}{100 \text{ GeV}} \right) \left(\frac{g_{*}}{100} \right)^{\frac{1}{6}} \text{ Hz}$$

$$h^{2} \Omega_{\text{GW}}^{\text{peak}} = 4 \times 10^{-7} \left(\frac{100}{g_{*}} \right)^{\frac{1}{3}} \begin{cases} \frac{(8\pi)^{1/3} \max(\mathbf{v}_{b}, c_{s})}{\beta/H} \left(\frac{\kappa \alpha}{1+\alpha} \right)^{2} & \text{if } H\tau_{\text{sh}} \simeq 1 \\ \frac{2}{\sqrt{3}} \left(\frac{(8\pi)^{1/3} \max(\mathbf{v}_{b}, c_{s})}{\beta/H} \right)^{2} \left(\frac{\kappa \alpha}{1+\alpha} \right)^{3/2} & \text{if } H\tau_{\text{sh}} < 1 \end{cases}$$

Available Codes

- Codes for the computation of the bounce action:
 - CosmoTransitions [Wainwright,'11]: via path deformation
 - AnyBubble [Masoumi,'17]: via a multiple shooting algorithm
 - BubbleProfiler [Athron eal,'19]: via semi-analytic algorithm [Akula eal,'16]
 - SimpleBounce [Sato,'19]: via gradient flow method
 - FindBounce [Guada eal,'18,'20]: via polygonal multifield method
 - OptiBounce [Bardsley,'21]: vial solving the ,reduced' minimization problem [Coleman,'77]

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Coming soon: BSMPTv3 [Biermann,MM,Santos,Viana,'23]

[Biermann, MM, Santos, Viana]

- Determination of tunneling path
- Computation of the bounce action, computation of the tunneling rate
- Computation of the nucleation temperature T_n , of the percolation temperature T_*
- Calculation of the latent heat release α , of the inverse time scale of the PT β/H
- Calculation of the peak frequency and the peak amplitude of the acoustic GWs

Why BSMPTv3

[Basler,MM,v1,'18] [Basler,MM,Müller,v2,'20]

[Biermann, MM, Santos, Viana, v3, '23]

- Optimized minimum tracing & tracking of temperature-dependent coexisting minimum phases over any temperature interval
- Numerical derivation of the bounce solution for any number of field dimensions
- More precise calculation of the nucleation temperature (compared to CosmoTransitions)
- Calculation of the percolation temperature (not implemented in CosmoTransitions)
- Calculation of the GW parameters $\alpha,\,\beta/H$
- Calculation of f^{peak} and $h^2 \Omega^{peak}$ of the (acoustic) GW spectrum
- Computation of signal-to-noise-ratio at LISA
- For all implemented models (CxSM, R2HDM, C2HDM, N2HDM, CP in the Dark)
- Embedded in the framework of the existing BSMPT code
 - -> consistent computation of all EWPT-related observables
 - -> easy user interface for implementing a new model
 - -> designed to use input from ScannerS

Gravitational Waves from SFOEWPT ín ,CP ín the Dark'



+Next-to-Minimal 2-Higgs Doublet Model:

[Azevedo,Ferreira,MM,Patel,Santos,Wittbrodt,'18]

$$\begin{split} V^{(0)} &= m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 + \frac{m_S^2}{2} \Phi_S^2 + \left(A \Phi_1^{\dagger} \Phi_2 \Phi_S + \text{ h.c.} \right) \\ &+ \frac{\lambda_1}{2} |\Phi_1|^4 + \frac{\lambda_2}{2} |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 + \lambda_4 |\Phi_1^{\dagger} \Phi_2|^2 + \frac{\lambda_5}{2} [(\Phi_1^{\dagger} \Phi_2)^2 + (\Phi_2^{\dagger} \Phi_1)^2] \\ &+ \frac{\lambda_6}{4} \Phi_S^4 + \frac{\lambda_7}{2} |\Phi_1|^2 \Phi_S^2 + \frac{\lambda_8}{2} |\Phi_2|^2 \Phi_S^2. \end{split}$$

* with one discrete \mathbb{Z}_2 symmetry: $\Phi_1 \to \Phi_1$, $\Phi_2 \to -\Phi_2$, $\Phi_S \to -\Phi_S$

one SM-like Higgs plus dark sector: h₁,h₂,h₃,H[±]

 + trilinear coupling A is complex: dark sector with explicit CP violation <- not constrained by electric dipole moment +General vacuum structure at T≠0:

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_1 + i\eta_1 \\ \zeta_1 + \omega_1 + i\Psi_1 \end{pmatrix}, \quad \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_2 + \omega_{CB} + i\eta_2 \\ \zeta_2 + \omega_2 + i(\Psi_2 + \omega_{CP}) \end{pmatrix}, \quad \Phi_S = \zeta_S + \omega_S$$

electroweak VEVs: ω_{1}, ω_{2} , CP-violating VEV: ω_{CP} charge-breaking VEV: ω_{CB} (unphysical; found to be zero for all of our scan points) Z₂-symmetry breaking VEV: ω_{5}

+General vacuum structure at T=0:

$$\begin{split} \Phi_1 &= \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_1 + i\eta_1\\ \zeta_1 + \nu_1 + i\Psi_1 \end{pmatrix}, \ \Phi_2 &= \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_2 + i\eta_2\\ \zeta_2 + i\Psi_2 \end{pmatrix}, \ \Phi_s &= \zeta_s\\ \langle \Phi_1 \rangle |_{T=0} &= \frac{1}{\sqrt{2}} \begin{pmatrix} 0\\ \mathbf{v}_1 \end{pmatrix}, \ \langle \Phi_2 \rangle |_{T=0} &= \begin{pmatrix} 0\\ 0 \end{pmatrix}, \ \langle \Phi_s \rangle |_{T=0} = 0 \end{split}$$

$$\omega_1 |_{T=0 \text{ GeV}} = v1 \equiv v = 246.22 \text{ GeV}$$

M. Mühlleitner (KIT), 14 Sept 2023

Scalars 2023, Warsaw

- + Scan in parameter space of the model w/ ScannerS [Coimbra eal,'13;MM eal,'20]
- *Keep only points compatible w/

theoretical constraints: bounded-from-below, perturbative unitarity, EW vacuum 🗸

experimental constraints: (EDMs automatically fulfilled)

- EW precision tests
 SM-like Higgs h compatibility w/:
- m_h=125 GeV
- Higgs Data [HiggsSignals]
- (- Higgs exclusion limits [HiggsBounds])
- BR(h->inv) < 0.11 [ATLAS,'19]
- $\mu(h \rightarrow \gamma \gamma)=1.12\pm0.09$ [CMS,'21]
- # DM observables (through MicrOMEGAs):
- relic density $\Omega_{obs}h^2$ =0.1200±0.0012 [Aghanim eal,'18] (require it to below)
- XENON1T exclusion limit [Aprile eal,'18]
- new LUX-ZEPLIN exclusion limit [Aalbers eal,'22]

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SM-like Higgs h has SM couplings by construction w/ exception of:

- hH^+H^- coupling modifies loop-ind. $h\gamma\gamma$ coupling
- h->h_ih_j decay (h_{i,j} dark sector particles), modifies total width & hence BRs
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Mass Parameter Distribution for SFOEWPT



[Biermann,MM,Müller,'22]

- points compatible w/ theor. & exp. constraints (ScannerS/grey), w/ NLO stable vacuum (BSMPT/orange) & w/ SFOEWPT (BSMPT/colored) scattered all over mass parameter planes → no further constraint on mass parameter space
- $m_{H\pm}$ range constrained due to $\mu_{\gamma\gamma}$ (from CMS)

Impact of Higgs-to-Photon Decay

[Biermann, MM, Müller, '22]



- increase for smaller $m_{H_{\pm}}$ (governed by λ_3)
- upper limit on $\mu_{\gamma\gamma}$: BFB and unitarity bounds \rightarrow restrict max. λ_3 value
 - => future increased precision in $\mu_{\gamma\gamma}$ can cut parameter space substantially

Higgs-to-Invisibles Decay



[Biermann, MM, Müller, '22]

- SFOEWPT points scattered across allowed ScannerS parameter space
- BR(h->inv) strongly correlated w/ μ_{VV} (V=W±,Z): for μ_{VV} ->1 SM-like Higgs BRs converge to SM values \rightarrow BR(h->inv) forbidden =>
- future increased precision in BR(h->inv) and μ_{VV} constrain parameter space, however, no further insights in strength of EWPT gained



GW from (S)FOEWPT in ,CP in the Dark'



- 3 points w/ SNR(LISA-3yrs)>10, compatible w/ all relevant theor. and exp. constraints

- all points lead to EW minimum at T=0 (no vacuum trapping)
- all of the LISA-sensitive points (colored points) have SFOEWPT: ξ_c >1

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GW from (S)FOEWPT in ,CP in the Dark'



M. Mühlleitner (KIT), 14 Sept 2023

DM Observables and GW



[Biermann, MM, Santos, Viana]

- Viable GW points (SNR(LISA-3yrs)>1 colored points): compatible w/ relic density (<Ωh²) above neutrino floor
 - testable at future direct detection experiments

Spontaneous CP Violation



- possibility of SFOEWPT & spontaneous CP violation (CPV)
- spontaneous Z₂ violation also possible => non-standard CPV transferred to visible sector
- interesting for EWBG!

- SNR(LISA-3yrs)>1 (colored) for max. $|\omega_{CP}|=O(10^{-1})$
- spontaneous Z_2 violation leads to plasma friction w/ (former) DM direction =>
- spontaneous CPV may escape run-away

50

40

Conclusions

- Generation of BAU through EWBG requires BSM physics: extended Higgs sectors
- SFOEWPT induces gravitational waves testable at LISA
- Code **BSMPT**: Calculation of loop-corrected effective potential incl. thermal masses
- BSMPTv3: Calculation of gravitational waves spectrum, signal-to-noise ratio at LISA
- Model ,CP in the Dark': SM-like Higgs, extended dark sector w/ explicit CP violation
- ,CP in the Dark': parameter points
 - * compatible w/ all relevant exp. (incl. DM observables) & theor. constraints
 - * strong first-order electroweak phase transition
 - * spontaneous CP and Z₂ violation possible \rightarrow CP violation transferred to visible sector
 - * gravitational waves spectrum testable at LISA
- Code BSMPTv3 to be released soon stay tuned.



Bijou

Bijou

How to choose v_b ?

see [Athron et al., '23] for a review and references within

- $v_b = 0.95$ for our plots; calculation of v_b is still an open question:
- <u>basic problem</u>: when does plasma friction match driving pressure of bubble expansion? (model-dependent out-of equilibrium calculation)
- *but* only two equations from energy-momentum tensor conservation for unknown v_b , plasma temperature and plasma velocities around bubble wall are unknown
- <u>often-made approximation</u>: local thermal equilibrium \rightarrow + entropy conservation
- *but* solving Boltzmann equation requires knowledge of collision integral, simplified by ansatz for distribution function (model-dependent!)
- BSMPTv3 provides:
 - v_w as input parameter or set to $v_w = 0.95$
 - estimate by [Lewicki et al., '22] (assuming steady-state ($\dot{v}_b = 0$) and local thermal equilibrium):

$$v_b \simeq \begin{cases} \sqrt{\frac{\Delta V}{\alpha \rho_{\gamma}}} & \text{if } \sqrt{\frac{\Delta V}{\alpha \rho_r(T_*)}} < v_{\text{CJ}} \\ 1 & \text{if } \sqrt{\frac{\Delta V}{\alpha \rho_r(T_*)}} > v_{\text{CJ}} \end{cases}$$

• estimate by [Laurent et al., '23] (assuming local thermal equilibrium):

$$v_{b} = \left(\left| \frac{3\alpha + \Psi - 1}{2\left(2 - 3\Psi + \Psi^{3}\right)} \right|^{\frac{p}{2}} + \left| v_{\text{CJ}} \left(1 - a \frac{(1 - \Psi)^{b}}{\alpha} \right) \right|^{\frac{p}{2}} \right)^{\frac{1}{p}}$$

with Chapman-Jouguet velocity $v_{\text{CJ}} = \frac{1}{1+\alpha} \left(c_s + \sqrt{\alpha^2 + \frac{2}{3}\alpha} \right)$ (expansion mode of chamical combustion, need not be satisfied in complexical phase transition. If since 2041

chemical combustion, need not be satisfied in cosmological phase transition [Laine, '94], $v_b > v_{CJ}$ in general (otherwise stopped by plasma friction))

 estimates of v_b in *local thermal equilibrium* serve as upper bound as v_b gets reduced by non-equilibrium effects!

$$\rho_r(T_*) = \frac{\pi^2}{30} g^*(T_*) T_*^4$$
rel. matter density
$$\Psi = \frac{\omega_t}{\omega_f} \quad \text{enthalpy ratio}$$

$$a = 0.2233 \quad \text{num. fit result}$$

$$b = 1.704 \quad \text{num. fit result}$$

$$p = -3.433 \quad \text{num. fit result}$$

$$c_s = \frac{1}{\sqrt{3}} \quad \text{sound speed}$$

Slide taken from Lisa Biermann

WHAT ABOUT SUPERCOOLING?



 \Rightarrow transition duration around 10 GeV for SNR(LISA-3yrs) > 1

 \rightarrow [Wang et al., '20]:

- * slight supercooling for $\alpha \leq 0.1$
- * *mild supercooling* for $0.1 \le \alpha \le 0.5 \rightarrow$ case for our SNR(LISA-3yrs) > 1 points
- * strong supercooling for $\alpha > 0.5$

+ Power Spectrum:

$$h^2 \Omega_{\rm GW} = h^2 \Omega_{\rm GW}^{\rm peak} \left(\frac{4}{7}\right)^{-\frac{7}{2}} \left(\frac{f}{f_{\rm peak}}\right)^3 \left[1 + \frac{3}{4} \left(\frac{f}{f_{\rm peak}}\right)^2\right]^{-\frac{7}{2}}$$

Nucleation and Percolation Temperatures



[Biermann, MM, Santos, Viana]

Spontaneous CP Violation



[Biermann,MM,Müller'22]

Strong first order electroweak phase transition

Baryogenesis in a Nutshell

