

# Enhancement of the $H^\pm W^\mp Z$ vertex in the three scalar doublet model

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# Charge assignments under $Z_2 \times \tilde{Z}_2$

	$(Z_2, \tilde{Z}_2)$ charge							
	$\Phi_1$	$\Phi_2$	$\eta$	$Q_L$	$L_L$	$u_R$	$d_R$	$e_R$
Type-I	(+, +)	(+, -)	(-, +)	(+, +)	(+, +)	(+, -)	(+, -)	(+, -)
Type-II	(+, +)	(+, -)	(-, +)	(+, +)	(+, +)	(+, -)	(+, +)	(+, +)
Type-X	(+, +)	(+, -)	(-, +)	(+, +)	(+, +)	(+, -)	(+, -)	(+, +)
Type-Y	(+, +)	(+, -)	(-, +)	(+, +)	(+, +)	(+, -)	(+, +)	(+, -)

$\Phi_1, \Phi_2$  are the active doublets

$\eta$  is the inert doublet

Symmetries:

$Z_2$  (unbroken) guarantees stability of DM

$\tilde{Z}_2$  (softly-broken) forbids FCNC at tree level

# The potential

$$\begin{aligned} V = & \mu_\eta^2 \eta^\dagger \eta + \mu_1^2 \Phi_1^\dagger \Phi_1 + \mu_2^2 \Phi_2^\dagger \Phi_2 - (\mu_3^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) \\ & + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \frac{1}{2} [\lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.}] + \frac{1}{2} \lambda_\eta (\eta^\dagger \eta)^2 \\ & + \rho_1 (\Phi_1^\dagger \Phi_1)(\eta^\dagger \eta) + \rho_2 |\Phi_1^\dagger \eta|^2 + \frac{1}{2} [\rho_3 (\Phi_1^\dagger \eta)^2 + \text{h.c.}] \\ & + \sigma_1 (\Phi_2^\dagger \Phi_2)(\eta^\dagger \eta) + \sigma_2 |\Phi_2^\dagger \eta|^2 + \frac{1}{2} [\sigma_3 (\Phi_2^\dagger \eta)^2 + \text{h.c.}] \end{aligned}$$

The scalar fields can be parametrised as

$$\Phi_i = \begin{bmatrix} w_i^+ \\ \frac{1}{\sqrt{2}}(h_i + v_i + iz_i) \end{bmatrix}, \quad (i = 1, 2), \quad \eta = \begin{bmatrix} \eta^+ \\ \frac{1}{\sqrt{2}}(\eta_H + i\eta_A) \end{bmatrix},$$

where  $v_i$  are the VEVs of  $\Phi_i$  with  $v_1^2 + v_2^2 = v^2 \simeq (246 \text{ GeV})^2$ . The ratio of the two VEVs is given by  $\tan \beta = v_2/v_1$ .

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# The Yukawa Lagrangian

$$\mathcal{L}_Y = - Y_u \overline{Q}_L i\sigma_2 \Phi_u^* u_R - Y_d \overline{Q}_L \Phi_d d_R - Y_e \overline{L}_L \Phi_e e_R + \text{h.c.},$$

The interaction terms

$$\begin{aligned} -\mathcal{L}_Y^{\text{int}} &= \sum_{f=u,d,e} \frac{m_f}{v} [\xi_h^f \overline{f} f h + \xi_H^f \overline{f} f H - 2i l_f \xi_f \overline{f} \gamma_5 f A] \\ &\quad + \frac{\sqrt{2}}{v} [V_{ud} \overline{u} (m_d \xi_d P_R - m_u \xi_u P_L) d H^+ + m_e \xi_e \overline{\nu} P_R e H^+ + \text{h.c.}], \end{aligned}$$

$\xi_h^f$  and  $\xi_H^f$  are defined by

$$\xi_h^f = \sin(\beta - \alpha) + \xi_f \cos(\beta - \alpha),$$

$$\xi_H^f = \cos(\beta - \alpha) - \xi_f \sin(\beta - \alpha),$$

SM-like limit or alignment limit defined by  $\sin(\beta - \alpha) \rightarrow 1$

# The Yukawa Lagrangian

	Mixing factor		
	$\xi_u$	$\xi_d$	$\xi_e$
Type-I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type-II	$\cot \beta$	$-\tan \beta$	$-\tan \beta$
Type-X	$\cot \beta$	$\cot \beta$	$-\tan \beta$
Type-Y	$\cot \beta$	$-\tan \beta$	$\cot \beta$

# The vertex

- Loop amplitude of  $H^\pm \rightarrow W^\pm V$  ( $V = Z, \gamma$ )

$$i\mathcal{M}(H^\pm \rightarrow W^\pm V) = igm_W V_V^{\mu\nu} \epsilon_{W\mu}(p_W) \epsilon_{V\nu}(p_V)$$

with  $V_V^{\mu\nu}$  written in terms of dimensionless form factors:

$$V_V^{\mu\nu} = g^{\mu\nu} F_V + \frac{p_V^\mu p_W^\nu}{m_W^2} G_V + i\epsilon^{\mu\nu\rho\sigma} \frac{p_{V\rho} p_{W\sigma}}{m_W^2} H_V$$

with  $p_W^\mu$  and  $p_V^\mu$  incoming momenta for  $W^\pm$  and  $V$ .

- For the case of  $V = \gamma$ , Ward identity  $V_\gamma^{\mu\nu} p_{\gamma\nu} = 0$ . implies

$$F_\gamma = \frac{G_\gamma}{2} \left( 1 - \frac{m_{H^\pm}^2}{m_W^2} \right)$$

where  $p_W^2 = m_W^2$  and  $(p_W + p_\gamma)^2 = m_{H^\pm}^2$ .

# The vertex

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with  $V_V^{\mu\nu}$  written in terms of dimensionless form factors:

$$V_V^{\mu\nu} = g^{\mu\nu} F_V + \frac{p_V^\mu p_W^\nu}{m_W^2} G_V + i\epsilon^{\mu\nu\rho\sigma} \frac{p_{V\rho} p_{W\sigma}}{m_W^2} H_V$$

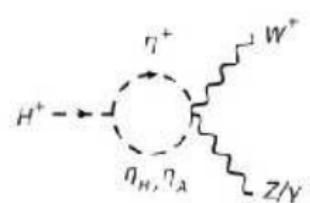
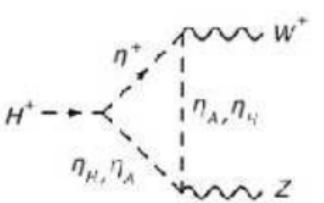
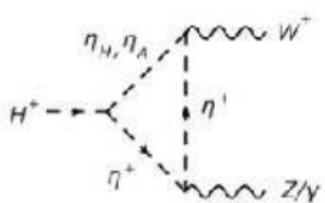
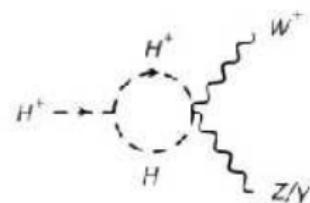
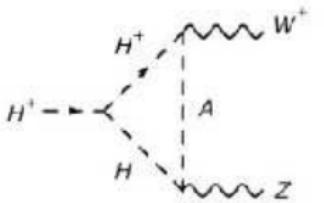
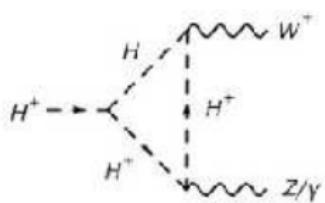
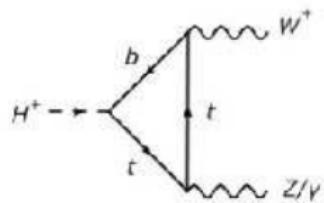
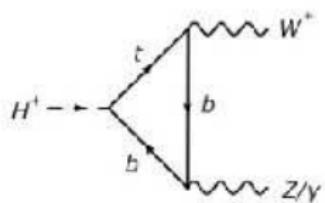
with  $p_W^\mu$  and  $p_V^\mu$  incoming momenta for  $W^\pm$  and  $V$ .

- The effective Lagrangian:

$$\mathcal{L}_{\text{eff}} = f_Z H^+ W_\mu^- Z^\mu + g_V H^+ F_W^{\mu\nu} F_{V\mu\nu} + i h_V \epsilon_{\mu\nu\rho\sigma} H^+ F_W^{\mu\nu} F_V^{\rho\sigma} + \text{h.c.}$$

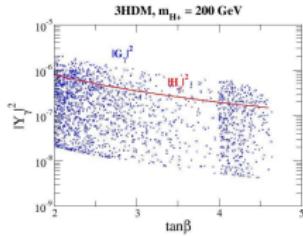
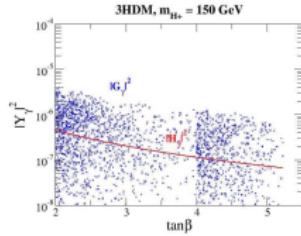
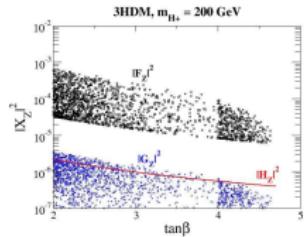
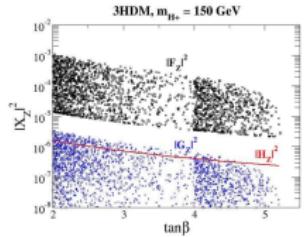
where  $F_W^{\mu\nu}$  and  $F_V^{\mu\nu}$  are the field strength tensors.

The coefficient  $f_Z$  has mass dimension one whereas  $g_V$  and  $h_V$  have mass dimension minus one.



**Figure :** The 1PI diagrams for the  $HWZ$  and  $HW\gamma$  vertices. The diagrams which vanish in the limit  $\sin(\beta - \alpha) = 1$  are not displayed.

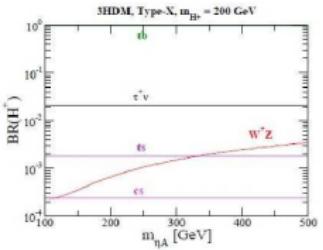
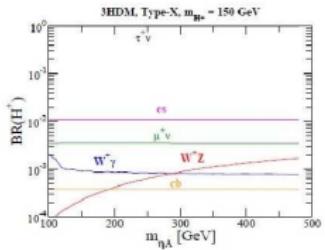
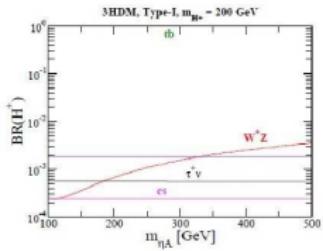
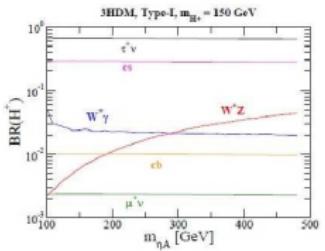
# Form Factors



Calculations are made in Type I and X (light  $m_{H^\pm}$  is more interesting)

$m_H = m_{H^\pm}$ ,  $-400^2 \text{ GeV}^2 < M^2 < 400^2 \text{ GeV}^2$ ,  $100 \text{ GeV} < m_A < 260$  (350) GeV,  $\tan\beta = 2.5$  in the last plot

# Branching Ratios



- If  $m_{H^\pm} < m_t$ :  $t \rightarrow H^\pm b$  dominant
- If  $m_{H^\pm} > m_t$ :  $H^\pm$ -strahlung dominant

# Cross sections

For the signature

$$pp \rightarrow b\bar{b}H^\pm W^\mp \rightarrow b\bar{b}W^\pm W^\mp V$$

$$\sigma_{S,V}^{\text{top}} = 2 \times \sigma_{t\bar{t}} \times [1 - \text{BR}(t \rightarrow H^\pm b)] \times \text{BR}(t \rightarrow H^\pm b) \times \text{BR}(H^\pm \rightarrow W^\pm V), \quad (1)$$

Also EW productions e.g.

$$pp \rightarrow H^\pm A / H^\pm H \rightarrow W^\pm V + X^0$$

$$pp \rightarrow H^+ H^- \rightarrow W^\pm V + X^\pm$$

$$\sigma_{S,V}^{\text{EW}} = (\sigma_{H^\pm A} + \sigma_{H^\pm H} + 2\sigma_{H^+ H^-}) \times \text{BR}(H^\pm \rightarrow W^\pm V), \quad (2)$$

	Type-I	Type-X
$\sigma_{S,Z}^{\text{top}} [\text{fb}]$	(390, 700, 29)	(15, 28, 1.6)
$\sigma_{S,\gamma}^{\text{top}} [\text{fb}]$	(940, 420, 1.4)	(35, 16, 0.075)
$\sigma_{S,Z}^{\text{EW}} [\text{fb}]$	(2.3, 7.5, 46)	(0.087, 0.30, 2.5)
$\sigma_{S,\gamma}^{\text{EW}} [\text{fb}]$	(5.5, 4.5, 2.2)	(0.20, 0.17, 0.12)

here we are considering the three cases  $m_{H^\pm} = 130, 150$  and  $170$  GeV

# Summary

- The scalar bosons from the inert doublet give an additional contribution
- $|F_Z|^2$  can be one order of magnitude greater than the one predicted in the 2HDM
- In Type I and X Yukawa interactions, branching ratios are enhanced (10% level)
- The detection with early data at Run 2 of  $H^\pm \rightarrow W^\pm Z$  signals could represent circumstantial evidence of a 3HDM structure of the Higgs sector