

# Exotic Dark Matter in 3HDMs

Venus Keus

**DIAS**

Institiúid Ard-Léinn | Dublin Institute for  
Bhaile Átha Cliath | Advanced Studies



**Scalars 2023**

An opportunity to discuss various aspects of scalar particles.

Based on work published and in progress

In collaboration with S. King, S. Moretti, D. Sokolowska, D. Rojas, J. Hernandez, N. Koivunen, K. Tuominen, L. Niemi, H. Haber, R. Santos, M. Ramsey-Musolf, K. Rummukainen, A. Dey, J. Thomson-Cooke

13.09.2023

# Ireland is finally joining CERN

## Ireland could join CERN by 2018 - Gianotti

Updated: Friday, 4 Nov 2016 14:06



## Trinity academics call on Ireland to join CERN

THE IRISH TIMES

by Leigh Mc Gowran

● 1 OCT 2016 □ SAVE ARTICLE

Opinion

Harris say benefits of joining Cern 'significant' as department prepares submission

Minister tells Dáil he has Taoiseach's full support in bid to join nuclear research agency



Opinion



Opinion

THE IRISH TIMES

Science Analysis

## A happy new year for Ireland and Cern

Irish scientists could at last participate in 'big science' experiments and work with the best in the world



THE IRISH TIMES

## Ireland should join Cern, says Oireachtas committee

Membership of organization is critical to becoming 'a global innovation leader'

Thu Nov 14 2016 - 11:58



## Why is Ireland not a member of Cern?

State has rich history in particle physics but will not cough up €1m Cern membership fee

Thu Jun 24 2016 - 01:00



## Government to consider Cern membership

Review will study benefits and costs of joining the European nuclear research lab

Thu Jan 30 2016 - 22:29



# You are cordially invited to ...

## Cosmology, Astrophysics, Theory and Collider Higgs 2024 conference (CATCH22+2)

1-5 May 2024  
Dublin, Ireland



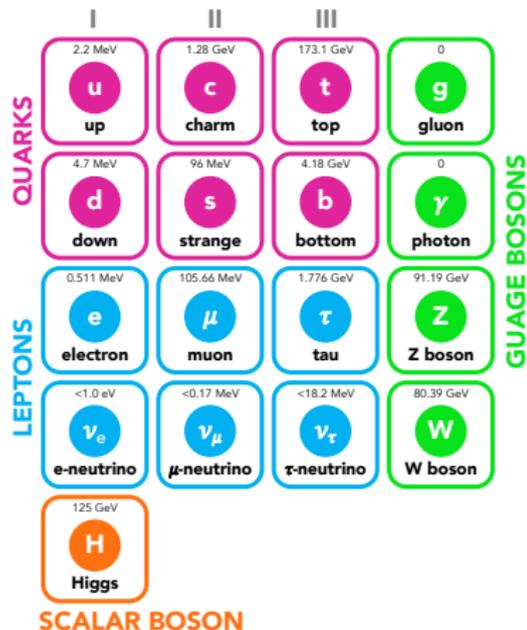
Webpage: <https://indico.cern.ch/e/catch24>

Photo credit: istock photo images

# The Standard Model

Its current formulation was finalised in the 70's and predicted:

- the W & Z bosons  
discovered in 1983
- the top quark  
discovered in 1995
- the tau neutrino  
discovered in 2000
- the Brout-Englert-Higgs mechanism  
a scalar boson discovered in 2012



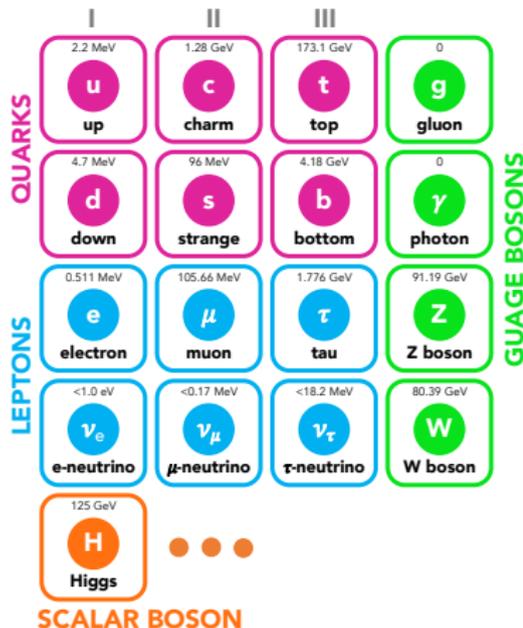
# ... and the need to go beyond

## What is missing:

- a suitable Dark Matter candidate
- a successful baryogenesis mechanism
  - strong first order phase transition
  - sufficient amount of CP violation
- a natural inflation framework
- an explanation for the fermion mass hierarchy
- a stable electroweak vacuum

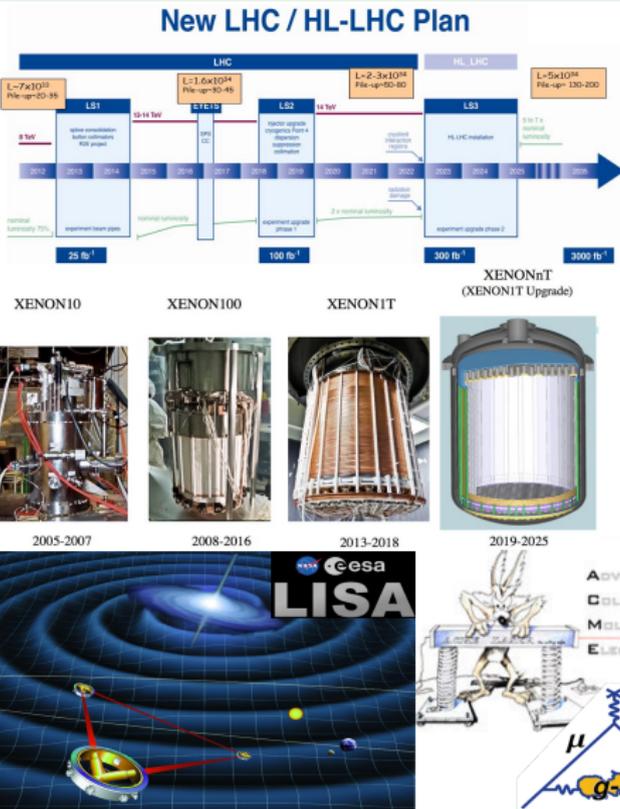
⇒ beyond the Standard Model

⇒ scalar extensions of the SM



# Complementary experimental probes of scalar extensions

- Collider experiments
  - LHC-RUN-III
  - HL-LHC
  - CEPC
- DM experiments
  - XENONnT
  - CTA
- GW experiments
  - DECIGO
  - LISA mission
- Precision experiments
  - $(g - 2)_\mu$
  - Advanced ACME



# The truth about Dark Matter

## The common misinformation:

For the first time, Fritz Zwicky in 1933: “The Coma cluster moves **too fast** for its apparent **gravitational pull** (due to its luminous matter) to stay together.”

⇒ Dark Matter within the cluster



# The truth about Dark Matter

## The common misinformation:

For the first time, Fritz Zwicky in 1933: “The Coma cluster moves **too fast** for its apparent **gravitational pull** (due to its luminous matter) to stay together.”

⇒ **Dark Matter within the cluster**

## The correct information:

Three years prior, Knut Lundmark in 1930 had already found evidence for Dark Matter and coined the term.



# The truth about Dark Matter

**Knut Lundmark**, *Lund Medd. No125 (1930) 1 – 10* (Thanks to D.Dravins and A. L’Huillier, Lund University for digging out the original paper, in German, my translation):

*“Under the condition that the mass-luminosity relation is valid for all stellar systems, the mass for the investigated systems can be computed using the total absolute magnitude  $M_{tot}$  which can be found when the distance is known and the total apparent  $m_{tot}$  is observed. The mass computed in this way, the luminous mass, does understandably not include the mass of the dark objects of the system (extinguished stars, dark clouds, meteors, comets, and so on). To determine the total mass or the gravitational mass, we need to rely on the five cases where one has detected an effect of rotation by spectrographical means. ... A comparison between the two kinds of masses gives an estimate of the ratio of luminous and dark matter for some stellar systems (Table 4).”*

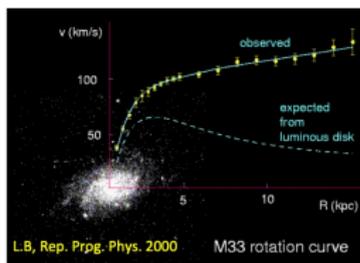


Tabelle 4.

Ratio:  
Luminous + Dark Matter  
Luminous Matter

Objekt	
Messier 81	100:1 (?)
N. G. C. 4594	30:1
Andromedanebel	20:1
Messier 51	10:1
Milchstraßensystem	10:1
Messier 33	6:1

From Lars Bergstrom’s talk (modified) at the Workshop on Off-the-Beaten-Track Dark Matter and Astrophysical Probes of Fundamental Physics (April 2015)





# Scalar extensions of the SM

## SM + scalar singlets [link](#)

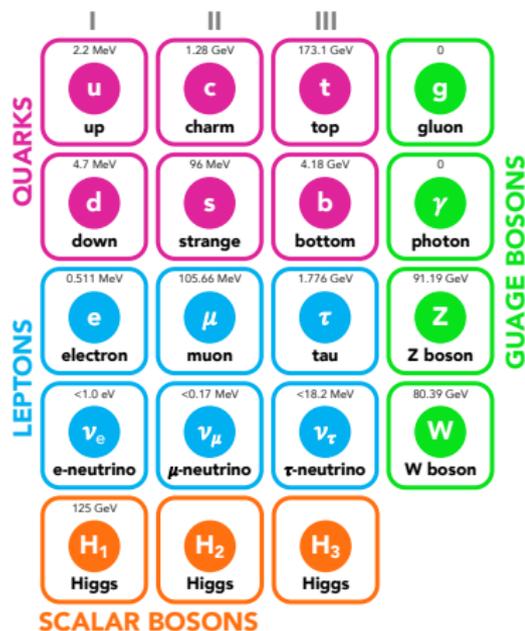
- Dark Matter **severely constrained**
- CP-violation **not possible**

## 2HDM: SM + a doublet [link](#)

- Dark Matter **constrained & CPV incompatible**
- CP-violation **severely constrained & DM incompatible**

## 3HDM: SM + 2 doublets [link](#)

- Dark Matter **many exotic possibilities**
- CP-violation **unbounded dark CP-violation**
- Inflation **easily achieved + exotic possibilities**
- Strong first order EWPT **easily achieved**
- Bonus: fermion mass hierarchy explanation



# Scalar singlet extension of SM

the SM Higgs doublet + a scalar singlet

 $\phi$ 
 $S$ 

$$\phi = \begin{pmatrix} G^+ \\ \frac{h+iG^0}{\sqrt{2}} \end{pmatrix}$$

$$S = \begin{pmatrix} s \\ \sqrt{2} \end{pmatrix}$$

$$\underbrace{S S \rightarrow \text{SM SM}}_{\text{pair annihilation}},$$

$$\underbrace{S \not\rightarrow \text{SM SM}}_{\text{stable}}$$

## SM + scalar singlet

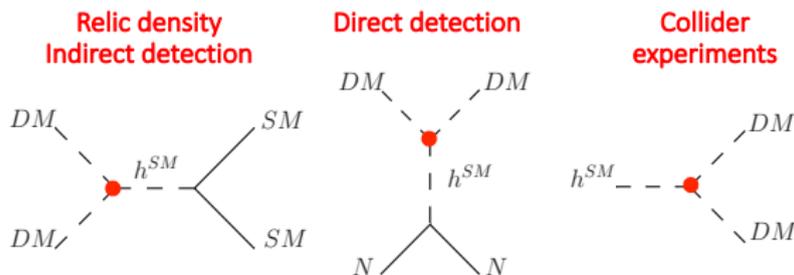
DM ✓, CPV ×

DM protected by a  $Z_2$  symmetry (+, -) from decaying to SM particles.

SM fields  $\rightarrow$  SM fields,  $\phi \rightarrow \phi$ ,  $S \rightarrow -S$

The Lagrangian and the vacuum are  $Z_2$  symmetric:  $\langle \phi \rangle = v$ ,  $\langle S \rangle = 0$

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{2}(\partial S)^2 - m_s^2 S^2 - \lambda_s S^4 - \lambda_{hs} \phi^2 S^2$$

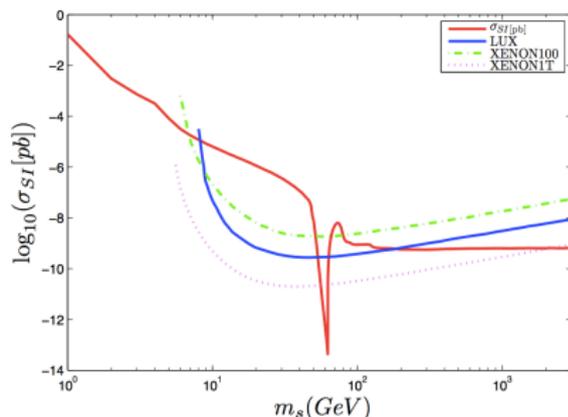


**Tension:** all relevant interactions are governed by the same coupling!

## SM + scalar singlet

DM ✓, CPV ×

- Bounded from below potential:  
 $h, s \rightarrow \infty \Rightarrow V > 0$
- Vacuum stability:  
 $\tau_{VEW} > \text{age of the universe}$
- Perturbative unitarity:  
 $|\lambda_i| \leq 4\pi, |\Lambda_i| \leq 8\pi$
- Higgs decays:  
 $BR(h \rightarrow inv.) < 20\% \Rightarrow \lambda_{hs} \text{ small}$
- Relic density:  
 $\lambda_{hs} \text{ large}$
- Direct and indirect detection:  
 $\lambda_{hs} \text{ small}$



# 2-Higgs doublet models (2HDMs)

the SM Higgs doublet + 1 scalar doublet

 $\phi_1$  $\phi_2$ 

$$\phi_1 = \begin{pmatrix} G^+ \\ \frac{h+iG^0}{\sqrt{2}} \end{pmatrix} \quad \phi_2 = \begin{pmatrix} H^+ \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$$

# $Z_2$ -symmetric 2HDM

DM  $\checkmark$ , CPV  $\times$ 

DM is protected by a  $Z_2$  symmetry (+, -) from decaying to SM particles:

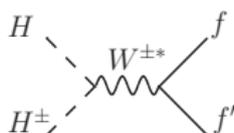
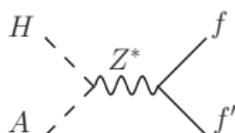
$$\text{SM fields} \rightarrow \text{SM fields}, \quad \phi_1 \rightarrow \phi_1, \quad \phi_2 \rightarrow -\phi_2$$

$Z_2$  symmetry: only  $\phi_1$  couples to fermions  $\phi_u = \phi_d = \phi_e = \phi_1$

$$-\mathcal{L}_{Yukawa} = Y_u \bar{Q}'_L i \sigma_2 \phi_u^* u'_R + Y_d \bar{Q}'_L \phi_d d'_R + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.}$$

$Z_2$  symmetry respected by the vacuum:  $\phi_1 = \begin{pmatrix} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix}$ ,  $\phi_2 = \begin{pmatrix} H^+ \\ \frac{H+iA}{\sqrt{2}} \end{pmatrix}$

DM candidate: the lightest neutral particle from the dark doublet



**Tension:** all scalar interactions are governed by the same coupling!  
Gauge couplings are fixed!

# More constraints in scalar doublet extensions of SM

Electroweak precision observables:

$S, T, U$  parameters

Flavour observables:

$$BR(B \rightarrow X_s \gamma), \quad B^0 - \bar{B}^0 \text{ mixing}$$

$$D_s \rightarrow \tau \nu_\tau, \quad D_s \rightarrow \mu \nu_\mu, \quad B \rightarrow D \tau \nu_\tau$$

LEP bounds:

$$m_{H^\pm} + m_{H,A} > m_{W^\pm}, \quad m_H + m_A > m_Z, \quad 2m_{H^\pm} > m_Z$$

$$m_{H^\pm} \gtrsim 70 - 90 \text{ GeV}$$

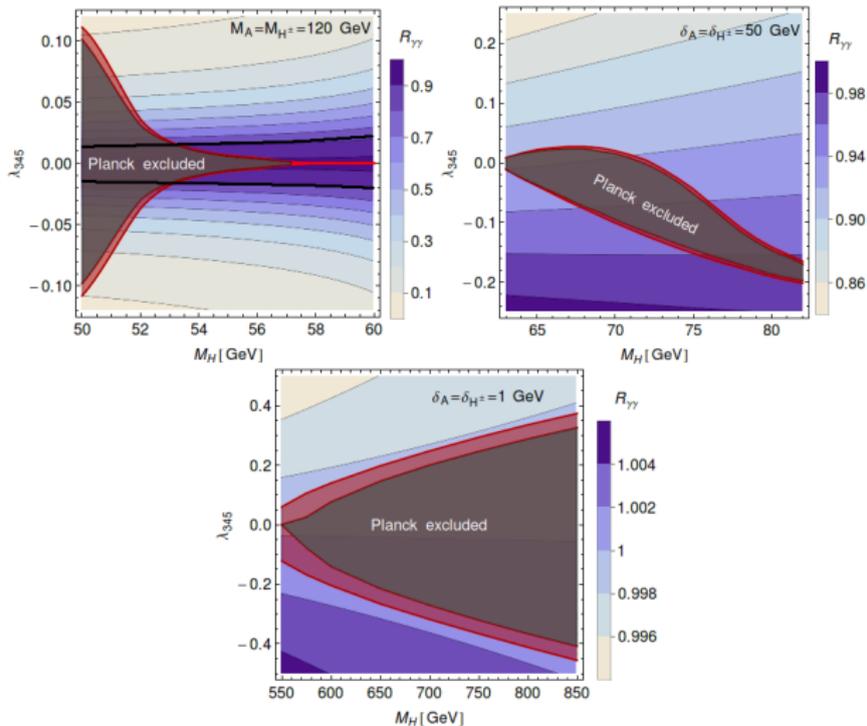
$$\text{if } M_H < 80 \text{ GeV and } M_A < 100 \text{ GeV} \Rightarrow M_A - M_H < 8 \text{ GeV}$$

LHC bound on the total decay signal strength:

$$\mu_{tot} = \frac{BR(h \rightarrow XX)}{BR(h_{SM} \rightarrow XX)} = 1.17 \pm 0.17$$

# $Z_2$ -symmetric 2HDM

DM ✓, CPV ✗



M. Krawczyk, D. Sokolowska, P. Swaczyna and B. Swiezewski, [JHEP 09 (2013) 055]

## CP-violating 2HDM

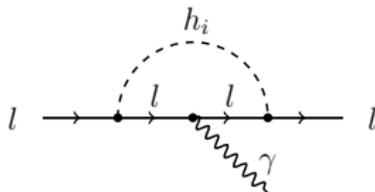
DM ×, CPV ✓

Break the  $Z_2$  symmetry and let the two doublets mix

$$\phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{v_1 + h_1^0 + ia_1^0}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{v_2 + h_2^0 + ia_2^0}{\sqrt{2}} \end{pmatrix}$$

No Dark Matter candidate!

Mixing doublets means  $h_i$  (mixtures of  $h_{1,2}^0, a_{1,2}^0$ ) are CP-mixed states



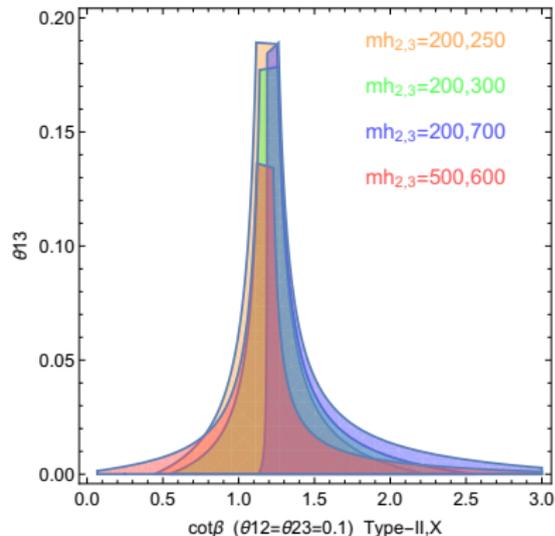
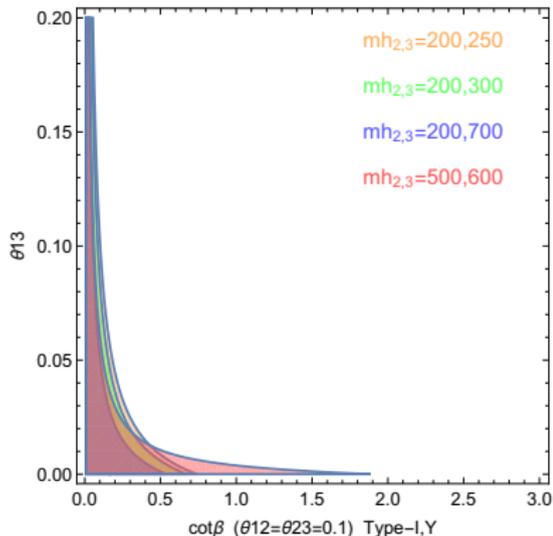
contributing to electric dipole moments (EDMs).

CP-violation is very constrained!

## CP-violating 2HDM

DM ×, CPV ✓

Parameter space allowed by the EDM bounds

implications for  $(g - 2)_\mu$ 

V. Keus, N. Koivunen, K. Tuominen, [JHEP 09, 059 (2018)]

# 3-Higgs doublet models (3HDMs)

2 scalar doublets + the SM Higgs doublet

$\phi_1, \phi_2$

$\phi_3$

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{h + iG^0}{\sqrt{2}} \end{pmatrix}$$

# $Z_2$ -symmetric 3HDM with dark CPV

DM is protected by a  $Z_2$  symmetry  $(-, -, +)$ :

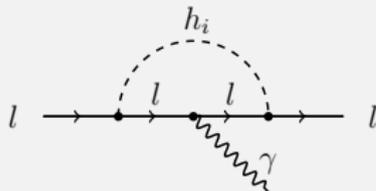
$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}, \quad \phi_3 \rightarrow \phi_3$$

$Z_2$  symmetry respected by the vacuum  $(0, 0, v)$ :

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix}$$

Only  $\phi_3$  can couple to fermions  $\phi_u = \phi_d = \phi_e = \phi_3$  and  $h_i = h$

$$-\mathcal{L}_{Yukawa} = Y_u \bar{Q}'_L i\sigma_2 \phi_u^* u'_R + Y_d \bar{Q}'_L \phi_d d'_R + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.}$$

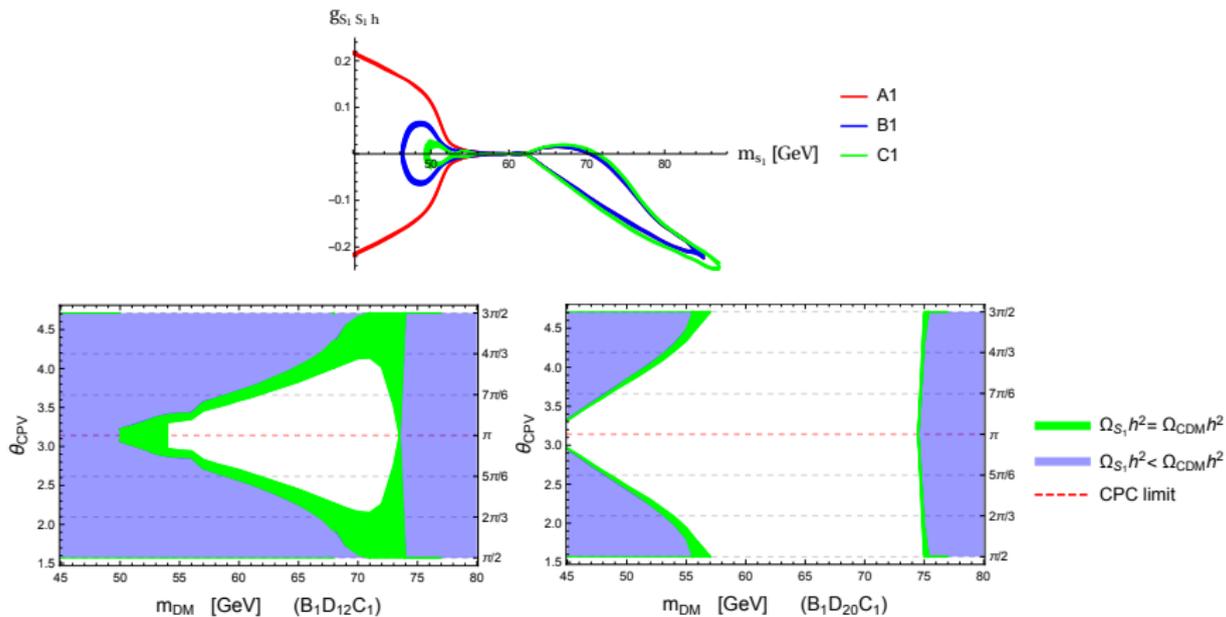


**No contributions to electric dipole moments (EDMs)**



# $Z_2$ -symmetric 3HDM with dark CPV

Due to co-annihilation with other dark particles



V. Keus, S. F. King, S. Moretti, D. Sokolowska, et al., [JHEP 12, 014 (2016)], V. Keus, [Phys. Rev. D 101, 073007 (2020)]

Dark CPV observables

# Multi-component Dark Matter in 3HDMs

2 scalar doublets + the SM Higgs doublet

$\phi_1, \phi_2$

$\phi_3$

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{h + iG^0}{\sqrt{2}} \end{pmatrix}$$

## 3HDM with a $Z_2 \times Z_2'$ symmetry

DM protected by a  $Z_2$  symmetry  $(-, +, +)$ , and  $Z_2'$  symmetry  $(+, -, +)$

$$\phi_1 \rightarrow -\phi_1, \quad \phi_2 \rightarrow -\phi_2, \quad \text{SM fields} \rightarrow \text{SM fields}, \quad \phi_3 \rightarrow \phi_3$$

$Z_2$  symmetry respected by the vacuum  $(0, 0, v)$ :

$$\phi_1 = \begin{pmatrix} H_1^+ \\ \frac{H_1 + iA_1}{\sqrt{2}} \end{pmatrix}, \quad \phi_2 = \begin{pmatrix} H_2^+ \\ \frac{H_2 + iA_2}{\sqrt{2}} \end{pmatrix}, \quad \phi_3 = \begin{pmatrix} G^+ \\ \frac{v+h+iG^0}{\sqrt{2}} \end{pmatrix}$$

The lightest neutral field from each doublet is a viable DM candidate:

$$m_{H_1} < m_{A_1} < m_{H_1^\pm} \qquad m_{H_2} < m_{A_2} < m_{H_2^\pm}$$

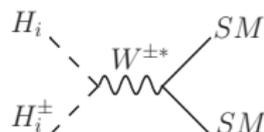
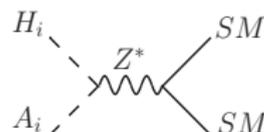
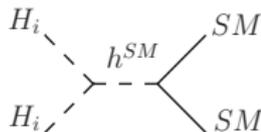
$Z_2$  symmetry: only  $\phi_3$  couples to fermions  $\phi_u = \phi_d = \phi_e = \phi_3$

$$-\mathcal{L}_{\text{Yukawa}} = Y_u \bar{Q}'_L i\sigma_2 \phi_u^* u'_R + Y_d \bar{Q}'_L \phi_d d'_R + Y_e \bar{L}'_L \phi_e e'_R + \text{h.c.}$$

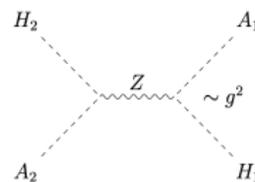
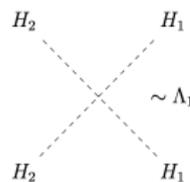
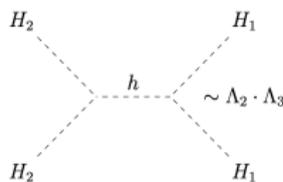
No FCNCs

# Two-component light $H_1$ and heavy $H_2$ DM

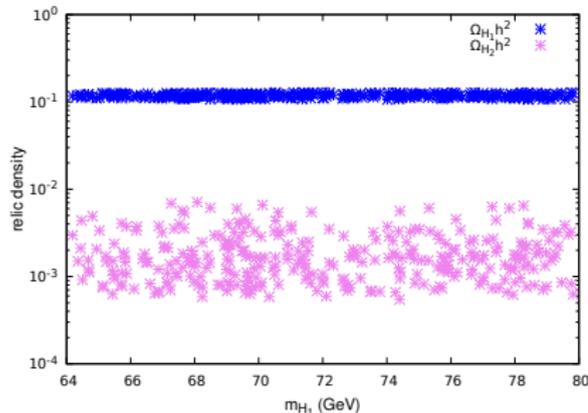
(Co)annihilations:



Conversions:

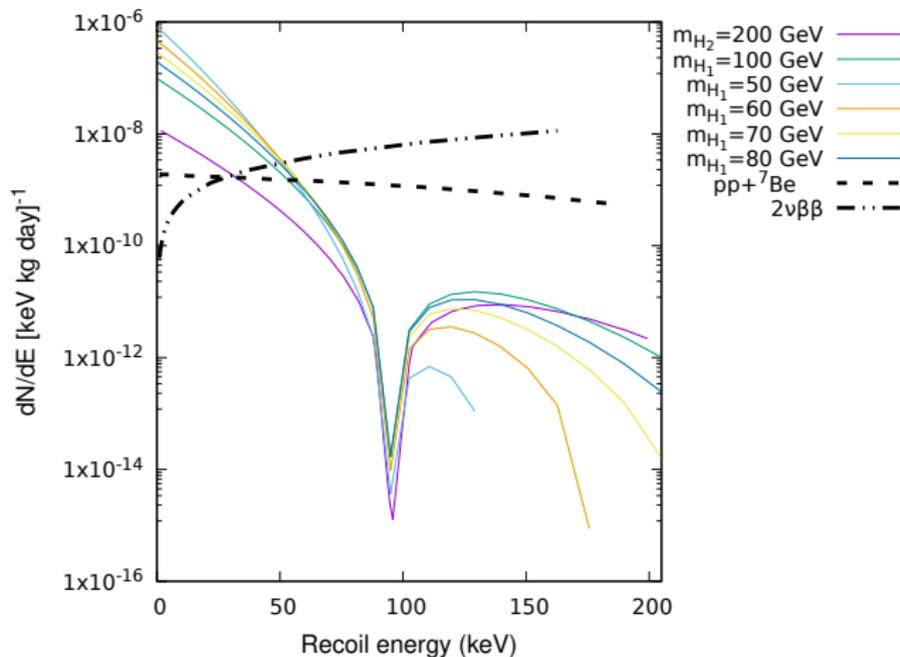


Relic density contributions:



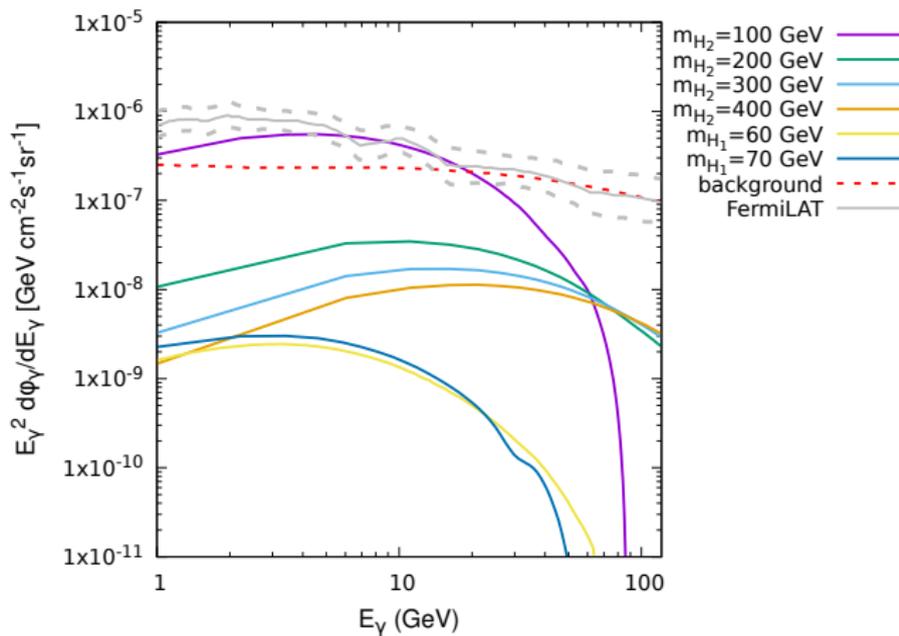
# Astrophysical probes: Direct detection at XENONnT/LZ

Light DM  $H_1$ : probed in the nuclear recoil energy event rate



# Astrophysical probes: Indirect detection at Fermi-LAT

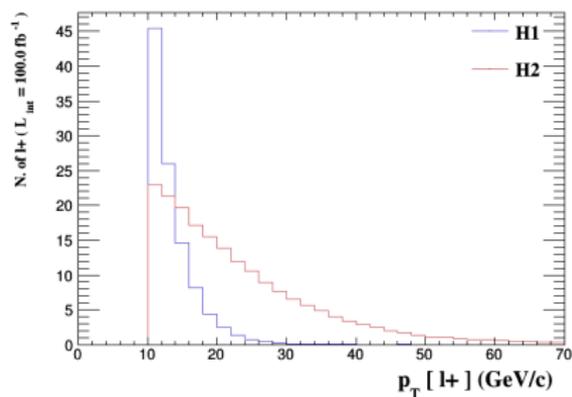
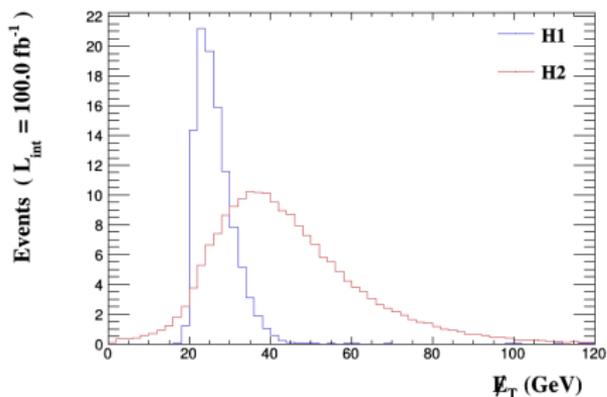
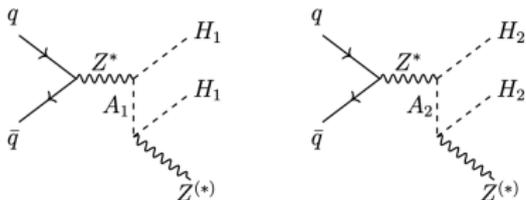
Heavy DM  $H_2$ : contributes to the photon flux from the galactic center



J. Hernandez, V. Keus, S. Moretti, D. Rojas, D. Sokolowska, [JHEP 03, 045 (2023)] and [arXiv:2012.11621]

# Collider probes: distributions of observables

$m_{H_2} - m_{H_1} > \cancel{E}_T$  resolution  $\Rightarrow$  visible effect in different distributions



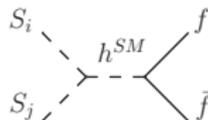
Missing transverse energy and transverse momentum of either lepton

J. Hernandez, V. Keus, S. Moretti, D. Rojas, D. Sokolowska, [JHEP 03, 045 (2023)] and [arXiv:2012.11621]

# Purely scalar extensions w/o a $Z_2 \times Z_2$ symmetry:

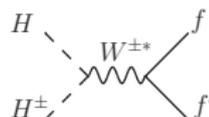
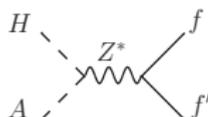
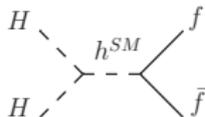
## SM + singlet(s):

- $\phi_{SM}, S \Rightarrow$  **DM**, **CPV**
- $\phi_{SM}, S_{1,2} \Rightarrow$  **DM**, **CPV**



## 2HDMs:

- $\phi_1, \phi_2 \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2 \Rightarrow$  **DM**, **CPV**

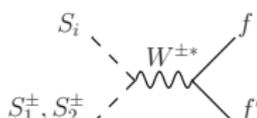
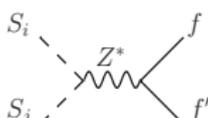
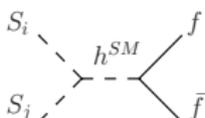


## 2HDM + singlet:

- $\phi_1, \phi_2, S \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2, S \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2, S \Rightarrow$  **DM**, **CPV**

## 3HDMs:

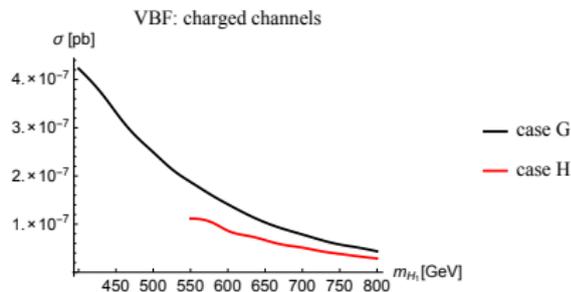
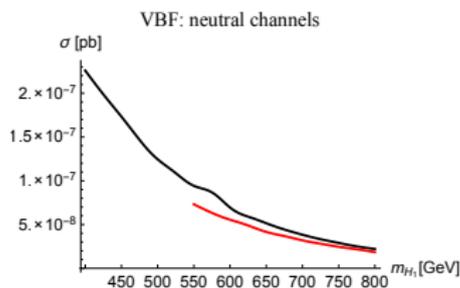
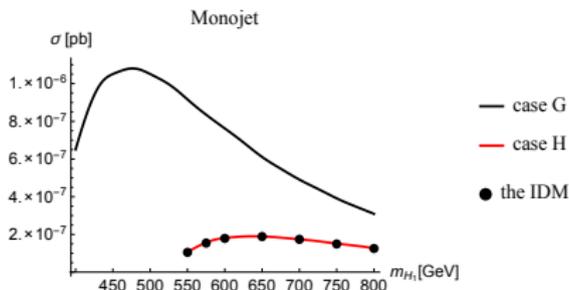
- $\phi_1, \phi_2, \phi_3 \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2, \phi_3 \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2, \phi_3 \Rightarrow$  **DM**, **CPV**
- $\phi_1, \phi_2, \phi_3 \Rightarrow$  **DM**, **DM**



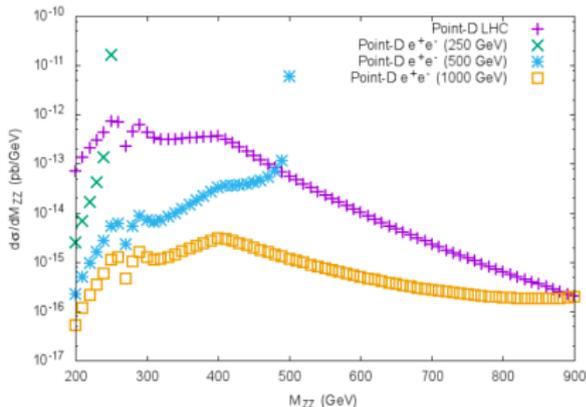
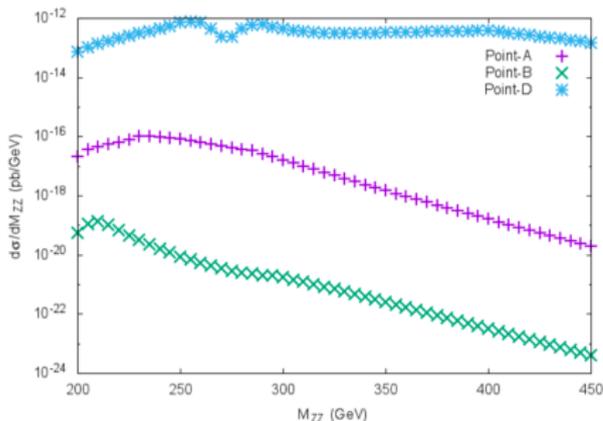
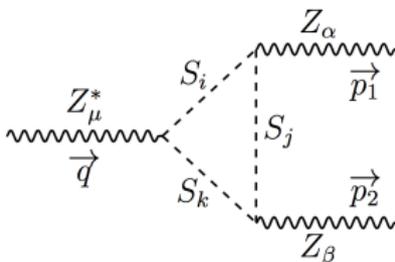
# BACKUP SLIDES

# Observable heavy scalar DM

Monojet and dijet channels in the heavy DM mass region:



# Dark CPV observables: the ZZZ vertex



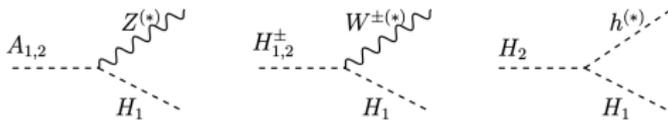
Differential  $f\bar{f} \rightarrow Z^* \rightarrow ZZ$  cross section at hadron and lepton colliders

back

J. Hernandez, V. Keus, S. Moretti, D. Rojas-Ciofalo, D. Sokolowska, [Phys. Rev. D 101, 095023 (2020)]

# Inert cascade decays at the LHC

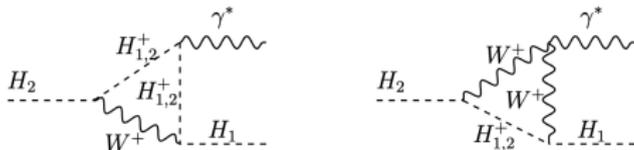
Tree level process:  $q\bar{q} \rightarrow Z^* \rightarrow H_1 A_{1,2} \rightarrow H_1 H_1 Z^* \rightarrow H_1 H_1 f\bar{f}$



(may be possible in 2HDM)

Loop level ggF process:  $gg \rightarrow h \rightarrow H_1 H_2 \rightarrow H_1 H_1 \gamma^* \rightarrow H_1 H_1 f\bar{f}$

Loop level VBF process:  $q_i q_j \rightarrow H_1 H_2 \rightarrow H_1 H_1 \gamma^* \rightarrow H_1 H_1 f\bar{f}$

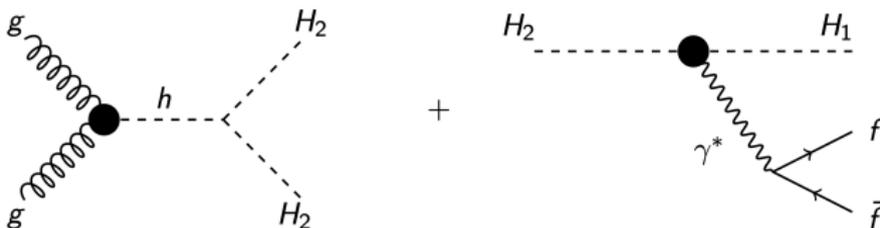


(smoking gun signature of 3HDM)

# The smoking gun signature

(see Atri Dey's talk)

$$\text{MET} + 4\mu: \quad gg \rightarrow h \rightarrow H_2 H_2 \rightarrow H_1 H_1 \gamma^* \gamma^* \rightarrow H_1 H_1 \ell^+ \ell^- \ell^+ \ell^-$$



Benchmark	$m_{H_1}$	$m_{H_2}$	$m_{A_1}$	$m_{A_2}$	$m_{H_1^\pm}$	$m_{H_2^\pm}$	$n$	$\theta_h$	$\sigma_{2\mu}$	$\sigma_{4\mu}$
BP1	50	55	95	104	116	127	0.83	0.105	0.02224	6.923
BP2	50	60	94	112	115	137	0.70	0.103	0.06	4.0

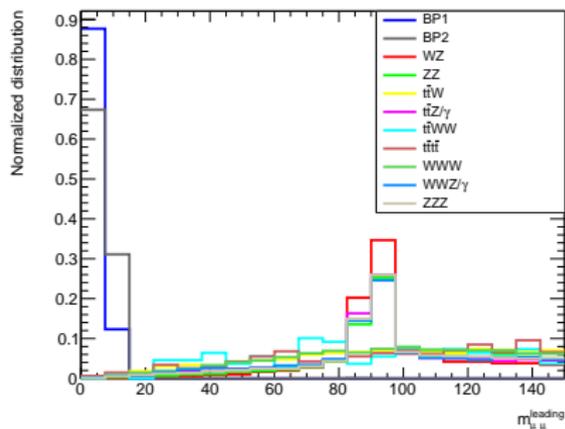
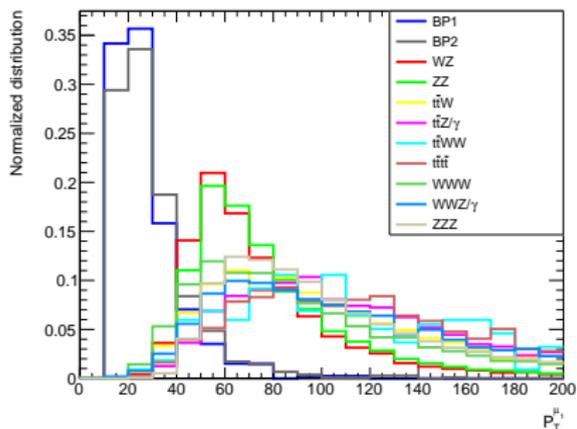
- Signal:  $\geq 3$   $-\mu$  with at least one pair of opposite sign  $\mu$  with  $\cancel{E}_T$ .
- Background:  $VV, VVV$  ( $V = W^\pm, Z, \gamma$ ) and  $t\bar{t}X$  ( $X = W^\pm, Z, \gamma, W^\pm W^\mp, t\bar{t}$ )

back

A. Dey, V. Keus, S. Moretti, C. Shepherd-Themistocleous [arXiv:2309.XXXX]

# Distributions and significance

(see Atri Dey's talk)



BP	$S(\text{Pre} - \text{selection})$	$S(\text{Cut} - A)$
BP1	$0.05 \sigma$	$3.77 \sigma$
BP2	$0.17 \sigma$	$13.67 \sigma$

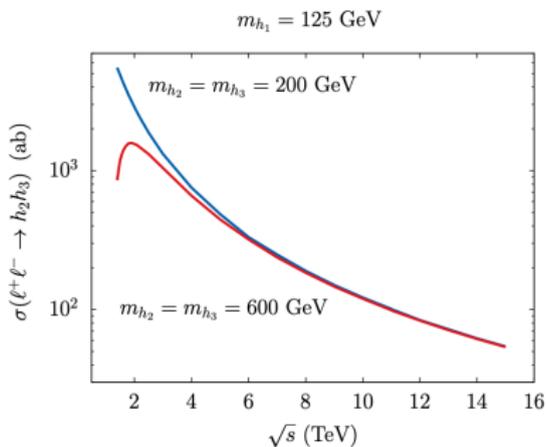
back

A. Dey, V. Keus, S. Moretti, C. Shepherd-Themistocleous [arXiv:2309.XXXX]

## P-conserving, CP-violating observables at future colliders

Undoubtable signal of CPV: simultaneous observation of

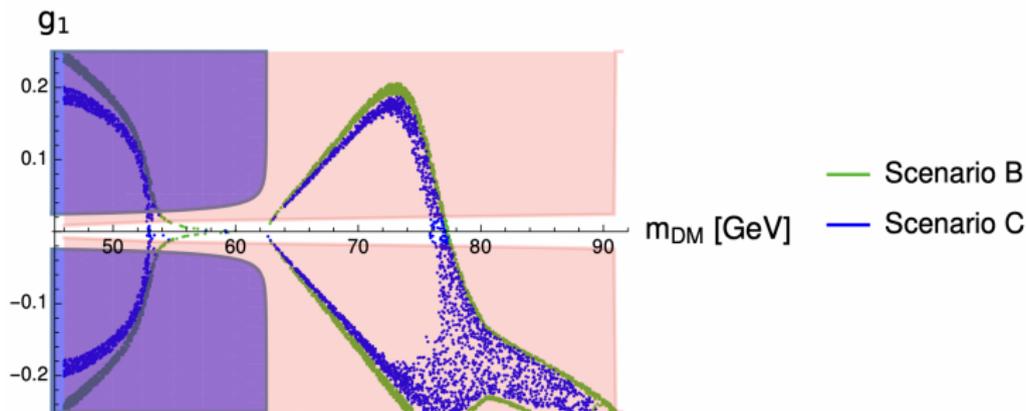
1.  $h_2 H^+ H^-$ ,  $h_3 H^+ H^-$ ,  $Z h_2 h_3$ ,
2.  $h_2 h_k h_k$ ,  $h_3 H^+ H^-$ ,  $Z h_2 h_3$ , (for  $k = 2$  or  $3$ ),
3.  $h_3 h_k h_k$ ,  $h_2 H^+ H^-$ ,  $Z h_2 h_3$ , (for  $k = 2$  or  $3$ ),
4.  $h_2 h_k h_k$ ,  $h_3 h_\ell h_\ell$ ,  $Z h_2 h_3$ , (for  $k, \ell = 2$  or  $3$ ).



# $Z_3$ 3HDM: Hermaphrodite DM $N_1 = H_1 + A_1$

Scenario B:  $m_{H_1} = m_{A_1} \ll m_{A_2} = m_{H_2} \ll m_{H_1^\pm} \sim m_{H_2^\pm}$

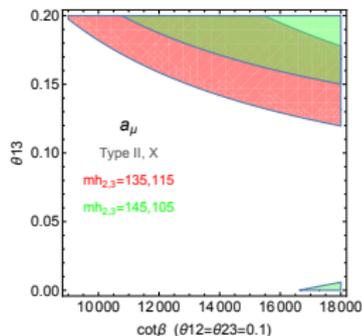
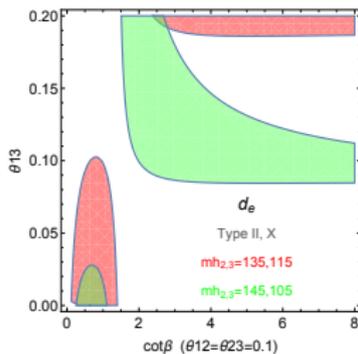
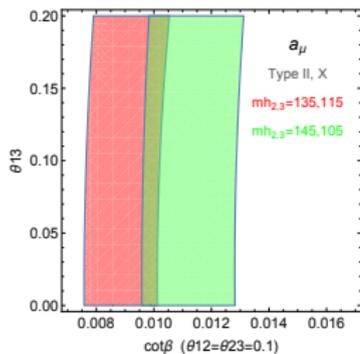
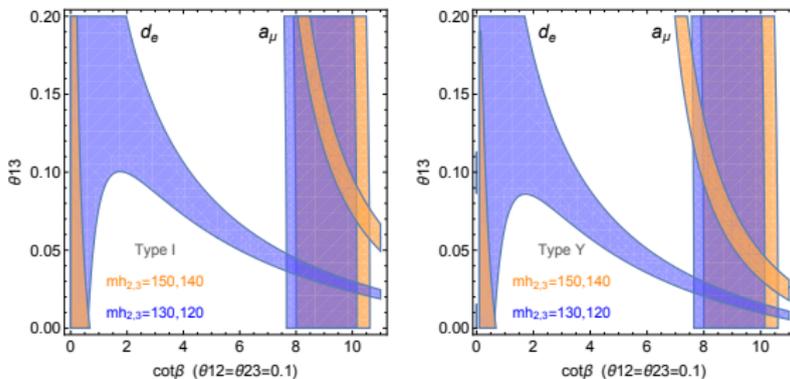
Scenario C:  $m_{H_1} = m_{A_1} \sim m_{A_2} = m_{H_2} \ll m_{H_1^\pm} \sim m_{H_2^\pm}$

[back](#)

A. Aranda, D. Hernández-Otero, J. Hernández-Sánchez, V. Keus, S. Moretti, D. Rojas-Ciofalo, T. Shindou, [Phys.

Rev. D 103, no.1, 015023 (2021)]

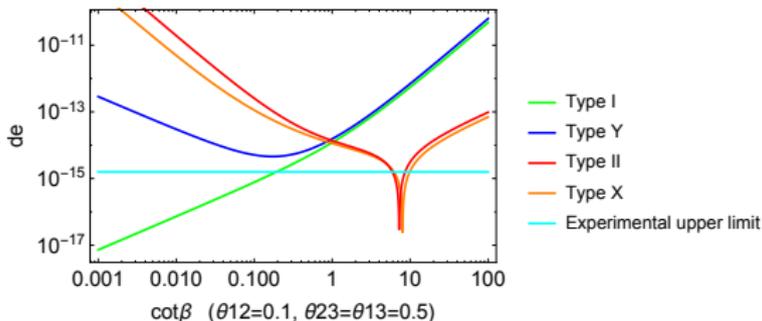
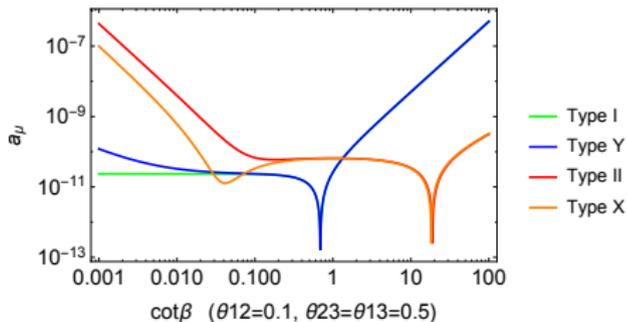
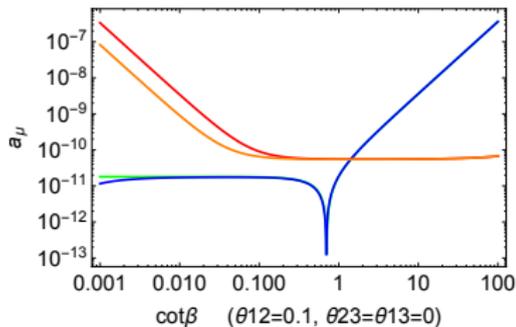
# Overlap between $d_e$ and $a_\mu$ regions in 2HDMs



back

V. Keus, N. Koivunen, K. Tuominen, [JHEP 09, 059 (2018)]

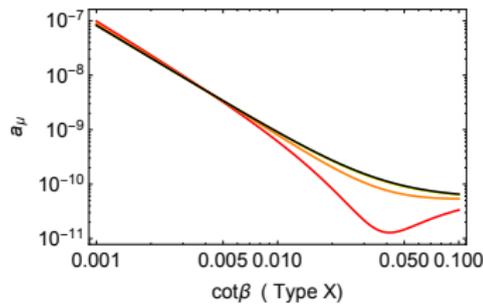
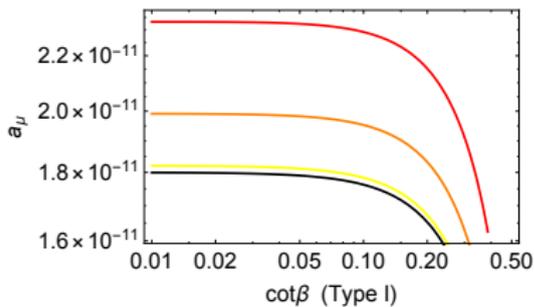
# $a_\mu$ with/without CPV and $d_e$



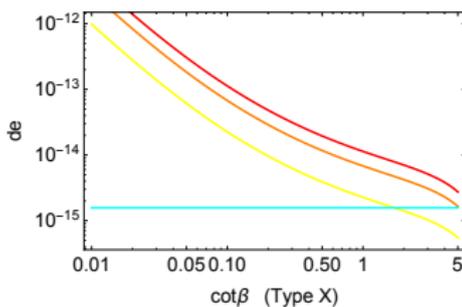
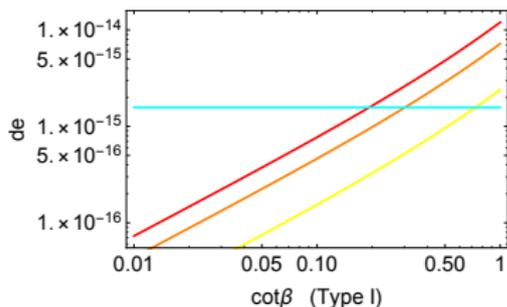
back

V. Keus, N. Koivunen, K. Tuominen, [JHEP 09, 059 (2018)]

# A closer look



- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0$
- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.1$
- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.3$
- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.5$



- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.1$
- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.3$
- $\theta_{12}=0.1, \theta_{23}=\theta_{13}=0.5$
- Experimental upper limit

back

V. Keus, N. Koivunen, K. Tuominen, [JHEP 09, 059 (2018)]